ECE4880J — Computer Vision

Guest Lecture on 3D Vision

Prof. He Wang

About Me

· 王鶴

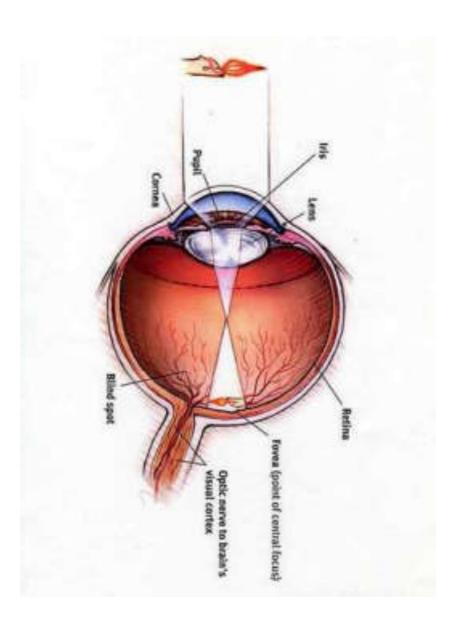
- Assistant Professor in Center on Frontiers of Computing Studies (CFCS)
- Joined PKU in September, 2021
- Received Ph.D. from Stanford in 2021
- Received Bachelor from Tsinghua in 2014
- Our lab: Embodied Perception and InteraCtion (EPIC) Lab
- Research interest: 3D vision, Robotics
- Homepage: https://hughw19.github.io/





Why 3D Vision?

Monocular Vision



Issue of 2D Vision

- We don't know true distance between pixels.
- Depth scale ambiguity



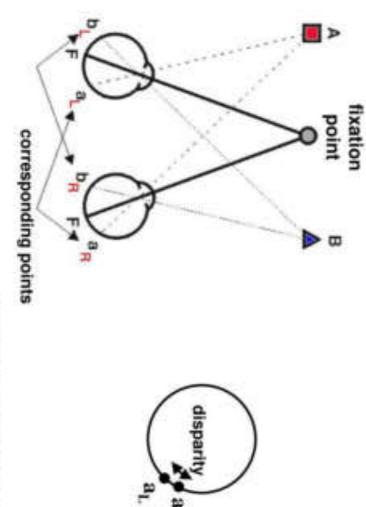
Courtesy side S. Lazebnik

Binocular Vision and Stereopsis

Human eyes are binocular.

 Senses distances through stereopsis

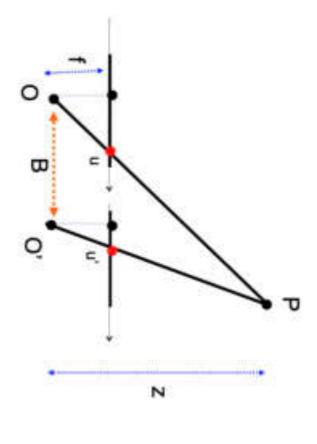
Human stereo geometry



http://webvision.med.utah.edu/space_perception.html

S. Brothfield, Chimson Univ., ECE 847,

Computing Depth



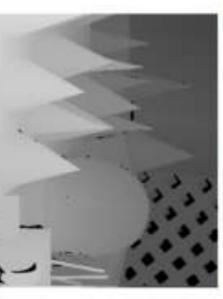
$$u - u' = \frac{B \cdot f}{z} = \text{disparity}$$

[Eq. 1]

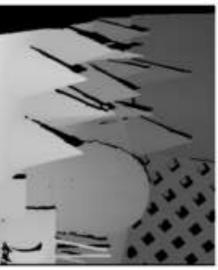
Note: Disparity is inversely proportional to depth

Disparity Maps





Disparity map / depth map



Disparity map with occlusions

Where are 3D Data from?

