

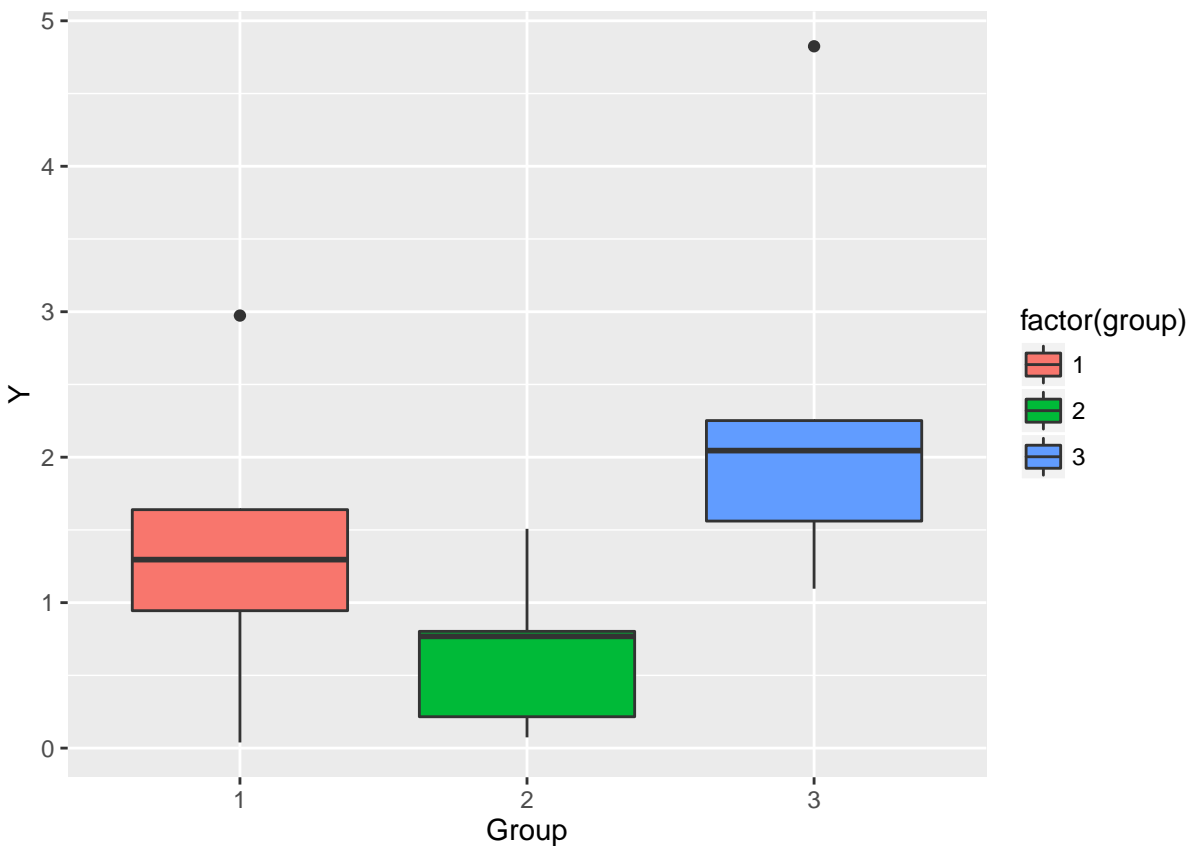
Home Work 2

Rick Galbo, Lost in Bayesian: Ergo not a nonparam overachiever

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Problem 1

```
##   group  mean
## 1     1 1.3785
## 2     2 0.6736
## 3     3 2.3557
```



There is an observable difference in the group means which will be tested for significance.

a) ANOVA *F*-Test

$H_0: \mu_1 = \mu_2 = \mu_3$ vs $H_1: \mu_i \neq \mu_j$ for some i, j

```
## Analysis of Variance Table
##
## Response: Y
##           Df Sum Sq Mean Sq F value Pr(>F)
## group      1  2.3873   2.3873   1.628 0.2243
## Residuals 13 19.0635   1.4664
```

Can see that this is not significant at the $\alpha = 0.05$ significance level.

