

InClass-A3 Sample Analysis

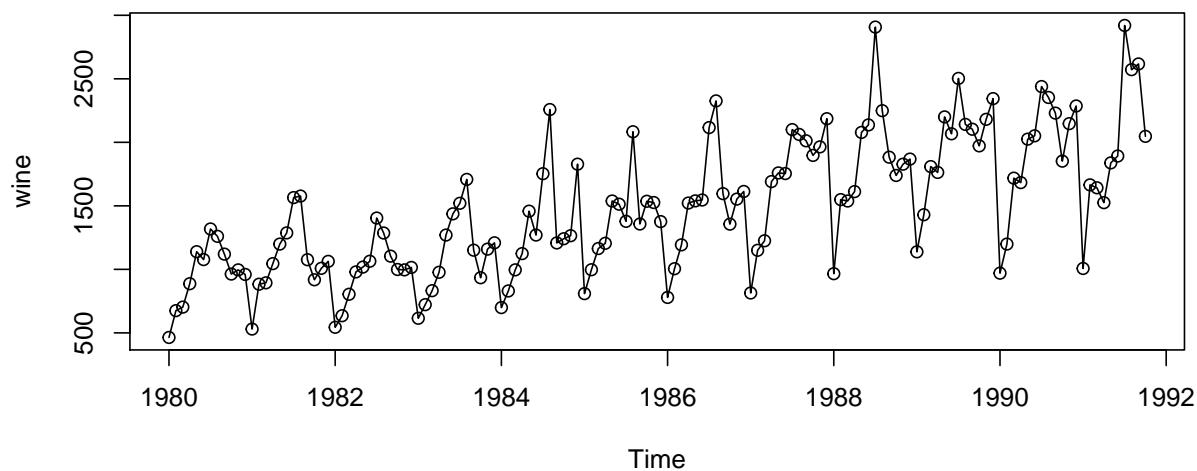
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Here is the code to load the data from the web.

```
source('https://nmimoto.github.io/R/TS-00.txt')

D <- read.csv("https://nmimoto.github.io/datasets/wine.csv")
D1 <- ts(D, start=c(1980,1), freq=12)
plot(D1, type='o')
```



Now your “D1” in R contains monthly wine sales in Australia.

We will take log of the data

1. auto.arima() analysis

```
Fit11 <- auto.arima(D1, lambda=0, stepwise=FALSE, approximation=FALSE)
Fit11
```

```
## Series: D1
## ARIMA(1,0,1)(0,1,1)[12] with drift
## Box Cox transformation: lambda= 0
##
## Coefficients:
##          ar1          ma1          sma1      drift
##          0.8930    -0.6841    -0.7372    0.0062
## s.e.    0.0785     0.1249     0.0951    0.0008
##
## sigma^2 estimated as 0.0125:  log likelihood=97.74
## AIC=-185.48   AICc=-185    BIC=-171.14
```

```
Randomness.tests(Fit11$residuals)
```

```
## B-L test H0: the series is uncorrelated
## M-L test H0: the square of the series is uncorrelated
## J-B test H0: the series came from Normal distribution
## SD          : Standard Deviation of the series
```

```
##          BL15  BL20  BL25  ML15  ML20    JB    SD
## [1,] 0.573 0.832 0.933 0.705 0.789 0.182 0.106
```

```
## ARIMA(1,0,1)x(0,1,1)[12] is suggested.
## Residual analysis shows adequacy by both L-B test and M-L test.
##
## Errors (after the log) seems to be normally distributed, and
## J-B test confirms that. (p-value > .05)
##
## We must investigate the choice of d, D, and drift
```

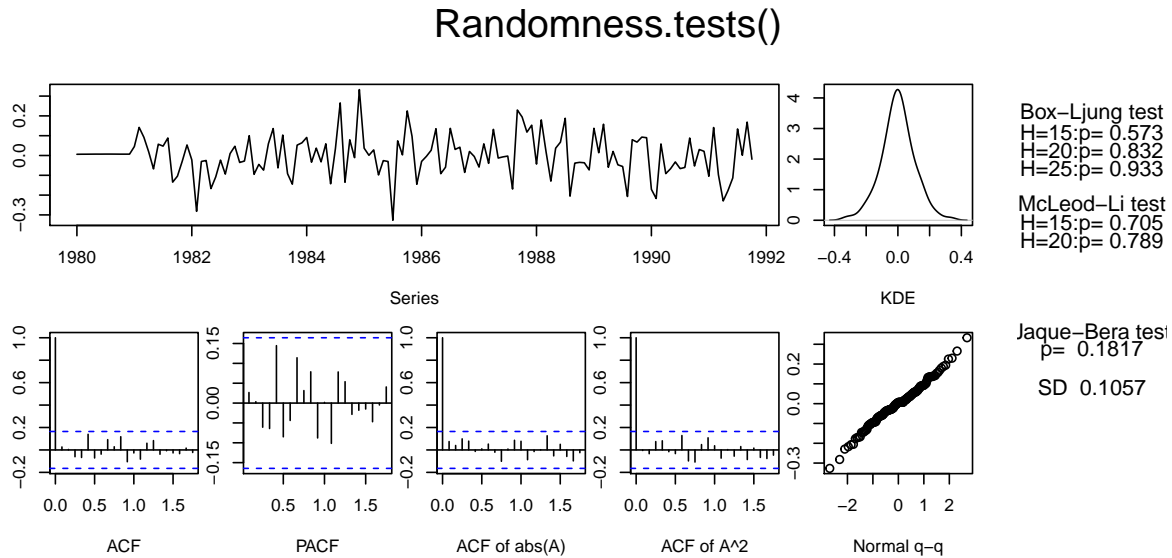
```
# Include drift
```

```
Fit12 <- Arima(D1, lambda=0, order=c(1,0,1), seasonal=c(0,1,1), include.drift=TRUE)
Fit12
```

```
## Series: D1
## ARIMA(1,0,1)(0,1,1)[12] with drift
## Box Cox transformation: lambda= 0
##
## Coefficients:
##          ar1          ma1          sma1      drift
##          0.8930    -0.6841    -0.7372    0.0062
## s.e.    0.0785     0.1249     0.0951    0.0008
```

```
##
## sigma^2 estimated as 0.0125: log likelihood=97.74
## AIC=-185.48 AICc=-185 BIC=-171.14
```

```
Randomness.tests(Fit12$residuals)
```