3D Data: from Sensors or Graphics



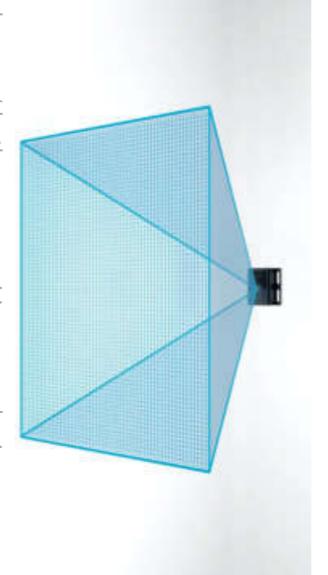
Real 3D data acquired by 3D sensing



Synthetic 3D data

Depth Sensors

- Depth sensors are a form of 3D range finder
- Measure multi-point distance information across a wide Field-of-View (FoV)



https://www.terabee.com/depth-sensors-precision-personal-privacy

Stereo Sensor

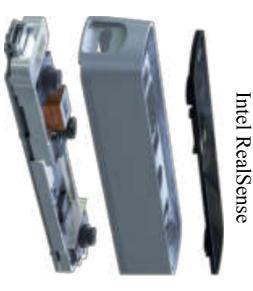
Compute disparity and turn into depth.



Stereolabs Zed







Occipital Structure Core

Stereo Vision

- Advantage:

 1. Robust to the illumination of direct sunlight
- 2. Low implementation cost

Drawback:

is hard and erroneous Finding correspondences along $Image_L$ and $Image_R$

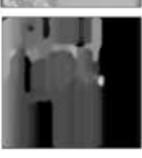
Failure of correspondence search



Occlusions, repetition

Textureless surfaces





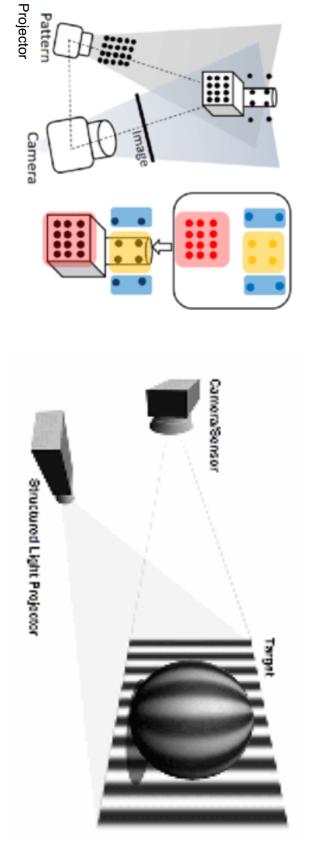
Non-Lambertian surfaces, specularities

Structured Light

- Belongs to active stereoscopic approaches
- One camera replaced by an infrared projection unit
- Generates a pattern by projecting on the imaged surface

Advantage

- 1. Simplify the correspondence problem Drawback:
- 1. Near field
- 2. Indoor



Time-of-Flight



Microsoft Kinect v2 (2013)



Microsoft Azure Kinect (2020)

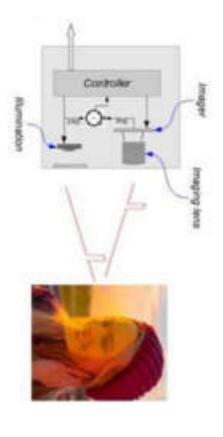


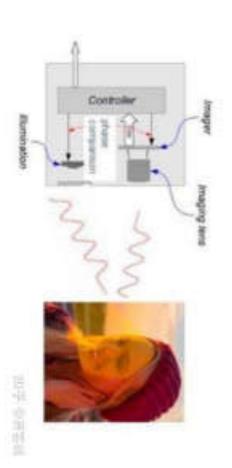
iPad Pro 2019 LiDAR

iToF vs. dToF

- dToF (the future)
- Direct time-of-flight
- Pulse wave
- Long range
- Theoretically higher precision but currently lower resolution
- Expensive (needs SPAD)

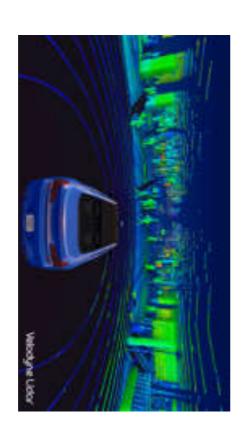
- iToF (Classic 3D imaging)
- Indirect time-of-flight
- Sin wave and solve for phase shift
- Lower range
- Lower precision but higher resolution
- Cheaper





LiDAR in Autonomous Driving Cars

- A ToF sensor (mostly dToF) + a rotating scanner
- High laser intensity that supports sensing up to 200 meters and more
- Currently pretty low resolution (32 beams are common)





