## Assignment 3: Search (Given: 14 Feb 2023, Due: 7 Mar 2023)

## **General instructions**

- Solutions are to be typed in the .ipynb file provided and uploaded in the lab course page in Moodle on the due date.
- Your code should be well commented and should be compatible with python3.
- For this assignment, you are allowed to import the libraries random and queue of python3. No other libraries may be imported.

```
In [1]: import random as rnd
import queue
```

## **Generate Maze**

A maze can be visualized as an arrangement of cells in a rectangular  $m \times m$  grid with walls between some pairs of cells.

- (a) Write a program that uses randomized depth-first search to generate a maze. The randomized depth-first search procedure is as follows: Starting from a given cell (say (0,0)), this algorithm produces a path that visits each cell in the grid according to the following recursive procedure.
  - If the current cell C has a neighbouring cell that is not yet visited, chose one of such cells (say C') at random and remove the wall between these two cells. Repeat with C' as the current cell.
  - If all neighbouring cells of the current cell C are already visited, then backtrack to the last cell  $\widehat{C}$  with a neighbouring cell  $\widehat{C}'$  that is not yet visited and repeat with  $\widehat{C}'$  as the current cell.

A sample output of a  $3 \times 3$  maze is along with the graph adjacency representation is as shown below. The bottom left corner of the maze is (0,0) and top right corner of the maze is (2,2).

```
In [2]: class Cell:
    def __init__(self,x,y,m) -> None:
        # coordinate is same as index
        self.m = m
        # x coordinate
        self.x = x
        # y coordinate
        self.y = y
        # for printing path, we need parent
        self.parent = None
```

```
# unique cell number for each cell
self.cell number = x*m + y
# isVisited during creating maze
self.isVisited = False
# isVisited during searches
self.isVisited_in_search = False
# list of adjacent cells
self.adjCells = []
# during bfs, to store information of distance
self.distance = 0
# manhattan distance heuristic
self.manhattan distance_to_last_cell = (m-1-x) + (m-1-y)
\# x and y will always be less than or equal to m-1
# if cell is neither in the corner nor the edge
if x not in [0,m-1] and y not in [0,m-1]:
 adjCells = [
    (x - 1, y), # up^
    (x,y+1), # right ->
    (x+1,y), # down v
    (x,y-1) # left
  self.adjCells = adjCells
elif x not in [0,m-1] and y in [0,m-1]:
  # left and right edge
 if y == 0:
  # left edge
    adjCells = [
      (x - 1, y), # up^
      (x,y+1), # right ->
      (x+1,y), # down v
      # () # left
    self.adjCells = adjCells
  else:
    # right edge
    adjCells = [
      (x - 1, y), # up^
      # (), # right ->
      (x+1,y), # down v
      (x,y-1) # left
    1
    self.adjCells = adjCells
elif x in [0,m-1] and y not in [0,m-1]:
  # top and bottom edge
  if x==0:
    # top edge
    adjCells = [
      # (), # up ^
      (x,y+1), # right ->
      (x+1,y), # down v
      (x,y-1) # left
```

```
self.adjCells = adjCells
 else:
    adjCells = [
      (x - 1, y), # up^
      (x,y+1), # right ->
     # (), # down v
      (x,y-1) # left
    self.adjCells = adjCells
else:
 # corners
 if (x,y) == (0,0):
    # top left corner
    adjCells = [
     # (), # up ^
     (x,y+1), # right ->
      (x+1,y), # down v
      # () # left
    1
    self.adjCells = adjCells
 elif (x,y) == (0,m-1):
   # top right corner
    adjCells = [
      # (), # up ^
      # (), # right ->
      (x+1,y), # down v
      (x,y-1) # left
    self.adjCells = adjCells
 elif (x,y) == (m-1,m-1):
    # bottom right corner
    adjCells = [
     (x - 1, y), # up^
      # (), # right ->
     # (), # down v
     (x,y-1) # left
    1
    self.adjCells = adjCells
 else:
   # bottom left corner
    adjCells = [
     (x - 1, y), # up^
     (x,y+1), # right ->
     # (), # down v
     # () # left
    1
    self.adjCells = adjCells
adjCell numbers = [
 adjCell[0]*m + adjCell[1] for adjCell in self.adjCells
self.adjCell numbers = list(adjCell numbers)
# the unique cell numbers of adj Cells
# list of walled neighbours
```

```
self.walled neighbours = list(self.adjCell numbers)
  # list of non walled neighbours
  self.non walled neighbours = [
    x for x in self.adjCell_numbers if x not in self.walled_neighbours
def generate_children_of_cell(self):
  # returns all cells which are adjacent to the current cell, whether w
  return self.adjCell numbers
def generate_non_walled_neighbours(self):
  # returns list of non-walled neighbours, the list contains the unique
  return self.non walled neighbours
def manhattan distance heuristic(self) -> int:
  # returns manhattan distance heuristic
  return self.manhattan_distance_to_last_cell
def print current cell(self):
  # utility function to print the attributes of the current cell
  print()
  print(f'the cell is {(self.x,self.y)}')
  print(f'the cell number is {self.cell number}')
  print(f'the adj Cells are {self.adjCells}')
  print(f'the adjCell numbers are {self.adjCell numbers}')
  print(f'the walled neighbours are {self.walled neighbours}')
  print(f'the non-walled neighbours are {self.non_walled_neighbours}')
  print()
def print_adjacency_list(self):
  # prints the list of non-walled neighbours of the current cell
  print()
  x = self.non walled neighbours
  y = [
    (int(cell number/self.m), cell number%self.m)
    for cell number in x
  print(f'Node {(self.x,self.y)}: ', end=' ')
  for coord in y:
    print(coord,end=' ')
  print()
  print()
# the below function is for the purpose of priority queue, when using p
def lt (self,other):
  return self.manhattan distance to last cell < other.manhattan distance
```

```
In [3]:
    class Maze:
        def __init__(self,m) -> None:
            # maze side length
            self.sides = m
            # list of 'Cell' Objects
            self.cells = [Cell(i,j,m) for i in range(m) for j in range(m)]
            # creating an empty dictionary to store all the cells with key as the
            # the reason for using dictionary is to access the elements fast
            self.cell_dictionary = dict()
```

```
for cell in self.cells:
    # the key of each cell is of the form 'cell {cell number}'
   self.cell dictionary[f'cell {cell.cell number}'] = cell
  # self.created maze = self.generate maze()
  # we call generate maze() function to generate a random maze
  self.generate_maze()
  # maze img is a list of list which is used to print the grid of maze
  self.maze img = [
    list(['' for _ in range(2*m + 1)]) for _ in range(2*m + 1)
  # calling create_maze_img() function to create the maze image
  self.create maze img()
  # since list is mutable, we have to create new list in every row
def generate_maze(self):
  # we are generating maze using randomized depth first search
  self.dfs_create_maze(self.cell_dictionary['cell_0'])
def child generator(self,cell: Cell):
  # returns the adjacent cells of the cell, the list will contain the c
  return cell.generate children of cell()
def dfs create maze(self,cell: Cell):
  # create maze function
  # length of maze
 m = self.sides
  # adj cells of the current cell
  adj cell number list = list(cell.generate children of cell())
  # adj cells = cell.generate children of cell().copy()
  # we are shuffling it in order to simulate randomized picking of cell
  rnd.shuffle(adj cell number list)