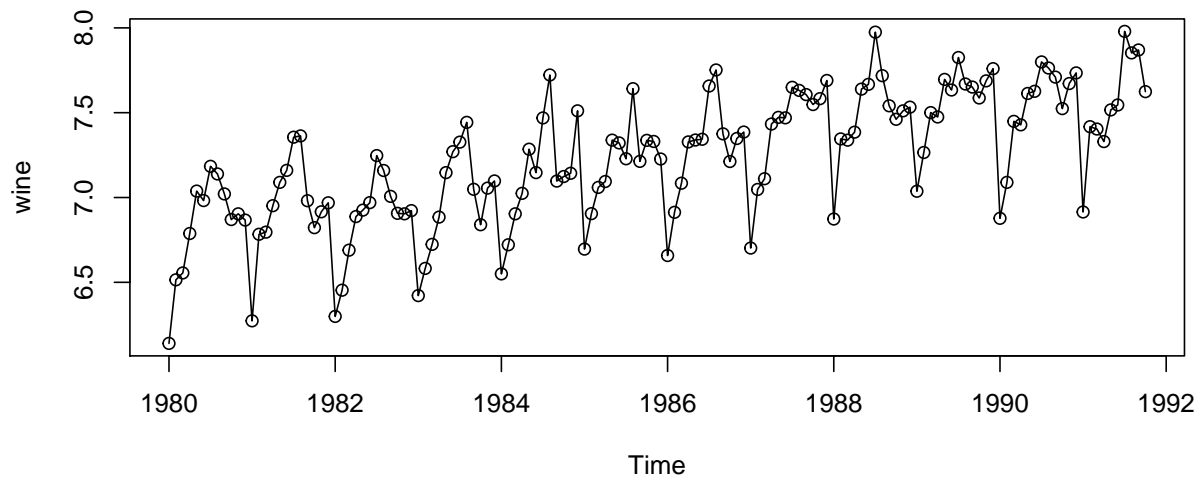


```
## B-L test H0: the series is uncorrelated
## M-L test H0: the square of the series is uncorrelated
## J-B test H0: the series came from Normal distribution
## SD : Standard Deviation of the series
```

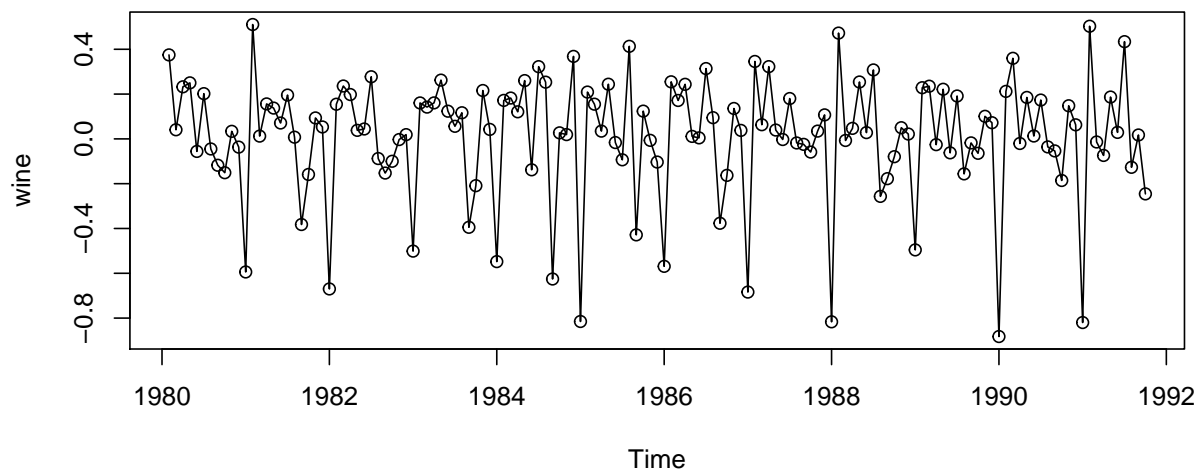
```
## BL15 BL20 BL25 ML15 ML20 JB SD
## [1,] 0.573 0.832 0.933 0.705 0.789 0.182 0.106
```

2. Preliminary Analysis

```
plot( log(D1), type='o')
```



```
plot( diff(log(D1)), type='o') # d=1
```



Stationarity Check

```
Stationarity.tests( diff(log(D1)))
```

```
## Warning in adf.test(A): p-value smaller than printed p-value
```

```
## Warning in pp.test(A): p-value smaller than printed p-value
```

```
## Warning in kpss.test(A): p-value greater than printed p-value
```

```
##          KPSS  ADF  PP  
## p-val:  0.1 0.01 0.01
```

```
Stationarity.tests( diff(log(D1, 12)))
```

```
## Warning in adf.test(A): p-value smaller than printed p-value
```

```
## Warning in pp.test(A): p-value smaller than printed p-value
```

```
## Warning in kpss.test(A): p-value greater than printed p-value
```

```
##          KPSS  ADF  PP  
## p-val:  0.1 0.01 0.01
```

```
## d=1 alone makes it stationary
```

