

salt4: Boxes

CS392-M1: *Rust, In Practice and in Theory*

Syntax

x	(variables, \mathcal{V})
n	(integers, \mathbb{Z})
$w ::= x \mid * w$	(place expression, \mathcal{W})
$e ::= () \mid n \mid \text{copy } w \mid w \mid \& w \mid \&\text{mut } w \mid w = e \mid \{ p \} \mid \text{box } e$	(expressions, \mathcal{E})
$s ::= \text{let } x = e \mid \text{let mut } x = e \mid e$	(statements, \mathcal{S})
$p ::= e \mid s ; p$	(programs, \mathcal{P})

Typing

l	(lifetimes, Lt)
$t ::= () \mid \text{i32} \mid \& w \mid \&\text{mut } w \mid \Box t$	(types, \mathcal{T})
$\tilde{t} ::= \lfloor t \rfloor \mid t \mid \Box \tilde{t}$	(partial types, $\tilde{\mathcal{T}}$)
$m ::= \text{imm} \mid \text{mut}$	(mutability)
$u ::= \langle \tilde{t} \rangle_l^m$	(slot types, $S_{\mathcal{T}}$)
$\Gamma \in \mathcal{V} \mapsto S_{\mathcal{T}}$	(contexts)
$\text{copyable}(t)$	(copyability)
$\Gamma \vdash \text{readable}(w)$	(readability)
$\Gamma \vdash \text{writable}(w)$	(writability)
$\Gamma \vdash \text{mutable}(w)$	(mutability)
$\Gamma \vdash \tilde{t} \approx \tilde{t}$	(type compatibility)
$\Gamma \vdash \tilde{t} : l$	(lifetimes)
$\Gamma \vdash w : u$	(place expressions)
$\Gamma \vdash \langle e : t \rangle_l \dashv \Gamma$	(expressions)
$\Gamma \vdash \langle s \rangle_l \dashv \Gamma$	(statements)
$\Gamma \vdash \langle p : t \rangle_l \dashv \Gamma$	(programs)

$$\begin{array}{c}
\frac{(x \mapsto \langle \tilde{t} \rangle_l^m) \in \Gamma}{\Gamma \vdash x : \langle \tilde{t} \rangle_l^m} \text{VAR} \qquad \frac{\Gamma \vdash w : \langle \& x \rangle_{l_1}^{m_1} \quad \Gamma \vdash x : \langle \tilde{t} \rangle_{l_2}^{m_2}}{\Gamma \vdash * w : \langle \tilde{t} \rangle_{l_2}^{m_2}} \text{DEREF} \\
\\
\frac{\Gamma \vdash w : \langle \&\text{mut } x \rangle_{l_1}^{m_1} \quad \Gamma \vdash x : \langle \tilde{t} \rangle_{l_2}^{m_2}}{\Gamma \vdash * w : \langle \tilde{t} \rangle_{l_2}^{m_2}} \text{MUTDEREF} \qquad \frac{\Gamma \vdash w : \langle \square \tilde{t} \rangle_l^m}{\Gamma \vdash * w : \langle \tilde{t} \rangle_l^m} \text{BOX} \\
\\
\frac{}{\Gamma \vdash \langle () : () \rangle_l \dashv \Gamma} \text{UNIT} \qquad \frac{n \in \mathbb{Z}}{\Gamma \vdash \langle n : \text{i32} \rangle_l \dashv \Gamma} \text{INT} \qquad \frac{\nexists y, j. (y \mapsto \langle \&\text{mut } *^j x \rangle_l^m) \in \Gamma}{\Gamma \vdash \text{readable}(*^k x)} \text{READABLE} \\
\\
\frac{}{\text{copyable}(\langle () \rangle)} \text{COPYUNIT} \qquad \frac{}{\text{copyable}(\text{i32})} \text{COPYINT} \qquad \frac{}{\text{copyable}(\& w)} \text{COPYREF} \\
\\
\frac{\Gamma \vdash w : \langle t \rangle_{l_1}^m \quad \Gamma \vdash \text{readable}(w) \quad \text{copyable}(t)}{\Gamma \vdash \langle \text{copy } w : t \rangle_{l_2} \dashv \Gamma} \text{PLACECOPY} \\
\\
\frac{\Gamma \vdash \text{readable}(*^k x) \quad \nexists y, j. (y \mapsto \langle \& *^j x \rangle_l^m) \in \Gamma}{\Gamma \vdash \text{writable}(*^k x)} \text{WRITABLE}
\end{array}$$