Summary of Different Depth Sensors

Medium	Limited	Range
Medium		
	Low	Power Consumption
Weak	Good	Bright-Light Performance
Good	Weak	Low-Light Performance
High	Low	Depth Accuracy
Slow	Medium	Response Time
High	Low	Compactness
High	Low	Material Cost
Medium	High	Software Complexity
STRUCTURED-LIGHT	STEREO VISION	CONSIDERATIONS
	STRUCTURED-LIGHT Medium High High	EO VISION

CAD Models from Graphics Community

- CAD: computer-aided design models
- Widely used in
- Graphics applications, including games, movies, animations, etc.
- 3D printing and fabrications
- •



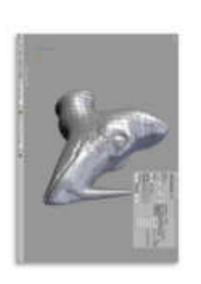
https://www.cadnav.com/3d-models.model-49123.html

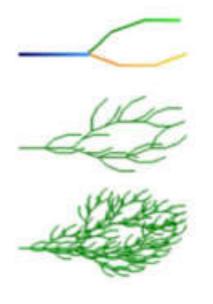


https://www.ptc.com/-/media/Images/CAD-Blog/2018/June/materialise/3d-printer.png?sc_lang=en

How to Obtain CAD Models

- Modeling by designers
- 3D shape synthesis algorithm
- Procedural modeling
- Generative models
- Acquired by 3D scans





Synthetic Datasets for 3D Objects

Large-scale Synthetic Objects: ShapeNet



ModelNet: absorbed by ShapeNet

Chang et al., "ShapeNet: An Information-Rich 3D Model Repository", *arXiv* Wu et al., "3D ShapeNets: A deep representation for volumetric shapes", *CVPR 2015* Choi et al., "A Large Dataset of Object Scans", *arXiv*

Datasets for Indoor 3D Scenes

Large-scale Synthetic Scenes: SceneNet

3D meshes 5M Photorealistic Images



Ankur et al., "Understanding RealWorld Indoor Scenes with Synthetic Data", CVPR 2016

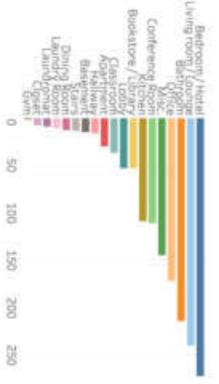
McCormac et al., "SceneNet RGB-D: Can 5M Synthetic Images Beat Generic ImageNet Pre-training on Indoor Segmentation?", ICCV 2017

Datasets for Indoor 3D Scenes

Large-scale Scanned Real Scenes: ScanNet

2.5 M Views in 1500 RGBD scans3D camera posessurface reconstructionsInstance-level semantic segmentations





Dai et al., "ScanNet: Richly-annotated 3D Reconstructions of Indoor Scenes", CVPR 2017

Datasets for Outdoor 3D Scenes

KITTI: LiDAR data, labeled by 3D bboxes



Semantic KITTI: LiDAR data, labeled per point



Waymo Open Dataset: LiDAR data, labeled by 3D b.boxes



3D Representations

2D Image Representations





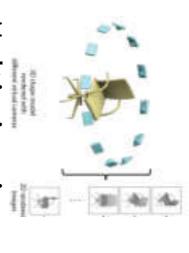
 $H \times W \times 3$

Multiple 3D Representations



Regular form

Irregular form



Multi-view images



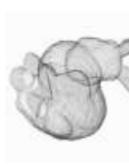
Depth



Volumetric



Surface Mesh

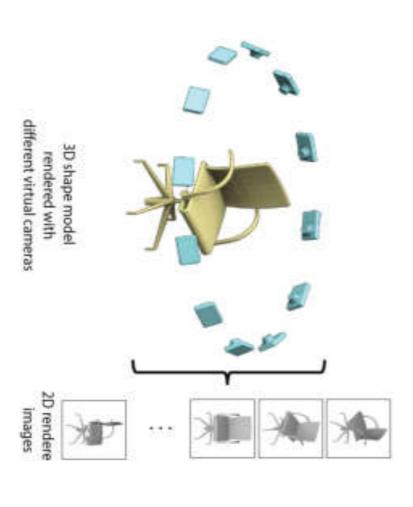


Point Cloud



Implicit representation

Multi-View Images



- Multiple images from different viewpoints
- Contain 3D information
- Indirect, not a true 3D representation

Depth Image



 A single-channel image filled by depth values
 A 2.5D representation

True 3D representation should enable distance measurement between two points.

