2

Visualization of Qualitative Data

SECTIONS

CHAPTER OBJECTIVES

In this chapter, we introduce graphs to visualize qualitative data such as a bar graph, a pie chart, a band graph and a line graph in Section 2.1.

In Section 2.2, we discuss visualization of summary data of single categorical variable using 『eStat』. Visualization of summary data of a categorical variable by a group is also discussed.

In Section 2.3, we discuss visualization of raw data of a categorical variable using 『eStat』. Visualization of raw data of a categorical variable by a group is also discussed.

2.1 Visualization of Qualitative Data

- Data of gender for students in a classroom, which are either a male or a female, are referred to as **qualitative data**. Data of marital status for employees in a company, which are either single or married, are also qualitative data. A bar graph, a pie chart, a band graph, and a line graph are used to visualize the qualitative data. These graphs are frequently used as an **exploratory data analysis** of the qualitative data.
- A **bar chart** (or **bar graph**) is a graph that presents the qualitative data with rectangular bars in a way that their heights (or lengths) are proportional to frequencies of their categories. Therefore, the frequencies of all categories in a categorical variable can be easily compared by watching the heights (or lengths) of the rectangular bars. We usually put some space between the rectangular bars to emphasize that they represent the distinct categories of a variable.

- The rectangular bars of the bar chart can be plotted either vertically or horizontally. One axis of the chart shows all categories of a variable, and the other axis represents the frequencies of each category. If the frequency of each category is represented as a vertical height of a bar drawn up and down in the bar graph, it is called a **vertical bar graph**. A bar can also be drawn left and right whose length is proportional to the frequency of each category and it is called a **horizontal bar graph**.
- A bar graph can be drawn after counting frequencies of all categories of a variable. If there is another categorical variable, frequencies of all categories of the first categorical variable can be counted for each category of the second categorical variable. For example, we can count the number of single and married employees for both a male and a female category. We can draw two bar graphs of the marital status for both the male and the female categories so that both graphs have the same scale of Y-axis to compare the frequencies of the male category with the frequencies of the female category easily. This graph is called a **separated bar graph** of the marital status by gender variable. In this case, the gender variable is called a **group variable** and the marital status is called an **analysis variable**.
- If a variable is analysed by using a group variable, there are many variants of bar graphs which compare visually well all categories of the group variable. A **stacked bar graph** divides a single bar, which represents the frequency of a category of the analysis variable, into pieces with different colors which are proportional to the frequency of each category of the group variable. A **ratio bar graph** draws that all bars (rectangles) of each category of the analysis variable have the same height and divides each bar into pieces with different colors which are proportional to the frequencies of each category of the group variable. A **side by side bar graph** is that in each category of the analysis variable rectangular bars of all categories of the group variable are drawn side by side ways for comparison using the same scale. If there are only two categories of the group variable, a **two-sided bar graph** (or a **bi-lateral bar graph)** can be used which draws bars of one category of the group variable in one side and bars of the other category of the group variable in the opposite direction. The direction can be either the left and right side of the Y-axis or the above and below of the X-axis.
- A **pie chart** is a graph that shows frequencies of all categories of the analysis variable by dividing a pie (circle) into pieces with different colors depending on angle which is proportional to the frequency of each category. We usually draw the largest piece of category in a clockwise order starting from 12 oclock so that the ratio can be compared well.

- A **doughnut chart** which removes a center circle of the pie chart can also be

used

- A **band graph** is similar to the ratio bar graph that shows frequencies of all categories of the analysis variable by dividing a rectangle into square pieces with different colors which are proportional to frequencies of all categories. It is also similar to the pie chart. The square pieces can be sorted in descending order by the frequencies of each category, but 『eStat』 draw the square pieces in the order of category values of a categorical variable.

- A **line graph** shows frequencies (or values) of all categories of an analysis variable in a two-dimensional graph. The X-axis shows names of categories and the Y-axis represents the scale of frequencies (or values) of all categories. Each pair of the values, the category name and its frequency, is marked as a point in a two-dimensional coordinate plane and two adjacent points are connected with a line. The line graph may be similar to the vertical bar graph which connects only top centers of each bar. The line graph is usually used to visualize time dependent data to watch its trend over time. For example, the yearly amount of export in a country can be visualized using the line graph.

Definition

Graphs for Qualitative Data

A **bar chart** (or bar graph) is a graph that shows qualitative data with rectangular bars with heights or lengths proportional to frequencies of their categories.

A **pie chart** is a graph that shows frequencies of all categories of an analysis variable by dividing a pie (circle) into pieces with different colors depending on angle which is proportional to the frequency of each category.

A **band graph** is similar to the ratio bar graph that shows frequencies of all categories of an analysis variable by dividing a rectangle into square pieces with different colors which are proportional to frequencies of all categories.

A **line graph** shows frequencies (or values) of all categories of an analysis variable in a two-dimensional graph.

- This chapter discusses how qualitative data are visualized using 『eStat』 by dividing the case of summary data (Section 2.2) and raw data (Section 2.3) and by dividing the case of single analysis variable and the case of an analysis varible with the group variable.

2.2 Visualization of Summary Data

- In this section visualization of summary data without a group variable and visualization of summary data with a group variable are discussed.

2.2.1 Summary Data of Categorical Variable

- If you investigated a gender of students in a class and reported the result as follows:

  'male', 'female', 'male', 'female', 'male'. 'male', .'male', 'female', 'female', 'male'...

  This data is called the **raw data** of the gender variable which is a categorical

variable.

- If you counted the number of 'male' students and 'female' students in the above raw data and reported the result as shown in Table 2.2.1.

Table 2.2.1 Summary data of the gender in a class

Gender	Students
Male	6
Female	4

This data is called the **summary data** of the gender variable.

- If the number of data increases, counting the number of cases in each category from the raw data of a categorical variable in order to make the summary data is not an easy task. One of the important functions of a statistical package is to organize the raw data into the summary data by counting the number of cases in each category. Because of this difficult task to generate the summary data from the raw data, governmental institutions usually provide statistics of a census to the public in the form of the summary data such as the number of population by gender or the number of population by region. These summary data can be downloaded from the governmental home page as an Excel file.
- An Excel file can be saved as a text file in CSV (comma separated value) format (refer <Figure A.2.6> in Appendix A) which can be loaded by 『eStat』 for data processing and analysis (refer Appendix A).
- This section discusses visualization of the summary data of a categorical variable which can also be found in textbooks of an elementary, a middle school, a high school and in governmental publications.

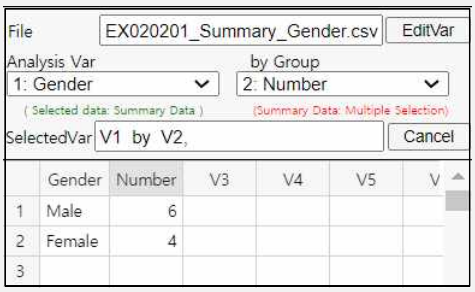
Example 2.2.1

(Gender Summary Data)

Enter the summary data of Table 2.2.1 to the sheet of 『eStat』 and save it as a file in CSV format. Using this data, draw a bar graph, a pie chart and a band graph with 『eStat』. Analyze the graphs and prepare a report using the MS Word (or any word processor you prefer).

Answer

- Enter the data of Table 2.2.1 to the sheet of 『eStat』 as in <Figure 2.2.1> and enter a variable name of V1 as 'Gender' and of V2 as 'Number' using [Edit Var] button located above the sheet (refer Appedix A.2).

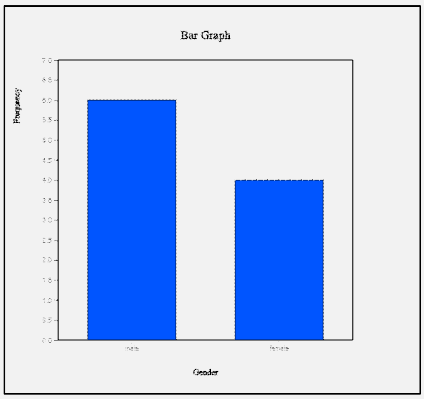


<Figure 2.2.1> Data input in 『eStat』

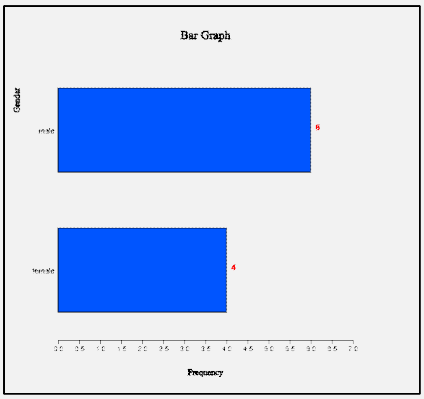
- Click the first variable name 'Gender' and then the second variable name 'Number'. Selected variables will be appeared in the box of the 'Selected Var' located above the sheet. You can select the variable '1: Gender' using the combo box of the 'Analysis Var' and the variable '2: Number' using the combo box of the 'By Group' located above the sheet as shown in <Figure 2.2.1>.

Example 2.2.1 Answer (continued)

- When variables are selected, a vertical bar graph which is the default graph of 『eStat』 is drawn as in <Figure 2.2.2>. The height of each bar (rectangle) is proportional to the frequency of each category in the gender variable and therefore, the frequencies of both the male and the female categories can be easily compared by watching the heights of bars. The bar graph shows that the number of male students is larger than the number of female students.
- A vertical bar graph which draws bars up and down as in <Figure 2.2.2> is widely used, but a horizontal bar graph which draws bars from left to right is often used if there are many categories. By clicking on the icon located above the Graph Area, a horizontal bar graph as in <Figure 2.2.3> will be appeared in the Graph Area. By checking the 'Frequency' box located below of the graph, the frequency of each bar. will be displayed.