$$\begin{array}{l}
\text{move}(\Gamma, x) = \Gamma[x \mapsto \langle [t] \rangle_l^m] \quad \text{where} \quad (x \mapsto \langle t \rangle_l^m) \in \Gamma \\
\text{move}(\Gamma, *^{k+1} x) =
\end{array}$$

$$\begin{array}{c}
\frac{\Gamma \vdash w : \langle t \rangle_{l_1}^m \quad \Gamma \vdash \text{writable}(w)}{\Gamma \vdash \langle w : t \rangle_{l_2} \dashv \text{move}(\Gamma, w)} \text{ PLACEMOVE} \\
\\
\frac{\Gamma \vdash x : \langle \&\text{mut } w \rangle_{l_1}^m \quad \Gamma \vdash \text{writable}(x)}{\Gamma \vdash \langle x : \&\text{mut } w \rangle_{l_2} \dashv \Gamma[x \mapsto \langle \&\text{mut } w \rangle_{l_1}^m]} \text{ PLACEMOVE} \quad \frac{\Gamma \vdash w : \langle t \rangle_{l_1}^m \quad \Gamma \vdash \text{readable}(w)}{\Gamma \vdash \langle \& w : \& w \rangle_{l_2} \dashv \Gamma} \text{ REF} \\
\\
\frac{(x \mapsto \langle t \rangle_l^{\text{mut}}) \in \Gamma}{\Gamma \vdash \text{mutable}(x)} \text{ MUTVAR} \quad \frac{(x \mapsto \langle \&\text{mut } w \rangle_l^m) \in \Gamma \quad \Gamma \vdash \text{mutable}(\&^k w)}{\Gamma \vdash \text{mutable}(\&^{k+1} x)} \text{ MUTDEREF} \\
\\
\frac{\Gamma \vdash w : \langle t \rangle_{l_1}^{\text{mut}} \quad \Gamma \vdash \text{writable}(w) \quad \Gamma \vdash \text{mutable}(w)}{\Gamma \vdash \langle \&\text{mut } w : \&\text{mut } w \rangle_{l_2} \dashv \Gamma} \text{ MUTREF} \quad \frac{}{\Gamma \vdash () \approx ()} \approx\text{-UNIT} \\
\\
\frac{}{\Gamma \vdash \text{i32} \approx \text{i32}} \approx\text{-INT} \quad \frac{\Gamma \vdash w_1 : \langle \tilde{t}_1 \rangle_{l_1}^{m_1} \quad \Gamma \vdash w_2 : \langle \tilde{t}_2 \rangle_{l_2}^{m_2} \quad \Gamma \vdash \tilde{t}_1 \approx \tilde{t}_2}{\Gamma \vdash \& w_1 \approx \& w_2} \approx\text{-REF} \\
\\
\frac{\Gamma \vdash w_1 : \langle \tilde{t}_1 \rangle_{l_1}^{m_1} \quad \Gamma \vdash w_2 : \langle \tilde{t}_2 \rangle_{l_2}^{m_2} \quad \Gamma \vdash \tilde{t}_1 \approx \tilde{t}_2}{\Gamma \vdash \&\text{mut } w_1 \approx \&\text{mut } w_2} \approx\text{-MUTREF} \quad \frac{\Gamma \vdash \tilde{t}_1 \approx \tilde{t}_2}{\Gamma \vdash \square \tilde{t}_1 \approx \square \tilde{t}_2} \approx\text{-BOX} \\
\\
\frac{\Gamma \vdash t_1 \approx \tilde{t}_2}{\Gamma \vdash \lfloor t_1 \rfloor \approx \tilde{t}_2} \approx\text{-PARTIAL}_1 \quad \frac{\Gamma \vdash \tilde{t}_1 \approx t_2}{\Gamma \vdash \tilde{t}_1 \approx \lfloor t_2 \rfloor} \approx\text{-PARTIAL}_2
\end{array}$$

$$\begin{aligned}
\text{write}(\Gamma, x, t) &= \Gamma[x \mapsto \langle t \rangle_l^m] \quad \text{where} \quad (x \mapsto \langle \cdot \rangle_l^m) \in \Gamma \\
\text{write}(\Gamma, \&^{k+1} x, t) &= \text{write}(\Gamma, \&^k w, t) \quad \text{where} \quad (x \mapsto \langle \&\text{mut } w \rangle_l^m) \in \Gamma
\end{aligned}$$

