

## Experiment 1-B Reciprocity Theorem

Aim: To verify the reciprocity theorem.

Theory: Consider 2-port (4-terminal) linear bilateral passive networks. Apply a voltage  $V_s$  across the first two terminals, say 1-1' and hence a current  $I$  flows through the shorted other two terminals say 2-2'. Next interchange the positions of the ammeter and the source voltage. The magnitude of the source voltage in the new position is set to  $V_s'$  and the corresponding current is  $I'$ .

The reciprocity theorem states that for passive bilateral network,

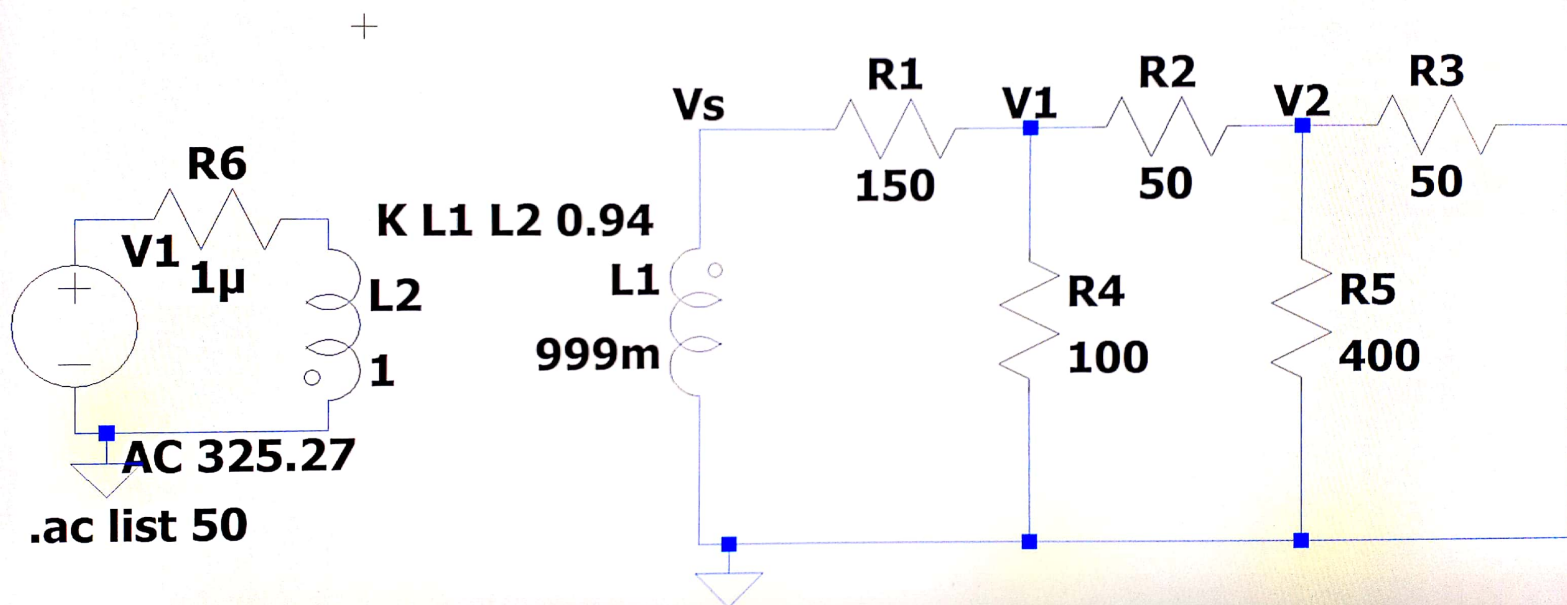
$$\frac{V_s}{I} = \frac{V_s'}{I'}$$

### LTSpice Circuit Diagrams:

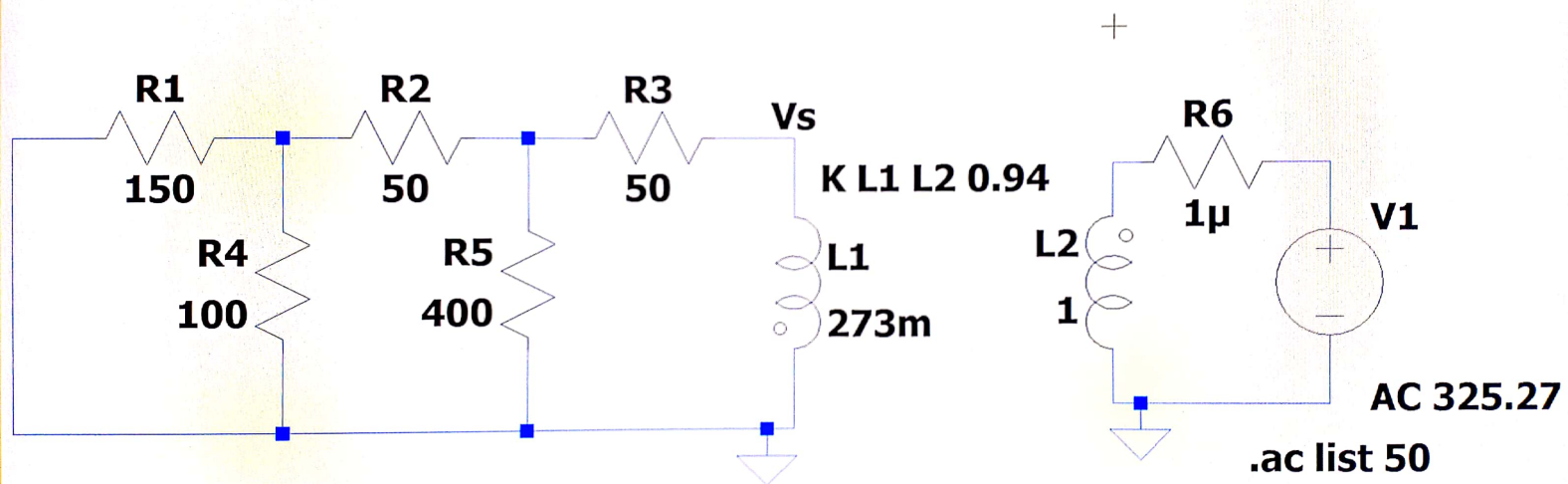
The diagrams for this experiment follows from the next page.

Note that the currents flowing through  $R_1, R_2, R_3, R_4$  and  $R_5$  are labelled as  $I_1, I_2, I_3, I_4, I_5$  and as  $I_1', I_2', I_3', I_4', I_5'$  in the first and the second configuration respectively; for the entire report.

## CONFIGURATION I



## CONFIGURATION II





Observation Table:(V<sub>s</sub>: input voltage in Config 1; V<sub>s</sub>' : in Config 2)

S.No.	V <sub>s</sub> (V)	I <sub>3</sub> (mA)	V <sub>s</sub> /I <sub>3</sub>	V <sub>s</sub> ' (V)	I <sub>1</sub> ' (mA)	V <sub>s</sub> '/I <sub>1</sub> '
01.	212.52	489	0.435	112.67	259	0.435
02.	186.66	430	0.434	161.89	373	0.434
03.	170.46	392	0.435	187.11	431	0.434

Inference / Sample Calculations:

In the observation table, for almost all the readings the ratio V<sub>s</sub>/I<sub>3</sub> was observed equal to V<sub>s</sub>'/I<sub>1</sub>'. This verifies the reciprocity theorem.