  # isVisited in creating maze is set to True
  cell.isVisited = True
  # for each cell in the adj cells
  for cell to be considered in adj_cell_number_list:
    cell_to_be_considered: int
    # using a try except block in order to catch any possible errors
    try:
      cellCheck = self.cell dictionary[f'cell {cell to be considered}']
      print(f'the key {cell_to_be_considered} not found')
    cellCheck: Cell
    if cellCheck.isVisited == False:
      # if cell is not visited
      # first remove wall between this cell and the picked cell
        cell.walled_neighbours.remove(cellCheck.cell_number)
      except:
        print(f'cell {cellCheck.cell number} not found in {cell.cell nu
      cell.non walled neighbours.append(cellCheck.cell number)
      # now remove wall between picked cell and this cell
```

```
try:
        cellCheck.walled neighbours.remove(cell.cell number)
      except:
        print(f'cell {cell.cell_number} not found in {cellCheck.cell_nu
      cellCheck.non walled neighbours.append(cell.cell number)
      # then call dfs create maze with the non visited cell
      self.dfs create maze(cellCheck)
  del adj cell number list
  # in order to save memory
def print_cells_of_maze(self):
  # utility function to print the cell number of cells of maze in the d
  for key,value in self.cell_dictionary.items():
    value: Cell
    print(key, value.cell number)
def create_maze_img(self):
  # in order to create the maze image
 m = self.sides
  for i in range(2*self.sides + 1):
    if i%2 == 0:
      for j in range(2*self.sides + 1):
        if i==0 or i==2*self.sides:
          # borders
          if j%2 == 0:
            self.maze img[i][j] = '+'
          else:
            self.maze img[i][j] = '---'
        # now we have to check if the neighbours are walled
        else:
          if j%2 == 0:
            self.maze_img[i][j] = '+'
            # we can check the list of non walled neighbours
            # this will also work if the cell is near the wall because
            (x,y) = (int((i-1)/2),int((j-1)/2))
            cNum = x*m + y
            # to check if the below cell is walled in order to decide w
            is_below_cell_walled = True
            try:
              current cell = self.cell dictionary[f'cell {cNum}']
            except:
              print(f'the key {cNum} not found ')
            current cell: Cell
            if cNum+m in current_cell.non_walled_neighbours:
              # if below cell is present in non walled neighbours, we u
```

```
is below cell walled = False
            if is_below_cell_walled:
              self.maze img[i][j] = '---'
            else:
              self.maze_img[i][j] = ' '
    else:
      for j in range(2*self.sides + 1):
        (x,y) = (int((i-1)/2), int((j-1)/2))
        if j==0 or j==2*self.sides:
          # for left and right boundaries
          self.maze_img[i][j] = '|'
        # if j%2 == 0:
        # self.maze_img[i][j] = '|'
        else:
          if j%2 == 1:
            self.maze img[i][j] = ''
          else:
            (x,y) = (int((i-1)/2),int((j-1)/2))
            cNum = x*m + y
            # to check if the right cell is walled in order to decide w
            is right cell walled = True
            # current cell = self.cell dictionary[f'cell {cNum}']
              current_cell = self.cell_dictionary[f'cell_{cNum}']
            except:
              print(f'the key {cNum} not found ')
            current cell: Cell
            if cNum+1 in current cell.non walled neighbours:
              # if right cell is in non-walled neighbours, we update is
              is right cell walled = False
            # self.maze img[i][j] = '|'
            if is right cell walled:
              self.maze_img[i][j] = '|'
            else:
              self.maze img[i][j] = ''
def print_maze(self):
  # utility function to print the adjacency list of maze cells and image
  for key, cell in self.cell dictionary.items():
    cell: Cell
    # cell.print current cell()
    cell.print adjacency list()
  for i in range(2*self.sides + 1):
    if i%2 == 0:
      for j in range(2 * self.sides + 1):
        if j%2 == 0:
          # print('+',end='')
```

```
print(self.maze_img[i][j],end='')
else:
    # print('---',end='')
    print(self.maze_img[i][j],end='')
print()
else:
    for j in range(2 * self.sides + 1):
        # if j==0 or j==2*self.sides:
        if j%2 == 0:
            # print('|',end='')
            print(self.maze_img[i][j],end='' if self.maze_img[i][j] == else:
            # print('',end='')
            print(self.maze_img[i][j],end=''')
print(self.maze_img[i][j],end=''')
```

```
In [4]: class Agent:
          def init (self, maze: Maze) -> None:
            # which maze is the agent present in
            self.in maze = maze
            # initial location of the agent is [0,0]
            self.initial loc = [0,0]
            # attribute to count the number of dfs explore
            self.dfs explore count = 0
            # attribute to count the number of bfs explore
            self.bfs_explore_count = 0
            # attribute to count the number of astar explore
            self.astar explore count = 0
          def is goal(self,cellNum):
            # if the agent is in the last cell, then goal state has reached
            m = self.in maze.sides
            if cellNum == m*m - 1:
              return True
            return False
          def dfs_search(self,print_path = True):
            # initializing dfs explore count to zero
            self.dfs explore count = 0
            maze = self.in maze
            cell dictionary = maze.cell dictionary
            # initializing the parent of each cell to None and is Visited in sear
            for i in range(maze.sides * maze.sides):
              cell = cell dictionary[f'cell {i}']
              cell: Cell
              cell.parent = None
              cell.isVisited_in_search = False
            # for ,cell in cell dictionary.items():
            for i in range(maze.sides * maze.sides):
              cell = cell dictionary[f'cell {i}']
              cell: Cell
              isPathFound = False
              # isPathFound is to check if path has been found
              # if path is found, then we can stop the dfs there
              if cell.isVisited in search == False:
```

```
# print(f'Going to cell {cell.cell number}')
      isPathFound = self.dfs explore(cell)
      # self.dfs explore(cell)
    if isPathFound == True:
      if print_path:
        print('Path found from initial cell to final cell using DFS')
        # self.print path(cell dictionary[f'cell {maze.sides * maze.sid
        self.print path(cell dictionary[f'cell {maze.sides * maze.sides
        print()
        print(f'the number of cells explored are {self.dfs explore coun
      # break
      return
  # self.print path(cell dictionary[f'cell {maze.sides * maze.sides - 1
def dfs_explore(self,current_cell: Cell):
  # print(f'coming to cell {current cell.cell number}')
  # dfs explore count increases whenever it comes to this function call
  self.dfs explore count += 1
  # updating is visited in search to True
  current cell.isVisited in search = True
 maze = self.in maze
  cell_dictionary = maze.cell_dictionary
  # taking the non-walled neighbours because agent can only go to those
  adj non walled neighbours = current cell.non walled neighbours
