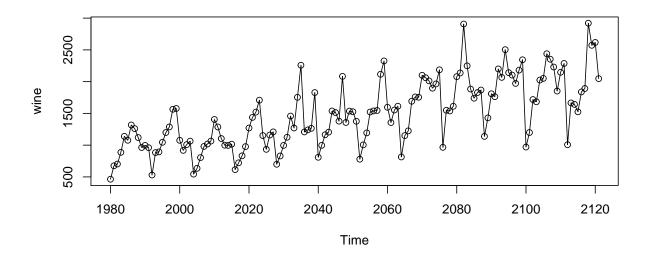
InClass-A3 Sample Analysis

Contents

Preliminary Analysis	2
1. Does "D1" look like stationary time series?	2
2. Take difference of D1 using diff(),	2
3. Should we take any transformation before differencing?	3
ARIMA(d=1) analysis	5
4. Use auto.arima() function to find best $ARIMA(p,\!d,\!q)$	5
5. Now we search for better ARIMA model without the guidance of AICc	6
ARIMA(d=0) with Linear Trend analysis	10
6. Another model we can fit this data is d=0 with linear trend model	10
7. Is the slope estimate you get in (6) consistent with	12
8. Use the following code to fit the regression line outside	13
Compare the two model	15
9. Perform 12-step forecast using the model from (5)	15
10. Perform 12-step forecast using the model from (6)	16
11. Perform Rolling 1-step prediction of last 42 observations	17
12. Perform Rolling 1-step prediction of last 42 observations	18
13. Which model do you like better and why? Model from (5) or (6)? $\dots \dots \dots \dots \dots$	20
Here is the code to load the data from the web.	
<pre>source('https://nmimoto.github.io/R/TS-00.txt')</pre>	
<pre>D <- read.csv("https://nmimoto.github.io/datasets/wine.csv") D1 <- ts(D, start=c(1980,1), freq=1) plot(D1, type='o')</pre>	



Now your "D1" in R contains monthly wine sales in Australia.

Preliminary Analysis

1. Does "D1" look like stationary time series?

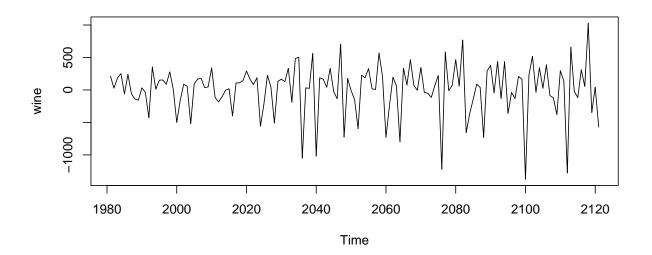
State your graphical observations and conclusions drawn from p-values form Stationarity.tests().

```
## Warning in adf.test(A): p-value smaller than printed p-value
## Warning in pp.test(A): p-value smaller than printed p-value
## Warning in kpss.test(A): p-value smaller than printed p-value
## KPSS ADF PP
## p-val: 0.01 0.01 0.01
## KPSS and ADF conflicting
```

2. Take difference of D1 using diff(),

plot it and check the stationarity. State your graphical observations and conclusions drawn from p-values form Stationarity.tests().

```
plot(diff(D1))
```



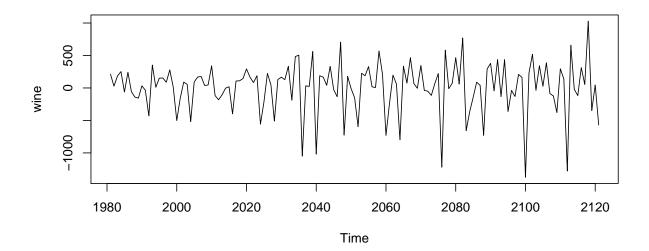
Stationarity.tests(diff(D1))

```
## Warning in adf.test(A): p-value smaller than printed p-value
## Warning in pp.test(A): p-value smaller than printed p-value
## Warning in kpss.test(A): p-value greater than printed p-value
## KPSS ADF PP
## p-val: 0.1 0.01 0.01
## d=1 is Stationary.
```

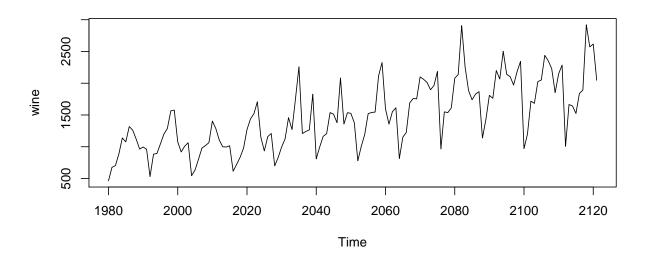
3. Should we take any transformation before differencing?

Why or why not? If yes, use Box-Cox power transformation. Pick your value of lambda.

