

Formulas

Binomial Pricing

$$\left. \begin{aligned} \Delta d S e^{s h} + B e^{r h} &= C_d \\ \Delta u S e^{s h} + B e^{r h} &= C_u \end{aligned} \right\} \Rightarrow$$

$$C_0 = \Delta S + B$$

$$\left\{ \begin{aligned} C_0 &= e^{-\delta T} (p^* C_u + (1-p^*) C_d) \\ p^* &= \frac{e^{(r-\delta)T} - d}{u - d} \end{aligned} \right.$$

$$\begin{cases} u = e^{(r-\delta)h + \sigma\sqrt{h}} \\ d = e^{(r-\delta)h - \sigma\sqrt{h}} \end{cases}$$

Put-Call Parity

$$C - P = S e^{-\delta T} - K e^{-rT}$$

Black-Scholes

$$C = S e^{-\delta T} N(d_1) - K e^{-rT} N(d_2)$$

$$P = K e^{-rT} N(d_2) - S e^{-\delta T} N(-d_1)$$

$$d_{1,2} = \frac{\ln(S/K) + (r - \delta \pm \frac{1}{2}\sigma^2)T}{\sigma\sqrt{T}}$$