

# **Machine Learning**

Noel Moreno Lemus, Ph.D.



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# Introduction

## Work in Progress

This is a Work in Progress project. The idea is to summarize all ML topics and how I see and understand them.

Machine learning is a rapidly growing field that enables computers to learn from data, without being explicitly programmed. The goal of machine learning is to build models that can make predictions or take actions based on input data, and improve their performance over time through experience.

## Note

Note that there are five types of callouts, including: **note**, **warning**, **important**, **tip**, and **caution**.

## Tip With Caption

This is an example of a callout with a caption.

## Expand To Learn About Collapse

This is an example of a ‘folded’ caution callout that can be expanded by the user. You can use `collapse="true"` to collapse it by default or `collapse="false"` to make a collapsible callout that is expanded

by default.

## **Overview of Machine Learning:**

Machine learning is a subfield of artificial intelligence that involves the development of algorithms and statistical models that allow computers to learn from data. There are three main types of machine learning: supervised learning, unsupervised learning, and reinforcement learning.

Supervised learning is the most common type of machine learning, in which a model is trained on a labeled dataset to make predictions about new, unseen data. Examples include linear regression, logistic regression, and decision trees.

Unsupervised learning involves discovering patterns in unlabeled data, such as clustering and dimensionality reduction.

Reinforcement learning involves training an agent to make decisions in an environment to maximize a reward.

## **Applications of Machine Learning**

Machine learning has many applications in various industries, including:

- Healthcare: for example, identifying potential health risks, diagnosing diseases, and creating personalized treatment plans
- Finance: for example, detecting fraudulent transactions, predicting stock prices, and identifying potential investment opportunities
- Retail: for example, personalizing product recommendations, optimizing pricing strategies, and improving supply chain efficiency
- Manufacturing: for example, predictive maintenance, quality control, and optimization of production processes



## *Key Concepts and Terminology*

- Transportation: for example, traffic prediction, autonomous driving, and fleet management
- Cybersecurity: for example, intrusion detection, anomaly detection, and threat intelligence

## **Key Concepts and Terminology**

Machine learning is a complex field with many technical terms and concepts. Some key terms and concepts that will be covered in this book include:

- Model: a representation of the relationships between input data and output predictions or actions
- Training: the process of fitting a model to a dataset
- Testing: the process of evaluating a model on new, unseen data
- Overfitting: when a model is too complex and performs well on the training data but poorly on the test data
- Regularization: a technique for preventing overfitting by adding a penalty term to the model's objective function
- Gradient descent: an optimization algorithm for finding the minimum of a function
- Neural networks: a type of model that is inspired by the structure and function of the human brain
- Convolutional neural networks (CNNs): a type of neural network designed for image recognition
- Recurrent neural networks (RNNs): a type of neural network designed for sequential data such as time series and natural language.

## Versions Used in this Book

```
import sys
print("Python version: {}".format(sys.version))
import pandas as pd
print("pandas version: {}".format(pd.__version__))
import matplotlib
print("matplotlib version: {}".format(matplotlib.__version__))
import numpy as np
print("NumPy version: {}".format(np.__version__))
import scipy as sp
print("SciPy version: {}".format(sp.__version__))
import IPython
print("IPython version: {}".format(IPython.__version__))
import sklearn
print("scikit-learn version: {}".format(sklearn.__version__))
```

```
Python version: 3.9.2 (default, Feb 28 2021, 17:03:44)
[GCC 10.2.1 20210110]
pandas version: 1.5.2
matplotlib version: 3.6.3
NumPy version: 1.24.1
SciPy version: 1.10.0
IPython version: 8.8.0
```

```
scikit-learn version: 1.2.0
```

**Part I.**

**Fundamentals**



# 1. Fundamentals of Machine Learning

## 1.1. Probability and Statistics

### 1.1.1. Introduction to Probability

#### 1.1.1.1. Definition of probability

Probability is a measure of the likelihood of an event occurring. It is a value between 0 and 1, where 0 indicates that an event will never occur and 1 indicates that an event will always occur.

Probability can be defined in different ways, but one of the most common ways is through the use of relative frequency. If we repeat an experiment many times and count the number of times an event of interest occurs, we can calculate the probability of that event as the ratio of the number of successful outcomes to the total number of trials. For example, if we flip a coin 10 times and it comes up heads 6 times, we can say that the probability of getting heads is  $6/10$  or 0.6.

Probability can also be defined through the use of theoretical models. For example, in the coin flipping example, we can assume that the coin is fair and that the probability of getting heads is 0.5.

Probability can be applied to many different types of events and situations, such as in gambling, finance, weather forecasting, medical diagnosis,

## 1. *Fundamentals of Machine Learning*

and many more. In machine learning, probability is used to model the uncertainty of predictions, estimate model parameters and evaluate model performance.