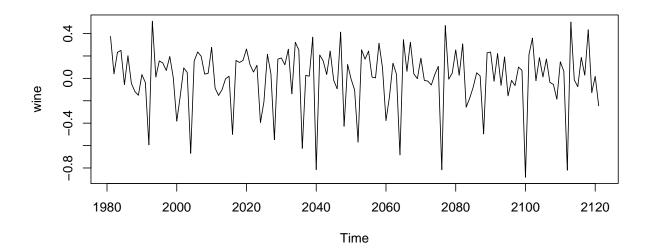
```
plot(diff(D1))
```



plot((D1))



plot(diff(log(D1)))



```
## Even though D1 passed the stationarity tests, it looks like it
## has increasing variance problem.
## This is probably due to D1 increasing as time goes on.
## Taking a log will solve this problem.
##
## Set lambda=0.
```

For all problems below lambda=0.

ARIMA(d=1) analysis

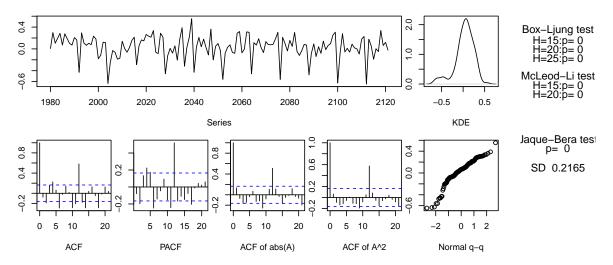
4. Use auto.arima() function to find best ARIMA(p,d,q)

model with constraint that d=1. What is the suggested model? (use stepwise=FALSE, approximation=FALSE option.) Does it pass the residual test for model adequacy? Copy and Paste the output from auto.arima() and Randomness.tests(). (not the plot)

```
Fit01 <- auto.arima(D1, d=1, lambda=0, stepwise=FALSE, approximation=FALSE)
Fit01</pre>
```

```
## Series: D1
## ARIMA(3,1,2)
## Box Cox transformation: lambda= 0
##
  Coefficients:
##
##
            ar1
                     ar2
                               ar3
                                        ma1
                                                 ma2
         1.2830
##
                                             0.9566
                 -0.3135
                           -0.2752
                                    -1.8894
         0.1063
                  0.1474
                            0.0929
                                     0.1135
                                             0.1178
## sigma^2 estimated as 0.04984: log likelihood=11.51
## AIC=-11.02
               AICc=-10.39
                               BIC=6.68
```

Randomness.tests()



```
##
     B-L test HO: the series is uncorrelated
##
     M-L test HO: the square of the series is uncorrelated
     J-B test HO: the series came from Normal distribution
##
##
                : Standard Deviation of the series
##
        BL15 BL20 BL25 ML15 ML20 JB
## [1,]
           0
                0
                     0
                          0
                               0 0 0.216
## ARIMA(3,1,2) is suggested.
##
## Residual analysis does not show adequate fit. P-value for Ljung-Box tests are
## too low, indicating there's still autocorrelation left in the residual.
##
## Acf plot comfirms this.
```

5. Now we search for better ARIMA model without the guidance of AICc.

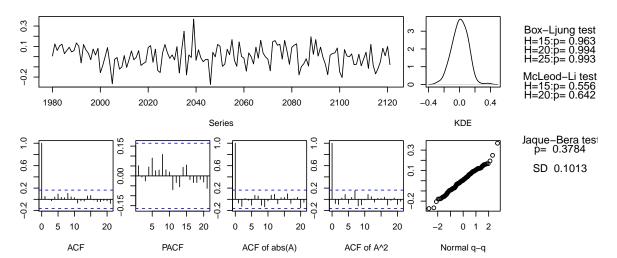
Start with ARIMA(15, 1, 15) with the drift model, use Arima() function to estimate parameters. Reduce p and/or q if the last parameter in AR or MA is not significant. Stop if the LAST parameter of both AR and MA term is significant. Remove the drift if not significant.

