## BYM2, Blending Error, and Covariate Bias

## Background

In a recent study by Riebler et al[1], an analysis was conducted on a new parameterization of a recently proposed model, the BYM2 model. The authors first state the importance of using scaling in a model in order for the interpretation and setting of hyper priors to be intuitive and then propose a new framework for model selection, the penalized complexity(PC) prior.

The BYM2 model has two hyper priors which a modeler needs to select for,  $\phi$  and  $\tau_b$ . When  $\phi$  is 0 the model is one that accounts for pure overdispersion of the relative risk attributed to random error. When  $\phi$  is 1 the model random effects are correlated via an intrinsic Gaussian Markov random field (referred to as the Besag model). The PC prior is one in which simplicity is the assumption, models need not introduce complexity if there is no proof of it in the data. This prior causes the BYM2 model to reduce itself in complexity from the Besag model to the overdispersion model to constant relative risk. This model is then tested against simulated data where the expected values are fluctuated along side different scenarios of overdispersion, i.e. constant relative risk, spatially uncorrelated and correlated error.

## **Proposal**

There are at least two remaining scenarios where the BYM2 model with the PC prior should be tested.

- The effect of blended sources of variation ie spatially and non spatially correlated.
- 2) The effects that the PC prior has on potential bias in  $\beta$  estimation.

These two points still need to be tested in the BYM2 model against more traditional models and the same methods of evaluation used by Riebler et al[1] could be used to test these effects. It will be important to see the effects of a PC prior when simulated data is a mixture of spatially correlated and uncorrelated overdispersion.

## References

[1] Andrea Riebler, Sigrunn H. Sorbye, Daniel Simpson, Harvard Rue. An intuitive Bayesian spatial model for disease mapping that accounts for scaling (2016).