Voxels



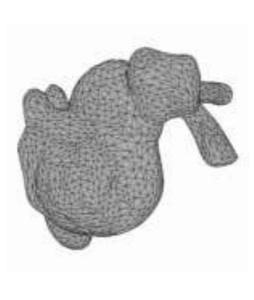
Voxels

- $H \times W \times D$
- Can be indexed
- An expensive geometry representation
- Not a surface representation
- Where is the surface?

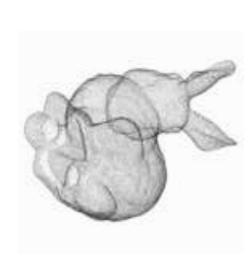
How to upsample?

30

Irregular 3D Representation



Mesh



Point Cloud

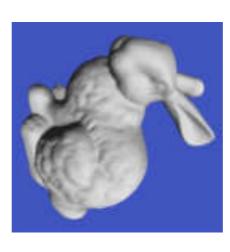


Implicit representation

- Irregular representation
- Model the 3D via capturing the surface or something on the surface

Mesh

Surface Mesh

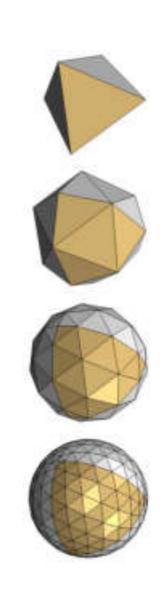




- A piece-wise Linear Surface Representation
- Both a geometry and surface representation

Mesh of Stanford Bunny

Different Kinds of Mesh in Different Resolutions



Triangle mesh at different resolutions



Quad mesh

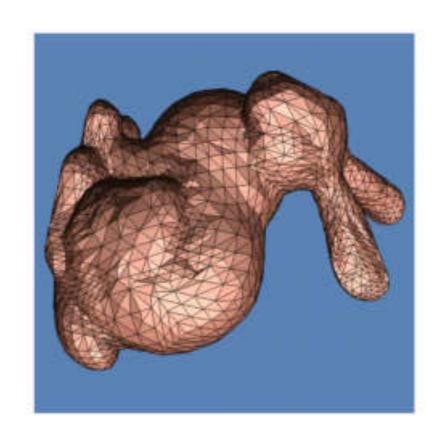
Triangle Mesh

- Mesh essentially is a graph: {vertex, edge}
- Faces are triangles

$$V = \{v_1, v_2, ..., v_n\} \subset \mathbb{R}^3$$

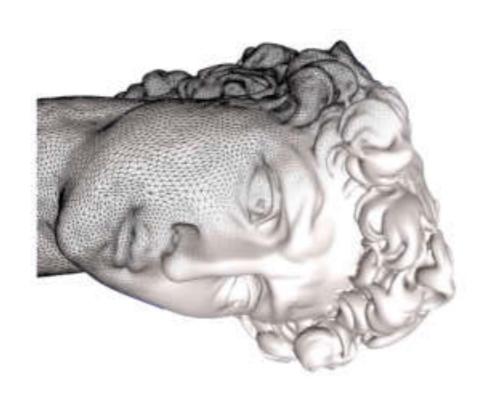
 $E = \{e_1, e_2, ..., e_k\} \subseteq V \times V$
 $F = \{f_1, f_2, ..., f_m\} \subseteq V \times V \times V$

http://graphics.stanford.edu/data/3Dscanrep/stanford-bunny-cebal-ssh.jpg http://www.stat.washington.edu/wxs/images/BUNMID.gif



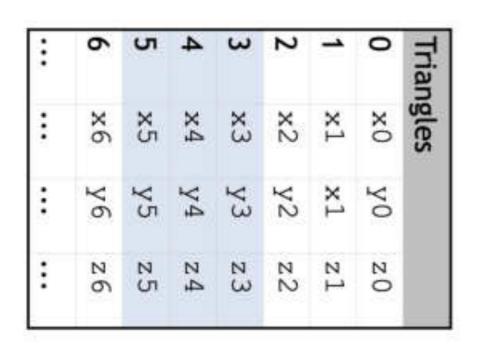
Data Structure for Mesh

- What information should be stored?
- Geometry: 3D coordinates
- Topology
- Attributes
- Normal, color, texture coordinates
- Per vertex, face, edge