What is your final model? Compare AICc of your final model to the ones you got from (4). Which one is lower? Why did this model was not suggested in (4)? Does this final model pass the residual adequacy test? (Only include the output of your final model. Model pram + Residual p-values.)

```
#- If you start removing AR(15) first
Arima(D1, lambda=0, order=c(15,1,15), include.drift=TRUE)
    #AR15 not significant.
```

```
#Arima(D1, lambda=0, order=c(14,1,15), include.drift=TRUE)
    #This gives estimation error. use CSS.
  Arima(D1, lambda=0, order=c(14,1,15), include.drift=TRUE, method="CSS")
    #MA15 not sig
  Arima(D1, lambda=0, order=c(14,1,14), include.drift=TRUE)
    #AR14 not sig
  Arima(D1, lambda=0, order=c(13,1,14), include.drift=TRUE)
    #AR13, MA14 both not sig
    # a) remove AR13 b) remove MA14
  Arima(D1, lambda=0, order=c(12,1,14), include.drift=TRUE)
    #a) MA14 not sig
  Arima(D1, lambda=0, order=c(13,1,13), include.drift=TRUE)
   #b) AR13 not sig
 Fit05 <- Arima(D1, lambda=0, order=c(12,1,13), include.drift=TRUE)
Fit05
## Series: D1
## ARIMA(12,1,13) with drift
## Box Cox transformation: lambda= 0
## Coefficients:
                    ar2
                                               ar5
##
           ar1
                             ar3
                                      ar4
                                                       ar6
                                                                ar7
##
        -0.129 -0.1408 -0.1249 -0.1166 -0.1477 -0.1350 -0.1231
## s.e.
        0.113
                 0.1182
                          0.1164
                                   0.1273
                                           0.1094
                                                    0.1196
                                                            0.1077
##
            ar8
                     ar9
                             ar10
                                      ar11
                                             ar12
                                                      ma1
                                                              ma2
##
        -0.1540 -0.1318 -0.1439 -0.1240 0.8481 -0.686 0.0612
## s.e.
        0.1189
                 0.1150
                          0.1220
                                   0.1177 0.1140
                                                    0.152 0.1148
##
                     ma4
                             ma5
                                                     ma8
                                                              ma9
            ma3
                                      ma6
                                             ma7
##
        -0.0590 -0.0427 0.1771 -0.1860 0.0520 0.0851 -0.0852
## s.e.
        0.1249
                 0.1682 0.1550
                                 0.1453 0.1125 0.1637
                                                           0.1361
##
          ma10
                  ma11
                            ma12
                                    ma13
                                          drift
        0.1419 -0.1909 -0.6793 0.4119 0.0063
##
## s.e. 0.1148
                 0.1400
                         0.2134 0.1866 0.0005
## sigma^2 estimated as 0.01263: log likelihood=106.74
## AIC=-159.49 AICc=-146.11 BIC=-79.87
    #a) b) MA13 barely sig
 Randomness.tests(Fit05$residuals)
```

Randomness.tests()



```
## B-L test H0: the series is uncorrelated
## M-L test H0: the square of the series is uncorrelated
## J-B test H0: the series came from Normal distribution
## SD : Standard Deviation of the series
## BL15 BL20 BL25 ML15 ML20 JB SD
## [1,] 0.963 0.994 0.993 0.556 0.642 0.378 0.101
```

```
#- If you start removing MA(15) first

Fit05b <- Arima(D1, lambda=0, order=c(15,1,13), include.drift=TRUE)
Fit05b</pre>
```

```
## Series: D1
## ARIMA(15,1,13) with drift
## Box Cox transformation: lambda= 0
##
## Coefficients:
```

Warning in sqrt(diag(x\$var.coef)): NaNs produced

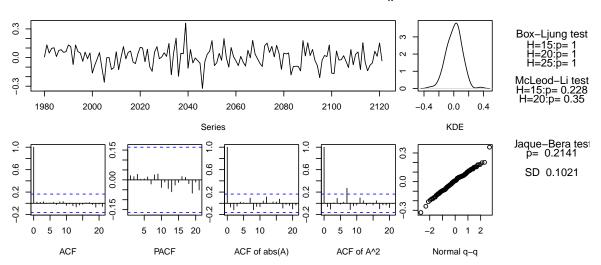
```
##
              ar1
                        ar2
                                  ar3
                                           ar4
                                                     ar5
                                                              ar6
                                                                        ar7
         -0.3565
##
                   -0.2038
                             -0.4819
                                       0.0531
                                                -0.0245
                                                          -0.004
                                                                   -0.0398
##
          0.1435
                     0.1482
                               0.1083
                                                                       NaN
                                           NaN
                                                     NaN
                                                              NaN
   s.e.
##
                        ar9
                                 ar10
                                          ar11
                                                   ar12
                                                           ar13
                                                                    ar14
              ar8
          -0.0786
                    -0.0096
                             -0.0218
                                       0.0205
##
                                                0.9518
                                                         0.3127
                                                                  0.1625
              NaN
                        NaN
                                  NaN
                                           NaN
                                                    NaN
                                                         0.1280
                                                                  0.1342
   s.e.
                                 {\tt ma2}
##
            ar15
                       ma1
                                          ma3
                                                    ma4
                                                            ma5
                                                                      ma6
##
          0.4459
                  -0.3953
                            -0.0707
                                      0.2296
                                               -0.4690
                                                         0.2688
                                                                  -0.2049
         0.1052
##
                    0.1523
                             0.1058
                                      0.0882
                                                0.0827
                                                         0.0969
                                                                   0.0889
   s.e.
                     ma8
                               ma9
                                       ma10
                                                 ma11
                                                           ma12
                                                                    ma13
             ma7
         0.1089
                  0.2317 -0.2969 0.2281
                                             -0.3225 -0.6477
##
                                                                  0.3400
```

```
## s.e. 0.0867 0.0962 0.0950 0.0815 0.0735 NaN 0.1668
## drift
## 0.0061
## s.e. 0.0017
##
## sigma^2 estimated as 0.01315: log likelihood=106.31
## AIC=-152.62 AICc=-135.72 BIC=-64.16
```

```
#AR15 not significant.
```

Randomness.tests(Fit05b\$residuals)