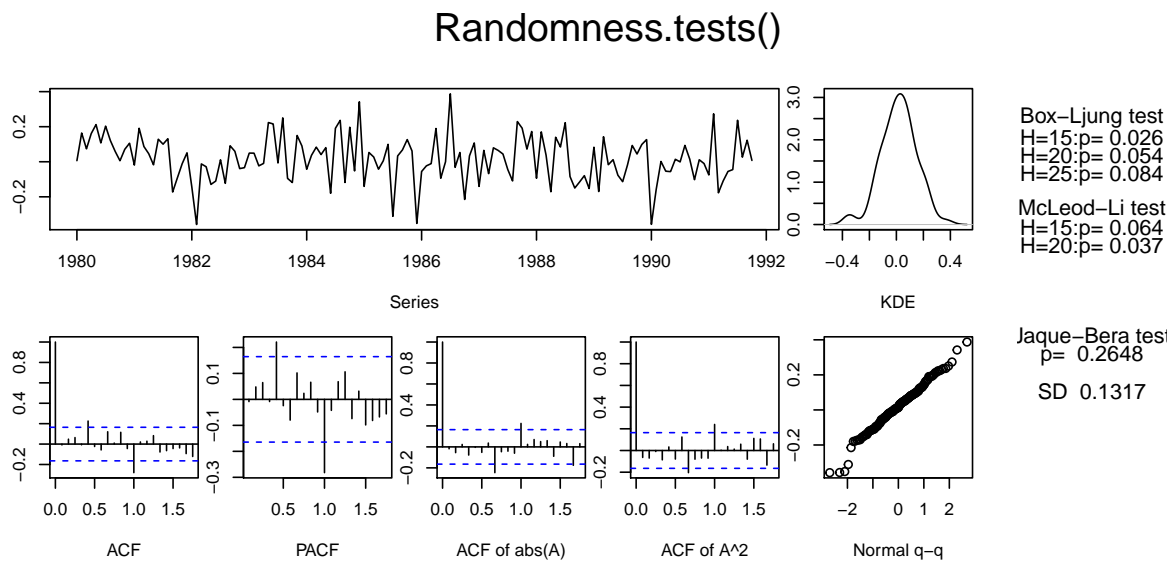
```
## D=1 alone makes it stationary
```

3. Difference only (d=1 D=0) model

```
Fit21 <- auto.arima(D1, d=1, D=0, lambda=0, stepwise=FALSE, approximation=FALSE)
Fit21
```

```
## Series: D1
## ARIMA(1,1,1)(1,0,0)[12]
## Box Cox transformation: lambda= 0
##
## Coefficients:
##          ar1      ma1      sar1
##      0.3604 -0.9522  0.8555
## s.e.  0.0876  0.0272  0.0395
##
## sigma^2 estimated as 0.01807:  log likelihood=76.3
## AIC=-144.6   AICc=-144.31   BIC=-132.81
```

```
Randomness.tests(Fit21$resid)
```



```
## B-L test H0: the series is uncorrelated
## M-L test H0: the square of the series is uncorrelated
## J-B test H0: the series came from Normal distribution
## SD : Standard Deviation of the series
```

```
## BL15 BL20 BL25 ML15 ML20 JB SD
## [1,] 0.026 0.054 0.084 0.064 0.037 0.265 0.132
```

```
## Arima(1,1,1)x(1,0,0)[12] suggested
## Residual does not show adequate fit. Large ACF at lag 12.
##
```

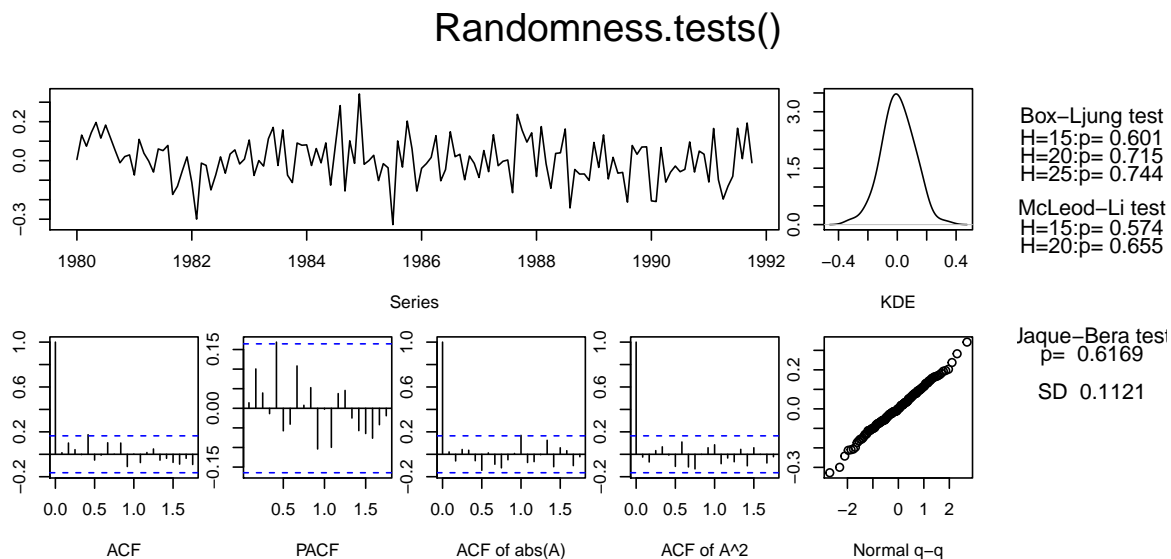
```
# Fit21b <- Arima(D1, lambda=0, order=c(1,1,1), seasonal=c(2,0,0))
# Fit21b
# Randomness.tests(Fit21b$resid)
```

```
## Estimation problem
```

```
Fit21c <- Arima(D1, lambda=0, order=c(1,1,1), seasonal=c(1,0,1))
Fit21c
```

```
## Series: D1
## ARIMA(1,1,1)(1,0,1)[12]
## Box Cox transformation: lambda= 0
##
## Coefficients:
##          ar1          ma1          sar1          sma1
##      0.1699   -0.8586   0.9924   -0.7314
## s.e.  0.1157   0.0683   0.0066   0.0999
##
## sigma^2 estimated as 0.01296:  log likelihood=93.67
## AIC=-177.34   AICc=-176.9   BIC=-162.6
```

```
Randomness.tests(Fit21c$resid)
```



```
## B-L test H0: the series is uncorrelated
## M-L test H0: the square of the series is uncorrelated
## J-B test H0: the series came from Normal distribution
## SD : Standard Deviation of the series
```

```
## BL15 BL20 BL25 ML15 ML20 JB SD
## [1,] 0.601 0.715 0.744 0.574 0.655 0.617 0.112
```

```
## Residual shows adequate fit.
```

```
Fit21d <- Arima(D1, lambda=0, order=c(1,1,1), seasonal=c(1,0,1),  
               include.drift=TRUE, method="CSS")  
Fit21d
```

```
## Series: D1  
## ARIMA(1,1,1)(1,0,1)[12] with drift  
## Box Cox transformation: lambda= 0  
##  
## Coefficients:  
##          ar1          ma1          sar1          sma1          drift  
##      -0.0006   -0.7195   0.9755   -0.6522   -0.0391  
## s.e.    0.1046    0.0689   0.0170    0.0803    0.0593  
##  
## sigma^2 estimated as 0.01345:  part log likelihood=99.44
```

```
## If method="CSS-MLE" (default) then gives error.  
## with CSS, drift not significant.
```

