

Modelling a brushed DC machine

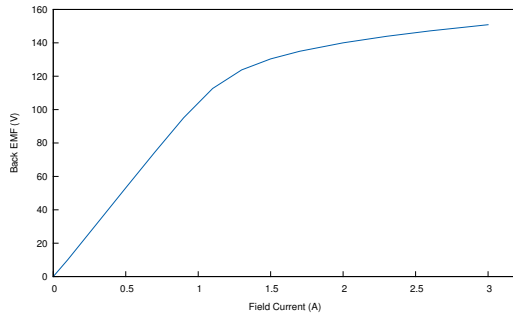
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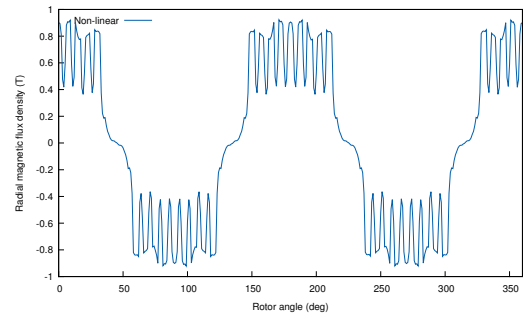
1 No-load operation

The no-load characteristics of the DC machine is given in the Fig 1(a) and the variation of radial flux density is given in Fig 1(b).

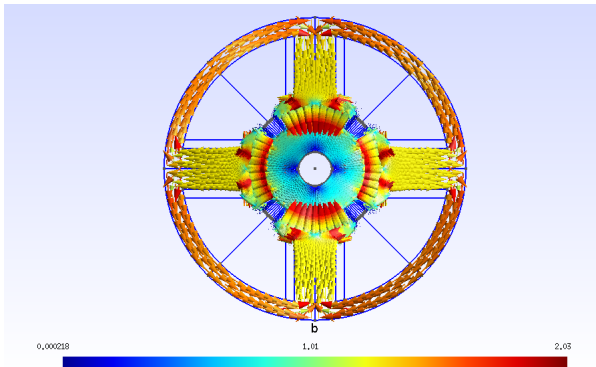
- Pole Flux= 0.014056 Wb
- $T_{rotor} = -0.01976$ Nm
- $T_{stator} = 0.02939$ Nm
- $T_{mb} = -0.02061$ Nm



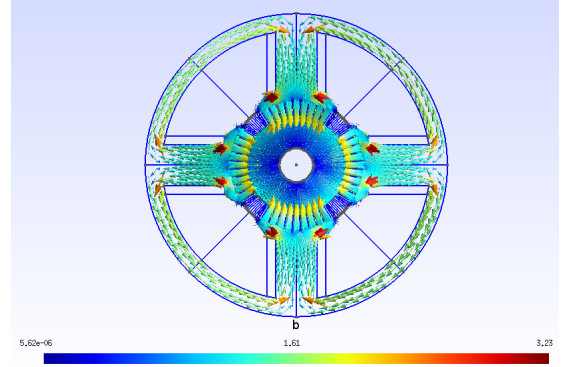
(a) No-load characteristics of DC motor



(b) Radial flux density around the airgap during no-load conditions



(c) Flux lines - saturation



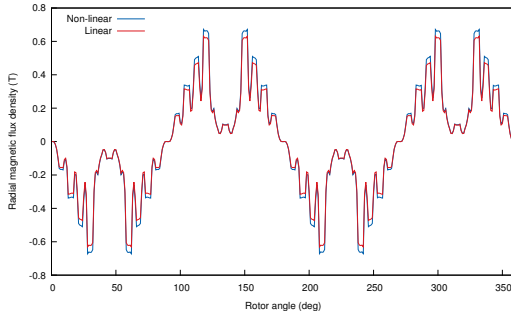
(d) Flux lines - without saturation

Figure 1: No-load operation of DC machine

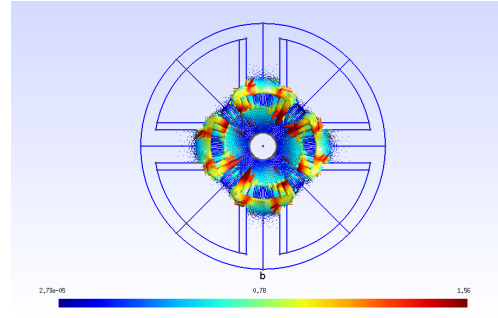
2 Operation with zero field current

The variation of radial flux density around the airgap under these condition is given in the Fig 2(a).

- Pole Flux= -6.92×10^{-7} Wb
- $T_{rotor} = -0.00236$ Nm
- $T_{stator} = 0.00934$ Nm
- $T_{mb} = -0.00293$ Nm



(a) B_{rad} around the airgap



(b) Flux lines - saturation

Figure 2: Zero Field current operation

3 Load operation

The variation of radial flux density under different loads is given in the Fig 3(a), Fig 3(b).