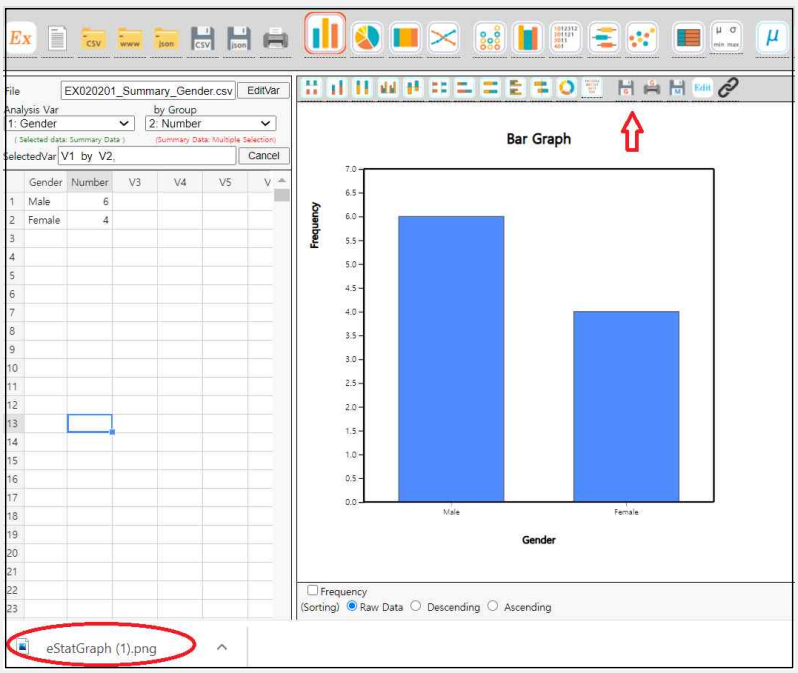


<Figure 2.2.2> Vertical bar graph of the number of male and female students.



<Figure 2.2.3> Horizontal bar graph of the number of male and female students.

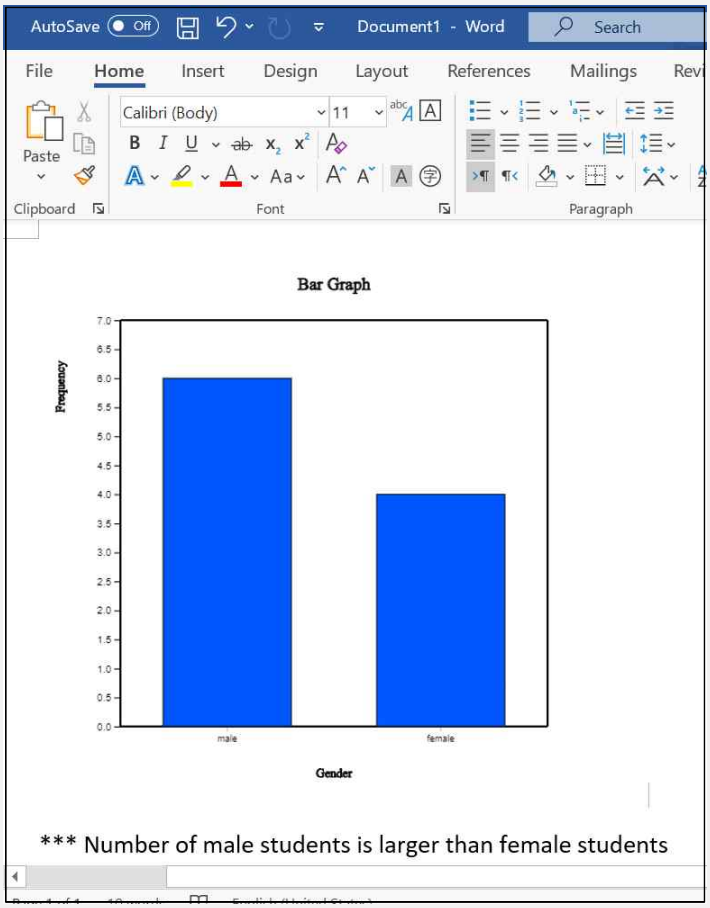
- By clicking the 'Graph Save' icon located above the Graph Area, the current graph of the Graph Area will be saved with a file name 'eStatGraph.png' which is shown at the bottom left corner of the main screen as in <Figure 2.2.4> (Refer Appendix A.4).



<Figure 2.2.4> Graph is saved by clicking the 'Graph Save' icon

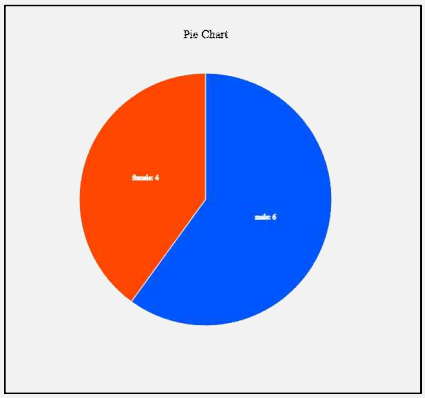
Example 2.2.1 Answer (continued)

- The location of the saved graph file is the download folder specified in your computer system. If you save another graph, eStatGraph(1).png will be created in the download folder. Number in parentheses of the file name will be increased whenever you save a new graph.
- You can copy this graph file from the download folder and paste to the MS Word as in <Figure 2.2.5>. You can also write comments about the graph if necessary.

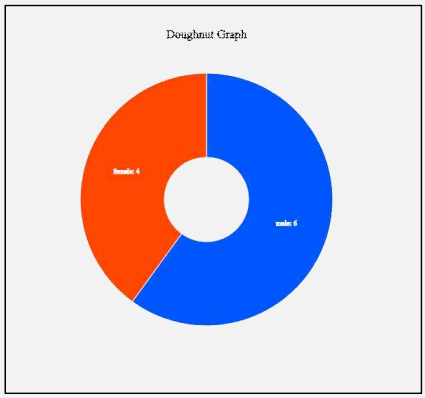


<Figure 2.2.5> Copied graph file of 『eStat』 to MS Word

- Click on the icon to display a pie chart as in <Figure 2.2.6> and click on the icon to display a doughnut graph as in <Figure 2.2.7> which is a pie chart but a small middle circle is cut off. The pie chart shows frequencies of the number of both male and female students by dividing a pie (circle) into pieces with two colors depending on angles which are proportional to the frequencies of each category.



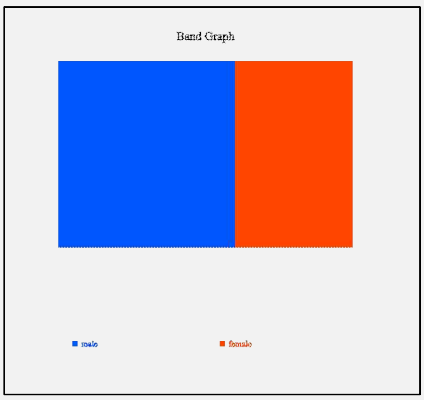
<Figure 2.2.6> Pie chart of the number of male and female students.



<Figure 2.2.7> Doughnut chart of the number of male and female students.

Example 2.2.1 Answer (continued)

- Click on the icon to display a band graph as in <Figure 2.2.8>. A band graph is a variant of the pie chart by dividing a rectangle into square pieces which are proportional to frequencies of each category. It is named after a rectangular shape with multiple square pieces which looks like a band.



<Figure 2.2.8> Band graph of the number of male and female students.

- International institutions such as UN, OECD and EU release their statistics to the public in the form of summary data and this data can be downloaded as an Excel file or a text file in CSV format. The following example shows how to download a file from the OECD and how to draw graphs using this file.

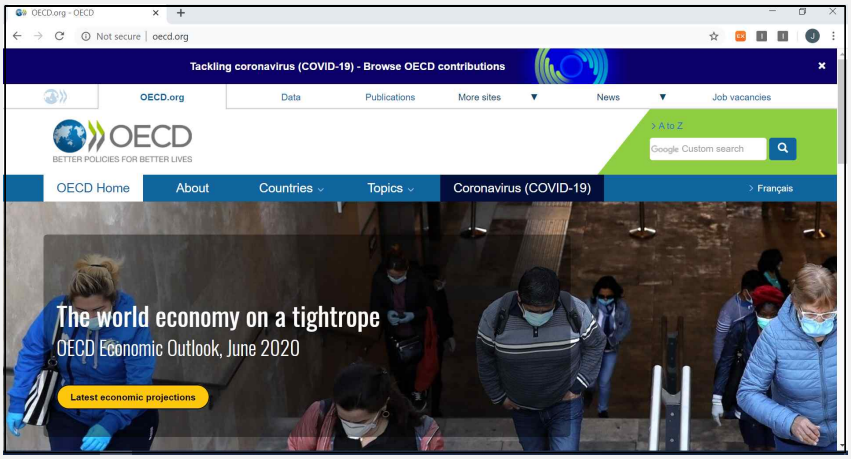
Example 2.2.2

(Life Expectancy at Birth : Source OECD)

From the home page of the OECD, https://www.oecd.org, download a data file of the life expectancy at birth. Copy the columns of the country name and 2017 data located at the last column to 『eStat』 system and save it as a file in CSV format. Using this data, draw a vertical bar graph and a horizontal bar graph in descending order of the life expectancy. Analyze the graphs.

Answer

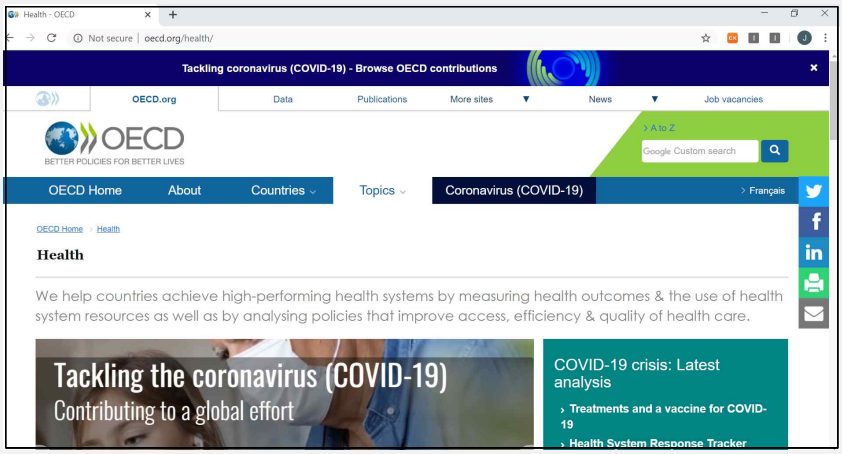
- The main screen of the OECD website as of June 2020, https://www.oecd.org, looks like as in <Figure 2.2.9>.