Simple Data Structure: Triangle List

- STL format (used in CAD)
- Stored information
- Face: 3 positions
- No connectivity information



Indexed Face Set

- Used in formats
- OBJ, OFF, WRL
- Stored information
- Vertex: position

Face: vertex indices

 Convention is to save vertices in counterclockwise order (right hand rule) for normal direction (pointing out)

:	6	5	4	2	2	≤	8	Ver
:	×	×	×4	×з	x2	×	×o	Vertices
:	У6	У5	у4	У3	у2		У0	SS
:	20	25	z4	z3	22	21	20	

:	ದ	72	ユ	to	Tria
Ė	ν5	٧2	v0	ν0	Triangles
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Point Cloud

Point Cloud

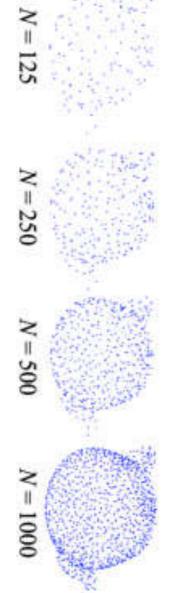


Point Cloud

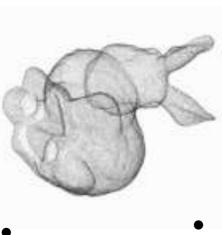


- Irregular and orderless data
- A light-weight geometric representation
- Compact to store
- Easy to understand and generally easy to build algorithms





Limitations of Point Cloud

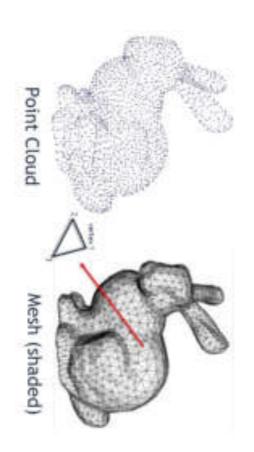


Point Cloud

- Point cloud is not a surface representation
- where is the surface?
- Point cloud = surface + sampling
- How to sample point clouds from a mesh surface?

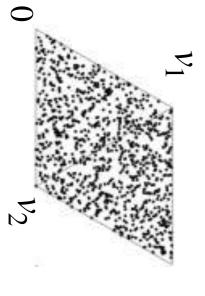
Sampling Strategy: Uniform Sampling

- 1. Compute the areas of each individual face
- 2. Compute the probability of each face and use it as weight
- 3. Independent identically distributed weights (i.i.d.) sample faces according to the
- 4. For each sampled face, uniformly sample from one triangle face



Uniform Sampling Points in a Triangle

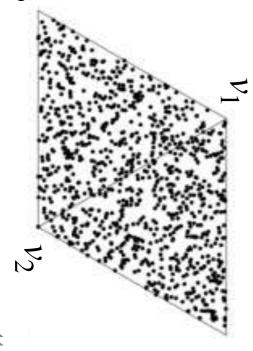
- Special case: for a triangle with one vertex at the origin and the others at positions v_1 and v_2 :
- To pick points uniformly distributed inside the triangle, we can do $x=a_1v_1+a_2v_2$, where a_1 and a_2 are uniform variates in the interval
- This gives points uniformly distributed in a quadrilateral. The points not in the triangle interior can then be transformed into the corresponding point inside the triangle.



Uniform Sampling Points in a Triangle

- General case: for a triangle with vertices ν_1, ν_2, ν_3 :
- $x = v_3 + a_1(v_1 v_3) + a_2(v_2 v_3) = a_1v_1 + a_2v_2 + (1 a_1 a_2)v_3$, where a_1 and a_2 are uniform variates in the interval $\left[0,1\right]$
- If $a_1 + a_2 \le 1$, then x will be inside the triangle (or on the edges);
- If $a_1 + a_2 > 1$, then x can be mapped back to the triangle interior via

$$x = (1 - a_1)\nu_1 + (1 - a_2)\nu_2 + (a_1 + a_2)\nu_3$$



Alternative Approach

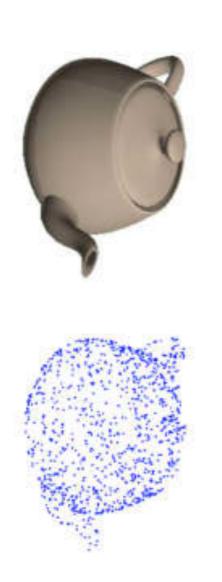
$$x = (1 - \sqrt{r_1})\nu_1 + \sqrt{r_1}(1 - r_2)\nu_2 + \sqrt{r_1}r_2\nu_3$$

• Here $r_1, r_2 \sim U(0,1)$.

