A seignment 1

CS131

Fall 
$$7025$$

Bossic Problems

1. coeff. matrix:

$$\begin{bmatrix}
1 - 2 - 2 \\
2 - 3 - 5 \\
-2 2 7
\end{bmatrix}$$

$$\begin{bmatrix}
2 - 2 - 2 \\
2 - 3 - 5
\end{bmatrix}$$

$$\begin{bmatrix}
2 - 2 - 2 \\
2 - 3 - 5
\end{bmatrix}$$

$$\begin{bmatrix}
2 - 2 - 2 \\
2 - 3 - 5
\end{bmatrix}$$

$$\begin{bmatrix}
2 - 3 - 5 \\
-2 2 7
\end{bmatrix}$$

$$\begin{bmatrix}
4 - 2 - 2 & 2 \\
2 - 3 - 5 & 2 \\
-2 & 2 7
\end{bmatrix}$$

$$\begin{bmatrix}
4 - 2 - 2 & 2 \\
2 - 3 - 5 & 2 \\
-2 & 2 7
\end{bmatrix}$$

$$\begin{bmatrix}
4 - 2 - 2 & 2 \\
2 - 3 - 5 & 2 \\
-2 & 2 7
\end{bmatrix}$$

$$\begin{bmatrix}
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\end{bmatrix}$$

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-2 & 2 7
\end{bmatrix}$$

$$\begin{bmatrix}
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2 - 3 - 5 & 2 \\
-2 & 2 7
\end{bmatrix}$$

$$\begin{bmatrix}
4 - 2 - 2 & 2 \\
2 - 3 - 5 & 2 \\
-2 & 2 7
\end{bmatrix}$$

2. 
$$x_1 + 2x_2 - x_3 + xy = t$$
  
 $x_1 + 3x_2 + 2x_4 = 15$   
 $-2x_1 - 6x_2 - 3x_4 = -27$   
3. Plug in values:  
 $(1) - 2(3) + 2 - 2(3) = 1 - 6 + 2 - 6 = -9$   
 $1 - 3 - 2 - 2(3) = 1 - 3 - 7 - 6 = -10$   
 $-3(1) + 8(3) - 6(2) + 4(3) = -3 + 24 - 12 + 12 = 21$   
 $2(3) - 7(2) + 7(3) = 6 - 14 + 21 = 13$ 

4. Agrented matrix:

$$\begin{bmatrix} 1 & -2 & -2 & -7 \\ -1^{+1} & 3^{-2} & 7^{-2} & 10 \\ 2 & -6 & -3 & -18 \end{bmatrix} \xrightarrow{R_{2} \leftarrow R_{2} + R_{1}}$$

$$\begin{bmatrix}
1 & -2 & -2 & -7 \\
0 & 1 & 0 & 3 \\
-2 & -6 & -3 & -18
\end{bmatrix}$$

$$R_3 \in R_3 - 2R_1$$

$$\begin{bmatrix} 1 & 0 & 0 & 3 \\ 0 & 1 & 0 & 3 \\ 0 & 1 & 0 & 3 \\ 0 & 0 & 1 & 2 \end{bmatrix} \quad \begin{array}{c} x_1 = 3 \\ x_2 = 3 \\ x_3 = 3 \end{array}$$

(3,3,2) is the unique solution.

$$\begin{cases} 9 & 5 & -7 & -5 & -9 \\ 5 & -7 & 1 & -2 & -9 \\ 5 & 7 & -5 & 2 & 1 \end{cases} \qquad \begin{cases} 9 & 5 & -7 & 5 & -9 \\ 5 & 7 & -5 & 2 & 1 \end{cases} \qquad \begin{cases} 9 & 5 & -7 & 5 & -9 \\ 5 & 7 & 1 & 70 & 2 & 2 & 90 \\ 5 & 1 & -10 & 6 & -5 \\ -5 & -7 & 5 & -2 & -1 \end{cases} \qquad \begin{cases} 9 & 5 & -7 & -5 & -9 \\ -5 & -9 & 21 & -14 & 15 \\ -5 & -7 & 5 & -2 & -1 \end{cases} \qquad \begin{cases} 9 & 5 & -7 & -5 & -9 \\ 20 & 26 & -4 & -4 & 6 \\ -5 & -7 & 5 & -2 & -1 \end{cases} \qquad \begin{cases} 9 & 5 & -7 & -5 & -9 \\ 20 & 26 & -4 & -4 & 6 \\ -10 & -20 & 5 & 0 & -8 \\ -5 & -7 & 5 & -7 & -1 \end{cases} \qquad \begin{cases} 9 & 3 & 6 & 2 \\ -10 & -20 & 5 & 0 & -8 \\ -5 & -7 & 5 & -7 & -1 \end{cases} \qquad \begin{cases} 9 & 3 & 6 & 2 \\ -10 & -20 & 5 & 0 & -8 \\ -5 & -7 & 5 & -7 & -1 \end{cases}$$