  # initializing isPath found to False
  isPath found = False
  for adjCellNum in adj non walled neighbours:
    try:
      adjCell = cell dictionary[f'cell {adjCellNum}']
    except:
      print(f'the key {adjCellNum} is not found')
    adjCell: Cell
    if adjCell.isVisited in search == False:
      # if adj non-walled neighbour is unvisited we set the parent of t
      adjCell.parent = current cell
      if self.is goal(adjCellNum):
        # if that cell is a goal state
        # print(f'Going to cell {adjCell.cell number}')
        # self.dfs explore count += 1
        # print('Path found')
        # print('Path found from initial cell to final cell using DFS')
        # self.print path(adjCell)
        # print()
        # if that cell is a goal state, we return True
        return True
      else:
```

```
# print(f'Going to cell {adjCell.cell number}')
        # we set the isPath to the value coming from the next function
        isPath_found = self.dfs_explore(adjCell)
        if isPath found:
          return isPath_found
        # print(f'Returned to {current cell.cell number}')
        # return isPath found
        continue
  # print(f'Returning from cell {current cell.cell number}')
  # we have to return isPath found from each dfs explore calls
  return isPath found
def bfs_search(self,print_path = True):
  # print('in bfs search')
  # initializing explore count to zero
  self.bfs explore count = 0
 maze = self.in maze
  cell dictionary = maze.cell dictionary
  # initializing each cell's parent to None and distance to -1 and isVi
  for i in range(maze.sides * maze.sides):
    cell = cell_dictionary[f'cell_{i}']
    cell: Cell
    cell.parent = None
    cell.isVisited in search = False
    cell.distance = -1
  # using a queue for dfs
 q = queue.Queue()
  # source cell is the cell from where we start bfs, in this case initi
  source cell = cell dictionary[f'cell {0}']
  source cell: Cell
  # q.put(source cell,timeout=0.0045)
 q.put(source cell)
  # q.put_nowait(source cell)
  source_cell.distance = 0
  # Use qsize() == 0 as a direct substitute, but be aware that either a
  # the above was a warning which came when trying to use while q.empty
 while not q.qsize() == 0:
    # print('executing while loop')
    # u cell = q.get(timeout=0.0045)
    # u cell = q.get nowait()
    # to verify its not a priority queue
    # print('printing queue')
    # for x in q.queue:
    # x: Cell
    # print(x.manhattan_distance_to_last_cell,end=' ')
    # print()
    # dequeueing the first cell in the queue
    u_cell = q.get()
```

```
# a cell gets explored only when it comes to while loop
    self.bfs explore count += 1
    u cell: Cell
    # updating the isvisited in search to True
    u_cell.isVisited_in_search = True
    # checking the non-walled neighbours of the current cell
    adj cell numbers = u cell.generate non walled neighbours()
    # for each non walled cell
    for cellNum in adj cell numbers:
      # cell to check = cell dictionary[f'cell {cellNum}']
      try:
        cell_to_check = cell_dictionary[f'cell_{cellNum}']
      except:
        print(f'the key {cellNum} not found')
      cell_to_check: Cell
      if cell to check.distance == -1:
        # if distance is -1, it means, it has not been visited yet
        cell to check.distance = u cell.distance + 1
        q.put(cell_to_check)
        # enqueuing into the queue
        # q.put(cell to check, timeout=0.0045)
        # q.put nowait(cell to check)
        cell_to_check.parent = u_cell
        # checking if the cell is a goal state
        if self.is goal(cellNum):
          if print path:
            print('Path Found from initial cell to final cell using BFS
            self.print path(cell to check)
            print()
            print(f'the number of vertices explore is {self.bfs explore
          del q
          return
    # return
  # del q
  # return
def astar search(self,print path = True):
  # initializing explore count to zero
  self.astar explore count = 0
  maze = self.in maze
  cell_dictionary = maze.cell_dictionary
  # initializing each cell's parent to None and distance to -1 and isVi
  for i in range(maze.sides * maze.sides):
    cell = cell_dictionary[f'cell_{i}']
    cell: Cell
    cell.parent = None
    cell.isVisited_in_search = False
    cell.distance = -1
  # using a priority queue
```

```
q = queue.PriorityQueue()
  source_cell = cell_dictionary[f'cell_{0}']
  source cell: Cell
  source_cell.distance = 0
  # q function is initially zero
  g_function = 0
  # entries into the queue are of the form (priority number, data)
  # priority queue is based on f = g + h
  q.put((source cell.manhattan distance heuristic()+g function, source c
 while not q.qsize() == 0:
    # to verify its a priority queue
    # print('printing queue')
    # for x in q.queue:
    # print(x[0],end=' ')
    # print()
    u cell = q.get()[1]
    # print(u cell)
    self.astar explore count += 1
    # only when we come to this while loop will we increment the explor
    u cell: Cell
    u_cell.isVisited_in_search = True
    # taking the adj cells which are non walled
    adj_cell_numbers = u_cell.generate_non_walled_neighbours()
    # for each cell in adj non walled neighbours
    for cellNum in adj_cell_numbers:
      try:
        cell to check = cell dictionary[f'cell {cellNum}']
      except:
        print(f'the key {cellNum} not found')
      cell_to_check: Cell
      if cell to check.distance == -1:
        cell to check.distance = u cell.distance + 1
        # q function is the distance
        to_add = ((cell_to_check.manhattan_distance_heuristic() + cell_
        q.put(to_add)
        # updating the parent cell
        cell to check.parent = u cell
        if self.is goal(cellNum):
          # checking if its a goal state
          if print path:
            print('Path Found from initial cell to final cell using A*'
            self.print_path(cell_to_check)
            print()
            print(f'the number of vertices explored is {self.astar expl
          del q
          return
def print path(self,cell: Cell):
  # this is the recursive print path function
  if not cell:
    # if cell is None, then return
```

```
return
            # else print path of parent and then print the current cell
            self.print path(cell.parent)
            print((cell.x,cell.y),end=' ')
          def print_parent(self):
            # utility function to print the parent of each cell
            cell dictionary = self.in maze.cell dictionary
            for _,cell in cell_dictionary.items():
             cell: Cell
              parent = cell.parent
              parent: Cell
              print(cell.cell_number, 'parent is', parent.cell_number if parent e
In [5]:
        # creating a new maze of side length 3
        maze = Maze(3)
        # maze.print cells of maze()
        maze.print_maze()
        # printing the adjacency list of maze cells and the image of maze
        search agent = Agent(maze)
        Node (0, 0): (1, 0)
        Node (0, 1): (0, 2)
        Node (0, 2): (1, 2) (0, 1)
        Node (1, 0): (0, 0) (1, 1)
        Node (1, 1): (1, 0) (1, 2)
        Node (1, 2): (1, 1) (0, 2) (2, 2)
        Node (2, 0): (2, 1)
        Node (2, 1): (2, 2) (2, 0)
        Node (2, 2): (1, 2) (2, 1)
        +---+
           +---+
```