<Figure 2.2.9> OECD home page

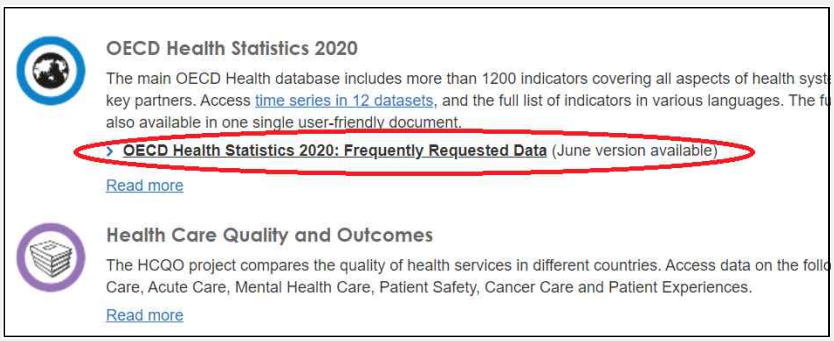
Example 2.2.2 Answer (continued)

- Select the menu **Topics > Health,** then the screen as in <Figure 2.2.10> will be appeared.



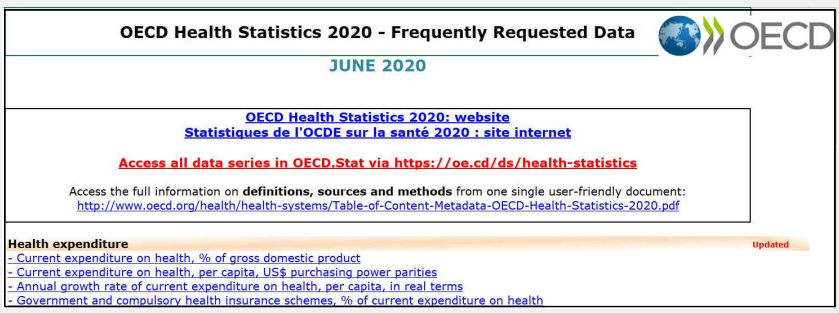
<Figure 2.2.10> OECD 'Topic' > 'Health' menu

- If you click on '**Explore all our data on health**', the screen as in <Figure 2.2.11> will be appeared.



<Figure 2.2.11> OECD Health Statistics

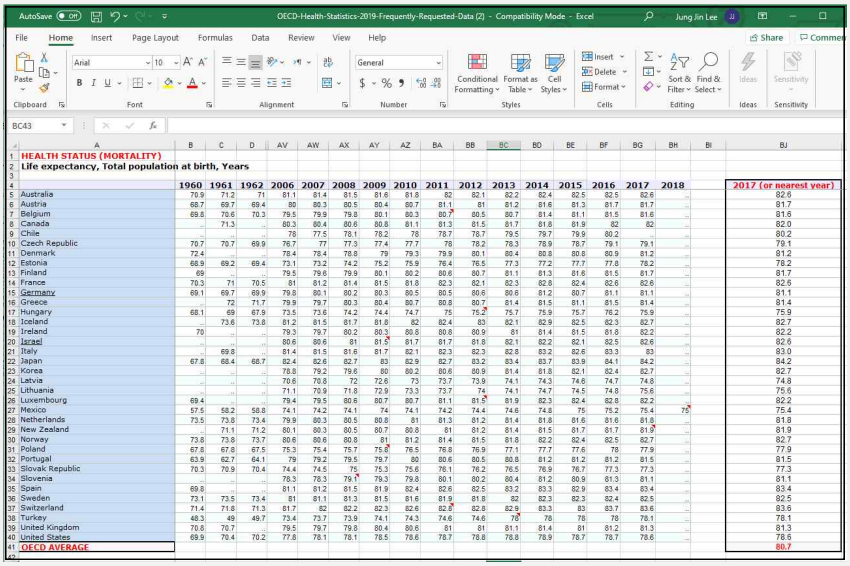
- If you click on '**> OECD Health Statistics 2020: Frequently Requested Data**', an Excel file of OECD-Health-Statistics-2019-Frequently-Requested-Data.xls is downloaded. If you open the Excel file, the menu as in <Figure 2.2.12> is appeared.



<Figure 2.2.12> OECD Statistics for life expectancy at birth

- If you click on '**Life expectancy at birth, total population**' in Health status (Mortality), an Excel file as in <Figure 2.2.13> will be appeared on the screen.

Example 2.2.2 Answer (continued)



HEALTH STATUS (MORTALITY)																	
Life expectancy, Total population at birth, Years																	
	1960	1961	1962	2006	2007	2008	2009	2010	2011	2012	2013	2014	2015	2016	2017	2018	2017 (or nearest year)
Australia	70.9	71.2	71	81.1	81.4	81.5	81.6	81.8	82	82.1	82.2	82.4	82.5	82.5	82.6	..	82.6
Austria	68.7	69.7	69.4	80	80.3	80.5	80.4	80.7	81.1	81	81.2	81.6	81.3	81.7	81.7	..	81.7
Belgium	69.8	70.6	70.3	79.5	79.9	79.8	80.1	80.3	80.7	80.5	80.7	81.4	81.1	81.5	81.6	..	81.6
Canada	..	71.3	..	80.3	80.4	80.6	80.8	81.1	81.3	81.5	81.7	81.9	81.9	82	82	..	82.0
Chile	..	..	..	78	77.5	78.1	78.2	78	78.7	78.7	79.5	79.7	79.9	80.2	..	..	80.2
Czech Republic	70.7	70.7	69.9	76.7	77	77.3	77.4	77.7	78	78.2	78.3	78.9	78.7	79.1	79.1	..	79.1
Denmark	72.4	..	..	78.4	78.4	78.8	79	79.3	79.9	80.1	80.4	80.8	80.8	80.9	81.2	..	81.2
Estonia	68.9	69.2	69.4	73.1	73.2	74.2	75.2	75.9	76.4	76.5	77.3	77.2	77.7	77.8	78.2	..	78.2
Finland	69	..	..	79.5	79.6	79.9	80.1	80.2	80.6	80.7	81.1	81.3	81.6	81.5	81.7	..	81.7
France	70.3	71	70.5	81	81.2	81.4	81.5	81.8	82.3	82.1	82.3	82.8	82.4	82.6	82.6	..	82.6
Germany	69.1	69.7	69.9	79.8	80.1	80.2	80.3	80.5	80.5	80.6	80.6	81.2	80.7	81.1	81.1	..	81.1
Greece	..	72	71.7	79.9	79.7	80.3	80.4	80.7	80.8	80.7	81.4	81.5	81.1	81.5	81.4	..	81.4
Hungary	68.1	69	67.9	73.5	73.6	74.2	74.4	74.7	75	75.2	75.7	75.9	75.7	76.2	75.9	..	75.9
Iceland	..	73.6	73.8	81.2	81.5	81.7	81.8	82	82.4	83	82.1	82.9	82.5	82.3	82.7	..	82.7
Ireland	70	..	..	79.3	79.7	80.2	80.3	80.8	80.8	80.9	81	81.4	81.5	81.8	82.2	..	82.2
Israel	..	..	..	80.6	80.6	81	81.5	81.7	81.7	81.8	82.1	82.2	82.1	82.5	82.6	..	82.6
Italy	..	69.8	..	81.4	81.5	81.6	81.7	82.1	82.3	82.3	82.8	83.2	82.6	83.3	83	..	83.0
Japan	67.8	68.4	68.7	82.4	82.6	82.7	83	82.9	82.7	83.2	83.4	83.7	83.9	84.1	84.2	..	84.2
Korea	..	..	..	78.8	79.2	79.6	80	80.2	80.6	80.9	81.4	81.8	82.1	82.4	82.7	..	82.7
Latvia	..	..	..	70.6	70.8	72	72.6	73	73.7	73.9	74.1	74.3	74.6	74.7	74.8	..	74.8
Lithuania	..	..	..	71.1	70.9	71.8	72.9	73.3	73.7	74	74.1	74.7	74.5	74.8	75.6	..	75.6
Luxembourg	69.4	..	..	79.4	79.5	80.6	80.7	80.7	81.1	81.5	81.9	82.3	82.4	82.8	82.2	..	82.2
Mexico	57.5	58.2	58.8	74.1	74.2	74.1	74	74.1	74.2	74.4	74.6	74.8	75	75.2	75.4	75	75.4
Netherlands	73.5	73.8	73.4	79.9	80.3	80.5	80.8	81	81.3	81.2	81.4	81.8	81.6	81.6	81.8	..	81.8
New Zealand	..	71.1	71.2	80.1	80.3	80.5	80.7	80.8	81	81.2	81.4	81.5	81.7	81.7	81.9	..	81.9
Norway	73.6	73.8	73.7	80.6	80.6	80.8	81	81.2	81.4	81.5	81.8	82.2	82.4	82.5	82.7	..	82.7
Poland	67.8	67.8	67.5	75.3	75.4	75.7	75.8	76.5	76.8	76.9	77.1	77.7	77.6	78	77.9	..	77.9
Portugal	63.9	62.7	64.1	79	79.2	79.5	79.7	80	80.6	80.5	80.8	81.2	81.2	81.2	81.5	..	81.5
Slovak Republic	70.3	70.9	70.4	74.4	74.5	75	75.3	75.6	76.1	76.2	76.5	76.9	76.7	77.3	77.3	..	77.3
Slovenia	..	..	..	78.3	78.3	79.1	79.3	79.8	80.1	80.2	80.4	81.2	80.9	81.3	81.1	..	81.1
Spain	69.8	..	..	81.1	81.2	81.5	81.9	82.4	82.6	82.5	83.2	83.3	82.9	83.4	83.4	..	83.4
Sweden	73.1	73.5	73.4	81	81.1	81.3	81.5	81.6	81.9	81.8	82	82.3	82.3	82.4	82.5	..	82.5
Switzerland	71.4	71.8	71.3	81.7	82	82.2	82.3	82.6	82.8	82.8	82.9	83.3	83	83.7	83.6	..	83.6
Turkey	48.3	49	49.7	73.4	73.7	73.9	74.1	74.3	74.6	74.6	75	78	78	78	78.1	..	78.1
United Kingdom	70.8	70.7	..	79.5	79.7	79.8	80.4	80.6	81	81	81.1	81.4	81	81.2	81.3	..	81.3
United States	69.9	70.4	70.2	77.8	78.1	78.1	78.5	78.6	78.7	78.8	78.8	78.9	78.7	78.7	78.6	..	78.6
OECD AVERAGE																	80.7

