Practice Final Solutions (2023) CAS CS 132 Fall 2024

B.
$$\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$
, $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$, $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$, $\begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix}$ + $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$ + $\begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix}$ + $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$ + $\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$ - $\begin{bmatrix} 1 \\ 0 \end{bmatrix}$

Problem 1

$$\begin{bmatrix}
1 & -1 & 1 & 4 & 3 \\
0 & 1 & -2^{*2} & -1^{*3} \\
0 & 0 & 1 & 1
\end{bmatrix}$$

$$\begin{bmatrix}
1 & -1 & 0 & 3 \\
0 & 1 & 0 & -1 \\
0 & 0 & 1 & 1
\end{bmatrix}$$

$$\begin{bmatrix}
1 & -1 & 0 & 3 \\
0 & 1 & 0 & -1 \\
0 & 0 & 1 & 1
\end{bmatrix}$$

$$\begin{bmatrix}
1 & -1 & 0 & 3 \\
0 & 1 & 0 & -1 \\
4 & 2 & 2 & 1
\end{bmatrix}$$

$$\begin{bmatrix}
1 & -1 & 0 & 3 \\
0 & 1 & 0 & -1 \\
4 & 2 & 2 & 1
\end{bmatrix}$$

$$\begin{bmatrix}
1 & -1 & 0 & 3 \\
0 & 0 & 1 & 1
\end{bmatrix}$$

$$\begin{bmatrix}
1 & -1 & 0 & 3 \\
0 & 0 & 1 & 1
\end{bmatrix}$$

$$\begin{bmatrix}
1 & -1 & 0 & 3 \\
0 & 0 & 1 & 1
\end{bmatrix}$$

$$\begin{bmatrix}
1 & -1 & 0 & 3 \\
0 & 0 & 1 & 1
\end{bmatrix}$$

$$\begin{bmatrix}
1 & -1 & 0 & 3 \\
0 & 0 & 1 & 1
\end{bmatrix}$$

$$\begin{bmatrix}
1 & -1 & 0 & 3 \\
0 & 0 & 1 & 1
\end{bmatrix}$$

$$\begin{bmatrix}
1 & -1 & 0 & 3 \\
0 & 0 & 1 & 1
\end{bmatrix}$$

$$\begin{bmatrix}
1 & -1 & 0 & 3 \\
0 & 0 & 1 & 1
\end{bmatrix}$$

$$\begin{bmatrix}
1 & 0 & 0 & 1 \\
0 & 0 & 1 & 1
\end{bmatrix}$$

$$\begin{bmatrix}
1 & 1 & 1 \\
-1 & 1 & 2
\end{bmatrix}$$

$$\begin{bmatrix}
1 & 1 & 1 \\
-1 & 1 & 2
\end{bmatrix}$$

$$\begin{bmatrix}
1 & 1 & 1 \\
-1 & 1 & 2
\end{bmatrix}$$

$$\begin{bmatrix}
1 & 1 & 1 & 2 \\
-1 & 1 & 2
\end{bmatrix}$$

$$\begin{bmatrix}
1 & 1 & 2 & 1 \\
-1 & 1 & 2
\end{bmatrix}$$

$$\begin{bmatrix}
1 & 1 & 2 & 1 \\
-1 & 1 & 2
\end{bmatrix}$$

$$\begin{bmatrix} 1 \\ -1 \\ 1 \end{bmatrix} + 2 \begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix} + (-1) \begin{bmatrix} -1 \\ 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 1+2+1 \\ -1+2 \\ 1+(-1) \end{bmatrix} \begin{bmatrix} 4 \\ 1 \\ 0 \end{bmatrix}$$

$$D \cdot 2 \begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix} + (-1) \begin{bmatrix} -1 \\ 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 2 + 1 \\ 7 + 0 \\ -1 \end{bmatrix} = \begin{bmatrix} 3 \\ 2 \\ -1 \end{bmatrix}$$

Problem 2	
	True
B.	False
	False
D	False

Tre E.

False

Problem 3

A.
$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

 $R_{3} \leftarrow R_{3} + 2R_{2} \begin{pmatrix} 0 & 3 & 0 \\ 1 & 0 & 0 \\ 1 & 0 & 0 \\ 2 & 0 & 1 \end{pmatrix}$ $R_{3} \leftarrow R_{3} + 2R_{2} \begin{pmatrix} 0 & 3 & 0 \\ 1 & 0 & 0 \\ 2 & 0 & 1 \end{pmatrix}$ $R_{3} \leftarrow R_{3} + 2R_{2} \begin{pmatrix} 0 & 3 & 0 \\ 1 & 0 & 0 \\ 2 & 0 & 1 \end{pmatrix}$