(b) Write a program to do DFS on a  $m \times m$  maze given in adjacency representation to find a route from the source cell (0,0) to the destination cell (m-1,m-1). Output the route and the number of cells explored.

```
In [6]: search_agent.dfs_search()
```

```
Path found from initial cell to final cell using DFS (0,\ 0)\ (1,\ 0)\ (1,\ 1)\ (1,\ 2)\ (2,\ 2) the number of cells explored are 6
```

(c) Write a program to do BFS on a  $m \times m$  maze given in adjacency representation to find a route from the source cell (0,0) to the destination cell (m-1,m-1). Output the route and the number of cells explored.

```
In [7]: search_agent.bfs_search()
```

```
Path Found from initial cell to final cell using BFS (0, 0) (1, 0) (1, 1) (1, 2) (2, 2) the number of vertices explore is 4
```

- (d) Write a program to do  ${\bf A}^*$  search on a  $m\times m$  maze given in adjacency representation to find a route from the source cell (0,0) to the destination cell (m-1,m-1). Use the Manhattan heuristic for  ${\bf A}^*$  search. The Manhattan distance between two cells of the maze (i,j) and  $(k,\ell)$  where  $i,j,k,\ell\in\{0,1\ldots,m-1\}$  is  $|i-k|+|j-\ell|.$  Output the route and the number of cells explored.
- In [8]: search\_agent.astar\_search()

```
Path Found from initial cell to final cell using A* (0, 0) (1, 0) (1, 1) (1, 2) (2, 2) the number of vertices explored is 4
```

```
In [9]: # to see the efficiency of dfs,bfs and astar
        bfs explore = 0
        dfs explore = 0
        astar explore = 0
        for i in range(1000):
          \# maze new = Maze(30)
          maxe new = Maxe(10)
          agent new = Agent(maze new)
          agent new.dfs search(print path=False)
          dfs_explore += agent_new.dfs_explore_count
          agent_new.bfs_search(print path=False)
          bfs explore += agent new.bfs explore count
          agent_new.astar_search(print_path=False)
          astar explore += agent new.astar explore count
          del agent_new
          del maze_new
        print(f'average number of vertices DFS explored: {dfs_explore/1000}')
        print(f'average number of vertices BFS explored: {bfs explore/1000}')
        print(f'average number of vertices A * explored: {astar_explore/1000}')
        average number of vertices DFS explored: 64.866
        average number of vertices BFS explored: 60.707
        average number of vertices A * explored: 54.101
```

## Sliding Blocks

Consider the sliding blocks puzzle where we are given a  $3 \times 3$  grid of blocks with each block containing a unique integer between 0 and 8. An example configuration is given below.