6.  $x_1 = -3 - x_2 + 4x_6 - 5x_7$   $x_2$  is free

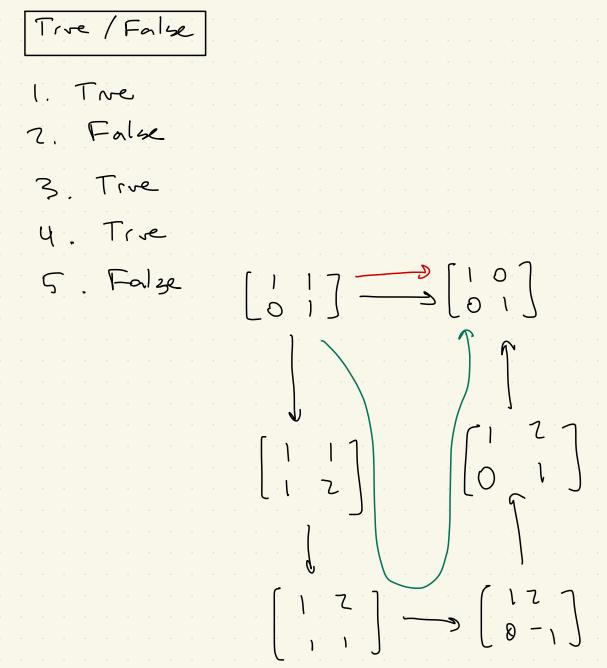
X3 = -4 - X6 - 3 X7 X4 is free

x5 = 2 - 5 x6 + 3 x7

to is free

X7 is free

7. 
$$\begin{cases} 1 - 1 - 2 & 1 \\ -1 & 2 & 1 \\ 2 & 4 & 2 \\ 2 & 3 & 2 & 4 \\ -2 & 1 & 2 & 4 \\ 2 & 1 & 2 & 4 \\ -2 & 1 & 2 & 4 \\ 2 & 1 & 2 &$$



6. True

7. False

8. Falze

9. Falu

X+y=1 X+y=2

x+y+z=1 x+y+z=2

X+7=3

The system is inconsistent exactly when

There are no values of h so that

the system has infinitely many solutions.

This would require the second equations to be a multiple of the first, which is not possible.

$$\begin{bmatrix} 2 & 6 & 1 \\ 3 & 9 & 0 \end{bmatrix}^{N}$$

$$\begin{bmatrix} 6 & 18 & 3 \\ 6 & 18 & 0 \end{bmatrix}^{N} \begin{bmatrix} 2 & 6 & 1 \\ 0 & 18 & 0 \end{bmatrix}^{N}$$

$$b) k = 0$$

$$k = 0$$

$$\begin{bmatrix} 0 & 2 & 1 \\ 3 & 9 & 0 \end{bmatrix}^{N} \begin{bmatrix} 1 & 3 & 0 \\ 0 & 1 & 1/2 \end{bmatrix}^{N}$$

$$k = \frac{7}{3}$$
 $h = \frac{9}{2}$ 

$$\begin{bmatrix} 27 & 2 & 1 \\ 3 & 9 & 9/2 \end{bmatrix} \sim \begin{bmatrix} 6 & 18 & 9 & 1 \\ 6 & 18 & 9 & 1 \end{bmatrix}$$

$$\lambda = \begin{bmatrix} 6 & 18 & 9 & 1 \\ 0 & 8 & 0 & 1 \end{bmatrix}$$