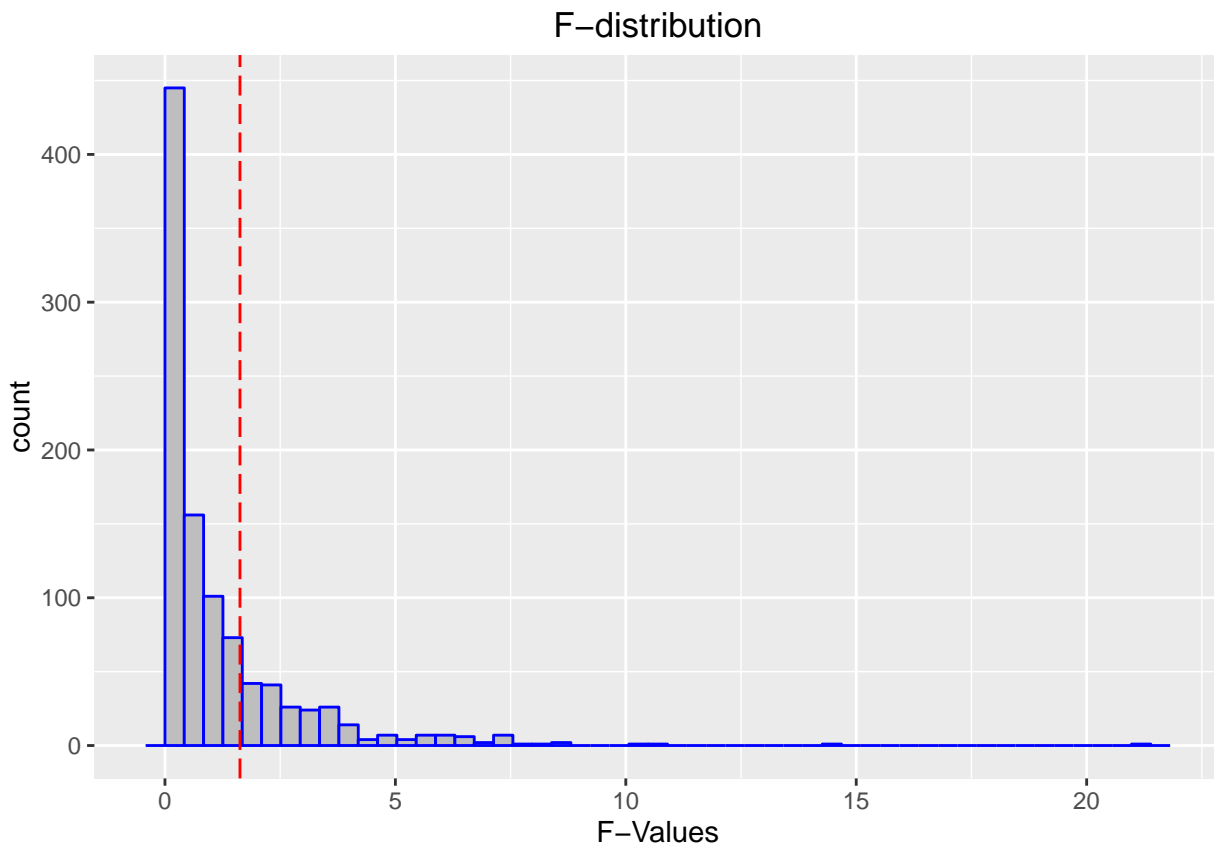
b) permutation F -test

$H_0 : t_1 = t_2 = \dots = t_k = 0$

$H_1 : t_1, t_2, \dots, t_k \text{ not all equal } 0$

p-value:

```
## [1] 0.232
```



This p-value is comparable to the ANOVA F -test value and is also non-significant.