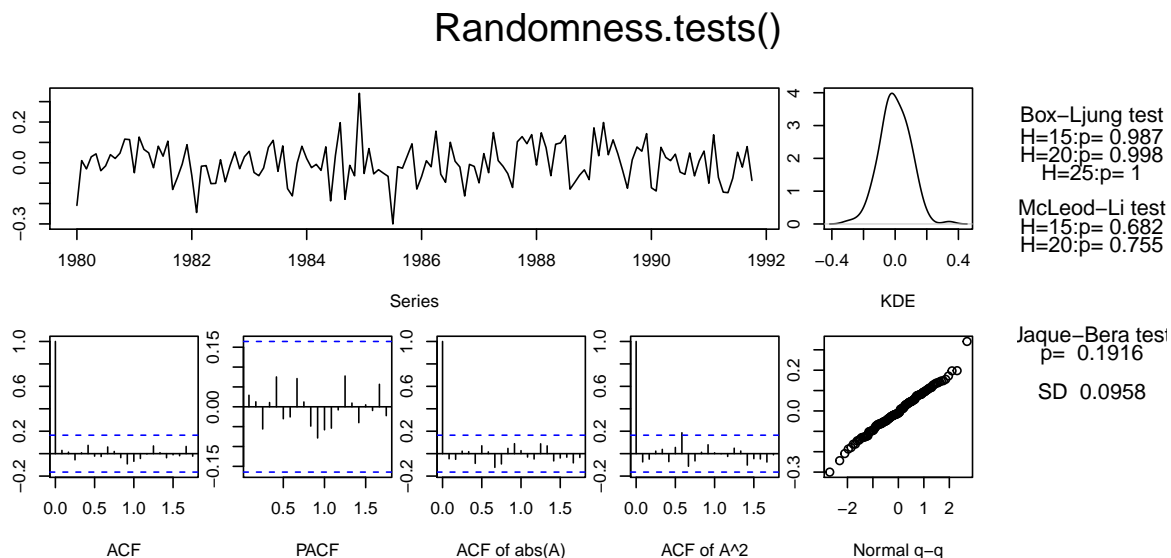

4. Linear Trend Model

From A3

```
Fit <- Arima(D1, lambda=0, xreg=time(D1), order=c(15,0,15))
Fit
```

```
## Series: D1
## Regression with ARIMA(15,0,15) errors
## Box Cox transformation: lambda= 0
##
## Coefficients:
##      ar1      ar2      ar3      ar4      ar5      ar6      ar7
##      -0.4723  0.7913  0.5113  0.0027 -0.0318 -0.0503 -0.0142
## s.e.    0.3530  0.0957  0.2695  0.0191  0.0199  0.0178  0.0280
##      ar8      ar9      ar10     ar11     ar12     ar13     ar14
##      -0.0407 -0.0407 -0.0241  0.0006  0.9731  0.4417 -0.8183
## s.e.    0.0204  0.0200  0.0232  0.0189  0.0151  0.3394  0.1029
##      ar15     ma1      ma2      ma3      ma4      ma5      ma6
##      -0.5307  0.5832 -0.6181 -0.4634 -0.1164  0.0422  0.0239
## s.e.    0.2802  0.3259  0.1441  0.2274  0.1003  0.1085  0.1560
##      ma7      ma8      ma9      ma10     ma11     ma12     ma13
##      -0.1091  0.0861  0.0428  0.1037 -0.0420 -0.9408 -0.5722
## s.e.    0.1015  0.1174  0.1072  0.1052  0.0945  0.1757  0.2920
##      ma14     ma15 intercept  xreg
##      0.5252  0.4557 -154.8316  0.0816
## s.e.    0.1807  0.2074   5.2452  0.0026
##
## sigma^2 estimated as 0.01176:  log likelihood=113.56
## AIC=-161.11  AICc=-140.34  BIC=-63.57
```

```
Randomness.tests(Fit$resid)
```



```
## B-L test H0: the series is uncorrelated
## M-L test H0: the square of the series is uncorrelated
## J-B test H0: the series came from Normal distribution
## SD : Standard Deviation of the series

## BL15 BL20 BL25 ML15 ML20 JB SD
## [1,] 0.987 0.998 1 0.682 0.755 0.192 0.096
```