123

785

064

At each step, the block containing 0 can swap places with an adjacent block.

```
In [10]: # it is required that we generate a maze which is solvable

def random_index(m: int):
    x = rnd.randrange(0,m)
    y = rnd.randrange(0,m)
    return (x,y)

def absolute_value(x: int):
    return x if x>=0 else -x
```

```
In [11]: # for different heuristics we have to change the lt function of the c
         class Grid State:
           def __init__(self,grid: list) -> None:
             self.grid = grid
             self.parent = None
             manhattan_distance_heuristic = 0
             m = len(grid)
             self.length of grid = m
             num = 1
             self.depth distance = -1
             # goal_grid = [
             # list([0 for in range(m)]) for in range(m)
             # 1
             # for i in range(m):
             # for j in range(m):
                   if (i,j) != (m-1,m-1):
                     goal grid[i][j] = num
                     num += 1
             number to index dictionary = dict()
             num = 1
             for i in range(m):
               for j in range(m):
                 if num!=m*m:
                    number_to_index_dictionary[num] = (i,j)
                    num += 1
             number_to_index_dictionary[0] = (m-1,m-1)
             for i in range(m):
               for j in range(m):
                 number_in_i_j = grid[i][j]
                 actual_pos_of_number = number_to_index_dictionary[number_in_i_j]
                 manhattan_distance_heuristic += absolute_value(i-actual_pos_of_nu
             self.manhattan distance heuristic = manhattan distance heuristic
             del number_to_index_dictionary
             self.children_state_of_this_state = list()
             self.number of misplaced blocks = self.compute number of mispaced til
             self.manhattan distance heuristic of zero = self.compute manhattan di
           # def compute manhattan distance heuristic(self):
           def __lt__(self,other):
             # return True
             return self.manhattan_distance_heuristic < other.manhattan_distance_h</pre>
             # return self.number of misplaced blocks < other.number of misplaced</pre>
             # return self.manhattan distance heuristic of zero < other.manhattan
           def compute number of mispaced tiles(self):
             grid = self.grid
             count = 0
             m = self.length of grid
             number = 1
```

```
for i in range(m):
    for j in range(m):
      if (i,j) == (m-1,m-1):
        if grid[i][j] != 0:
          count += 1
      else:
        if grid[i][j] != number:
          count += 1
        number += 1
  return count
def compute_manhattan_distance_of_zero(self):
  grid = self.grid
 x = 0
  y = 0
 m = self.length_of_grid
  for i in range(m):
    for j in range(m):
      if grid[i][j] == 0:
        x = i
        y = i
        \# since m-1 will always be greater than or equal to x and y
        return (m-1)-x + (m-1) - y
```

```
In [12]: class Sliding Block Grid:
           def __init__(self, m=3,input_puzzle = True,depth_for_generating_sovable
              self.sides =m
              self.rows = m
              self.columns = m
              self.pos_zero = [0,0]
              self.grid = [
               list([-1 for _ in range(m)]) for _ in range(m)
              self.depth = depth for generating sovable maze
             # to create new list in each row
              # number = 0
              # while number < m*m:</pre>
                i,j = random index(m)
                 if self.grid[i][j] == -1:
                  self.grid[i][j] = number
              #
                   if number == 0:
                     self.pos zero = [i,j]
                   number += 1
              if input puzzle == True:
               self.grid = [
                  list([int(input()) for _ in range(m)]) for _ in range(m)
              elif input puzzle == False:
               self.create solvable puzzle()
              self.current_grid_state = Grid_State(self.grid)
              # list of states
```

```
# self.solution = list()
def create_solvable_puzzle(self):
  # to create solvable puzzle
 m = self.sides
  grid = [
    list([0 for in range(m)]) for in range(m)
  number = 1
  for i in range(m):
    for j in range(m):
      if (i,j) == (m-1,m-1):
        grid[i][j] = 0
      else:
        grid[i][j] = number
        number+=1
  # depth = rnd.randrange(10,20)
  # depth = int(input())
  depth = self.depth
  i = m-1
  j = m-1
  # continue from here
  for in range(depth):
    actionList = self.possible actions to create solvable maze(i,j,m)
    action = rnd.choices(actionList, k=1)[0]
    if action=='u':
      grid[i][j], grid[i-1][j] = grid[i-1][j], grid[i][j]
      i,j = i-1,j
    elif action=='d':
      grid[i][j], grid[i+1][j] = grid[i+1][j], grid[i][j]
      i,j = i+1,j
    elif action=='1':
      grid[i][j], grid[i][j-1] = grid[i][j-1], grid[i][j]
      i,j = i,j-1
    elif action == 'r':
      grid[i][j], grid[i][j+1] = grid[i][j+1], grid[i][j]
      i,j = i,j+1
    else:
      pass
  self.grid = grid
def possible_actions_to_create_solvable_maze(self,i: int, j:int, m:int)
  # neither corner nor edge
  if i not in [0,m-1] and j not in [0,m-1]:
    return ['u','r','d','l']