c) Kruskal-Wallis Test

p-value:

```
## [1] 0.0491
```

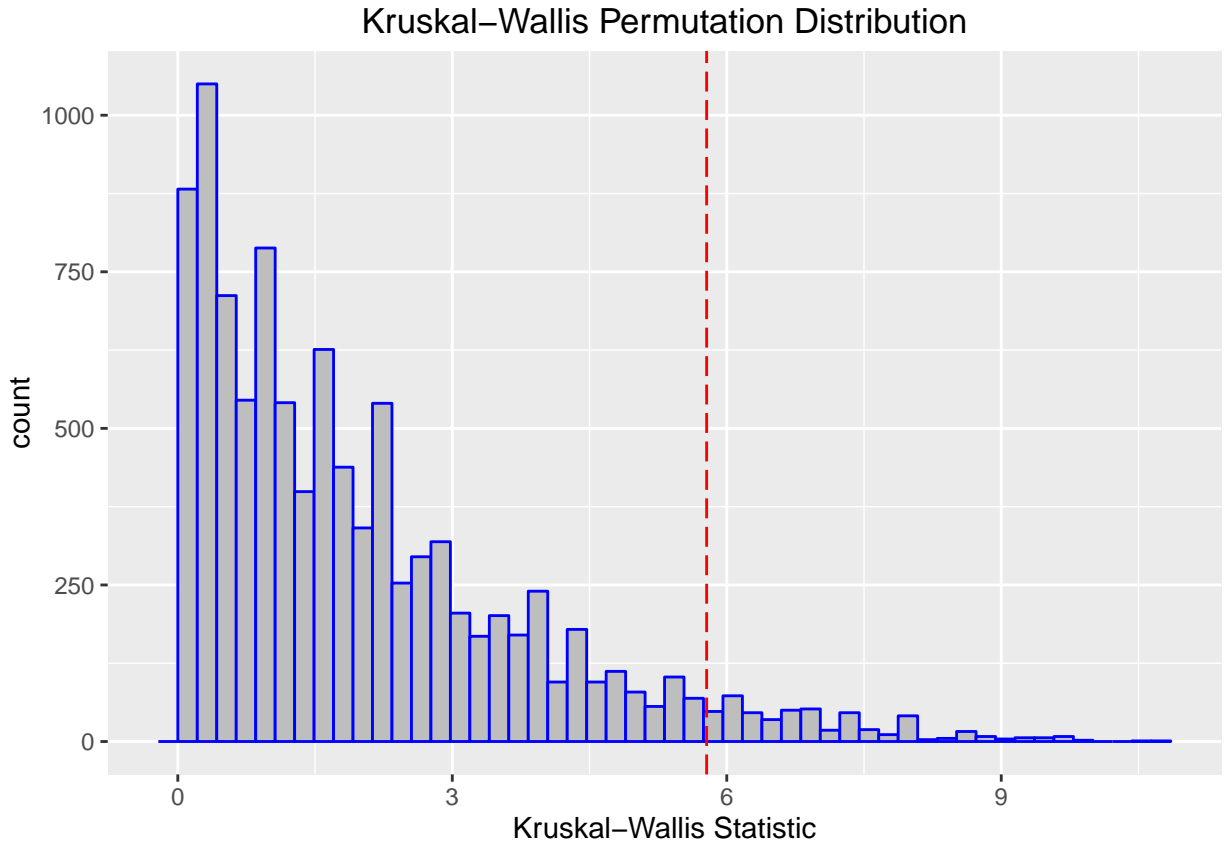
```
##
```

```
## Kruskal-Wallis rank sum test
```

```
##
```

```
## data: Y and group
```

```
## Kruskal-Wallis chi-squared = 5.78, df = 2, p-value = 0.05558
```

