

## salt4: Boxes

CS392-M1: *Rust, In Practice and in Theory*

# Syntax

$x$	(variables, $\mathcal{V}$ )
$n$	(integers, $\mathbb{Z}$ )
$w ::= x \mid * w$	(place expression, $\mathcal{W}$ )
$e ::= () \mid n \mid \text{copy } w \mid w \mid \& w \mid \&\text{mut } w \mid w = e \mid \{ p \} \mid \text{box } e$	(expressions, $\mathcal{E}$ )
$s ::= \text{let } x = e \mid \text{let mut } x = e \mid e$	(statements, $\mathcal{S}$ )
$p ::= e \mid s ; p$	(programs, $\mathcal{P}$ )

# Typing

$l$	(lifetimes, $\text{Lt}$ )
$t ::= () \mid \text{i32} \mid \& w \mid \&\text{mut } w \mid \square t$	(types, $\mathcal{T}$ )
$\tilde{t} ::= [t] \mid t \mid \square \tilde{t}$	(partial types, $\tilde{\mathcal{T}}$ )
$m ::= \text{imm} \mid \text{mut}$	(mutability)
$u ::= \langle \tilde{t} \rangle_l^m$	(slot types, $\mathbb{S}_{\mathcal{T}}$ )
$\Gamma \in \mathcal{V} \mapsto \mathbb{S}_{\mathcal{T}}$	(contexts)
$\text{copyable}(t)$	(copyability)
$\Gamma \vdash \text{readable}(w)$	(readability)
$\Gamma \vdash \text{writable}(w)$	(writability)
$\Gamma \vdash \text{mutable}(w)$	(mutability)
$\Gamma \vdash \tilde{t} \approx \tilde{t}$	(type compatibility)
$\Gamma \vdash \tilde{t} : l$	(lifetimes)
$\Gamma \vdash w : u$	(place expressions)
$\Gamma \vdash \langle e : t \rangle_l \dashv \Gamma$	(expressions)
$\Gamma \vdash \langle s \rangle_l \dashv \Gamma$	(statements)
$\Gamma \vdash \langle p : t \rangle_l \dashv \Gamma$	(programs)

$$\begin{array}{c}
\frac{(x \mapsto \langle \tilde{t} \rangle_l^m) \in \Gamma}{\Gamma \vdash x : \langle \tilde{t} \rangle_l^m} \text{ VAR} \quad \frac{\Gamma \vdash w : \langle \& x \rangle_{l_1}^{m_1} \quad \Gamma \vdash x : \langle \tilde{t} \rangle_{l_2}^{m_2}}{\Gamma \vdash *w : \langle \tilde{t} \rangle_{l_2}^{m_2}} \text{ DEREF} \\
\\
\frac{\Gamma \vdash w : \langle \&\text{mut } x \rangle_{l_1}^{m_1} \quad \Gamma \vdash x : \langle \tilde{t} \rangle_{l_2}^{m_2}}{\Gamma \vdash *w : \langle \tilde{t} \rangle_{l_2}^{m_2}} \text{ MUTDEREF} \quad \frac{\Gamma \vdash w : \langle \Box \tilde{t} \rangle_l^m}{\Gamma \vdash *w : \langle \tilde{t} \rangle_l^m} \text{ BOX} \\
\\
\frac{}{\Gamma \vdash \langle (\textcolor{red}{O}) : (\textcolor{red}{O}) \rangle_l \dashv \Gamma} \text{ UNIT} \quad \frac{n \in \mathbb{Z}}{\Gamma \vdash \langle n : \textcolor{red}{i32} \rangle_l \dashv \Gamma} \text{ INT} \quad \frac{\nexists y, j. (y \mapsto \langle \&\text{mut } *^j x \rangle_l^m) \in \Gamma}{\Gamma \vdash \text{readable}(*^k x)} \text{ READABLE} \\
\\
\frac{}{\text{copyable}(\textcolor{red}{O})} \text{ COPYUNIT} \quad \frac{}{\text{copyable}(\textcolor{red}{i32})} \text{ COPYINT} \quad \frac{}{\text{copyable}(\& w)} \text{ COPYREF} \\
\\
\frac{\Gamma \vdash w : \langle t \rangle_{l_1}^m \quad \Gamma \vdash \text{readable}(w) \quad \text{copyable}(t)}{\Gamma \vdash \langle \text{copy } w : t \rangle_{l_2} \dashv \Gamma} \text{ PLACECOPY} \\
\\
\frac{\Gamma \vdash \text{readable}(*^k x) \quad \nexists y, j. (y \mapsto \langle \& *^j x \rangle_l^m) \in \Gamma}{\Gamma \vdash \text{writable}(*^k x)} \text{ WRITABLE}
\end{array}$$