<Figure 2.2.13> OECD Statistics for life expectancy at birth

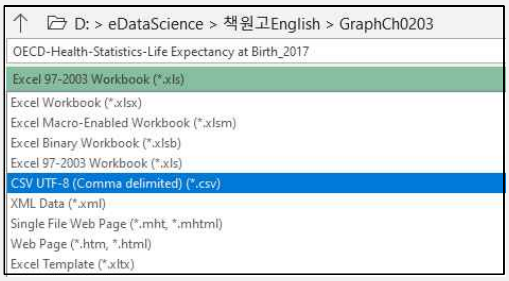
- The easiest way to make a file in CSV format is to copy the country name to the first column of the sheet of 『eStat』 and the column of 2017 data located at the last column of this Excel file to the second column of the sheet of 『eStat』 as in <Figure 2.2.14>. After you provide variable names 'Country' and 'Years' by using **[Edit Var]** of 『eStat』, save the data as a file, for example, 'EX020202_**OECD_LifeExpectancy.csv**' in CSV format,.

	Country	LifeExp	V3	V4
1	Australia	82.6		
2	Austria	81.7		
3	Belgium	81.6		
4	Canada	82.0		
5	Chile	80.2		
6	Czech Republic	79.1		
7	Denmark	81.2		
8	Estonia	78.2		
9	Finland	81.7		
10	France	82.6		
11	Germany	81.1		
12	Greece	81.4		
13	Hungary	75.9		
14	Iceland	82.7		
15	Ireland	82.2		
16	Israel	82.6		
17	Italy	83.0		
18	Japan	84.2		
19	Korea	82.7		
20	Latvia	74.8		
21	Lithuania	75.6		
22	Luxembourg	82.2		
23	Mexico	75.4		
24	Netherlands	81.8		
25	New Zealand	81.9		

<Figure 2.2.14> OECD life expectancy at birth in 2017

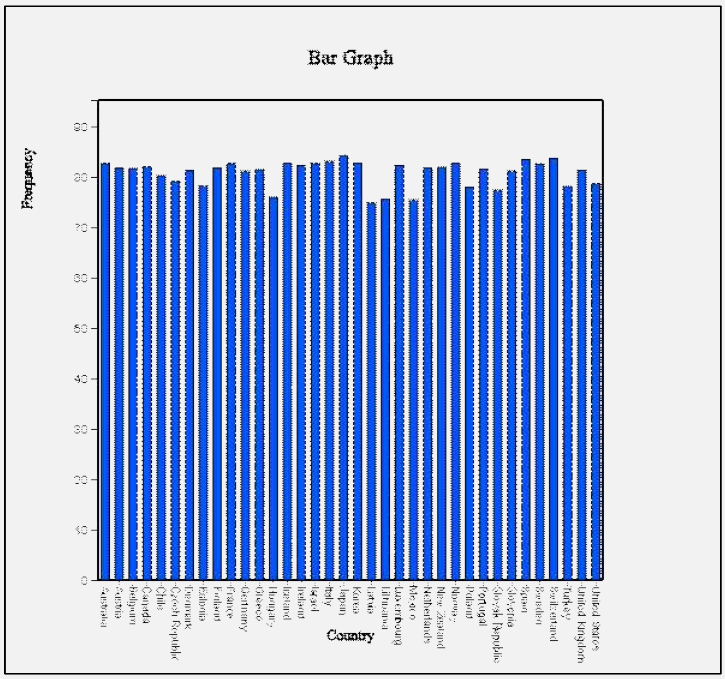
Example 2.2.2 Answer (continued)

- Another way is to edit the Excel file in <Figure 2.2.13> with only two columns, the country name and 2017 data similar to <Figure 2.2.14>, and save it as a file in CSV format. In this case, the first row should have variable names such as 'Country' and 'Number' (refer Appendix A.2).. In order to save this file in CSV format, select the Excel menu **'File' > 'Save As',** then a dialogue box as in <Figure 2.2.15> will be appeared. Select the option '**CSV Utf-8**', then the file will be saved in CSV format in the download folder of your computer. Note that, if you are using an European version of Excel, you have to change the delimiter of semicolon ';' with comma ',' before you save the file (refer Excel option).



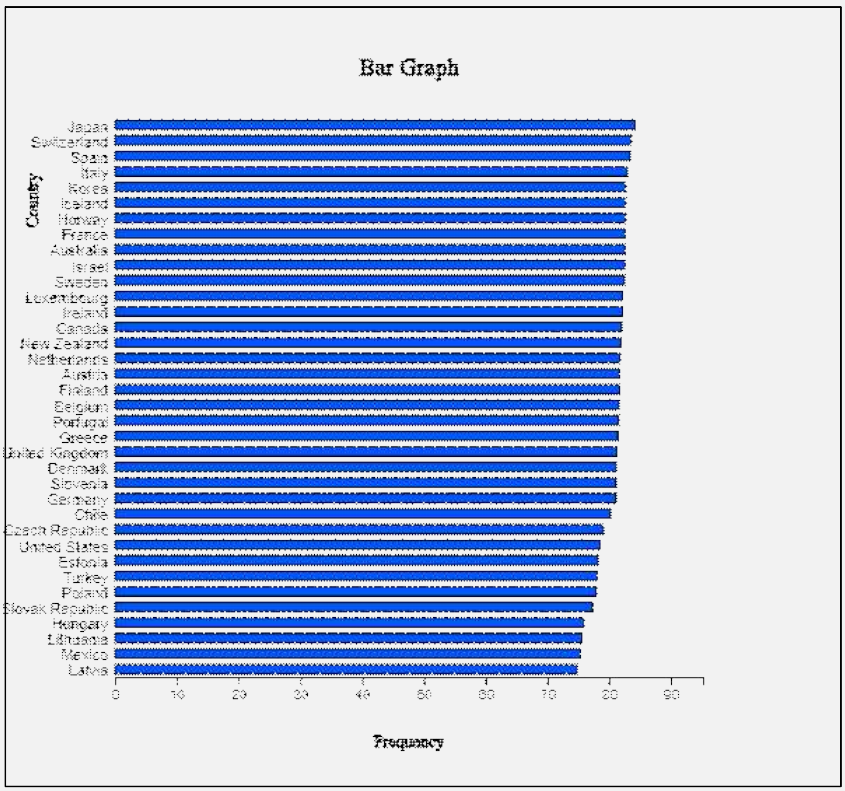
<Figure 2.2.15> OECD

- Click the variable names 'Country' and 'Number' on the sheet of 『eStat』, then a vertical bar graph of the life expectancy will be appeared as in <Figure 2.2.16>. If the characters of the country name are too small to see, you can enlarge the screen by holding the [Ctrl] key and rolling up the wheel mouse. You can click on the icon located above the Graph Area to draw a horizontal bar graph as in <Figure 2.2.17>.
- It is sometimes convenient to compare data using a horizontal bar graph after sorting. If you check a sorting option 'Descending' located below the graph, a horizontal bar graph sorted by descending order of the life expectancy at the birth will be appeared as in <Figure 2.2.17>. It is easy to check that Japan is the longest life expectancy, Switzerland is the second and Latvia is the shortest.



<Figure 2.2.16> Vertical bar graph of OECD life expectancy at birth in 2017

Example 2.2.2 Answer (continued)



<Figure 2.2.17> Horizontal bar graph of OECD life expectancy at birth, 2017

[Practice 2.2.1]

(Alcohol Expenditure: OECD)

Draw a bar graph using the following data in 『eStat』 system and analyze the graph.

Ex ⇨ eBook ⇨ PR020201_OECD_AlcoholExpenditure_2013.csv

[Practice 2.2.2]

(Obesity Ratio: World)

Draw a bar graph using the following data in 『eStat』 system and analyze the graph.

Ex ⇨ eBook ⇨ PR020202_WORLD_ObesityRatio_Age15over__2017

2.2.2 Summary Data of Categorical Variable with Group

- The summary data as in Table 2.2.1 can be easily extended if you survey the gender of two classes in a school as in Table 2.2.2. It is the summary data of the gender variable for two classes (groups), classes of 5-1 and 5-2. In this case, we usually want to compare the summary data between two classes (groups) using graphs as the following example.

Table 2.2.2 Summary data of two classes

Gender	5-1	5-2
Male	16	12
Female	14	18

Example 2.2.3

(Gender Summary Data of Two Classes)

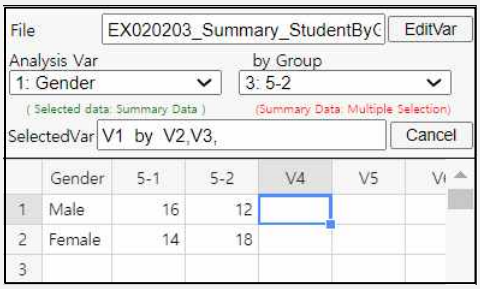
A file of the summary data in Table 2.2.2 is saved at the following location of 『eStat』 system.

Ex ⇨ eBook ⇨ EX020203_Summary_StudentByGender

Using this data, draw a bar graph, a pie chart and a band graph. Use 『eStat』.