Randomness.tests()



```
## B-L test H0: the series is uncorrelated
## M-L test H0: the square of the series is uncorrelated
## J-B test H0: the series came from Normal distribution
## SD : Standard Deviation of the series
## BL15 BL20 BL25 ML15 ML20 JB SD
## [1,] 1 1 0.228 0.35 0.214 0.102
```

```
Depending of what you remove first you end up with either
   ARIMA(12,1,13) with drift, or ARIMA(15,1,13) with drift.
    (lambda is set to 0).
##
##
##
   I will use ARIMA(12,1,13) with drift to answer questions below.
##
##
   AICc of Fit05 is -146.11. AICc of Fit01 is -10.39. Based on AICc,
   ARIMA(12,1,13) should have been reported by auto.arima(), but
##
   was not looked at, because maximum p and q of the default setting is 5.
##
   The model fit of both ARIMA(12,1,13) with drift and
   ARIMA(15,1,13) with drift is adequate by residual analysis.
```

ARIMA(d=0) with Linear Trend analysis

6. Another model we can fit this data is d=0 with linear trend model.

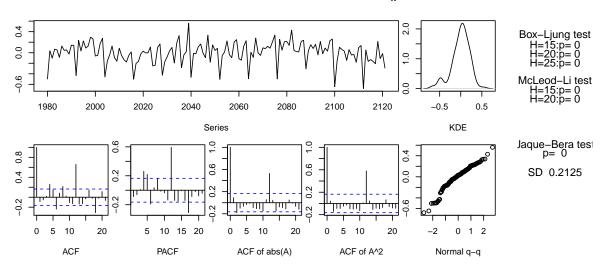
Use auto.arima() with d=0 and xreg=time(D1) option to find best ARMA(p,q) model to go on top of the linear trend. Don't forget to use the same lambda as before. What is your linear trend model? Does this final model pass the residual adequacy test?

(Model pram + Residual p-values.)

```
Fit06 <- auto.arima(D1, stepwise=FALSE, approximation=FALSE,
                                         lambda=0, xreg=time(D1))
 Fit06
## Series: D1
## Regression with ARIMA(4,0,1) errors
## Box Cox transformation: lambda= 0
##
##
  Coefficients:
##
            ar1
                     ar2
                              ar3
                                            -0.6627
##
         1.0148
                 -0.2605
                          0.1093
                                   -0.3121
                                                                 0.0065
                                                        -6.1249
## s.e.
         0.0999
                  0.1211
                          0.1176
                                    0.0837
                                             0.0734
                                                         0.7148
                                                                 0.0004
##
## sigma^2 estimated as 0.04715:
                                   log likelihood=18.35
## AIC=-20.69
                AICc=-19.61
                               BIC=2.95
```

Randomness.tests(Fit06\$residuals)

Randomness.tests()

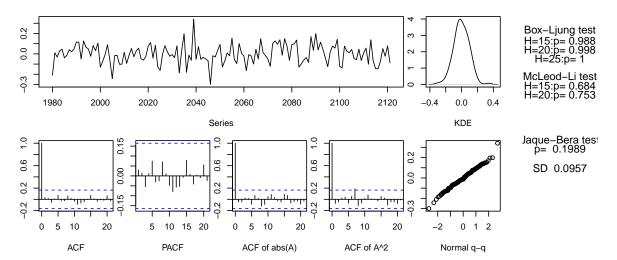


```
## B-L test H0: the series is uncorrelated
## M-L test H0: the square of the series is uncorrelated
## J-B test H0: the series came from Normal distribution
## SD : Standard Deviation of the series
```

```
BL15 BL20 BL25 ML15 ML20 JB
## [1,]
       0 0 0 0
                              0 0 0.212
## Model fit is not adequate. P-value is too low for all
## L-B test.
## There's significant autocorrelation at lag 12.
## Should try ARMA with higher p,q like we did in #5.
 Fit06b <- Arima(D1, order=c(15,0,15), xreg=time(D1), lambda=0)
 Fit06b
## Series: D1
## Regression with ARIMA(15,0,15) errors
## Box Cox transformation: lambda= 0
## Coefficients:
## Warning in sqrt(diag(x$var.coef)): NaNs produced
##
                    ar2
                            ar3
                                    ar4
                                            ar5
                                                     ar6
                                                              ar7
            ar1
##
        -0.4765 0.7913 0.5179 0.0028 -0.0316 -0.0511 -0.0146
            NaN 0.1081 0.1210 0.0196
                                        0.0208
## s.e.
                                                 0.0094
                                                          0.0223
            ar8
                    ar9
                            ar10
                                    ar11
                                           ar12
                                                   ar13
                                                            ar14
        -0.0411 -0.041 -0.0240 0.0006 0.9728 0.4459 -0.8184
##
        0.0207
                         0.0234 0.0195 0.0152
## s.e.
                    \mathtt{NaN}
                                                    \mathtt{NaN}
##
                            ma2
                                              ma4
                                                     ma5
                                                             ma6
           ar15
                    ma1
                                     ma3
        -0.5375 0.5869 -0.6199 -0.4733 -0.1190 0.044 0.0293
##
                        0.1573   0.1992   0.1041   0.088   0.1449
## s.e.
        0.1101
                    {\tt NaN}
##
            ma7
                    ma8
                            ma9
                                  ma10
                                           ma11
                                                    ma12
                                                            ma13
##
        -0.1085 0.0821 0.0420 0.1038 -0.0402 -0.9426 -0.577
## s.e.
        0.1027 0.1189 0.1167 0.1104
                                        0.1028 0.1050
                                                             NaN
##
          ma14
                  ma15 intercept
                                     xreg
##
        0.5308 0.4618
                          -6.7277 0.0068
## s.e. 0.1523 0.1204
                          0.4158 0.0002
##
## sigma^2 estimated as 0.01175: log likelihood=113.56
## AIC=-161.11 AICc=-140.33 BIC=-63.57
```