$$\begin{array}{lll}
\text{move}(\Gamma, x) = \Gamma[x \mapsto \langle \lfloor t \rfloor \rangle_l^m] & \text{where} & (x \mapsto \langle t \rangle_l^m) \in \Gamma \\
\text{move}(\Gamma, *^{k+1} x) =
\end{array}$$

$$\begin{array}{c}
\frac{\Gamma \vdash w : \langle t \rangle_{l_1}^m \quad \Gamma \vdash \text{writable}(w)}{\Gamma \vdash \langle w : t \rangle_{l_2} \dashv \text{move}(\Gamma, w)} \text{PLACEMOVE} \\
\\
\frac{\Gamma \vdash x : \langle \&\text{mut } w \rangle_{l_1}^m \quad \Gamma \vdash \text{writable}(x)}{\Gamma \vdash \langle x : \&\text{mut } w \rangle_{l_2} \dashv \Gamma[x \mapsto \langle \lfloor \&\text{mut } w \rfloor \rangle_{l_1}^m]} \text{PLACEMOVE} \quad \frac{\Gamma \vdash w : \langle t \rangle_{l_1}^m \quad \Gamma \vdash \text{readable}(w)}{\Gamma \vdash \langle \& w : \& w \rangle_{l_2} \dashv \Gamma} \text{REF} \\
\\
\frac{(x \mapsto \langle t \rangle_l^{\text{mut}}) \in \Gamma}{\Gamma \vdash \text{mutable}(x)} \text{MUTVAR} \quad \frac{(x \mapsto \langle \&\text{mut } w \rangle_l^m) \in \Gamma \quad \Gamma \vdash \text{mutable}(*^k w)}{\Gamma \vdash \text{mutable}(*^{k+1} x)} \text{MUTDEREF} \\
\\
\frac{\Gamma \vdash w : \langle t \rangle_{l_1}^{\text{mut}} \quad \Gamma \vdash \text{writable}(w) \quad \Gamma \vdash \text{mutable}(w)}{\Gamma \vdash \langle \&\text{mut } w : \&\text{mut } w \rangle_{l_2} \dashv \Gamma} \text{MUTREF} \quad \frac{}{\Gamma \vdash \langle \rangle \approx \langle \rangle} \approx\text{-UNIT} \\
\\
\frac{\Gamma \vdash i32 \approx i32}{\Gamma \vdash \& i32 \approx \& i32} \approx\text{-INT} \quad \frac{\Gamma \vdash w_1 : \langle \tilde{t}_1 \rangle_{l_1}^{m_1} \quad \Gamma \vdash w_2 : \langle \tilde{t}_2 \rangle_{l_2}^{m_2} \quad \Gamma \vdash \tilde{t}_1 \approx \tilde{t}_2}{\Gamma \vdash \& w_1 \approx \& w_2} \approx\text{-REF} \\
\\
\frac{\Gamma \vdash w_1 : \langle \tilde{t}_1 \rangle_{l_1}^{m_1} \quad \Gamma \vdash w_2 : \langle \tilde{t}_2 \rangle_{l_2}^{m_2} \quad \Gamma \vdash \tilde{t}_1 \approx \tilde{t}_2}{\Gamma \vdash \&\text{mut } w_1 \approx \&\text{mut } w_2} \approx\text{-MUTREF} \quad \frac{\Gamma \vdash \tilde{t}_1 \approx \tilde{t}_2}{\Gamma \vdash \Box \tilde{t}_1 \approx \Box \tilde{t}_2} \approx\text{-BOX} \\
\\
\frac{\Gamma \vdash t_1 \approx \tilde{t}_2}{\Gamma \vdash \lfloor t_1 \rfloor \approx \tilde{t}_2} \approx\text{-PARTIAL}_1 \quad \frac{\Gamma \vdash \tilde{t}_1 \approx t_2}{\Gamma \vdash \tilde{t}_1 \approx \lfloor t_2 \rfloor} \approx\text{-PARTIAL}_2
\end{array}$$

$$\begin{aligned}
\text{write}(\Gamma, x, t) &= \Gamma[x \mapsto \langle t \rangle_l^m] \quad \text{where} \quad (x \mapsto \langle \cdot \rangle_l^m) \in \Gamma \\
\text{write}(\Gamma, *^{k+1} x, t) &= \text{write}(\Gamma, *^k w, t) \quad \text{where} \quad (x \mapsto \langle \&\text{mut } w \rangle_l^m) \in \Gamma
\end{aligned}$$