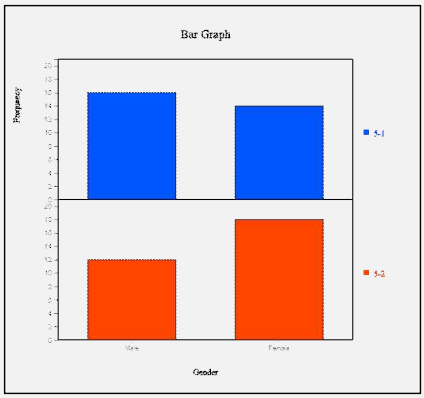
Answer

- If you load the data file from 『eStat』, it looks like as in <Figure 2.2.18>.

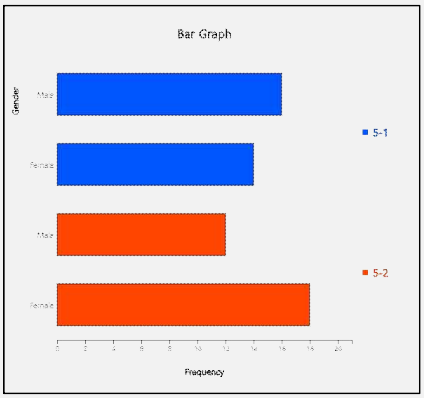


<Figure 2.2.18> Load file of summary data

- Click the variable names 'Gender', '5-1' and '5-2' sequentially, then the selected variables will be appeared at the box of 'Selected Var' located above the sheet. You can select the variable '1: Gender' using the combo box of the 'Analysis Var' and the variable '2: 5-1' and '3: 5-2' using the combo box of the 'By Group' located above the sheet.
- When the variables are selected, a vertical bar graph which is the default graph of 『eStat』 is drawn using the number of male and female students in both classes as in <Figure 2.2.19>. A bar graph is drawn for each class and the heights of bars are the frequencies of male and female students. Two bar graphs has the same scale of Y-axis and therefore, the frequencies of each class can be easily compared. This bar graph is called a separated vertical bar graph for each class. By clicking the icon , a separated horizontal bar graph can be drawn as in <Figure 2.2.20>



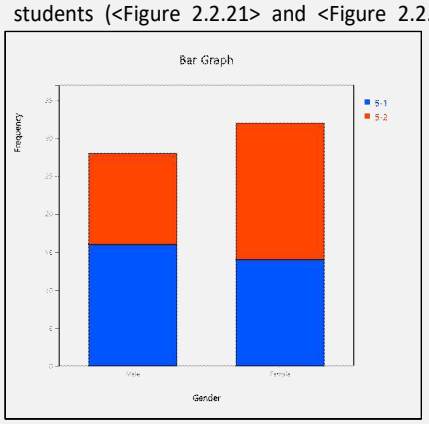
<Figure 2.2.19> Separated vertical bar graph of the gender distribution by class.



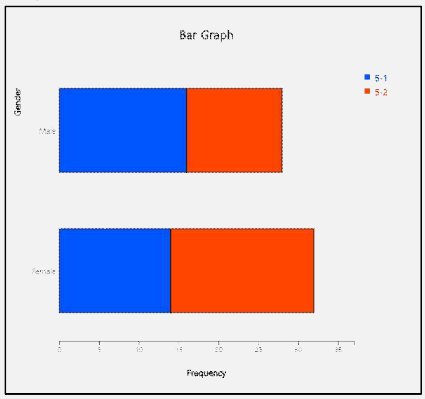
<Figure 2.2.20> Separated horizontal bar graph of the gender distribution by class.

Example 2.2.3 Answer (continued)

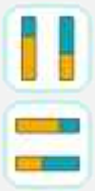
- For the summary data of two groups, there are many variants of showing bar graphs in order to compare two groups visually well. If you click on the icon or the icon , a stacked bar graph is drawn that divides a single bar into pieces with different colors which are proportional to the frequencies of male and female students (<Figure 2.2.21> and <Figure 2.2.22>).



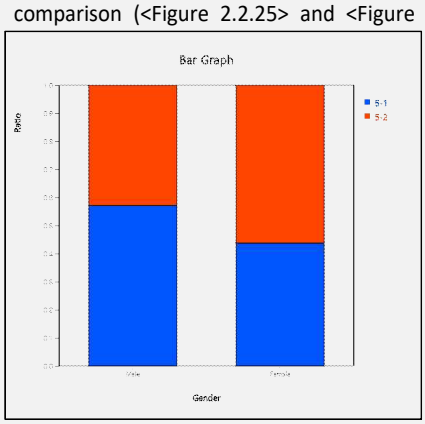
<Figure 2.2.21> Stacked vertical bar graph of the gender by class



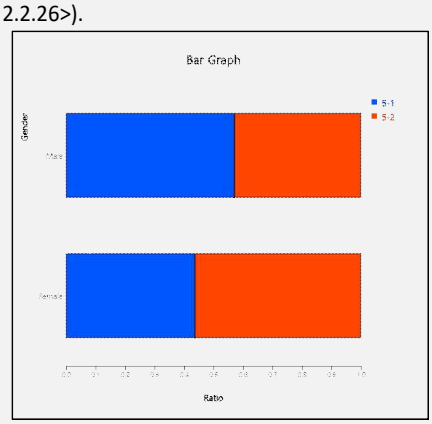
<Figure 2.2.22> Stacked horizontal bar graph of the gender by class



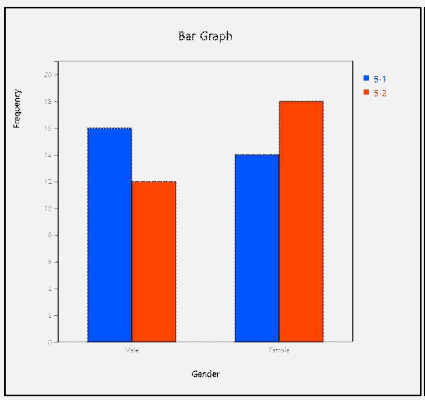
- If you click on the icon or the icon , a ratio bar graph is drawn in which bars with the same height are divided into pieces with different colors which are proportional to the frequencies of male and female students (<Figure 2.2.23> and <Figure 2.2.24>). If you click on the icon or the icon , a side-by-side bar graph is drawn which draws the bars of each group category sideways for comparison (<Figure 2.2.25> and <Figure 2.2.26>).



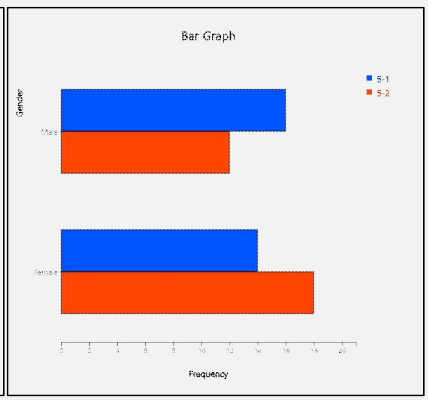
<Figure 2.2.23> Ratio vertical bar graph of the gender by class.



<Figure 2.2.24> Ratio horizontal bar graph of the gender by class.



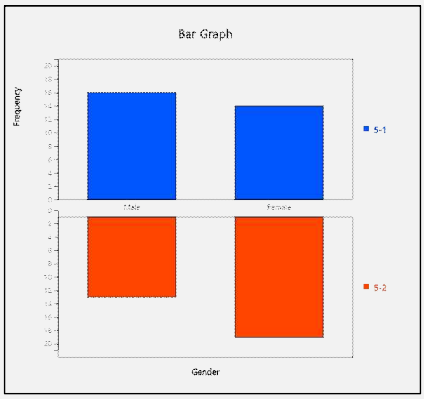
<Figure 2.2.25> Side-by-side vertical bar graph of the gender by class.



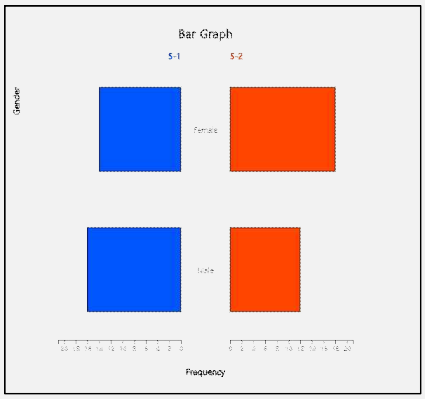
<Figure 2.2.26> Side-by-side horizontal bar graph of the gender by class.

Example 2.2.3 Answer (continued)

- If there are only two categories of the group variable like this example, then by clicking on the icon or the icon , a two-sided (or bi-lateral) bar graph is drawn which draws the bars in the opposite direction either the above and below of X-axis (<Figure 2.2.27>), or the left and right of Y-axis (<Figure 2.2.28>).



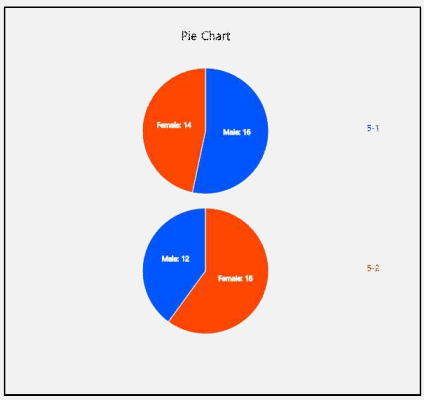
<Figure 2.2.27> Two-sided vertical bar graph of the gender by class.



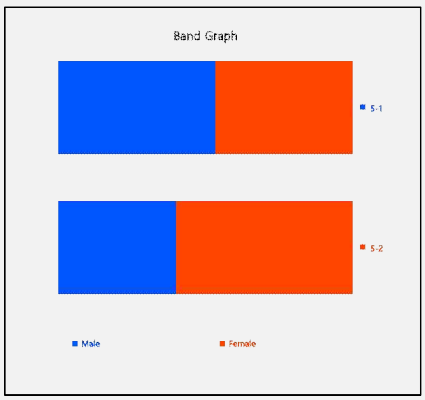
<Figure 2.2.28> Bi-lateral horizontal bar graph of the gender by class.

- By clicking on the icon , a pie chart is drawn as in <Figure 2.2.29> which has two pie charts for classes of '5-1' and '5-2'. Each pie chart shows the frequencies of the number of male and female students by dividing a pie (circle) into pieces with two colors depending on angles which are proportional to the frequencies of each category.