Randomness.tests(Fit06b\$residuals)

Randomness.tests()



```
## B-L test H0: the series is uncorrelated
## M-L test H0: the square of the series is uncorrelated
## J-B test H0: the series came from Normal distribution
## SD : Standard Deviation of the series

## BL15 BL20 BL25 ML15 ML20 JB SD
## [1,] 0.988 0.998  1 0.684 0.753 0.199 0.096
```

```
## Model fit is now adequate. AR15 and MA15 both significant.
## Slope and intercept basically unchanged from before.
```

7. Is the slope estimate you get in (6) consistent with

the drift term you had in (5)?

Fit05

```
## Series: D1
## ARIMA(12,1,13) with drift
## Box Cox transformation: lambda= 0
##
##
   Coefficients:
##
             ar1
                       ar2
                                ar3
                                          ar4
                                                    ar5
                                                              ar6
                                                                        ar7
         -0.129
                  -0.1408
                                                          -0.1350
##
                            -0.1249
                                      -0.1166
                                                -0.1477
                                                                   -0.1231
##
           0.113
                   0.1182
                             0.1164
                                       0.1273
                                                 0.1094
                                                           0.1196
                                                                     0.1077
   s.e.
##
                                ar10
                                          ar11
                                                   ar12
                                                                      ma2
              ar8
                        ar9
                                                             ma1
         -0.1540
                   -0.1318
                             -0.1439
                                       -0.1240
                                                 0.8481
                                                          -0.686
                                                                  0.0612
##
           0.1189
                              0.1220
## s.e.
                    0.1150
                                        0.1177
                                                 0.1140
                                                           0.152
                                                                  0.1148
##
                       ma4
                                ma5
                                          ma6
                                                   ma7
                                                            ma8
                                                                      ma9
              ma3
##
         -0.0590
                   -0.0427
                             0.1771
                                      -0.1860
                                                0.0520
                                                        0.0851
                                                                 -0.0852
## s.e.
          0.1249
                    0.1682
                             0.1550
                                       0.1453
                                               0.1125
                                                        0.1637
                                                                  0.1361
```

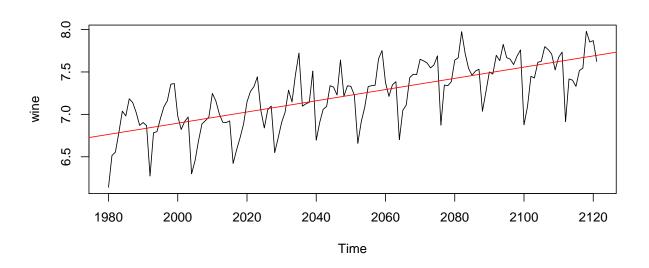
```
##
                                              drift
           ma10
                     ma11
                              ma12
                                       ma13
##
         0.1419
                 -0.1909
                           -0.6793 0.4119
                                             0.0063
                            0.2134 0.1866
                                             0.0005
         0.1148
                  0.1400
##
## sigma^2 estimated as 0.01263:
                                   log likelihood=106.74
## AIC=-159.49
                 AICc=-146.11
                                 BIC=-79.87
Fit06b
## Series: D1
## Regression with ARIMA(15,0,15) errors
## Box Cox transformation: lambda= 0
## Coefficients:
## Warning in sqrt(diag(x$var.coef)): NaNs produced
##
                      ar2
                              ar3
             ar1
                                       ar4
                                                ar5
                                                          ar6
                                                                   ar7
                           0.5179
##
         -0.4765
                  0.7913
                                   0.0028
                                            -0.0316
                                                      -0.0511
                                                               -0.0146
                  0.1081
                           0.1210
                                   0.0196
                                             0.0208
                                                       0.0094
## s.e.
             NaN
                                                                0.0223
##
             ar8
                      ar9
                              ar10
                                       ar11
                                               ar12
                                                        ar13
                                                                 ar14
                           -0.0240
                                    0.0006
##
         -0.0411
                  -0.041
                                             0.9728
                                                     0.4459
                                                              -0.8184
          0.0207
                            0.0234
                                    0.0195
                                             0.0152
##
                                                        {\tt NaN}
                                                               0.1054
  s.e.
                      {\tt NaN}
##
            ar15
                      ma1
                               ma2
                                         ma3
                                                  ma4
                                                          ma5
                                                                  ma6
##
         -0.5375
                  0.5869
                           -0.6199
                                    -0.4733
                                              -0.1190
                                                       0.044
                                                               0.0293
## s.e.
          0.1101
                      NaN
                            0.1573
                                     0.1992
                                               0.1041
                                                       0.088
                                                               0.1449
##
             ma7
                      ma8
                              ma9
                                     ma10
                                               ma11
                                                         ma12
                                                                 ma13
##
         -0.1085
                  0.0821
                           0.0420 0.1038
                                           -0.0402
                                                     -0.9426
                                                               -0.577
                           0.1167 0.1104
                                             0.1028
## s.e.
          0.1027
                  0.1189
                                                       0.1050
                                                                  NaN
##
           ma14
                   ma15
                          intercept
                                        xreg
                            -6.7277
##
         0.5308
                 0.4618
                                     0.0068
## s.e.
        0.1523
                 0.1204
                             0.4158 0.0002
##
## sigma^2 estimated as 0.01175: log likelihood=113.56
## AIC=-161.11
                 AICc=-140.33
                                 BIC=-63.57
## drift term from Fit05 is 0.0061.
## xreg (slope) term from Fit06b is 0.0068.
## They are close and therefore consistent.
## At this point, we can not decide on which model is more
## plausible. We will do more test on #8.
```