### 1.1.1.2. **Random variables and events**

A random variable is a variable that takes on different values based on the outcome of a random experiment. The values of a random variable can be numerical or categorical, and the probability of each value is defined by a probability distribution.

For example, in a coin-tossing experiment, the random variable  $X$  can take on the values of “heads” or “tails”. The probability of getting heads is 0.5, and the probability of getting tails is also 0.5. We can represent the probability distribution of  $X$  in a table or a graph.

An event is a set of outcomes from a random experiment. For example, in a coin-tossing experiment, the event “getting heads” is the set {heads}, and the event “getting tails” is the set {tails}.

A random variable is said to be discrete if it can take on only a countable number of values and continuous if it can take on any value in an interval.

For example, in a dice-rolling experiment, the random variable  $X$  can take on the values 1, 2, 3, 4, 5, or 6.  $X$  is a discrete random variable.

On the other hand, in a temperature measurement experiment, the random variable  $X$  can take on any value between -273.15 and infinity (the absolute zero and the maximum temperature).  $X$  is a continuous random variable.

In machine learning, random variables are used to represent the input and output of a model, the parameters of a model and the noise in the data. Understanding the properties of random variables and the events they can generate is important to design and analyze machine learning algorithms.

*1.2. Linear Algebra*

**1.1.1.3. Sample space and event space**

**1.1.1.4. Axioms of probability**

**1.2. Linear Algebra**

**1.3. Optimization**

**1.4. Data Preprocessing and Feature Engineering**





**Part II.**

**Optimization**



Optimization can mean different things. Mathematically speaking, it is possible to write an optimization problem in the form of:

$$\min_{x \in R^n} f_i(x), (i = 1, 2, \dots, M)$$



**Part III.**

**Supervised Learning**



Supervised learning is a type of machine learning where the model is trained on labeled data, where the desired output is provided for each input. The goal of supervised learning is to learn a mapping from inputs to outputs, so that the model can make predictions on new, unseen data.

Supervised learning can be further divided into two categories: regression and classification. In regression, the output variable is continuous, and the goal is to predict a numerical value. For example, predicting the price of a house based on its square footage. In classification, the output variable is categorical, and the goal is to predict a class label. For example, classifying an email as spam or not spam.

Supervised learning algorithms can be linear or non-linear, parametric or non-parametric, and they can be based on different assumptions and mathematical models. Some examples of supervised learning algorithms are linear regression, logistic regression, decision trees, k-nearest neighbors, and neural networks.

Supervised learning is widely used in many applications, such as image and speech recognition, natural language processing, and predictive modeling. In this section, we will discuss the fundamentals of supervised learning, including the types of problems it can solve, the evaluation metrics used to measure its performance, and the algorithms and techniques used to solve those problems.





## 2. Linear Regression

Linear regression is a statistical method for modeling the relationship between a dependent variable (also known as the response variable) and one or more independent variables (also known as predictor variables). The goal of linear regression is to find the line of best fit (i.e., the line that best represents the relationship between the variables) through a set of data points. The equation of the line of best fit is represented by a linear equation of the form  $y = mx + b$ , where  $y$  is the dependent variable,  $x$  is the independent variable,  $m$  is the slope of the line, and  $b$  is the y-intercept. Linear regression can be used for both simple linear regression (one independent variable) and multiple linear regression (more than one independent variable).

$$Y_i = \beta_0 + \beta_1 \times X_i$$

$$\hat{\beta}_1 = \frac{\sum_{i=1}^n (X_i - \bar{X})(Y_i - \bar{Y})}{\sum_{i=1}^n (X_i - \bar{X})^2}$$

to estimate the intercept  $\beta_0$  we can use the following:

$$\hat{\beta}_0 = \bar{Y} - \hat{\beta}_1 \times \bar{X}$$

## 2. Linear Regression

### 2.1. Learning by Examples

For this example, we will be using salary data from Kaggle. The data consists of two columns, years of experience and the corresponding salary. The data can be downloaded from [here](#).

```
/home/nmlemus/dev/ml/lib/python3.9/site-packages/IPython/core/formatters.py:
```