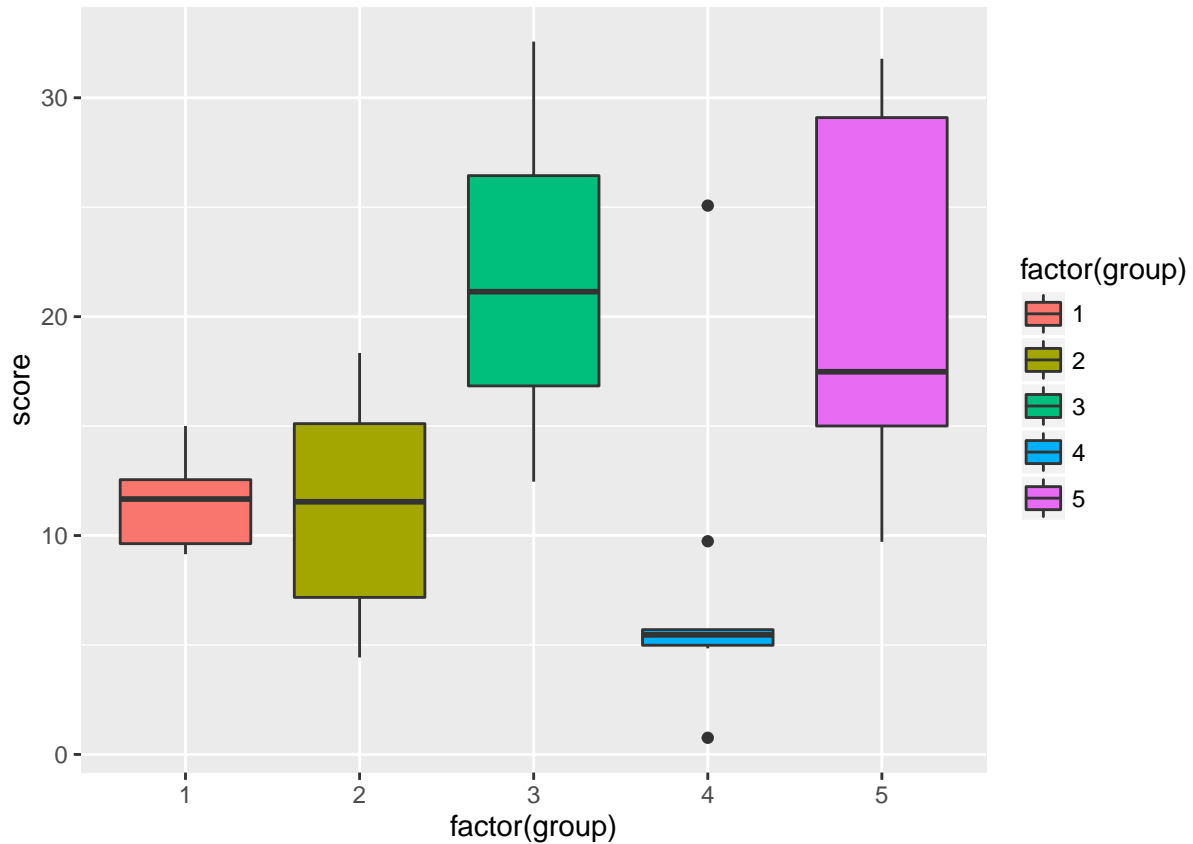


d)

We can see that for all the test performed that the p-value was never significant at the $\alpha = 0.05$ level except for the Kruskal-Wallis when done by hand. However, this was only slightly significant and very close to the programmed version of the test. The Kruskal-Wallis test was the most significant and did the best at detecting the difference in the groups because it is a rank based test and was able to perform more accurately on a small sample with outliers. The nature of the F-test allows for skew due to outliers.

Problem 2

After loading the data set, run a Kruskal-Wallis test to identify if there are differences between the ranked values belonging to each group.