Seasonal ARMA

```
Fit51 <- auto.arima(D1, d=0, D=0, lambda=0, xreg=time(D1),
                    stepwise=FALSE, approximation=FALSE)
Fit51
```

```
## Series: D1
## Regression with ARIMA(1,0,0)(1,0,0)[12] errors
## Box Cox transformation: lambda= 0
##
## Coefficients:
##          ar1      sar1  intercept      xreg
##          0.3660  0.8393  -134.4431  0.0713
## s.e.      0.0784  0.0410   25.8403  0.0130
##
## sigma^2 estimated as 0.01749: log likelihood=80.41
## AIC=-150.82 AICc=-150.38 BIC=-136.05
```

```
Randomness.tests(Fit51$resid)
```

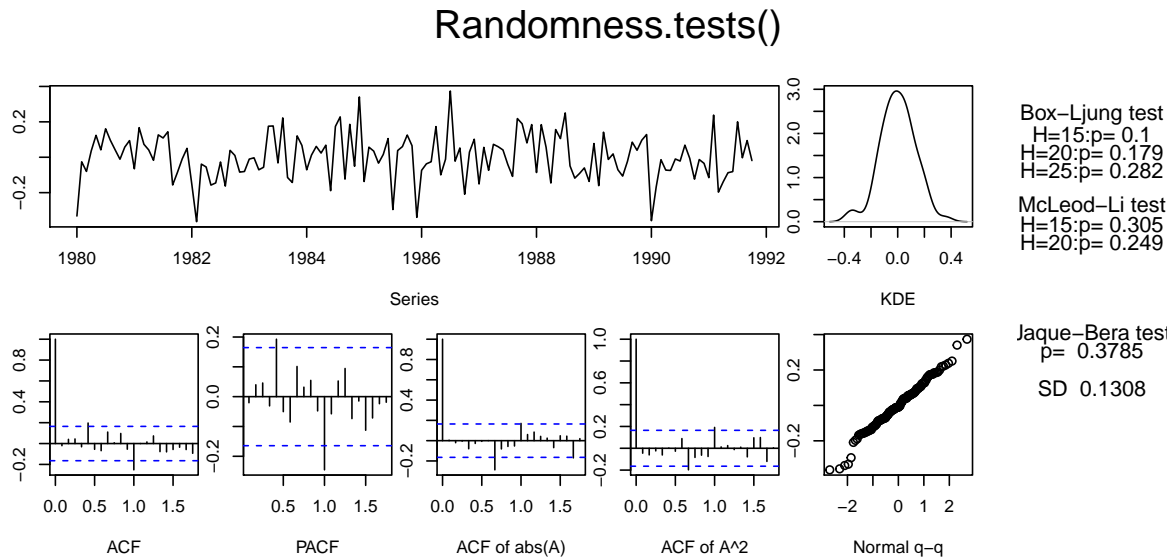
```
## B-L test H0: the series is uncorrelated
## M-L test H0: the square of the series is uncorrelated
## J-B test H0: the series came from Normal distribution
## SD : Standard Deviation of the series

## BL15 BL20 BL25 ML15 ML20 JB SD
## [1,] 0.1 0.179 0.282 0.305 0.249 0.378 0.131
```

```
Fit52 <- Arima(D1, lambda=0, xreg=time(D1), order=c(1,0,0), seasonal=c(1,0,1))
Fit52
```

```
## Series: D1
## Regression with ARIMA(1,0,0)(1,0,1)[12] errors
## Box Cox transformation: lambda= 0
##
## Coefficients:
##          ar1      sar1      sma1  intercept      xreg
##          0.3549  0.9881  -0.7033  -140.8826  0.0746
## s.e.      0.0786  0.0108   0.1202   12.0115  0.0060
##
## sigma^2 estimated as 0.01342: log likelihood=94.77
## AIC=-177.54 AICc=-176.92 BIC=-159.81
```

```
Randomness.tests(Fit51$resid)
```



```
## B-L test H0: the series is uncorrelated
## M-L test H0: the square of the series is uncorrelated
## J-B test H0: the series came from Normal distribution
## SD : Standard Deviation of the series
```

```
## BL15 BL20 BL25 ML15 ML20 JB SD
## [1,] 0.1 0.179 0.282 0.305 0.249 0.378 0.131
```

```
Fit52 <- Arima(D1, lambda=0, xreg=time(D1), order=c(1,0,0), seasonal=c(2,0,2))
Fit52
```

```
## Series: D1
## Regression with ARIMA(1,0,0)(2,0,2)[12] errors
## Box Cox transformation: lambda= 0
##
## Coefficients:
##      ar1      sar1      sar2      sma1      sma2  intercept      xreg
##      0.3498  0.1027  0.8803  0.2497 -0.7501 -142.2997  0.0753
## s.e.  0.0789  0.0815  0.0763  0.2168  0.1810   11.1703  0.0056
##
## sigma^2 estimated as 0.01276: log likelihood=95.72
## AIC=-175.45 AICc=-174.36 BIC=-151.8
```

```
Randomness.tests(Fit51$resid)
```

```
## B-L test H0: the series is uncorrelated
## M-L test H0: the square of the series is uncorrelated
## J-B test H0: the series came from Normal distribution
## SD : Standard Deviation of the series
```

```
##      BL15 BL20 BL25 ML15 ML20 JB SD
## [1,] 0.1 0.179 0.282 0.305 0.249 0.378 0.131
```

```
Fit52 <- Arima(D1, lambda=0, xreg=time(D1), order=c(1,0,0), seasonal=c(3,0,3))
Fit52
```

```
## Series: D1
## Regression with ARIMA(1,0,0)(3,0,3)[12] errors
## Box Cox transformation: lambda= 0
##
## Coefficients:
```

```
## Warning in sqrt(diag(x$var.coef)): NaNs produced
```

```
##      ar1      sar1      sar2      sar3      sma1      sma2      sma3
##      0.3567  1.1329 -0.1353  0.0007 -0.8441  0.0264 -0.0790
## s.e.      NaN  0.1468  0.1624  0.0157  0.0531  0.1667  0.1601
##      intercept      xreg
##      -140.4321  0.0744
## s.e.      10.9536  0.0055
##
## sigma^2 estimated as 0.01299: log likelihood=96.14
## AIC=-172.28 AICc=-170.6 BIC=-142.72
```

```
Randomness.tests(Fit51$resid)
```

```
## B-L test H0: the series is uncorrelated
## M-L test H0: the square of the series is uncorrelated
## J-B test H0: the series came from Normal distribution
## SD : Standard Deviation of the series
```

```
##      BL15 BL20 BL25 ML15 ML20 JB SD
## [1,] 0.1 0.179 0.282 0.305 0.249 0.378 0.131
```

```
Fit52 <- Arima(D1, lambda=0, xreg=time(D1), order=c(5,0,4), seasonal=c(1,0,1))
Fit52
```

```
## Series: D1
## Regression with ARIMA(5,0,4)(1,0,1)[12] errors
## Box Cox transformation: lambda= 0
##
## Coefficients:
##      ar1      ar2      ar3      ar4      ar5      ma1      ma2
##      0.0386 -0.5063 -0.2393  0.2270  0.2628  0.2256  0.8071
## s.e.  0.5987  0.2435  0.3111  0.4598  0.2308  0.6415  0.3719
##      ma3      ma4      sar1      sma1 intercept      xreg
##      0.5866  0.0294  0.9889 -0.6661 -140.7492  0.0745
## s.e.  0.4659  0.5931  0.0093  0.1190  16.3265  0.0082
##
## sigma^2 estimated as 0.01222: log likelihood=102.23
## AIC=-176.46 AICc=-173.15 BIC=-135.08
```

```
Randomness.tests(Fit51$resid)
```

```
## B-L test H0: the series is uncorrelated
## M-L test H0: the square of the series is uncorrelated
## J-B test H0: the series came from Normal distribution
## SD : Standard Deviation of the series

## BL15 BL20 BL25 ML15 ML20 JB SD
## [1,] 0.1 0.179 0.282 0.305 0.249 0.378 0.131
```