- By clicking on the icon , a band graph is drawn as in <Figure 2.2.30> which has two band graphs for classes of '5-1' and '5-2'. Each band graph shows the frequencies of the number of male and female students by dividing a rectangle into squares with two colors which are proportional to the frequencies of each category.



<Figure 2.2.29> Pie charts for gender distribution in two classes.



<Figure 2.2.30> Band graphs for gender distribution in two classes.

Example 2.2.4

(Male and Female Population by Age Groups)

In 2015, the male and female populations by age groups in Korea are shown in Table 2.2.3. Using this data, draw a vertical bar graph by age groups and then find appropriate graphs to analyze the characteristics of this data easily.

Table 2.2.3 male and female populations by age groups in Korea (KOSTAT Census 2015, unit 10,000 persons)

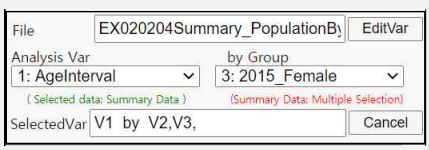
Age Interval	2015 Male	2015 Female
00 - 04	115	109
05 - 09	116	109
10 - 14	126	116
15 - 19	166	151
20 - 24	181	158
25 - 29	158	145
30 - 34	185	176
35 - 39	193	186
40 - 44	214	207
45 - 49	215	212
50 - 54	209	205
55 - 59	192	194
60 - 64	134	141
65 - 69	102	110
70 - 74	79	97
75 - 79	55	80
80 - 84	28	54
over 85	13	39

Answer

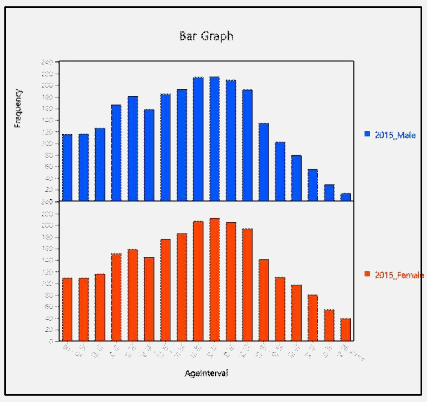
- The data of Table 2.2.3 can be loaded from 『eStat』 using the following address.

  Ex ⇨ eBook ⇨ EX020204_Summary_PopulationByGender.csv.

- Click on the variable name of the first variable, 'AgeInterval' followed by the second variable '2015_Male' and the third variable '2015_Female'. As shown in <Figure 2.2.31>, you may select the 'AgeInterval' variable from the 'Analysis Var' box and '2015_Male' and '2015_Female' variables sequentially from the 'By Group box. When these variables are selected, a separated vertical bar graph as shown in <Figure 2.2.32> which separates the male and female populations with the same scale of Y-axis will be appeared in the Graph Area.



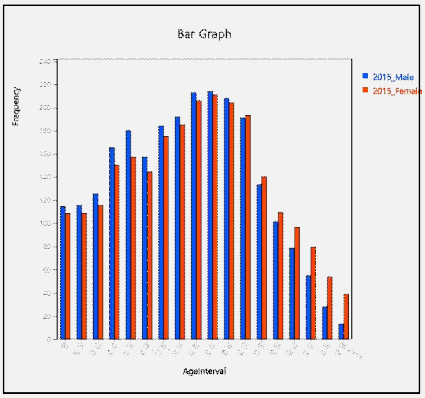
<Figure 2.2.31> Variable selection for analysis



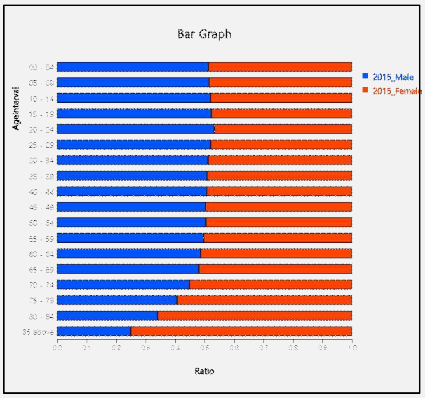
<Figure 2.2.32> Separated vertical bar graph of population by age group and by gender

Example 2.2.4 Answer (continued)

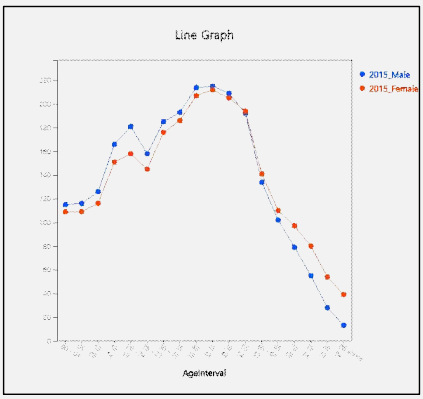
- Among ten possible bar graphs such as  , a side-by-side bar graph as <Figure 2.2.33> would be useful, because it shows the comparison of the number of male and female populations in each age interval. A ratio bar graph as <Figure 2.2.34> which shows directly the proportions of male and female populations in each age interval can also be useful. In each of the graphs, you can easily see that the female population is getting larger than the male population after the age interval of 50s and more. A line graph as in <Figure 2.2.35> can also be used to see this kind of patterns.
- An overall distribution of the male and female populations by age group can be observed by using a two-sided (bi-lateral) horizontal bar graph as in <Figure 2.2.36> which is usually called a population pyramid. Currently, Korea has an age-specific population structure which looks like a jar. In other words, the population in age intervals of 40 to 50 is higher than the population in age intervals of 30 or less which is gradually decreasing. It would cause many problems in the future society such as the population decrease, the medicare budget increase etc.



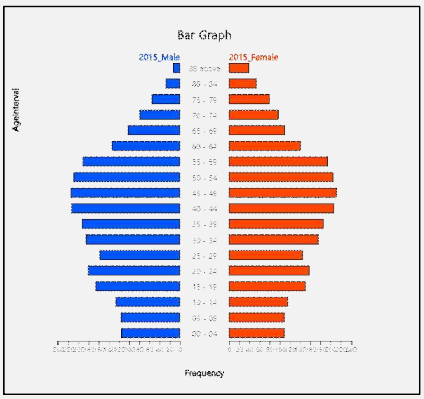
<Figure 2.2.33> Side-by-side vertical bar graph of population by age and by gender



<Figure 2.2.34> Proportional horizontal bar graph of population by age and by gender



<Figure 2.2.35> Line graph of population by age and by gender



<Figure 2.2.36> Bi-lateral horizontal bar graph of population by age and by gender

[Practice 2.2.3]	**(Death Rates of Virginia)** For each of five age groups (50–54, 55–59, 60–64, 65–69, 70–74), death rates are measured per 1000 population per year in Virginia. They are cross-classified by population group such as Rural/Male, Rural/Female, Urban/Male and Urban/Female. This data are saved at the following location of 『eStat』 system. Ex ⇨ eBook ⇨ PR020203_Rdatasets_VADeaths.csv Draw appropriate graphs to analyze characteristics of the data.

- In general, if there are many groups (columns) on the summary data, you can compare the difference between groups for each category of the analysis variable using different kinds of graphs. If there are many groups, it is recommended that you draw several kinds of graphs, because each graph can show you different characteristics of data.
- If data are observed over time, it is called a time series and a line graph is usually used to observe a trend over time. The X-axis includes values of a time variable which are spaced equally and Y-axis represents a scale of all time series data. Each pair of data, time and value is marked as a point in a two-dimensional coordinate plane and two adjacent points are connected with a line.

Example 2.2.5	**(OECD Export – Import by Country)** In 2017, import and export data of OECD countries are stored at the following location of 『eStat』 system. Ex ⇨ eBook ⇨ EX020205_OECD_ExportImport_2017.csv. Draw a line graph to find out characteristics of export and import by country.
Answer	◆ Retrieve the file from 『eStat』 which will show the data as in <Figure 2.2.37>.

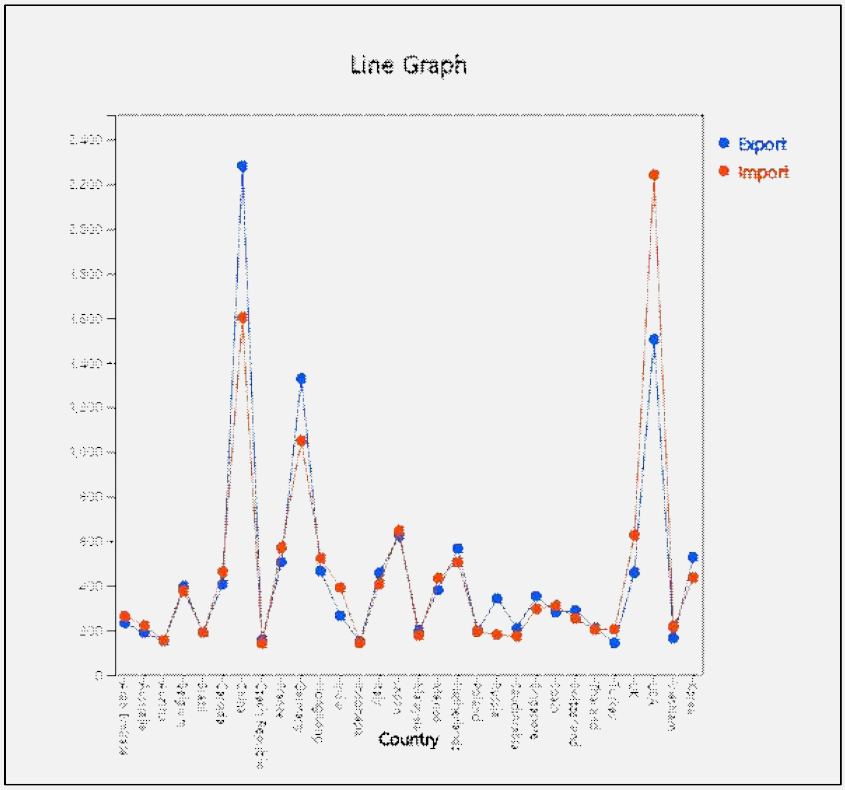
File OECD_ExportImport__2017.csv EditVar
Analysis Var: 1: Country (Selected data: Summary Data) — by Group: 3: Import (Summary Data: Multiple Selection)
SelectedVar: V1 by V2,V3, Cancel

	Country	Export	Import	V4
1	Arab Emirate	233	264	
2	Australia	189	221	
3	Austria	153	155	
4	Belgium	399	376	
5	Brazil	191	189	
6	Canada	408	462	
7	China	2281	1602	
8	Czech Republic	158	141	
9	France	506	572	
10	Germany	1329	1050	
11	HongKong	465	523	
12	India	266	392	
13	Indonesia	150	143	
14	Italy	459	409	
15	Japan	625	648	
16	Malaysia	200	176	
17	Mexico	381	435	
18	Netherlands	567	506	
19	Poland	198	194	
20	Russia	343	182	
21	SaudiArabia	210	173	
22	Singapore	352	297	
23	Spain	282	312	
24	Switzerland	290	252	
25	Thailand	211	202	

<Figure 2.2.37>
Export-Import data of
OECD countries

Example 2.2.5 Answer (continued)

- Click on the line graph icon, then click the variable names of 'Country', 'Export', 'Import' to draw a line graph as in <Figure 2.2.38>.
- Looking in the Graph, we can see that China and Germany have lots of surplus in trade and USA has lots of loss.