$$\begin{aligned}
\text{replace}(\& *^{k+1} w_1, w_1, \& w_2) &= \& *^k w_2 \\
\text{replace}(\& *^{k+1} w_1, w_1, \&\text{mut } w_2) &= \& *^k w_2 \\
\text{replace}(\&\text{mut} *^{k+1} w_1, w_1, \& w_2) &= \&\text{mut} *^k w_2 \\
\text{replace}(\&\text{mut} *^{k+1} w_1, w_1, \&\text{mut } w_2) &= \&\text{mut} *^k w_2 \\
\text{replace}(t_1, w, t_2) &= t_1 \\
\text{replace}(\lfloor t_1 \rfloor, w, t_2) &= \lfloor \text{replace}(t_1, w, t_2) \rfloor \\
\text{replace}(\Gamma, w, t_2) &= \{x \mapsto \langle \text{replace}(\tilde{t}_1, w, t_2) \rangle_l^m : (x \mapsto \langle \tilde{t}_1 \rangle_l^m) \in \Gamma\}
\end{aligned}$$

$$\text{update}(\Gamma, w, t_2) = \text{replace}(\text{write}(\Gamma, w, t_2), w, t_2)$$

$$\text{drop}(\Gamma, l) = \Gamma \setminus \{x \mapsto \langle \tilde{t} \rangle_l^m : (x \mapsto \langle \tilde{t} \rangle_l^m) \in \Gamma\}$$

$$\begin{array}{c}
\frac{}{\Gamma \vdash \text{i32} : l} \text{INTLFTM} \quad \frac{G \vdash w : \langle t \rangle_{l_1}^m \quad l_1 \leq l_2}{\Gamma \vdash \& w : l_2} \text{REFLFTM} \\
\\
\frac{\Gamma \vdash w : \langle t \rangle_{l_1}^m \quad l_1 \leq l_2}{\Gamma \vdash \&\text{mut } w : l_2} \text{MUTREFLFTM} \quad \frac{\Gamma \vdash t : l}{\Gamma \vdash \Box t : l} \text{BOXLFTM} \\
\\
\frac{\Gamma_1 \vdash w : \langle \tilde{t}_1 \rangle_{l_1}^{\text{mut}} \quad \Gamma_1 \vdash e : t_2 \dashv \Gamma_2 \quad \Gamma_2 \vdash \tilde{t}_1 \approx t_2}{\Gamma_2 \vdash t_2 : l_1 \quad \Gamma_3 = \text{update}(\Gamma, w, t_2) \quad \Gamma_3 \vdash \text{writable}(w)} \vdash \Gamma_3 \text{ ASSIGN} \\
\\
\frac{\Gamma_1 \vdash \langle p : t \rangle_{l+1} \dashv \Gamma_2 \quad \Gamma_2 \vdash t : l}{\Gamma_1 \vdash \langle \{ p \} : t \rangle_l \dashv \text{drop}(\Gamma_2, l+1)} \text{BLOCK} \quad \frac{\Gamma_1 \vdash \langle e : t \rangle_l \dashv \Gamma_2 \quad x \notin \text{dom}(\Gamma_2)}{\Gamma_1 \vdash \langle \text{let } x = e \rangle_l \dashv \Gamma_2[x \mapsto \langle t \rangle_l^{\text{imm}}]} \text{LET} \\
\\
\frac{\Gamma_1 \vdash \langle e : t \rangle_l \dashv \Gamma_2 \quad x \notin \text{dom}(\Gamma_2)}{\Gamma_1 \vdash \langle \text{let mut } x = e \rangle_l \dashv \Gamma_2[x \mapsto \langle t \rangle_l^{\text{mut}}]} \text{LETMUT} \quad \frac{\Gamma_1 \vdash \langle e : t \rangle_l \dashv \Gamma_2}{\Gamma_1 \vdash \langle e \rangle_l \dashv \Gamma_2} \text{EXPRSTMT} \\
\\
\frac{\Gamma_1 \vdash \langle s \rangle_l \dashv \Gamma_2 \quad \Gamma_2 \vdash \langle p : t \rangle_l \dashv \Gamma_3}{\Gamma_1 \vdash \langle s ; p : t \rangle_l \dashv \Gamma_3} \text{PROG}
\end{array}$$