```
Fit52 <- Arima(D1, lambda=0, xreg=time(D1), order=c(0,0,0), seasonal=c(0,0,0))
Fit52
```

```
## Series: D1
## Regression with ARIMA(0,0,0) errors
## Box Cox transformation: lambda= 0
##
## Coefficients:
##      intercept      xreg
##      -150.3167   0.0793
## s.e.    13.0042   0.0065
##
## sigma^2 estimated as 0.07206: log likelihood=-13.74
## AIC=33.48 AICc=33.65 BIC=42.34
```

```
Randomness.tests(Fit51$resid)
```

```
## B-L test H0: the series is uncorrelated
## M-L test H0: the square of the series is uncorrelated
## J-B test H0: the series came from Normal distribution
## SD : Standard Deviation of the series

## BL15 BL20 BL25 ML15 ML20 JB SD
## [1,] 0.1 0.179 0.282 0.305 0.249 0.378 0.131
```

```
Fit52 <- Arima(D1, lambda=0, xreg=time(D1), order=c(1,0,0), seasonal=c(3,0,0))
Fit52
```

```
## Series: D1
## Regression with ARIMA(1,0,0)(3,0,0)[12] errors
## Box Cox transformation: lambda= 0
##
## Coefficients:
##      ar1      sar1      sar2      sar3 intercept      xreg
##      0.3607  0.4517  0.2502  0.2198  -133.2316  0.0707
## s.e.   0.0782  0.0847  0.0951  0.0910   17.9158  0.0090
##
## sigma^2 estimated as 0.01446: log likelihood=92.27
## AIC=-170.53 AICc=-169.7 BIC=-149.84
```

```
Randomness.tests(Fit51$resid)
```

```
## B-L test H0: the series is uncorrelated
## M-L test H0: the square of the series is uncorrelated
## J-B test H0: the series came from Normal distribution
## SD : Standard Deviation of the series
```

```
## BL15 BL20 BL25 ML15 ML20 JB SD
## [1,] 0.1 0.179 0.282 0.305 0.249 0.378 0.131
```

```
Fit52 <- Arima(D1, lambda=0, xreg=time(D1), order=c(1,0,1), seasonal=c(3,0,1))
Fit52
```

```
## Series: D1
## Regression with ARIMA(1,0,1)(3,0,1)[12] errors
## Box Cox transformation: lambda= 0
##
## Coefficients:
## ar1 ma1 sar1 sar2 sar3 sma1 intercept
## 0.7749 -0.5039 1.1739 -0.0402 -0.1341 -0.9482 -139.8386
## s.e. 0.1373 0.1935 0.1142 0.1423 0.1098 0.1546 13.9300
## xreg
## 0.0741
## s.e. 0.0070
##
## sigma^2 estimated as 0.01207: log likelihood=98.44
## AIC=-178.87 AICc=-177.51 BIC=-152.27
```

```
Randomness.tests(Fit51$resid)
```

```
## B-L test H0: the series is uncorrelated
## M-L test H0: the square of the series is uncorrelated
## J-B test H0: the series came from Normal distribution
## SD : Standard Deviation of the series
```

```
## BL15 BL20 BL25 ML15 ML20 JB SD
## [1,] 0.1 0.179 0.282 0.305 0.249 0.378 0.131
```

```
# Skip some parameters (Phis, Thetas, icpt, xreg)
Fit <- Arima(D1, lambda=0, xreg=time(D1), order=c(15,0,15),
            fixed=c(NA,NA,NA,NA,NA,NA,NA,NA,NA,NA,NA,NA,NA,NA,NA,
                    NA,NA,NA,NA,NA,NA,NA,NA,NA,NA,NA,NA,NA,NA,NA,
                    NA,NA ) )
```

```
Fit
Randomness.tests(Fit$resid)
```

```
# Skip some parameters (Phis, Thetas, icpt, xreg)
Fit <- Arima(D1, lambda=0, xreg=time(D1), order=c(15,0,15), method="CSS",
            fixed=c(NA,NA,NA,NA,NA,NA,NA,NA,NA,NA, 0,NA,NA,NA,NA,
                    NA,NA,NA,NA,NA,NA,NA,NA,NA, 0, 0,NA,NA,NA,NA,
```

```

NA,NA ) )

Fit
Randomness.tests(Fit$resid)

# Skip some parameters (Phis, Thetas, icpt, xreg)
Fit <- Arima(D1, lambda=0, xreg=time(D1), order=c(15,0,14), method="CSS"),
      fixed=c(NA,NA,NA,NA,NA, NA,NA,NA, 0, 0, 0,NA,NA,NA,NA,
              NA, 0,NA, 0,NA, NA,NA,NA, 0, 0, 0,NA,NA,NA,
              NA,NA ) )

Fit
Randomness.tests(Fit$resid)

# Skip some parameters (Phis, Thetas, icpt, xreg)
Fit <- Arima(D1, lambda=0, xreg=time(D1), order=c(15,0,14), method="CSS"),
      fixed=c(NA, 0,NA,NA,NA, NA,NA, 0, 0, 0, 0,NA,NA,NA,NA,
              NA, 0,NA, 0,NA, 0,NA, 0, 0, 0, 0,NA,NA,NA,
              NA,NA ) )

Fit
Randomness.tests(Fit$resid)

# Skip some parameters (Phis, Thetas, icpt, xreg)
Fit <- Arima(D1, lambda=0, xreg=time(D1), order=c(15,0,13), method="CSS"),
      fixed=c(NA, 0,NA,NA,NA, NA,NA, 0, 0, 0, 0,NA,NA,NA,NA,
              NA, 0,NA, 0,NA, 0,NA, 0, 0, 0, 0,NA,NA,
              NA,NA ) )

Fit
Randomness.tests(Fit$resid)

# Skip some parameters (Phis, Thetas, icpt, xreg)
Fit <- Arima(D1, lambda=0, xreg=time(D1), order=c(15,0,12), method="CSS"),
      fixed=c(NA, 0,NA,NA,NA, NA,NA, 0, 0, 0, 0,NA,NA,NA,NA,
              NA, 0,NA, 0,NA, 0,NA, 0, 0, 0, 0,NA,
              NA,NA ) )

Fit
Randomness.tests(Fit$resid)

# Skip some parameters (Phis, Thetas, icpt, xreg)
Fit <- Arima(D1, lambda=0, xreg=time(D1), order=c(15,0,12),
      fixed=c(NA, 0,NA,NA,NA, NA,NA, 0, 0, 0, 0,NA,NA,NA,NA,
              NA, 0,NA, 0,NA, 0,NA, 0, 0, 0, 0,NA,
              NA,NA ) )

Fit
Randomness.tests(Fit$resid)