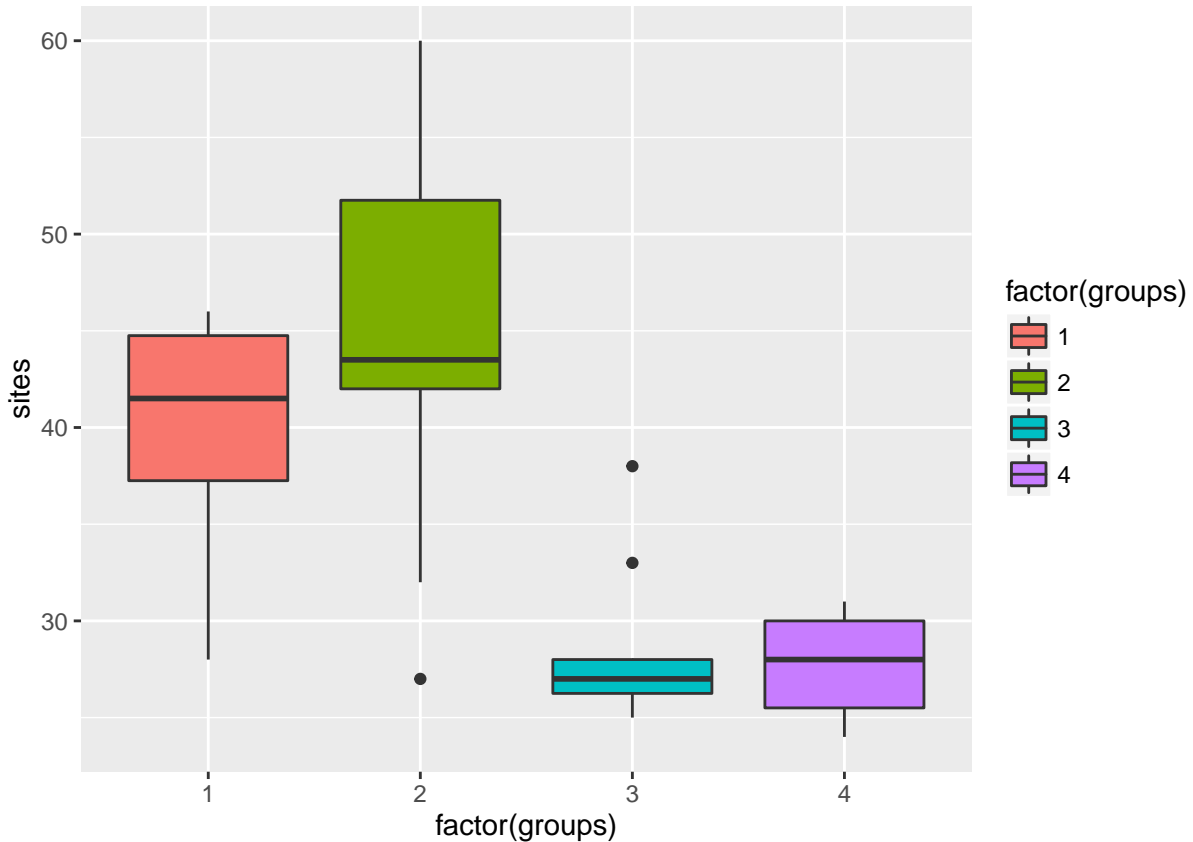
```
##  
## Kruskal-Wallis rank sum test  
##  
## data: dat2$score and dat2$group  
## Kruskal-Wallis chi-squared = 26.0329, df = 4, p-value = 3.116e-05
```

The p-value from the Kruskal-Wallis test is very small, $p = 3.116e-05$. Since we have five groups performing 10 different tests, which will create false positives by chance. To correct for this we reduce the significance level using the Bonferroni cut-off. This reduces the alpha level to match the number of test preformed. It is what is considered a conservative correction.

```
## [1] 0.005
```

We can see that even though we have made a conservative correction of alpha that the test statistic is still significant.

Problem 3



```
##  
## Kruskal-Wallis rank sum test  
##  
## data: sites and groups  
## Kruskal-Wallis chi-squared = 22.8524, df = 3, p-value = 4.335e-05
```

Here the data is loaded and plotted to show the difference between the groups. A Kruskal-Wallis test is performed to see if the ranks between any of the groups are significantly different. This test produced a p-value of 4.335e-05 which is significant at the 0.05 level. However, since there are 4 groups it is good to check the Bonferroni cut-off on alpha.

```
## [1] 0.008333333
```

The test p-value is still significant after this conservative correction.