I Configuration 1 - when voltage source is connected to 1-1' and ammeter to 2-2'.

$$R_{eff} = R_1 + (R_4 \parallel (R_2 + R_3 \parallel R_5))$$

$$= R_1 + R_4 \parallel \left( R_2 + \frac{R_3 \cdot R_5}{R_3 + R_5} \right)$$

$$= 150 + 100 \parallel \left( 50 + \frac{50 \cdot 400}{50 + 400} \right)$$

$$= 150 + 100 \parallel 94.44 = 198.57 \Omega$$

$$I_1 = \frac{212.52}{198.57}$$

( $\therefore$  by ohm's law,  $I_1 = V_s / R_{eff}$ )

$$= 1.07 \text{ A.}$$



$$I_2 = I_1 \times \frac{100}{100 + 50 + 400 \parallel 50}$$

$$= I_1 \times 0.514 = 0.55 \text{ A}$$

$$I_4 = I_1 - I_2 = 0.52 \text{ A}$$

$$I_3 = I_2 \times \frac{400}{400 + 50} = 0.49 \text{ A}$$

$$I_5 = I_2 - I_3 = 0.06 \text{ A}$$

$$V_1 = V_s - R_1 I_1 \text{ (junction of } R_1, R_2, R_4)$$

$$= 212.52 - 150 \times 1.07 = 52.02 \text{ V}$$

$$V_2 = V_1 - R_2 I_2 \text{ (junction of } R_2, R_3, R_5)$$

$$= 52.02 - 50 \times 0.55 = 24.52 \text{ V}$$

$$\star I_1 = 1.07 \text{ A}, I_2 = 0.55 \text{ A}, I_3 = 0.49 \text{ A}$$

$$I_4 = 0.52 \text{ A}, I_5 = 0.06 \text{ A}$$

$$V_1 = 52.02 \text{ V}, V_2 = 24.52 \text{ V}$$

II Configuration 2 - when voltage source is connected to 2-2' and ammeter to 1-1'.

$$R_{\text{eff}} = R_3 + (R_5 \parallel (R_2 + (R_1 \parallel R_4)))$$

$$= 50 + (400 \parallel (50 + \frac{150 \cdot 100}{150 + 100}))$$

$$= 50 + 400 \parallel 110 = 79.33 \text{ A}$$

$$136.27 \Omega$$

$$I_3' = V_{s1} / R_{\text{eff}} \text{ (by ohm's law)}$$

$$= 112.67 / 136.27 = 0.83 \text{ A}$$



$$I_2' = I_3' \times \frac{400}{400 + 50 + 100 || 150}$$

$$= I_3' \times 0.784 = 0.83 \text{ A} \times 0.784 = 0.65 \text{ A}$$

$$I_5' = I_3' - I_2' = 0.83 \text{ A} - 0.65 \text{ A} = 0.18 \text{ A}$$

$$I_1' = I_2' \times \frac{100}{100 + 150}$$

$$= 0.65 \text{ A} \times 0.4 = 0.26 \text{ A}$$

$$I_4' = I_2' - I_1' = 0.65 \text{ A} - 0.26 \text{ A} = 0.39 \text{ A}$$

$$V_3 = V_5' - R_3 I_3' \text{ (junction of } R_2, R_3, R_5)$$

$$= 112.67 - 50 \times 0.83 = 71.17 \text{ V}$$

$$V_4 = V_3 - R_2 I_2' \text{ (junction of } R_1, R_2, R_4)$$

$$= 71.17 - 50 \times 0.65 = 38.67 \text{ V}$$

★  $I_1' = 0.26 \text{ A}$ ,  $I_2' = 0.65 \text{ A}$ ,  $I_3' = 0.83 \text{ A}$   
 $I_4' = 0.39 \text{ A}$ ,  $I_5' = 0.18 \text{ A}$   
 $V_3 = 71.17 \text{ V}$ ,  $V_4 = 38.67 \text{ V}$

Discussion: The values of the ratios  $V_5/I_3$  and  $V_5'/I_1'$  are very similar for all the readings recorded in the table. Therefore the experiment was successful in verifying the reciprocity theorem. Besides, the values of branch currents for the two configurations corresponding to the first reading were calculated theoretically using Ohm's law.

and Kirchhoff's rules. The values of the branch currents  $I_3$  and  $I_1'$  were extremely close to the values that were predicted theoretically through calculations.