```

```
# Skip some parameters (Phis, Thetas, icpt, xreg)
Fit <- Arima(D1, lambda=0, xreg=time(D1), order=c(15,0,15))
Fit
Randomness.tests(Fit$resid)

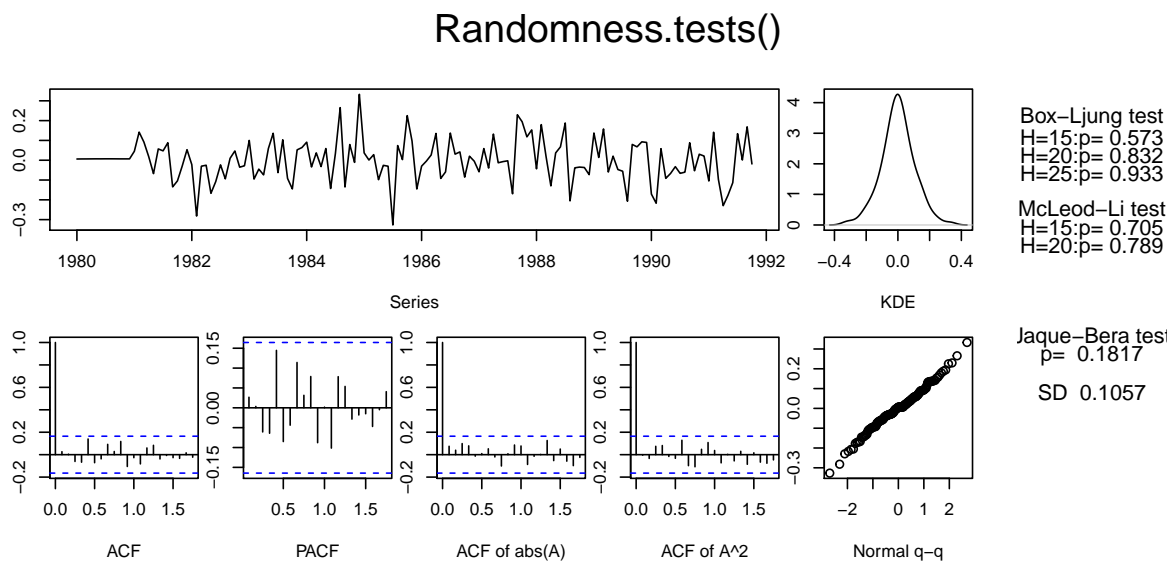
# Skip some parameters (Phis, Thetas, icpt, xreg)
Fit <- Arima(D1, lambda=0, xreg=time(D1), order=c(14,0,14))
Fit
Randomness.tests(Fit$resid)
```