  # edge
  elif i not in [0,m-1] and j in [0,m-1]:
    if j==0:
      # left edge
      return ['u','r','d']
    else:
      # right edge
      return ['u','d','l']
```

```
elif i in [0,m-1] and j not in [0,m-1]:
    if i==0:
      # top edge
      return ['r','d','l']
    else:
      # bottom edge
      return ['u','r','l']
  # corners
  else:
    if (i,j) == (0,0):
      # top left
      return ['r','d']
    elif (i,j) == (0,m-1):
      # top right
      return ['d','l']
    elif (i,j) == (m-1,m-1):
      # bottom right
      return ['u','1']
    else:
      # bottom left
      return ['u', 'r']
def print current state of grid(self):
  print()
  for i in range(self.sides):
    for j in range(self.sides):
      print(self.grid[i][j],end=' ')
    print()
  # print(f'position of zero is {self.pos zero}')
  print()
def is goal state(self,grid: list):
  number = 1
  m = self.sides
  for i in range(m):
    for j in range(m):
      if (i,j) = (m-1,m-1) and grid[i][j] == number:
        number += 1
      elif (i,j) == (m-1,m-1):
        if grid[i][j] != 0:
          return False
      else:
        return False
  return True
```

```
In [13]: class Agent:
    def __init__(self,puzzle_grid: Sliding_Block_Grid) -> None:

        self.in_puzzle = puzzle_grid
        self.in_grid = puzzle_grid.grid.copy()
        self.length_of_puzzle = puzzle_grid.sides
        self.pos_agent = puzzle_grid.pos_zero
        # need not write list(puzzle_grid.pos_zero) because whenever pos_zero
```

```
# since list is call by reference
  self.grid_state = Grid_State(puzzle_grid.grid.copy())
  # grid state is initialized with a copy of the list
  # so any modification in this list will not affect in the original li
  self.solution_list = list()
  self.astar_explore_count_manhattan_distance = 0
  self.astar_explore_count_number_of_misplaced_blocks = 0
  self.astar explore count manhattan distance of zero = 0
def possible actions(self):
  m = self.length of puzzle
  i = self.pos agent[0]
  j = self.pos agent[1]
  # neither corner nor edge
  if i not in [0,m-1] and j not in [0,m-1]:
    return ['u','r','d','l']
  # edge but not corner
  elif i in [0,m-1] and j not in [0,m-1]:
    if i==0:
      # top edge
      return ['r','d','l']
      # bottom edge
      return ['r','l','u']
  elif i not in [0,m-1] and j in [0,m-1]:
    if j==0:
      # left edge
      return ['u','r','d']
      # right edge
      return ['u','d','l']
  # corner
  else:
    if (i,j) == (0,0):
      # top left
      return ['r','d']
    if (i,j) == (0,m-1):
      # top right
      return ['d','1']
    if (i,j) == (m-1,m-1):
      # bottom right
      return ['u','1']
      # bottom left
      return ['u','r']
def possible actions from state(self,grid state: Grid State):
 m = self.length of puzzle
  pos_agent = self.find_pos_zero(grid_state)
  i = pos agent[0]
  j = pos_agent[1]
  # neither corner nor edge
  if i not in [0,m-1] and j not in [0,m-1]:
    return ['u','r','d','l']
  # edge but not corner
```

```
elif i in [0,m-1] and j not in [0,m-1]:
    if i==0:
      # top edge
      return ['r','d','l']
    else:
      # bottom edge
      return ['r','l','u']
  elif i not in [0,m-1] and j in [0,m-1]:
    if j==0:
      # left edge
      return ['u','r','d']
    else:
      # right edge
      return ['u','d','l']
  # corner
  else:
    if (i,j) == (0,0):
      # top left
      return ['r','d']
    if (i,j) == (0,m-1):
      # top right
      return ['d','l']
    if (i,j) == (m-1,m-1):
      # bottom right
      return ['u','1']
    else:
      # bottom left
      return ['u', 'r']
def is goal state(self,grid state: Grid State):
  number = 1
  m = self.length of puzzle
  grid = grid state.grid
  for i in range(m):
    for j in range(m):
      if (i,j) != (m-1,m-1) and grid[i][j] == number:
        number += 1
      elif (i,j) == (m-1,m-1):
        if grid[i][j] != 0:
          return False
      else:
        return False
  return True
def create_copy(self,puzzle_grid: list):
  copy = [None for in range(self.length of puzzle)]
  for i in range(self.length_of_puzzle):
    copy[i] = list(puzzle_grid[i])
  return copy
def find_pos_zero(self,grid_state: Grid_State):
  grid = grid state.grid
  for i in range(self.length of puzzle):
    for j in range(self.length of puzzle):
      if grid[i][j] == 0:
```

```
return (i,j)
def child generator(self) -> Grid State:
  current_state_of_grid = self.in_puzzle.grid
  copy_of_current_state_of_grid = self.create_copy(current_state_of_grid
  possible_actions = self.possible_actions()
  num_possible_actions = len(possible_actions)
  children list = [
    self.create_copy(copy_of_current_state_of_grid) for _ in range(num_
  for i in range(num_possible_actions):
    self.do action(children list[i],possible actions[i])
  children states = [
    Grid State(child grid) for child grid in children list
  return children states
def child_generator_from_state(self, grid_state: Grid_State):
  grid = list(grid state.grid)
  possible actions = self.possible actions from state(grid state)
  num possible actions = len(possible actions)
  children list = [
    self.create_copy(grid) for _ in range(num_possible_actions)
  children states = [
    Grid_State(child_list) for child_list in children_list
  for i in range(num possible actions):
