MODULE *modified_petersons_algo*

EXTENDS *Integers*

VARIABLES $pc0$, $pc1$, $turn$, $intr0$, $intr1$

$TypeOK \triangleq$
$\land\ pc0 \in 0 \,..\, 7$
$\land\ pc1 \in 0 \,..\, 7$
$\land\ turn \in \{0, 1\}$
$\land\ intr0 \in \{0, 1\}$
$\land\ intr1 \in \{0, 1\}$

Change the algo so that in $P0$, Replace $turn = 1$ by $turn = 0$ and in $P1$, replace $turn = 0$ by $turn = 1$ and again check for mutual exclusion principle

asynchronous system

for $i = 0, 1$

the algorithm is

```
0 : while(True){
1 :     //non critical section
2 :     intr[i] = True
3 :     turn = i//MODIFIED
4 :     while(turn ≜ 1 and intr[1 − i] ≜ 1)//wait
5 :     //critical section
6 :     intr[i] = 0
7 : }
```

$Init0 \triangleq$
$\land\ turn = 0$
$\land\ intr0 = 0$
$\land\ pc0 = 0$

$Init1 \triangleq$
$\land\ turn = 0$
$\land\ intr1 = 0$
$\land\ pc1 = 0$

$Init \triangleq Init0 \land Init1$

$L01 \triangleq$
$\land\ pc0 = 0$
$\land\ pc0' = 1$
$\land$ UNCHANGED $\langle turn, intr0, intr1 \rangle$

$L12 \triangleq$
$\land\ pc0 = 1$
$\land\ pc0' = 2$

$\land$ UNCHANGED $\langle turn,\ intr0,\ intr1\rangle$

$L23 \triangleq$
$\land\ pc0 = 2$
$\land\ pc0' = 3$
$\land\ intr0' = 1$
$\land$ UNCHANGED $\langle intr1,\ turn\rangle$

$L34 \triangleq$
$\land\ pc0 = 3$
$\land\ pc0' = 4$
$\land\ turn' = 0$
$\land$ UNCHANGED $\langle intr0,\ intr1\rangle$

$L44 \triangleq$
$\land\ pc0 = 4$
$\land\ pc0' = 4$
$\land\ turn = 1$
$\land\ intr1 = 1$
$\land$ UNCHANGED $\langle intr0,\ intr1,\ turn\rangle$

$L45 \triangleq$
$\land\ pc0 = 4$
$\land\ pc0' = 5$
$\land\ (turn = 0 \lor intr1 = 0)$
$\land$ UNCHANGED $\langle turn,\ intr0,\ intr1\rangle$

$L56 \triangleq$
$\land\ pc0 = 5$
$\land\ pc0' = 6$
$\land$ UNCHANGED $\langle intr0,\ intr1,\ turn\rangle$

$L67 \triangleq$
$\land\ pc0 = 6$
$\land\ pc0' = 7$
$\land\ intr0' = 0$
$\land$ UNCHANGED $\langle intr1,\ turn\rangle$

$L70 \triangleq$
$\land\ pc0 = 7$
$\land\ pc0' = 0$
$\land$ UNCHANGED $\langle turn,\ intr0,\ intr1\rangle$

$SLOGP \triangleq$ UNCHANGED $\langle pc0,\ intr0,\ intr1,\ turn\rangle$

for the second system

$M01 \triangleq$
$\land\ pc1 = 0$
$\land\ pc1' = 1$
$\land$ UNCHANGED $\langle turn,\ intr0,\ intr1 \rangle$

$M12 \triangleq$
$\land\ pc1 = 1$
$\land\ pc1' = 2$
$\land$ UNCHANGED $\langle turn,\ intr0,\ intr1 \rangle$

$M23 \triangleq$
$\land\ pc1 = 2$
$\land\ pc1' = 3$
$\land\ intr1' = 1$
$\land$ UNCHANGED $\langle intr0,\ turn \rangle$

$M34 \triangleq$
$\land\ pc1 = 3$
$\land\ pc1' = 4$
$\land\ turn' = 1$
$\land$ UNCHANGED $\langle intr0,\ intr1 \rangle$

$M44 \triangleq$
$\land\ pc1 = 4$
$\land\ pc1' = 4$
$\land\ turn = 0$
$\land\ intr0 = 1$
$\land$ UNCHANGED $\langle intr0,\ intr1,\ turn \rangle$

$M45 \triangleq$
$\land\ pc1 = 4$
$\land\ pc1' = 5$
$\land\ (turn = 1 \lor intr0 = 0)$
$\land$ UNCHANGED $\langle turn,\ intr0,\ intr1 \rangle$

$M56 \triangleq$
$\land\ pc1 = 5$
$\land\ pc1' = 6$
$\land$ UNCHANGED $\langle intr0,\ intr1,\ turn \rangle$

$M67 \triangleq$
$\land\ pc1 = 6$
$\land\ pc1' = 7$
$\land\ intr1' = 0$
$\land$ UNCHANGED $\langle intr0,\ turn \rangle$

$M70 \triangleq$

$\land\ pc1 = 7$
$\land\ pc1' = 0$
$\land$ UNCHANGED $\langle turn,\ intr0,\ intr1\rangle$

$SLOGQ \triangleq$ UNCHANGED $\langle pc1,\ intr0,\ intr1,\ turn\rangle$

$Next\_First \triangleq$
$\lor\ L01$
$\lor\ L12$
$\lor\ L23$
$\lor\ L34$
$\lor\ L45$
$\lor\ L56$
$\lor\ L67$
$\lor\ L70$
$\lor\ SLOGP$

$Next\_Second \triangleq$
$\lor\ M01$
$\lor\ M12$
$\lor\ M23$
$\lor\ M34$
$\lor\ M45$
$\lor\ M56$
$\lor\ M67$
$\lor\ M70$
$\lor\ SLOGQ$

$Next \triangleq (Next\_First \land$ UNCHANGED $pc1) \lor (Next\_Second \land$ UNCHANGED $pc0)$

$Mutual\_Exclusion \triangleq (pc0 \neq 5) \lor (pc1 \neq 5)$

we need justice conditions, because here in this example, it can happen that
the scheduler never schedules one process
we want to avoid such runs ?????

justice conditions

$J00 \triangleq pc0 \neq 0$
$J02 \triangleq pc0 \neq 2$
$J03 \triangleq pc0 \neq 3$

we cannot write $pc0 \neq 4$, because that's not a requirement, it should be proven
$J04 \triangleq \neg((pc0 = 4) \land ((turn = 0) \lor (intr1 = 0)))$
$J05 \triangleq pc0 \neq 5$
$J06 \triangleq pc0 \neq 6$
$J07 \triangleq pc0 \neq 7$

for the process 1

$J10 \triangleq pc1 \neq 0$
$J12 \triangleq pc1 \neq 2$
$J13 \triangleq pc1 \neq 3$

$J14 \triangleq \neg((pc1 = 4) \land ((turn = 0) \lor (intr0 = 0)))$
$J15 \triangleq pc1 \neq 5$
$J16 \triangleq pc1 \neq 6$
$J17 \triangleq pc1 \neq 7$

the below justice conditions are to ensure that the scheduler is fair

$J \triangleq$
$\land J00$
$\land J02$
$\land J03$
$\land J04$
$\land J05$
$\land J06$
$\land J07$
$\land J10$
$\land J12$
$\land J13$
$\land J14$
$\land J15$
$\land J16$
$\land J17$

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