8. Use the following code to fit the regression line outside

of auto.arima(), and test the regression residuals for stationarity. Is the estimate consistent with (6)? (Replace lambda with your lambda)

```
D2 <- BoxCox(D1, lambda=0)
Reg <- lm(D2~time(D2))
summary(Reg)
```

```
##
## Call:
## lm(formula = D2 ~ time(D2))
##
## Residuals:
##
       Min
                      Median
                                    3Q
                  1Q
                                            Max
   -0.72153 -0.11939 0.03217 0.17556 0.59503
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) -6.3264336 1.1271356 -5.613 1.03e-07 ***
## time(D2)
               0.0066111 0.0005496 12.029 < 2e-16 ***
##
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2684 on 140 degrees of freedom
## Multiple R-squared: 0.5083, Adjusted R-squared: 0.5048
## F-statistic: 144.7 on 1 and 140 DF, p-value: < 2.2e-16
  plot(D2)
  abline(Reg, col="red")
```



Stationarity.tests(Reg\$residuals)

```
## Warning in adf.test(A): p-value smaller than printed p-value
## Warning in pp.test(A): p-value smaller than printed p-value
## Warning in kpss.test(A): p-value greater than printed p-value
## KPSS ADF PP
## p-val: 0.1 0.01 0.01
```

```
## Large, small, small p-values unaniously indicates that
## the Regression residuals are stationary.
## This means that model in (#5) is not a good model(necessary) for the data,
## even though ARMA residual analysis looked good on #5.
## We should be modeling this data with
## Yt = Linear Trend + ARMA error
## as in #6.
```

Compare the two model

9. Perform 12-step forecast using the model from (5).

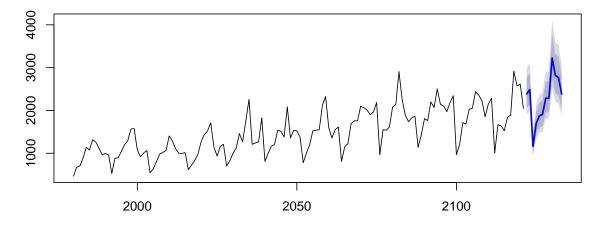
What is the 95% PI for the next observation? Include the numbers here.

```
forecast(Fit05, 12)
```

```
##
        Point Forecast
                          Lo 80
                                   Hi 80
                                             Lo 95
                                                       Hi 95
## 2122
              2383.929 2061.805 2756.380 1909.2958 2976.553
## 2123
              2486.541 2144.839 2882.681 1983.3926 3117.328
## 2124
              1165.406 1001.926 1355.560 924.8835 1468.478
## 2125
              1696.449 1456.237 1976.285 1343.1679 2142.650
## 2126
              1868.304 1602.821 2177.761 1477.9128 2361.817
## 2127
              1911.142 1633.666 2235.748 1503.4791 2429.342
## 2128
              2288.551 1956.208 2677.355 1800.2840 2909.244
## 2129
              2282.224 1949.905 2671.180 1794.0473 2903.238
## 2130
              3223.748 2751.203 3777.456 2529.7749 4108.093
## 2131
              2819.906 2406.211 3304.728 2212.3798 3594.261
## 2132
              2766.423 2356.006 3248.334 2163.9995 3536.551
## 2133
              2380.877 2027.637 2795.656 1862.3804 3043.726
```

```
plot(forecast(Fit05, 12))
```

Forecasts from ARIMA(12,1,13) with drift



```
## Older version of the question wrongly said CI instead of PI.
## We are getting Prediction Interval for next 12 observations.
## Assuming Normality, 95% PI for next obs is
```