    self.do_action_from_state(children_states[i],possible_actions[i])
  return children states
def do action from state(self,grid state: Grid State, action: str):
  pos agent = self.find pos zero(grid state)
  i = pos_agent[0]
  j = pos agent[1]
  grid = grid state.grid
  if action == 'u':
    grid[i][j], grid[i-1][j] = grid[i-1][j], grid[i][j]
  elif action == 'r':
    grid[i][j], grid[i][j+1] = grid[i][j+1], grid[i][j]
  elif action == 'd':
    grid[i][j], grid[i+1][j] = grid[i+1][j], grid[i][j]
  elif action == '1':
    grid[i][j], grid[i][j-1] = grid[i][j-1], grid[i][j]
  else:
    pass
def do_action(self,grid: list, action: str):
  i = self.pos agent[0]
  j = self.pos_agent[1]
  if action == 'u':
    grid[i][j], grid[i-1][j] = grid[i-1][j], grid[i][j]
  elif action == 'r':
    grid[i][j], grid[i][j+1] = grid[i][j+1], grid[i][j]
  elif action == 'd':
    grid[i][j], grid[i+1][j] = grid[i+1][j], grid[i][j]
  elif action == '1':
```

```
grid[i][j], grid[i][j-1] = grid[i][j-1], grid[i][j]
  else:
    pass
def astar search using manhattan(self,print route = True):
  self.astar_explore_count_manhattan_distance = 0
  initial_state = self.grid_state
  # create a queue
  q = queue.PriorityQueue()
  # tuple is priority number, data
  g_function = 0
  # depth distance is the g function
  initial state.depth distance = 0
  # priority is based on f function = g+h
  tuple_to_be_added = (initial_state.manhattan_distance heuristic + g_f
  q.put(tuple_to_be_added)
  if self.is_goal_state(initial_state) or initial_state.manhattan_dista
    if print route:
      print('Solution found')
      self.print solution(initial state)
    return
  while not q.qsize == 0:
    self.astar explore count manhattan distance += 1
    u_state = q.get()[1]
    u_state: Grid_State
    children states = self.child generator from state(u state)
    for child state in children states:
      child state: Grid State
      child state.parent = u state
      if self.is goal state(child state) or child state.manhattan dista
        if print route:
          print('Solution found')
          self.print solution(child state)
        return
      child_state.depth_distance = u_state.depth_distance + 1
      tuple to be added to priority queue = (child state.manhattan dist
      # print('not yet found')
      g.put(tuple to be added to priority queue)
def astar search using number of misplaced blocks(self,print route = Tr
  self.astar explore count number of misplaced blocks = 0
  initial state = self.grid state
  initial_state.depth_distance = 0
  # create a queue
  q = queue.PriorityQueue()
  # tuple is priority number, data
  tuple to be added = (initial state number of misplaced blocks + initi
  q.put(tuple_to_be_added)
  if self.is goal state(initial state) or initial state.number of mispl
    if print route:
      print('Solution found')
      self.print_solution(initial_state)
```

```
return
 while not q.qsize == 0:
    self.astar_explore count_number_of_misplaced blocks += 1
    u_state = q.get()[1]
    u state: Grid State
    children states = self.child generator from state(u state)
    for child state in children states:
      child_state: Grid_State
      child state.parent = u state
      if self.is goal state(child state) or child state.number of mispl
        if print route:
          print('Solution found')
          self.print_solution(child_state)
        return
      child_state.depth_distance = u_state.depth_distance + 1
      tuple to be added to priority queue = (child state.number of misp
      # print('not yet found')
      q.put(tuple to be added to priority queue)
def astar_search_using_manhattan_distance_of_zero(self,print_route = Tr
  self.astar explore count manhattan distance of zero = 0
  initial_state = self.grid_state
  # create a queue
  q = queue.PriorityQueue()
  # tuple is priority number, data
  initial state.depth distance = 0
 tuple to be added = (initial state manhattan distance heuristic of ze
  q.put(tuple to be added)
  if self.is goal state(initial state):
    if print route:
      print('Solution found')
      self.print_solution(initial_state)
    return
 while not q.qsize == 0:
    self.astar explore count manhattan distance of zero += 1
    u_state = q.get()[1]
    u_state: Grid_State
    children_states = self.child_generator_from_state(u_state)
    for child state in children states:
      child_state: Grid_State
      child_state.parent = u_state
      if self.is_goal_state(child_state):
        if print route:
          print('Solution found')
          self.print solution(child state)
      child_state.depth_distance = u_state.depth_distance + 1
```

```
tuple to be added to priority queue = (child state.manhattan dist
      # print('not yet found')
      q.put(tuple_to_be_added_to_priority_queue)
def print grid(self,grid state: Grid State):
  print()
  grid = grid state.grid
  for i in range(self.length_of_puzzle):
    for j in range(self.length_of_puzzle):
      print(grid[i][j],end=' ')
    print()
  print()
def print_solution(self,state_of_grid: Grid_State):
  if state_of_grid == None:
    return
  self.print solution(state of grid.parent)
  self.print grid(state of grid)
```

```
In [15]: puzzle = Sliding_Block_Grid(3)
   puzzle.print_current_state_of_grid()
   agent = Agent(puzzle_grid=puzzle)
```