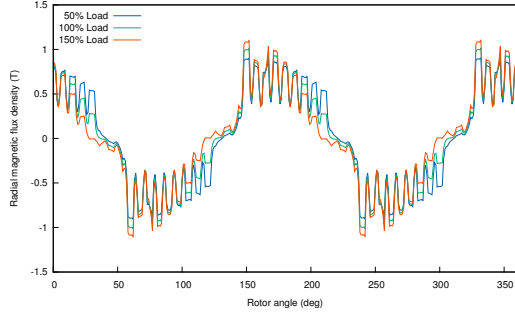
Pole flux computation The pole flux was computed using the formula given in the lab manual and the value was found to be -4.29×10^{-8} Wb which is close enough to the value computed by Gmsh i.e. -6.92×10^{-7} Wb

Torque comparison According to the data of the machine given, we found the rated torque and the torque calculated by the FEM model is given in the table below

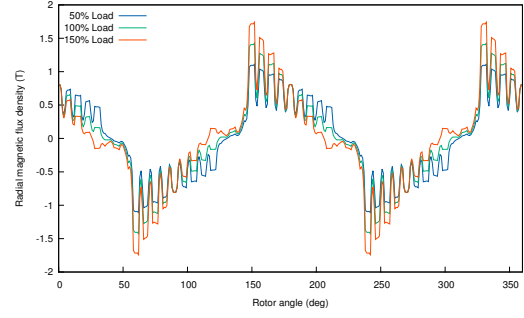
$$T_{rated} = 94.54 \text{ Nm} \quad (1)$$

Torque (Nm)	Saturation	Without saturation
T_{rotor}	96.0055	96.5586
T_{stator}	98.2271	99.616
T_{mb}	97.4709	97.9595

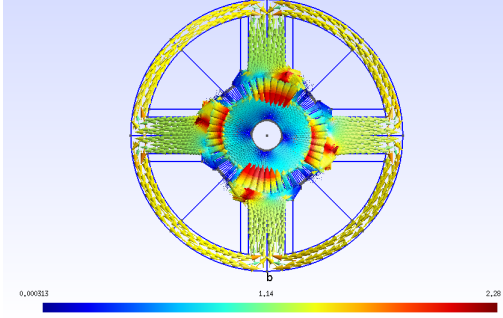
The differences in percent for the different torques ranges between 1-4 %.



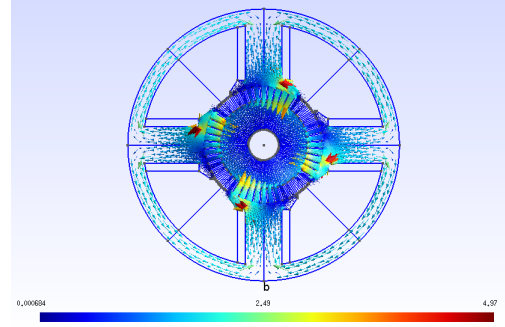
(a) B_{rad} around the airgap - saturation



(b) B_{rad} around the airgap - without saturation



(c) Flux lines - saturation



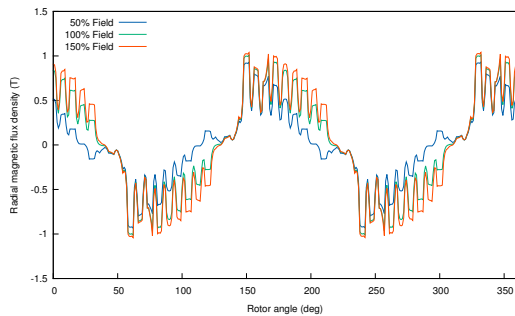
(d) Flux lines - without saturation

Figure 3: Load operation - different loadings

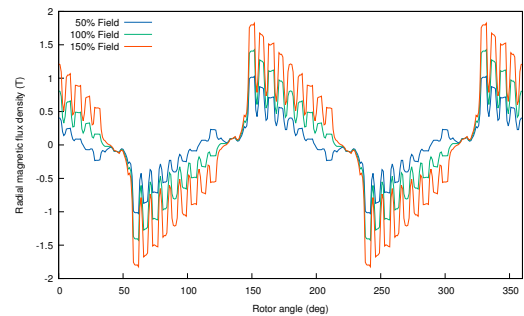
Computation of k_e In this case, we have considered the torque at the rotor airgap i.e. T_{rotor} as the reference value for computing the value of k_e . The computed values are tabulated below

Value of k_e		
Loading	Saturation	Without saturation
50%	78.9102	73.1843
100%	80.2051	73.1837
150%	81.4494	73.1843

Variation of B_{rad} for different field conditions The variation of radial flux density for different field conditions is given in Fig 4(a) and in Fig 4(b).



(a) B_{rad} around the airgap - saturation



(b) B_{rad} around the airgap - without saturation

Figure 4: Load operation - different excitation conditions

4 Other questions

Average Torque

- For non-linear case $T_{\text{avg}} = 97.2345 \text{ Nm}$
- For linear case $T_{\text{avg}} = 98.0447 \text{ Nm}$

When is torque null? Torque is proportional to the pole flux and the armature current. So, when either of them is zero then torque produced is null.

When is the pole flux maximum? The flux is at its maximum when the field current is at the maximum value and the armature current is at the minimum value as the flux is proportional to field current. However, when the machine is loaded, flux will be influenced by armature current because of the armature reaction.

When is the pole flux minimum? The flux is at its minimum when the field current is at the minimum value and the armature current is at the maximum value.

Symmetry If we have used symmetry for this model, then the smallest part of the machine that could be modelled will be half of the machine cut diagonally such that it contains two poles of the machine completely.

In such a case, the boundary conditions at the outer part of the yoke would be that the flux at that point is zero. Along the symmetric line, the derivative of the normal component of the flux is zero. This is due to the fact that amount of flux entering one part of the rotor (symmetric line) is equal to the amount of flux leaving the other part of the rotor.