10. Perform 12-step forecast using the model from (6).

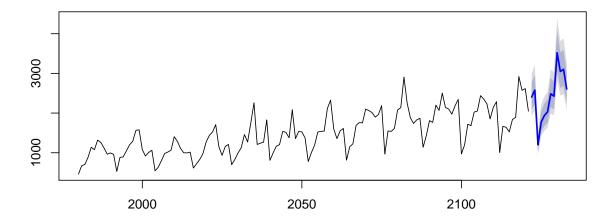
What is the 95% PI for the next observation? Include the numbers here. (Remember that your forecast() needs xreg. See slide (6-5))

```
h=12
forecast(Fit06b, h, xreg=last(time(D1))+(1:h)/frequency(D1))
```

```
##
        Point Forecast
                          Lo 80
                                   Hi 80
                                             Lo 95
                                                       Hi 95
## 2122
              2402.444 2085.221 2767.926 1934.6183 2983.398
## 2123
              2578.940 2236.241 2974.156 2073.6653 3207.330
## 2124
              1201.127 1040.651 1386.351 964.5702 1495.699
## 2125
              1772.715 1535.119 2047.084 1422.5199 2209.121
## 2126
              1937.720 1678.018 2237.614 1554.9418 2414.725
## 2127
              2030.426 1755.982 2347.762 1626.0520 2535.361
## 2128
              2485.653 2149.599 2874.244 1990.5051 3103.972
## 2129
              2424.606 2096.848 2803.596 1941.6790 3027.644
              3518.213 3041.743 4069.319 2816.2208 4395.189
## 2130
              3047.903 2634.624 3526.012 2439.0393 3808.760
## 2131
              3102.146 2678.221 3593.172 2477.7894 3883.828
## 2132
## 2133
              2605.651 2247.112 3021.398 2077.7380 3267.697
```

```
plot(forecast(Fit06b, h, xreg=last(time(D1))+(1:h)/frequency(D1)))
```

Forecasts from Regression with ARIMA(15,0,15) errors

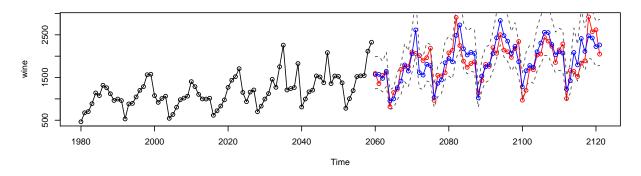


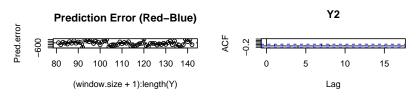
11. Perform Rolling 1-step prediction of last 42 observations

retrospectively using model from (5). Report prediction rMSE. Compare that with sigma-hat from the model.

```
#- Set options
Y <- D1
                           # Original data
window.size <- 80
                          # Window size for estimation
Arima.order \leftarrow c(12,1,13) # Arima(p,d,q) order
pred.plot <- TRUE</pre>
                           # do you want plot at end?
#- set Arima() options:
include.mean = FALSE
include.drift = TRUE
lambda
         = 0
                            # NULL=no transformaton. O=Log
xreg
         = NULL
                            # NULL=no xreg. TRUE=Linear Trend is present
seasonal = c(0, 0, 0)
                            # seasonal component
#- then use the function
Rolling1step.forecast(Y, window.size, Arima.order, pred.plot,
                        include.mean, include.drift, lambda, xreg, seasonal)
```

```
##
## Last 62 obs fit retrospectively
## with Rolling 1-step prediction
## Average prediction error: -44.8632
## root Mean Squared Error: 261.1243
```





```
## mean pred error rMSE
## [1,] -44.8632 261.1243
```

```
#Rolling1step.forecast.old(Y, window.size, Arima.order, pred.plot,
# include.mean, include.drift, lambda, xreg, seasonal)
```

```
# Transforming Sigma Back

D2     <- BoxCox(D1, lambda=0)
D.base <- D2[length(D1)-(42:1)]  # last 42 obs in D1
Y     <- rnorm(1000*42, 0, 0.1120268)  # simulating normal data with same theoretical model rMSE
Y2 <- Y+rep(D.base, times=1000)  # add
X     <- InvBoxCox(Y2, lambda = 0) #inverse transform
sd(X)</pre>
```