$$\begin{aligned}
\text{replace}(\& \&^{k+1} w_1, w_1, \& w_2) &= \& \&^k w_2 \\
\text{replace}(\& \&^{k+1} w_1, w_1, \&\text{mut } w_2) &= \& \&^k w_2 \\
\text{replace}(\&\text{mut } \&^{k+1} w_1, w_1, \& w_2) &= \&\text{mut } \&^k w_2 \\
\text{replace}(\&\text{mut } \&^{k+1} w_1, w_1, \&\text{mut } w_2) &= \&\text{mut } \&^k w_2 \\
\text{replace}(t_1, w, t_2) &= t_1 \\
\text{replace}(\lfloor t_1 \rfloor, w, t_2) &= \lfloor \text{replace}(t_1, w, t_2) \rfloor \\
\text{replace}(\Gamma, w, t_2) &= \{x \mapsto \langle \text{replace}(\tilde{t}_1, w, t_2) \rangle_l^m : (x \mapsto \langle \tilde{t}_1 \rangle_l^m) \in \Gamma\} \\
\\
\text{update}(\Gamma, w, t_2) &= \text{replace}(\text{write}(\Gamma, w, t_2), w, t_2)
\end{aligned}$$

$$\text{drop}(\Gamma, l) = \Gamma \setminus \{x \mapsto \langle \tilde{t} \rangle_l^m : (x \mapsto \langle \tilde{t} \rangle_l^m) \in \Gamma\}$$

$$\begin{array}{c}
\frac{}{\Gamma \vdash \mathbf{i32} : l} \text{INTLFTM} \qquad \frac{G \vdash w : \langle t \rangle_{l_1}^m \quad l_1 \leq l_2}{\Gamma \vdash \mathbf{\&} w : l_2} \text{REFLFTM} \\
\\
\frac{\Gamma \vdash w : \langle t \rangle_{l_1}^m \quad l_1 \leq l_2}{\Gamma \vdash \mathbf{\&mut} w : l_2} \text{MUTREFLFTM} \qquad \frac{\Gamma \vdash t : l}{\Gamma \vdash \mathbf{\square} t : l} \text{BOXLFTM} \\
\\
\frac{\Gamma_1 \vdash w : \langle \tilde{t}_1 \rangle_{l_1}^{\text{mut}} \quad \Gamma_1 \vdash e : t_2 \dashv \Gamma_2 \quad \Gamma_2 \vdash \tilde{t}_1 \approx t_2 \quad \Gamma_3 = \text{update}(\Gamma, w, t_2) \quad \Gamma_3 \vdash \text{writable}(w)}{\Gamma_1 \vdash \langle w = e : \mathbf{(\color{red}{})} \rangle_{l_2} \dashv \Gamma_3} \text{ASSIGN} \\
\\
\frac{\Gamma_1 \vdash \langle p : t \rangle_{l+1} \dashv \Gamma_2 \quad \Gamma_2 \vdash t : l}{\Gamma_1 \vdash \langle \mathbf{\{ p \}} : t \rangle_l \dashv \text{drop}(\Gamma_2, l+1)} \text{BLOCK} \qquad \frac{\Gamma_1 \vdash \langle e : t \rangle_l \dashv \Gamma_2 \quad x \notin \text{dom}(\Gamma_2)}{\Gamma_1 \vdash \langle \mathbf{let} \ x = e \rangle_l \dashv \Gamma_2[x \mapsto \langle t \rangle_l^{\text{imm}}]} \text{LET} \\
\\
\frac{\Gamma_1 \vdash \langle e : t \rangle_l \dashv \Gamma_2 \quad x \notin \text{dom}(\Gamma_2)}{\Gamma_1 \vdash \langle \mathbf{let mut} \ x = e \rangle_l \dashv \Gamma_2[x \mapsto \langle t \rangle_l^{\text{mut}}]} \text{LETMUT} \qquad \frac{\Gamma_1 \vdash \langle e : t \rangle_l \dashv \Gamma_2}{\Gamma_1 \vdash \langle e \rangle_l \dashv \Gamma_2} \text{EXPRSTMT} \\
\\
\frac{\Gamma_1 \vdash \langle s \rangle_l \dashv \Gamma_2 \quad \Gamma_2 \vdash \langle p : t \rangle_l \dashv \Gamma_3}{\Gamma_1 \vdash \langle s \mathbf{;} p : t \rangle_l \dashv \Gamma_3} \text{PROG}
\end{array}$$