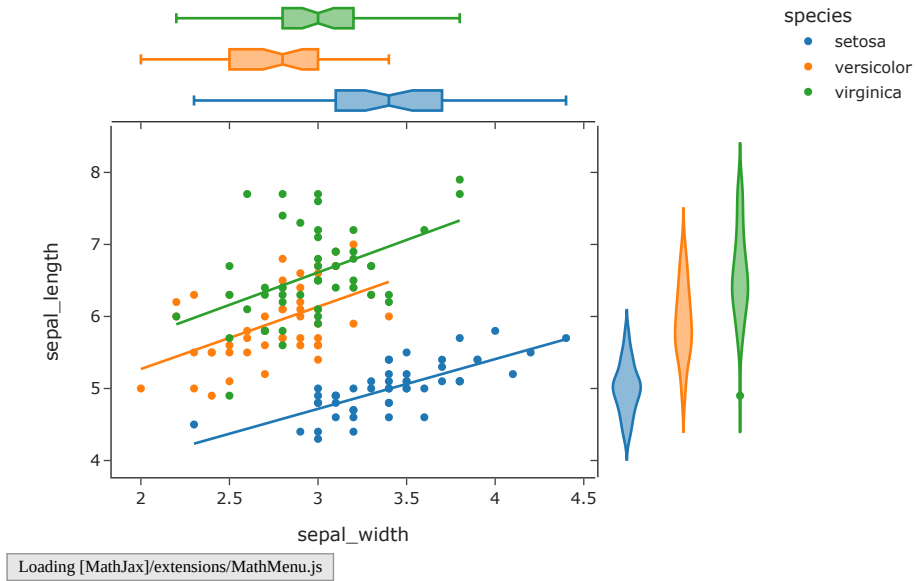
```
In future versions `DataFrame.to_latex` is expected to utilise the base impl
```

	YearsExperience	Salary
0	1.1	39343.0
1	1.3	46205.0
2	1.5	37731.0
3	2.0	43525.0
4	2.2	39891.0

```
import plotly.express as px
import plotly.io as pio
pio.renderers.default = "notebook+pdf"
pio.kaleido.scope.default_format = "png"
df = px.data.iris()
fig = px.scatter(df, x="sepal_width", y="sepal_length",
                 color="species",
                 marginal_y="violin", marginal_x="box",
                 trendline="ols", template="simple_white")
fig.show()
```

```
Unable to display output for mime type(s): text/html
```

## 2.1. Learning by Examples



## 2. Linear Regression

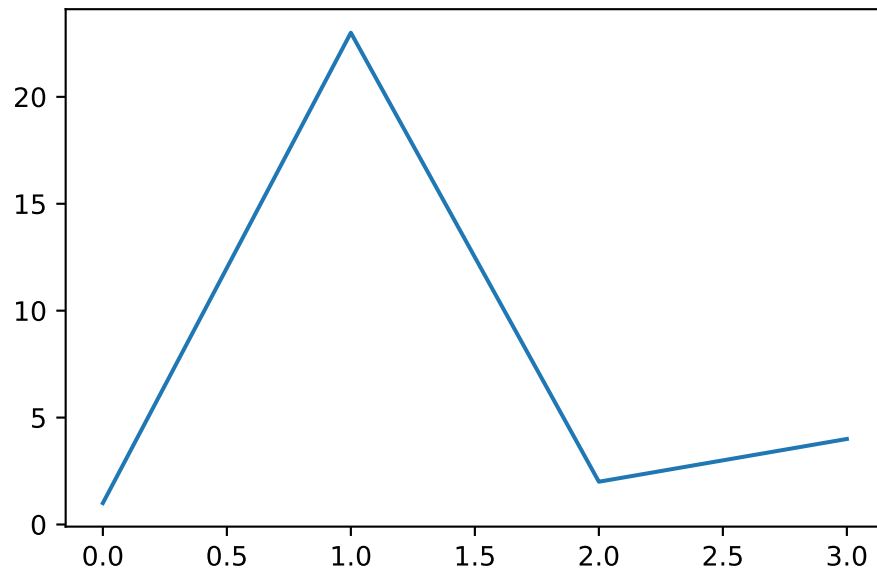


Figure 2.1.: Simple Plot

### **3. Logistic Regression**



## **4. Decision Trees and Random Forests**





## **5. Support Vector Machines**



## **6. Neural Networks**



## **Part IV.**

# **Unsupervised Learning**



## **7. Unsupervised Learning**

### **7.1. Clustering**

### **7.2. Dimensionality Reduction**

### **7.3. Anomaly Detection**





**Part V.**

**Deep Learning**



## **8. Neural Networks and Backpropagation**



## **9. Convolutional Neural Networks (CNNs)**



## **10. Recurrent Neural Networks (RNNs)**





## **11. Applications in Computer Vision and Natural Language Processing**



**Part VI.**

**Advanced Topics**



## 12. Graph Neural Networks



## **13. Reinforcement Learning**





## 14. Generative Models



## **15. Model Interpretability**



## 16. Conclusion

In summary, this book has no content whatsoever.



## References





## **A. Appendices**

### **A.1. Mathematical Proofs**

### **A.2. Additional Resources**