[1] 498.8376

12. Perform Rolling 1-step prediction of last 42 observations

retrospectively using model from (6). Report prediction rMSE. Compare that with sigma-hat from the model.

```
#- Set options
Y <- D1
                           # Original data
window.size <- 100
                          # Window size for estimation
Arima.order \leftarrow c(15,0,15) # Arima(p,d,q) order
pred.plot <- TRUE</pre>
                          # do you want plot at end?
#- set Arima() options:
include.mean = TRUE
include.drift = FALSE
lambda = 0
                          # NULL=no transformaton. O=Log
        = TRUE
                        # NULL=no xreg. TRUE=Linear Trend is present
xreg
seasonal = c(0, 0, 0)
                         # seasonal component
#- then use the function
Rolling1step.forecast(Y, window.size, Arima.order, pred.plot,
                        include.mean, include.drift, lambda, xreg, seasonal)
##
       i= 18 MLE-CSS failed. Using CSS.
```

```
## i= 18 MLE-CSS failed. Using CSS.

## Warning in predict.Arima(object, n.ahead = h, newxreg = xreg): MA part
## of model is not invertible

## i= 26 MLE-CSS failed. Using CSS.

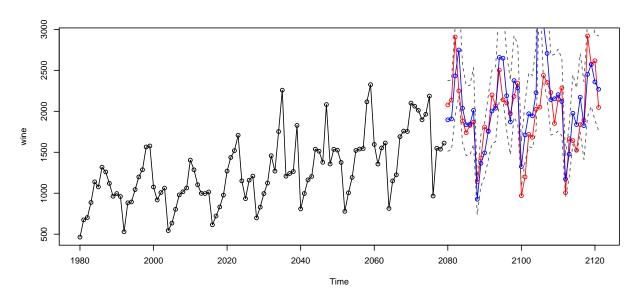
## Warning in predict.Arima(object, n.ahead = h, newxreg = xreg): MA part
## of model is not invertible

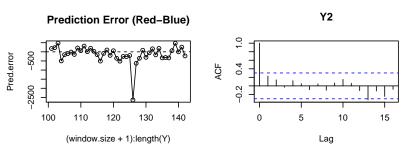
## i= 27 MLE-CSS failed. Using CSS.

## Warning in predict.Arima(object, n.ahead = h, newxreg = xreg): MA part
## of model is not invertible
```

```
MLE-CSS failed. Using CSS.
##
       i = 38
## Warning in predict.Arima(object, n.ahead = h, newxreg = xreg): MA part
## of model is not invertible
               MLE-CSS failed. Using CSS.
##
       i = 39
## Warning in predict.Arima(object, n.ahead = h, newxreg = xreg): MA part
## of model is not invertible
##
       i = 42
               MLE-CSS failed. Using CSS.
## Warning in predict.Arima(object, n.ahead = h, newxreg = xreg): MA part
## of model is not invertible
##
## Last 42 obs fit retrospectively
##
       with Rolling 1-step prediction
     Average prediction error: -135.2106
##
```

488.934





mean pred error rMSE ## [1,] -135.2106 488.934

##

root Mean Squared Error:

13. Which model do you like better and why? Model from (5) or (6)?

Write down your mathematical model, and list estimates for all parameters. You can type using following notation. (you may not need to use some of them)

```
## Both models were fitting and adequate,
## but in #8, regression residuals were stationary.
## This indicates Linear Trend + ARMA has no problem fitting/explaining
## the data, and therefore, no need for ARIMA with d=1.
## Model from #6 is my best model.
Fit06b
## Series: D1
## Regression with ARIMA(15,0,15) errors
## Box Cox transformation: lambda= 0
##
## Coefficients:
## Warning in sqrt(diag(x$var.coef)): NaNs produced
##
             ar1
                      ar2
                              ar3
                                       ar4
                                                ar5
                                                          ar6
                                                                   ar7
                   0.7913
                                   0.0028
                                            -0.0316
                                                      -0.0511
##
         -0.4765
                           0.5179
                                                               -0.0146
                                   0.0196
## s.e.
             NaN
                  0.1081
                           0.1210
                                             0.0208
                                                       0.0094
                                                                0.0223
##
             ar8
                      ar9
                              ar10
                                       ar11
                                               ar12
                                                        ar13
                                                                 ar14
                           -0.0240
##
         -0.0411
                  -0.041
                                     0.0006
                                             0.9728
                                                      0.4459
                                                              -0.8184
## s.e.
          0.0207
                      NaN
                            0.0234
                                     0.0195
                                             0.0152
                                                         NaN
                                                               0.1054
                               ma2
##
            ar15
                      ma1
                                         ma3
                                                          ma5
                                                                  ma6
##
         -0.5375
                  0.5869
                           -0.6199
                                     -0.4733
                                              -0.1190
                                                        0.044
                                                               0.0293
## s.e.
          0.1101
                      NaN
                            0.1573
                                      0.1992
                                               0.1041
                                                        0.088
                                                               0.1449
##
                      ma8
                              ma9
                                      ma10
                                               ma11
                                                         ma12
             ma7
                                                                 ma13
##
         -0.1085
                  0.0821
                           0.0420
                                   0.1038
                                            -0.0402
                                                      -0.9426
                                                               -0.577
## s.e.
          0.1027
                   0.1189
                           0.1167
                                   0.1104
                                             0.1028
                                                       0.1050
                                                                  NaN
##
           ma14
                    ma15
                          intercept
                                        xreg
##
         0.5308
                 0.4618
                            -6.7277
                                      0.0068
         0.1523
                 0.1204
                             0.4158
                                     0.0002
##
## sigma^2 estimated as 0.01175: log likelihood=113.56
## AIC=-161.11
                 AICc=-140.33
                                 BIC=-63.57
```

• Mathematical expression:

$$Y_t = \mbox{observation}$$

$$Y_t = a + bt + X_t$$
 X_t is ARIMA(15,0,15)

$$X_{t} = \phi_{1}X_{t-1} + \phi_{1}X_{t-1} + \phi_{2}X_{t-2} + \dots + \phi_{15}X_{t-15} + e_{t} + \theta_{1}e_{t-1} + \dots + \theta_{15}e_{t-15}$$

$$e_{t} \sim WN(0, \sigma^{2})$$

TS Class Webpage – R resource page