$$\begin{bmatrix} 0 & 1 & 0 \\ 3 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 1 & 0 \\ 3 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & 0 \\ 3 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$(AE) = E^{T}A^{T}$$

$$\begin{bmatrix} 11 & 11 & 11 \\ 12 & 12 & 12 \\ 33 & 33 & 33 \end{bmatrix} \xrightarrow{\beta_{1} \leftrightarrow \beta_{2}} \begin{bmatrix} 22 & 22 & 22 \\ 11 & 11 & 11 \\ 33 & 33 & 33 \end{bmatrix}$$

$$\begin{bmatrix}
11 & 11 & 11 \\
12 & 12 & 12 \\
33 & 33
\end{bmatrix}
\xrightarrow{\begin{array}{c} 22 & 22 & 22 \\
11 & 11 & 11 \\
33 & 33 & 33
\end{array}$$

$$\begin{bmatrix}
22 & 22 & 22 \\
11 & 11 & 11 \\
33 & 33 & 33
\end{array}$$

$$\begin{bmatrix}
2 & 2 & 22 & 22 \\
33 & 33 & 33
\end{array}
\xrightarrow{\begin{array}{c} 33 & 33 & 33 \\
33 & 33 & 33
\end{array}}
\xrightarrow{\begin{array}{c} 23 & 33 & 33 \\
33 & 33 & 33
\end{array}}$$

$$A \cdot A - XI = \begin{bmatrix} 1-\lambda & 1 & 4 \\ 0 & 1-\lambda & -1 \\ 0 & 1 & 3-\lambda \end{bmatrix}$$

$$\begin{vmatrix} 0 & 0 & (3-1)(1-\lambda)+1 \end{vmatrix}$$

$$+(A-\lambda I) = -\frac{1}{2}(1-\lambda)$$

$$+(A-\lambda I) = -\frac{1}{(1-\lambda)}$$

$$(1-\lambda)(\lambda^2-4\lambda+3+0)=$$

$$(1-\lambda)(\lambda^{2}-4\lambda+3+1)=$$

$$(1-\lambda)(\lambda-2)$$

=(1-1)(1-1)(1-1)=

$$A - T = \begin{cases} 0 & 1 & 4 \\ 0 & 0 & -1 \\ 0 & 1 & 2 \end{cases} \sim \begin{cases} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 0 \end{cases}$$

$$Nul(A - T) = span \begin{cases} 1 \\ 0 \\ 0 \\ 0 \end{cases}$$

$$A - 2I = \begin{bmatrix} -1 & 1 & 4 \\ 0 & -1 & -1 \\ 0 & 1 & 1 \end{bmatrix} \sim \begin{bmatrix} 1 & -1 & -4 \\ 0 & 1 & 1 \\ 0 & 0 & 0 \end{bmatrix} \sim \begin{bmatrix} 3 & -1 & 1 \\ 0 & 1 & 1 \\ 0 & 0 & 0 \end{bmatrix} = \text{Span} \left\{ \begin{bmatrix} 3 \\ -1 \\ 1 \end{bmatrix} \right\}$$

$$\begin{bmatrix} 3 & + \begin{bmatrix} -1 \\ -1 \end{bmatrix} + \begin{bmatrix} 4 \\ -1 \\ 3 \end{bmatrix} = \begin{bmatrix} 6 \\ -2 \\ z \end{bmatrix}$$

C. A is not diagonalizable.

There is no eigenbasis of R3 for A.

Problem 5 A. No B. [0] [1] C. A~ [01218] ~ [01206] X, is free *1 = - 2 x3 - 6 x5 to is free *4 = - 2 x5 x< is free 07-000

$$det(B) = (-1)^{3} \cdot 3 \cdot 2 \cdot (-4)(7) =$$

E. Yes

Problem G
$$\chi$$

A. $\begin{cases} \cos x_1 & \sin x_1 \\ \cos x_2 & \sin x_2 \\ \cos x_3 & \sin x_3 \\ \cos x_4 & \sin x_4 \end{cases} \begin{bmatrix} \beta_1 \\ \beta_2 \end{bmatrix} = \begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \end{bmatrix}$

B. $\cos (\chi + \hat{\alpha}) =$

cos x sin (
$$\hat{a}$$
) + sin x cos (\hat{a})

By the populos of least square

 $\|X \begin{bmatrix} \hat{\beta}_1 \\ \hat{\beta}_2 \end{bmatrix} - Y \| \leq \|X \begin{bmatrix} \sin(\hat{a}) \end{bmatrix} - Y \|$

(os(\hat{a}))

()
$$\beta_1$$
 (β_2 (β_3 (β_4) β_2 (β_4) where β_1 (β_4) where β_1 (β_2) β_3 (β_4) β_4 (β_4) β_4