Practice Final Solutions CAS CS 132

Fall 2024

Problem 1

A. A. $\begin{bmatrix} 0 & 1 & 0 & -5 \\ 0 & 0 & 1 & 1 \end{bmatrix}$ x_1 is free $x_2 = 5 \times 4$ $x_3 = - \times 4$ x_4 is free $x_4 = 5 \times 4$

 $\mathbf{P} \cdot \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \end{bmatrix} \begin{bmatrix} 0 \\ 5 \\ 1 \end{bmatrix}$

. No. O is an eigenvalue

$$P^{-1} = \frac{1}{-2+3} \begin{bmatrix} 1 & 3 \\ -1 & -2 \end{bmatrix} = \begin{bmatrix} 1 & 3 \\ -1 & -2 \end{bmatrix}$$

= [-19-54]

$$\frac{1}{+3} \begin{bmatrix} 1 & 3 \\ -1 & -2 \end{bmatrix} = \begin{bmatrix} 1 & 3 \\ -1 & -3 \end{bmatrix}$$

$$\frac{1}{1} \begin{bmatrix} 8 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} 1 & 3 \\ -1 & -2 \end{bmatrix}$$

3.

$$B = \begin{bmatrix} -2 - 3 \\ 1 \end{bmatrix} \begin{bmatrix} 2 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} 1 & 3 \\ -1 & -2 \end{bmatrix}$$

$$= \begin{bmatrix} -2 - 3 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} 2 & 0 \\ 1 & 2 \end{bmatrix}$$

Problem 3

A.
$$A = \begin{bmatrix} 4 & -8 \\ 2 & 6 \end{bmatrix}$$

B = $\begin{bmatrix} -8 & 4 \\ 6 & 2 \end{bmatrix}$

B.

$$\frac{1}{2} = \frac{1}{2} = \frac{1$$

$$2e + 6 = (6 - 8 - 4)^{2} + (6 - 8 - 4)^{2} + (6 - 2)^{2}$$

$$= (6 - 8 - 4)^{2} + (6 - 2)^{2}$$

$$= (4 + 16)^{2} = (60)^{2} = 4 (60)^{2}$$

$$= (4 + 16)^{2} = (12 + 16)^{2}$$

 $\alpha = \frac{(14), (14)}{(14), (14)} = \frac{40}{160} = \frac{1}{4}$

$$\frac{1}{4} \begin{bmatrix} 12 \\ -4 \end{bmatrix} = \begin{bmatrix} 3 \\ -1 \end{bmatrix}$$

$$\| \vec{r} \| = \| \begin{bmatrix} 3 \\ -1 \end{bmatrix} - \begin{bmatrix} 4 \\ 1 \end{bmatrix} = \| \begin{bmatrix} -1 \\ -3 \end{bmatrix} \| = \begin{bmatrix} 10 \\ -3 \end{bmatrix} \| = \begin{bmatrix} 10 \\ 10 \end{bmatrix}$$
area = $\frac{1}{4} (4(50) \cdot 50) = 20$

(half the determinent

Problem 4 A. False B. Tre C. Trre D. False E. False F. Tre G. Tre

$$T = \begin{bmatrix} 0 & 0 & 1 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix}$$

D. Yes

$$\begin{bmatrix} -1 & 0 & 1 & 1 \\ 1 & -1 & 0 \\ 0 & 1 & -1 \end{bmatrix} \sim \begin{bmatrix} 1 & 0 & -1 \\ 1 & 0 & -1 \\ 0 & 1 & -1 \end{bmatrix} \wedge \begin{bmatrix} 1 & 0 & -1 \\ 0 & 1 & -1 \\ 0 & 0 & 0 \end{bmatrix}$$

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Problem G

$$AA^{T} = \begin{bmatrix} 1 & 1 & 0 & 7 \\ 3 & 1 & 1 & -2 \end{bmatrix} \begin{bmatrix} 1 & 3 & 1 \\ 1 & 1 & 1 \\ 0 & 1 & 1 \\ 2 & -7 & 1 \end{bmatrix}$$

$$=\begin{bmatrix} 6 & 0 & 7 \\ 0 & 15 \end{bmatrix}$$

$$\sigma_{1} = \pi$$

$$\sigma_{2} = \pi$$