0 7 8

(a) Use A\* search to start from any given initial configuration and reach the goal configuration

123

456

780

7 8 0

with the sum of Manhattan distances of the blocks from their goal positions as the heuristic. The Manhattan distance of a pair of blocks occupying the integer n at the locations (i,p) and (j,q) (where  $i,j,p,q\in\{0,\ldots,8\}$  and  $n\in\{0,\ldots,8\}$ ) is given by |i-j|+|p-q|. Print the total number of steps taken to reach the goal and the blocks configuration at each step.

```
In [16]: agent.astar_search_using_manhattan()
print(f'Astar search using total manhattan distance as heuristic explored

Solution found

1 2 3
4 5 6
0 7 8

1 2 3
4 5 6
7 0 8
```

Astar search using total manhattan distance as heuristic explored 3 state  ${\bf s}$ 

- (b) Repeat part (a) with the following alternative heurisitics.
  - 1. the number of misplaced blocks
- 2. the Manhattan distance of the "0" block alone instead of the sum

Compare the performance of the three heuristics using the size of the explored list as the measure.

```
Solution found
         1 2 3
         4 5 6
         0 7 8
         1 2 3
         4 5 6
         7 0 8
         1 2 3
         4 5 6
         7 8 0
         Astar search using total number of misplaced tiles as heuristic explored
         3 states
In [18]: # before running this cell change the lt function of GridState
         agent.astar_search_using_manhattan_distance_of_zero()
         print(f'astar search using manhattan distance of zero as heuristic explor
         Solution found
         1 2 3
         4 5 6
         0 7 8
         1 2 3
         4 5 6
         7 0 8
         1 2 3
         4 5 6
         7 8 0
         astar search using manhattan distance of zero as heuristic explored 3 sta
In [22]: # to compute efficiency
         explored_astar = 0
         for _{in} range(100):
           puzzle_new = Sliding Block Grid(input_puzzle=False)
           agent new = Agent(puzzle new)
           agent new.astar search using manhattan(False)
           explored astar += agent new.astar explore count manhattan distance
           del agent new
```

the average number of vertices explored is 568.0

print(f'the average number of vertices explored is {explored\_astar/100}')

del puzzle\_new

```
In [23]: # before running this cell change the __lt__ function of GridState

explored = 0
for _ in range(100):
    puzzle_new = Sliding_Block_Grid(input_puzzle=False)
    agent_new = Agent(puzzle_new)
    agent_new.astar_search_using_number_of_misplaced_blocks(False)
    explored += agent_new.astar_explore_count_number_of_misplaced_blocks
    del agent_new
    del puzzle_new
    print(f'the average number of vertices explored is {explored/100}')
```

the average number of vertices explored is 964.92

```
In []: # before running this cell change the __lt__ function of GridState

explored = 0
for i in range(100):
    puzzle_new = Sliding_Block_Grid(input_puzzle=False,depth_for_generating
    agent_new = Agent(puzzle_new)
    agent_new.astar_search_using_manhattan_distance_of_zero(False)
    explored += agent_new.astar_explore_count_manhattan_distance_of_zero
    del agent_new
    del puzzle_new
    print(f'the average number of vertices explored is {explored/100}')
```

```
In []:
```