<Figure 2.2.38> Line graph of Export-Import of OECD countries

[Practice 2.2.4]

(Income of OECD Countries)

National incomes of OECD countries in 2000, 2005, 2010 and 2015 are saved at the following location of 『eStat』 system.

Ex ⇨ OECD ⇨ PR020204_OECD_NationalIncome_2017.csv.

Draw a line graph of the national incomes for each country.

[Practice 2.2.5]

(Average Temperatures by Season in Korea)

Average temperatures of each season were observed from 1973 to 2016 in Korea and data are saved at the following location of 『eStat』 system.

Ex ⇨ eBook ⇨ PR020205_Summary_TemperatureBySeason.csv

Draw a line graph of the temperatures by season and observe their characteristics.

2.3 Visualization of Raw Data

- Section 2.2 describes how to visualize the summary data of a categorical variable. This section describes how to visualize qualitative data in the form of raw data. In general, the raw data are processed by counting the number of data in each category of a categorical variable using a statistical package and the resulted summary data are visualized as in Section 2.2. 『eStat』 system enables this kind of work easily.
- This section describes how to visualize the raw data in the case of qualitative data without groups and with groups.

2.3.1 Raw Data of Categorical Variable

Example 2.3.1

(Survey on Gender – Raw Data)

There are 10 students in a class and gender (male or female) data are collected as follows. This kind of data are called as raw data.

male, female, male, female, male, male, male, female, male, female

In order to use a statistical package, the raw data are usually arranged as a column as in Table 2.3.1 with numeric coding (1: male, 2: female). Coding is not compulsory depending on packages, but 『eStat』 system allows the raw data of both with coding and without coding (character data).

Table 2.3.1 Gender Survey (1:Male, 2:Female)

Gender
1
2
1
2
1
1
1
2
1
2

Data of Table 2.3.1 are saved at the following address in 『eStat』 system.

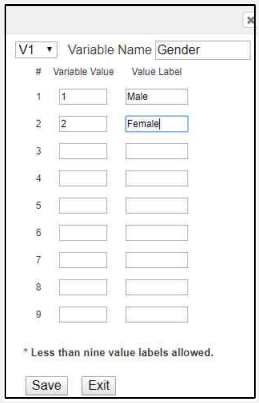
Ex ⇨ eBook ⇨ EX020301_Raw_Gender.csv

Use 『eStat』 to draw a bar graph, a pie chart, and a band graph to find out characteristics of the raw data.

Example 2.3.1 Answer

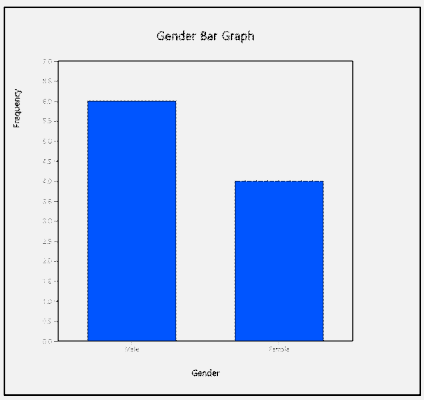
- Enter the gender data of Table 2.3.1 on the sheet of 『eStat』 system or load the file from Ex ⇨ eBook ⇨ EX020301_Raw_Gender.csv.
- If you enter the data, give a variable name 'Gender' using [Edit Var] button as shown in <Figure 2.3.1> and provide value labels to values 1 and 2 (1 for Male and 2 for Female). If the data are edited using the value labels, it must be saved with JSON format file (click on the icon) to ensure that the edited information is not lost. If you want to load a file in JSON format to 『eStat』 system, you must also use the icon which is the icon of JSON file open.

Example 2.3.1 Answer (continued)

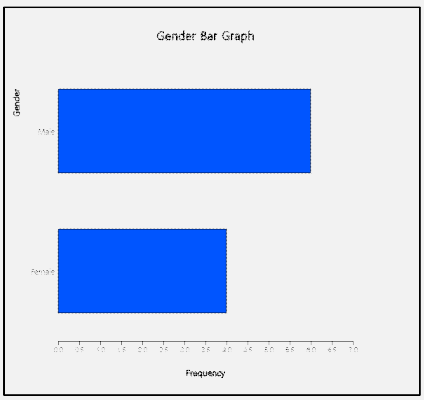


<Figure 2.3.1> Value label using [Edit Var]

- Click on the variable name 'Gender' to draw a vertical bar graph as shown in <Figure 2.3.2>. A bar graph was drawn after counting frequencies of each gender category, i.e. six males and four females. A basic function of statistical packages such as 『eStat』 is to examine a frequency distribution of the raw data and draw a graph using this frequency distribution.
- The vertical bar graph such as <Figure 2.3.2> is frequently used. If there are a large number of categories, a horizontal bar graph as in <Figure 2.3.3> can also be used (click on the icon in 『eStat』).

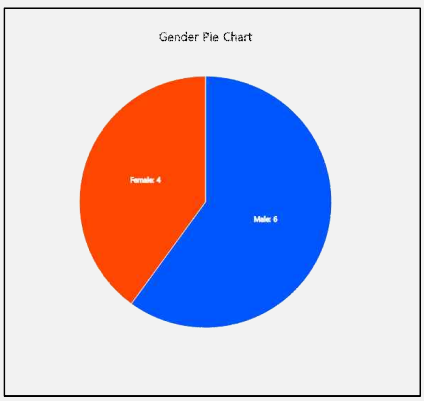


<Figure 2.3.2> Vertical bar graph of gender

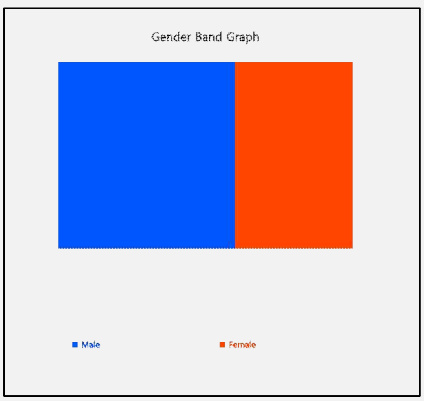


<Figure 2.3.3> Horizontal bar graph of gender

- Click on the icon in 『eStat』 to draw a pie chart (<Figure 2.3.4>) and click on the icon to draw a band graph (<Figure 2.3.5>). Click on the icon to draw a doughnut graph.



<Figure 2.3.4> Pie chart of gender



<Figure 2.3.5> Band graph of gender

[Practice 2.3.1]

(Preference of Mathematics)

In an elementary school, gender (1: male, 2: female) and math preference (1: good, 2: ordinary, 3: no) of students were surveyed and saved at the following location of 『eStat』 system.

Ex ⇨ eBook ⇨ PR020301_Raw_MathPreferenceByGender.csv.

Draw a bar graph, a pie chart, a band graph of the math preference.

2.3.2 Raw Data of Categorical Variable with Group

Example 2.3.2

(Survey on Gender and Marital Status – Raw Data with Group)

In addition to the gender data of Example 2.3.1, marital status (1: Single 2: Married, 3: Other) was also surveyed as in Table 2.3.2. Compare characteristics of marital status by gender (male and female) using a bar graph, a pie chart, a band graph, and a line graph. Data are saved at the following location of 『eStat』.

Ex ⇨ eBook ⇨ EX020302_Raw_MaritalByGender.csv

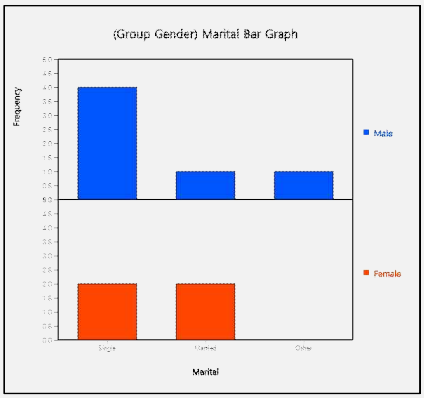
Table 2.3.2 Survey of gender and Marital status

Gender (1:Male, 2:Female)	Marital Status (1:Single, 2:Married, 3:Other)
1	1
2	2
1	1
2	1
1	2
1	1
1	1
2	2
1	3
2	1

Example 2.3.2 Answer

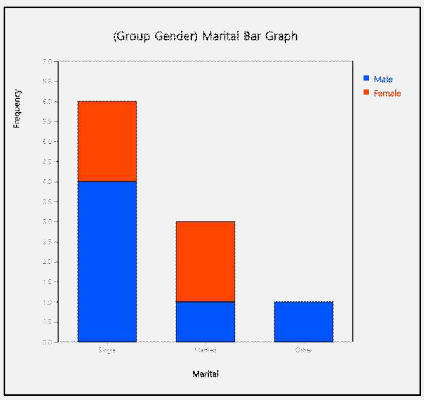
- Enter the gender and marital status data of Table 2.3.2 on the sheet of 『eStat』 system. Use [Edit Var] button to enter a variable name as 'Gender' and its value labels as 'Male' for value 1 and 'Female' for value 2. Similarly, enter a variable name as 'Marital' and its value labels as 'Single' for 1, 'Married' for 2 and 'Other' for 3.
- The data edited for their variable names and value labels must be saved in JSON format file (click on the icon) to ensure that the information is not lost. When recalling again, you must also click on the JSON Open icon .
- If you click on the 'marital' and 'gender' variable names sequentially, a separated vertical bar graph of marital status by gender is drawn as in <Figure 2.3.6>.