Evaluation

$\ell ::= \ell_x$	(locations, \mathcal{L})
$v ::= \textcolor{red}{\circ} \mid n \mid \ell$	(values, \mathbb{V})
$\tilde{v} ::= \perp \mid v$	(partial values, $\tilde{\mathbb{V}}$)
$r ::= \langle \tilde{v} \rangle_l$	(slot types, $\mathbb{S}_{\mathbb{V}}$)

$S \in \mathcal{L} \mapsto \mathbb{S}_{\mathbb{V}}$	(store)
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$S \vdash \langle e \Downarrow v \rangle_l \dashv S$	(expressions)
$S \vdash \langle s \rangle_l \dashv S$	(statements)
$S \vdash \langle p \Downarrow v \rangle_l \dashv S$	(programs)

$$\begin{array}{c}
\frac{}{S \vdash x \rightsquigarrow \ell_x} \text{LOCVAR} \qquad \frac{S \vdash w \rightsquigarrow \ell_x \quad (\ell_x \mapsto \langle \ell_y \rangle_l) \in S}{S \vdash * w \rightsquigarrow \ell_y} \text{LOCDEREF} \\[10pt]
\frac{}{S \vdash \langle \textcolor{red}{()} \Downarrow \textcolor{red}{()} \rangle_l \dashv S} \text{UNIT} \qquad \frac{n \in \mathbb{Z}}{S \vdash \langle n \Downarrow n \rangle_l \dashv S} \text{INT} \\[10pt]
\frac{S \vdash w \rightsquigarrow \ell_x \quad (\ell_x \mapsto \langle v \rangle_{l_1}) \in S}{S \vdash \langle \text{copy } w \Downarrow v \rangle_{l_2} \dashv S} \text{PLACECOPY} \qquad \frac{S \vdash w \rightsquigarrow \ell_x \quad (\ell_x \mapsto \langle v \rangle_{l_1}) \in S}{S \vdash \langle w \Downarrow v \rangle_{l_2} \dashv S[\ell_x \mapsto \langle \perp \rangle_{l_1}]} \text{MOVE} \\[10pt]
\frac{S \vdash w \rightsquigarrow \ell_x}{S \vdash \langle \& w \Downarrow \ell_x \rangle_l \dashv S} \text{REF} \qquad \frac{S \vdash w \rightsquigarrow \ell_x}{S \vdash \langle \&\text{mut } w \Downarrow \ell_x \rangle_l \dashv S} \text{MUTREF} \\[10pt]
\frac{S \vdash w \rightsquigarrow \ell_x \quad (\ell_x \mapsto \langle \tilde{v} \rangle_{l_1}) \in S_1 \quad S_1 \vdash \langle e \Downarrow v \rangle_{l_2} \dashv S_2}{S_1 \vdash \langle w = e \Downarrow \textcolor{red}{()} \rangle_{l_2} \dashv S_2[\ell_x \mapsto \langle v \rangle_{l_1}]} \text{ASSIGN}
\end{array}$$

$$\text{drop}(S, l) = S \setminus \{ \ell \mapsto \langle \tilde{v} \rangle_l : (\ell \mapsto \langle \tilde{v} \rangle_l) \in S \}$$

$$\begin{array}{c}
\frac{S_1 \vdash \langle p \Downarrow v \rangle_{l+1} \dashv S_2}{S_1 \vdash \{ p \} \Downarrow v \dashv \text{drop}(S_2, l+1)} \text{BLOCK} \qquad \frac{S_1 \vdash \langle e \Downarrow v \rangle_l \dashv S_2}{S_1 \vdash \langle \textcolor{red}{\text{let } x = e} \rangle_l \dashv S_2[\ell_x \mapsto \langle v \rangle_l]} \text{LET} \\[10pt]
\frac{S_1 \vdash \langle e \Downarrow v \rangle \dashv S_2}{S_1 \vdash \langle \textcolor{red}{\text{let mut } x = e} \rangle \dashv S_2[\ell_x \mapsto \langle v \rangle_l]} \text{LETMUT} \qquad \frac{S_1 \vdash \langle e \Downarrow v \rangle_l \dashv S_2}{S_1 \vdash \langle e \rangle_l \dashv S_2} \text{EXPRSTMT} \\[10pt]
\frac{S_1 \vdash \langle s \rangle_l \dashv S_2 \quad S_2 \vdash \langle p \Downarrow v \rangle_l \dashv S_3}{S_1 \vdash \langle s ; p \Downarrow v \rangle_l \dashv S_3} \text{PROG}
\end{array}$$