5. Rolling 1-step with D=1 model

Fit12

```
## Series: D1
## ARIMA(1,0,1)(0,1,1)[12] with drift
## Box Cox transformation: lambda= 0
##
## Coefficients:
##          ar1          ma1          sma1      drift
##          0.8930   -0.6841   -0.7372   0.0062
## s.e.    0.0785    0.1249    0.0951   0.0008
##
## sigma^2 estimated as 0.0125:  log likelihood=97.74
## AIC=-185.48   AICc=-185    BIC=-171.14
```

Randomness.tests(Fit12\$resid)



```
## B-L test H0: the series is uncorrelated
## M-L test H0: the square of the series is uncorrelated
## J-B test H0: the series came from Normal distribution
## SD : Standard Deviation of the series
```

```
## BL15 BL20 BL25 ML15 ML20 JB SD
## [1,] 0.573 0.832 0.933 0.705 0.789 0.182 0.106
```

Arima(1,0,1)x(0,1,1)[12] w drift

```

#- Set options
Y <- D1                                # Original data
window.size <- 100                     # Window size for estimation
Arima.order <- c(1,0,1)               # Arima(p,d,q) order
pred.plot   <- TRUE                    # do you want plot at end?

#- set Arima() options:
include.mean = TRUE                    #
include.drift = TRUE                   #
lambda       = 0                       # NULL=no transformon. 0=Log
xreg         = NULL                    # NULL=no xreg. TRUE=Linear Trend is present
seasonal     = c(0, 1, 1)              # seasonal component

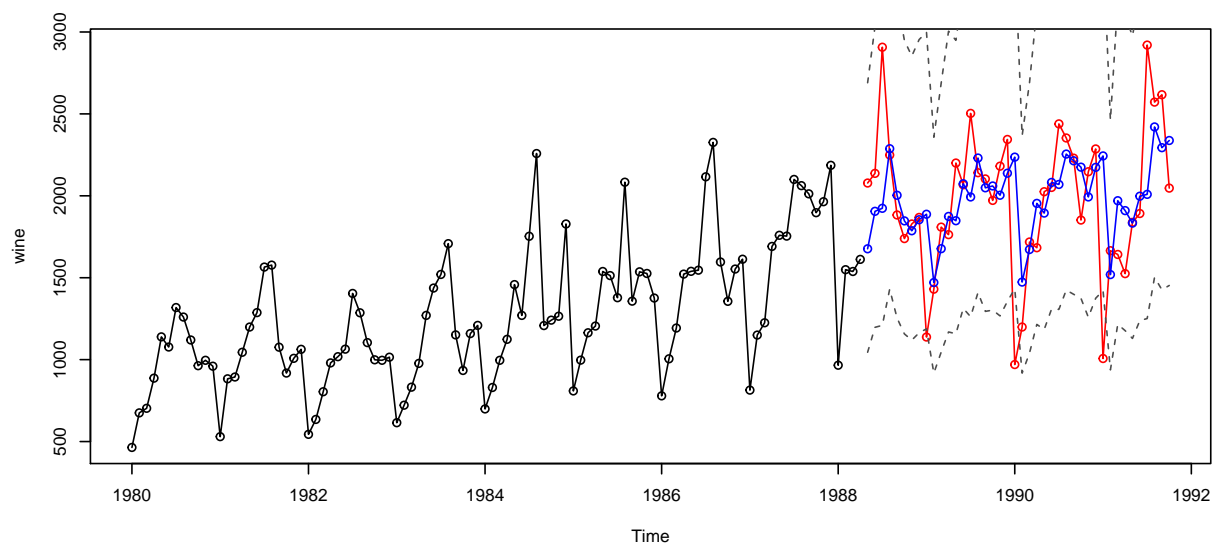
#- then use the function
Rolling1step.forecast(Y, window.size, Arima.order, pred.plot,
                      include.mean, include.drift, lambda, xreg, seasonal)

```

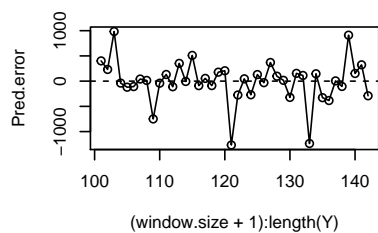
```

##
## Last 42 obs fit retrospectively
## with Rolling 1-step prediction
## Average prediction error: -7.055
## root Mean Squared Error: 413.9975

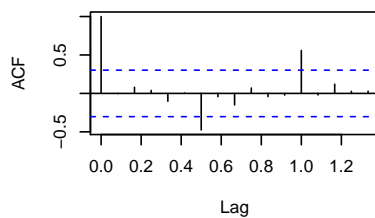
```



Prediction Error (Red-Blue)



Y2



```
##      mean pred error      rMSE
## [1,]          -7.055 413.9975
```

TS Class Webpage – R resource page