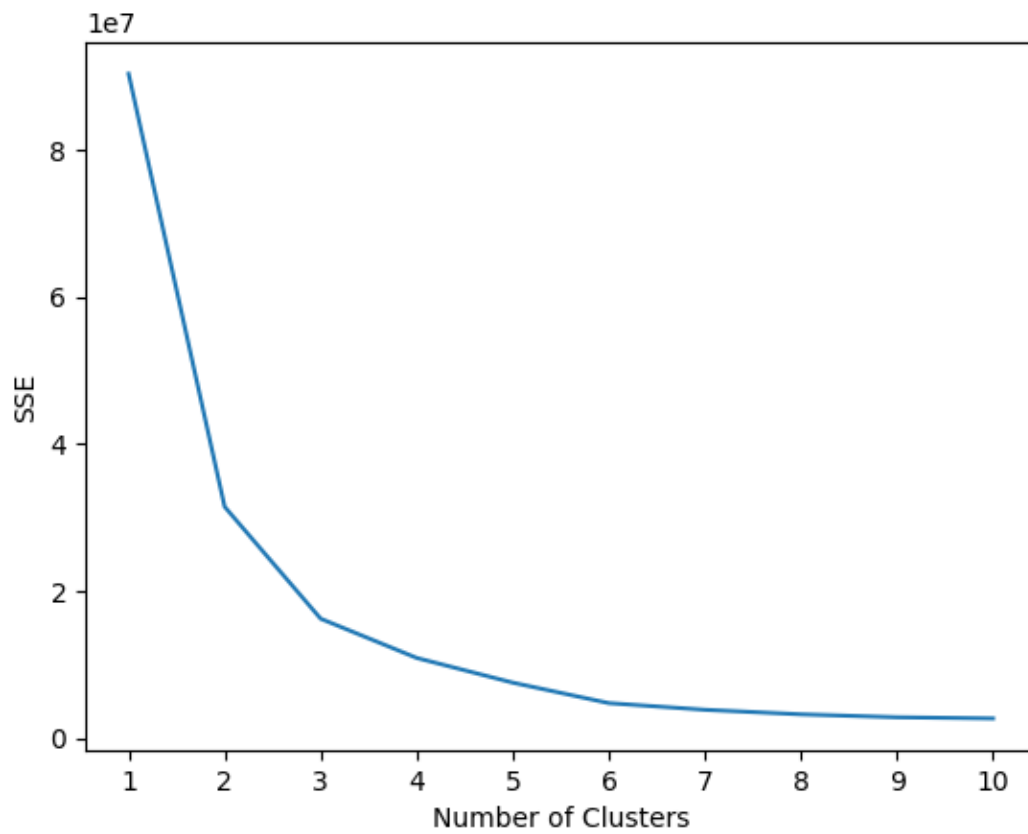


1. What is the right number of clusters for this problem? Why?

I used elbow method. Based on the graph below, after $k=3$, there is not many changes in SSE. So, I decided $k = 3$.



2. For each of the test data, find the nearest cluster centroid and place the test data into that cluster.

Please see the 'cluster' column in the following chart.

----- RESULT -----															
	univ_rank	first_initial	last_initial	cit_2017	cit_2018	cit_2019	cit_2020	cit_2021	cit_2022	h_index	i_10_index	cluster	cit_2022_p1	cit_2022_p2	cit_2022_p3
0	51	I	P	38	102	159	245	277	381	16	24	1	324	343	309.703125
1	51	S	M	153	333	510	749	963	1048	31	59	0	1245	626	1099.923077
2	51	A	B	5524	8950	12526	14204	16734	17508	60	88	2	2912	2912	2701.333333
3	51	W	H	161	183	206	215	179	262	22	33	1	156	343	309.703125
4	51	F	N	70	96	88	133	157	156	16	24	1	197	343	309.703125
5	51	M	I	238	386	641	602	1025	1249	41	110	0	1245	626	1099.923077
6	51	R	F	41	115	210	312	473	554	15	21	1	576	343	309.703125
7	51	S	J	54	72	113	139	144	141	9	9	1	164	343	309.703125
8	51	S	Z	135	92	160	184	238	332	24	34	1	443	343	309.703125
9	51	J	Z	1678	2066	2635	3253	4319	4125	23	30	2	2912	2912	2701.333333
10	52	E	G	151	147	156	152	169	167	31	85	1	156	343	309.703125
11	52	M	C	85	121	202	264	376	383	28	65	1	328	343	309.703125
12	52	W	E	1375	1264	1038	998	947	784	37	65	0	1118	626	1099.923077
13	52	A	D	183	286	356	395	449	490	22	31	1	698	343	309.703125
14	52	R	C	89	128	103	109	108	103	20	39	1	141	343	309.703125
15	52	V	C	19	22	52	116	172	188	13	21	1	139	343	309.703125
16	52	T	B	503	463	584	722	945	893	46	163	0	947	626	1099.923077
17	52	W	A	47	82	98	128	178	346	17	35	1	196	343	309.703125
18	52	K	A	139	125	84	80	74	47	16	24	1	88	343	309.703125
19	52	S	H	205	201	220	210	202	107	21	29	1	213	343	309.703125

3. Tabulate the following predictions for the 2022 citation numbers for the test set, using the average difference magnitude to evaluate them:

(1) same as the 2022 citation number of the nearest neighbor from the training set;

Refer to the 'cit_2022_p1' column.

(2) same as the point nearest the cluster centroid;

Refer to the 'cit_2022_p2' column.

(3) average of all others from the training set in the same cluster.

Refer to the 'cit_2022_p3' column.

4. Draw conclusions from the comparison.

```

----- CLUSTERS INFO -----
cluster1
  centroid: [ 801.30769231  815.30769231  827.          919.92307692 1067.23076923]
  value of cit_2022 of nearest data point from centroid: 626
  average of cit_2022 in cluster1: 1099.92
cluster2
  centroid: [184.0625   203.296875 219.515625 241.09375  281.34375 ]
  value of cit_2022 of nearest data point from centroid: 343
  average of cit_2022 in cluster2: 309.70
cluster3
  centroid: [1794.33333333 1920.33333333 2151.66666667 2358.33333333 2698.66666667]
  value of cit_2022 of nearest data point from centroid: 2912
  average of cit_2022 in cluster3: 2701.33

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Average difference of prediction 1: 866.80
Average difference of prediction 2: 961.10
Average difference of prediction 3: 940.43

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The prediction method (1) using values same as the 2022 citation number of the nearest neighbor from the training set have the lowest difference with the actual value of cit_2022 in test datasets.