# Evaluation

$\ell ::= \ell_x$	(locations, $\mathcal{L}$ )
$v ::= \textcolor{red}{\circ} \mid n \mid \ell$	(values, $\mathbb{V}$ )
$\tilde{v} ::= \perp \mid v$	(partial values, $\tilde{\mathbb{V}}$ )
$r ::= \langle \tilde{v} \rangle_l$	(slot types, $\mathbb{S}_{\mathbb{V}}$ )
$S \in \mathcal{L} \mapsto \mathbb{S}_{\mathbb{V}}$	(store)
$S \vdash \langle e \Downarrow v \rangle_l \dashv S$	(expressions)
$S \vdash \langle s \rangle_l \dashv S$	(statements)
$S \vdash \langle p \Downarrow v \rangle_l \dashv S$	(programs)

$$\frac{}{S \vdash x \rightsquigarrow \ell_x} \text{LOCVAR} \qquad \frac{S \vdash w \rightsquigarrow \ell_x \quad (\ell_x \mapsto \langle \ell_y \rangle_l) \in S}{S \vdash *w \rightsquigarrow \ell_y} \text{LOCDEREF}$$

$$\frac{}{S \vdash \langle \textcolor{red}{(\textcircled{O})} \Downarrow \textcolor{red}{(\textcircled{O})} \rangle_l \dashv S} \text{UNIT} \qquad \frac{n \in \mathbb{Z}}{S \vdash \langle n \Downarrow n \rangle_l \dashv S} \text{INT}$$

$$\frac{S \vdash w \rightsquigarrow \ell_x \quad (\ell_x \mapsto \langle v \rangle_{l_1}) \in S}{S \vdash \langle \text{copy } w \Downarrow v \rangle_{l_2} \dashv S} \text{PLACECOPY} \qquad \frac{S \vdash w \rightsquigarrow \ell_x \quad (\ell_x \mapsto \langle v \rangle_{l_1}) \in S}{S \vdash \langle w \Downarrow v \rangle_{l_2} \dashv S[\ell_x \mapsto \langle \perp \rangle_{l_1}]} \text{MOVE}$$

$$\frac{S \vdash w \rightsquigarrow \ell_x}{S \vdash \langle \textcolor{red}{\&} w \Downarrow \ell_x \rangle_l \dashv S} \text{REF} \qquad \frac{S \vdash w \rightsquigarrow \ell_x}{S \vdash \langle \textcolor{red}{\&mut} w \Downarrow \ell_x \rangle_l \dashv S} \text{MUTREF}$$

$$\frac{S \vdash w \rightsquigarrow \ell_x \quad (\ell_x \mapsto \langle \tilde{v} \rangle_{l_1}) \in S_1 \quad S_1 \vdash \langle e \Downarrow v \rangle_{l_2} \dashv S_2}{S_1 \vdash \langle w = e \Downarrow \textcolor{red}{(\textcircled{O})} \rangle_{l_2} \dashv S_2[\ell_x \mapsto \langle v \rangle_{l_1}]} \text{ASSIGN}$$

$$\text{drop}(S,l) = S \setminus \{\ell \mapsto \langle \tilde{v} \rangle_l : (\ell \mapsto \langle \tilde{v} \rangle_l) \in S\}$$

$$\frac{S_1 \vdash \langle p \Downarrow v \rangle_{l+1} \dashv S_2}{S_1 \vdash \{ p \} \Downarrow v \dashv \text{drop}(S_2, l+1)} \text{BLOCK} \qquad \frac{S_1 \vdash \langle e \Downarrow v \rangle_l \dashv S_2}{S_1 \vdash \langle \text{let } x = e \rangle_l \dashv S_2[\ell_x \mapsto \langle v \rangle_l]} \text{LET}$$

$$\frac{S_1 \vdash \langle e \Downarrow v \rangle \dashv S_2}{S_1 \vdash \langle \text{let mut } x = e \rangle \dashv S_2[\ell_x \mapsto \langle v \rangle_l]} \text{LETMUT} \qquad \frac{S_1 \vdash \langle e \Downarrow v \rangle_l \dashv S_2}{S_1 \vdash \langle e \rangle_l \dashv S_2} \text{EXPRSTMT}$$

$$\frac{S_1 \vdash \langle s \rangle_l \dashv S_2 \quad S_2 \vdash \langle p \Downarrow v \rangle_l \dashv S_3}{S_1 \vdash \langle s ; p \Downarrow v \rangle_l \dashv S_3} \text{PROG}$$