Example 2.3.2 Answer (continued)

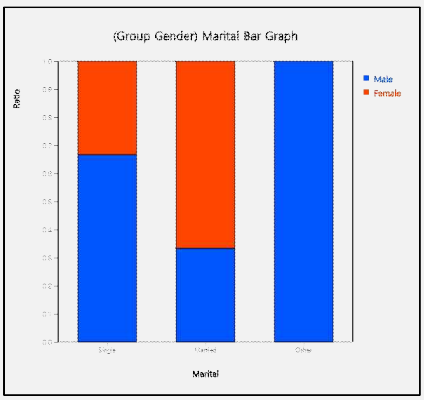


<Figure 2.3.6> Vertical bar graph of marital status by gender

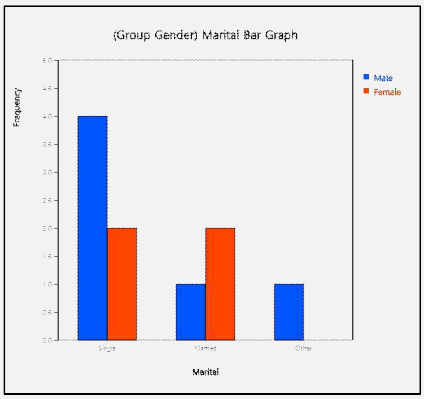
- This separated bar graph by gender can be modified in a different form using the icons () below the main icons which are a vertical stacked (<Figure 2.3.7>), a ratio (<Figure 2.3.8>), a side-by-side (<Figure 2.3.9>), a bi-lateral (Figure 2.3.10) and a horizontal separated (<Figure 2.3.11>), a stacked (<Figure 2.3.12>), a ratio (<Figure 2.3.13>), a side-by-side (<Figure 2.3.14>), a bi-lateral (Figure 2.3.15).



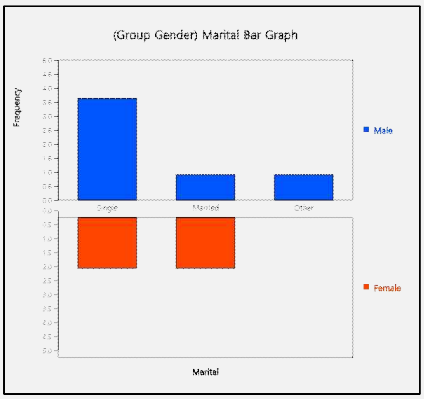
<Figure 2.3.7> Vertical stacked bar graph of marital status by gender



<Figure 2.3.8> Vertical proportional bar graph of marital status by gender

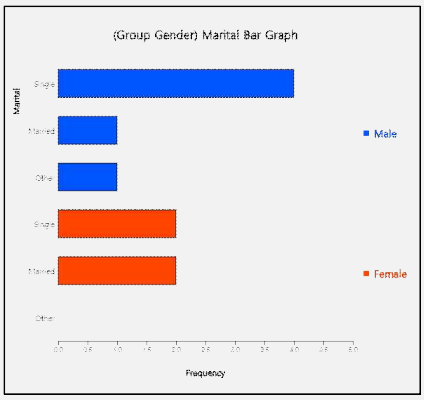


<Figure 2.3.9> Vertical side by side bar graph of marital status by gender

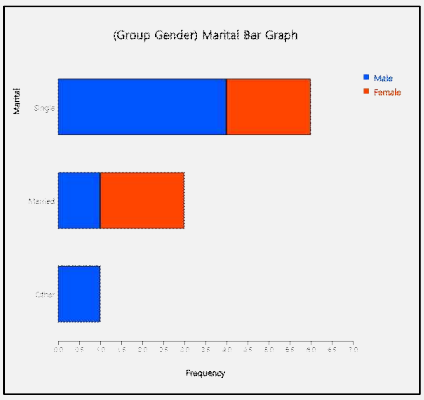


<Figure 2.3.10> Vertical bi-lateral bar graph of marital status by gender

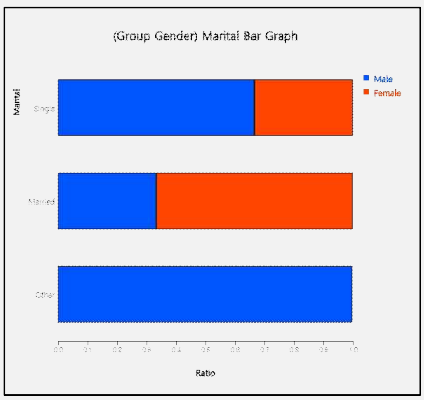
Example 2.3.2 Answer (continued)



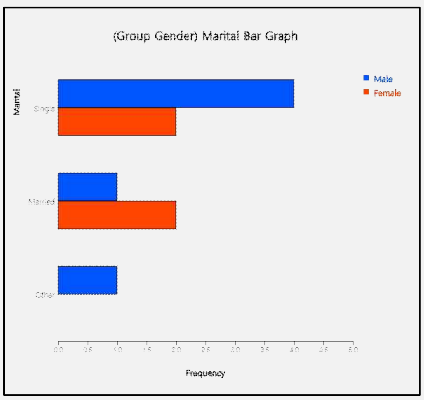
<Figure 2.3.11> Horizontal bar graph of marital status by gender



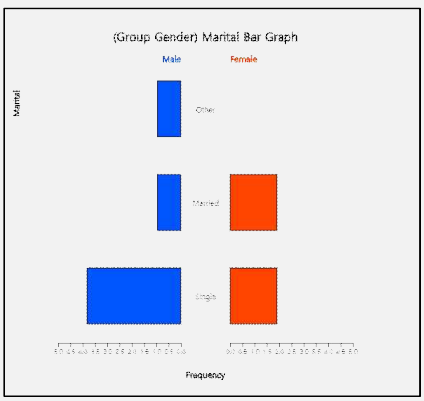
<Figure 2.3.12> Horizontal stacked bar graph of marital status by gender



<Figure 2.3.13> Horizontal proportional bar graph of marital status by gender



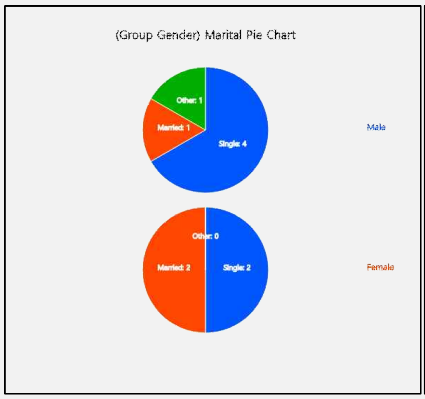
<Figure 2.3.14> Horizontal side by side bar graph of marital status by gender



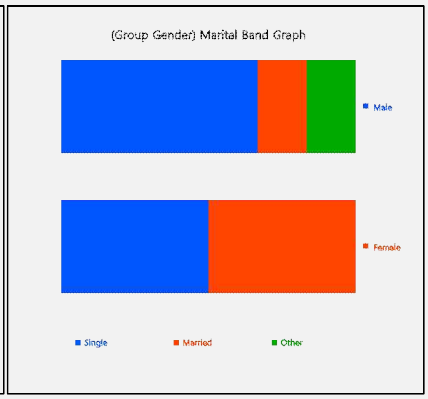
<Figure 2.3.15> Horizontal bi-lateral bar graph of marital status by gender

- Click on the icons and in 『eStat』 to draw a pie chart as in <Figure 2.3.16> and a band graph as in <Figure 2.3.17>. It is easy to observe which categories in each group account for a large percentage of the total data.

Example 2.3.2 Answer (continued)



<Figure 2.3.16> Pie chart of marital status by gender



<Figure 2.3.17> Band graph of marital status by gender

[Practice 2.3.2]

(Preference of Mathematics by Gender)

In an elementary school, gender (1: male, 2: female) and math preference (1: good, 2: ordinary, 3: no) of students were surveyed and saved at the following location of 『eStat』 system.

⇨ eBook ⇨ PR020302_Raw_MathPreferenceByGender.csv.

Draw a bar graph, a pie chart and a band graph of the math preference by gender.

Exercise

2.1 Describe qualitative data and give examples.

2.2 Describe summary data and raw data using examples.

2.3 From the home page of the OECD, download any interesting data for you in Excel format and do the following:

1) Save data as an Excel file in CSV format.
2) Retrieve the file in 1) to 『eStat』 system.
3) Draw appropriate graphs using 『eStat』 and save results as graph files.
4) Prepare a report using the MS Word.

Multiple Choice Exercise

2.1 How do you call the following form of organized data?

Gender	Number of Student
male	6
female	4

① Discrete Data ② Summary Data
③ Raw Data ④ Continuous Data

2.2 How do you call the following type of data?

Gender (1:Male, 2:Female)	Marital Status (1:Single, 2:Married, 3:Other)
1	**1**
2	**2**
1	**1**
2	**1**
1	**2**
1	**1**
1	**1**
2	**2**
1	**3**
2	**1**

① Discrete Data ② Summary Data
③ Raw Data ④ Continuous Data

2.3 Which of the following graphs is used for visualizing qualitative data?

① bar graph ② histogram
③ stem and leaf plot ④ scatter plot

2.4 Which of the following graphs is NOT used for visualizing qualitative data?

① bar graph ② histogram
③ pie chart ④ band graph

2.5 Which graph is useful for data observed over time, such as annual exports?

① bar graph ② histogram
③ pie chart ④ line graph

(Answers)
2.1 ②, 2.2 ③, 2.3 ①, 2.4 ②, 2.5 ④