- Proof:
- If this is true for one triangle, it is true for all triangles, as we can find an affine transformation between them
- Use $v_1 = (0,0), v_2 = (1,0), v_3 = (0,1)$
- Prove x is always inside the triangle.
- Show that the probability to be within an area of (0,x) imes(0,y) is always

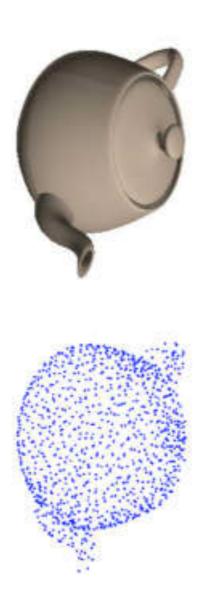
Sampling Strategy: Uniform Sampling

- Usually the easiest to implement
- Issue: Irregularly spaced sampling



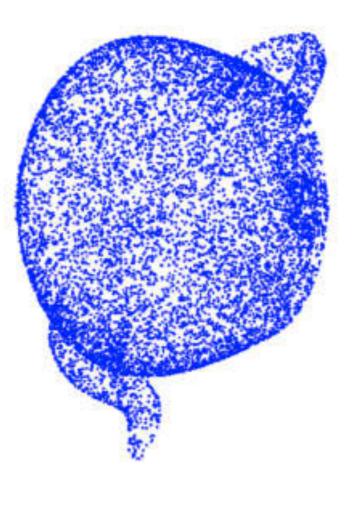
Farthest Point Sampling (FPS)

- Goal: Sampled points are far away from each other
- NP-hard problem
- What is a greedy approximation method?



Iterative Furthest Point Sampling

Step 1: Over sample the shape by any fast method (e.g., uniformly sample N=10,000 i.i.d. samples)

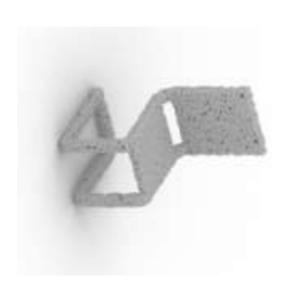


Iterative Furthest Point Sampling

Step 2: Iteratively select K points

```
U is the initial big set of points S = \{\}
                       for i=1 to K find a point u \in U with the largest distance to S
                                                                                                 add a random point from U to S
add u to S
```

Visualization: Uniform Sampling vs. FPS



• FPS



Uniform sampling

With the same number of sampled points.

Wang et al. Rethinking Sampling in 3D Point Cloud Generative Adversarial Networks.

How to measure the distance between two point clouds?





Chamfer distance We define the Chamfer distance be-

tween
$$S_1, S_2 \subseteq \mathbb{R}^3$$
 as:
$$d_{CD}(S_1, S_2) = \sum_{x \in S_1} \min_{y \in S_2} \|x - y\|_2 + \sum_{y \in S_2} \min_{x \in S_1} \|x - y\|_2$$



A Point Set Generation Network for 3D Object Reconstruction from a Single Image, CVPR 2016

tween $S_1, S_2 \subseteq \mathbb{R}^3$ as: Chamfer distance We define the Chamfer distance be-

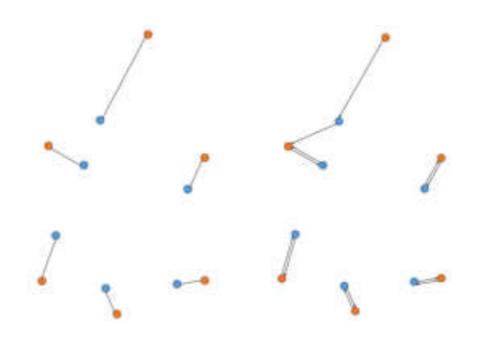
$$d_{CD}(S_1, S_2) = \sum_{x \in S_1} \min_{y \in S_2} ||x - y||_2 + \sum_{y \in S_2} \min_{x \in S_1} ||x - y||_2$$

size $s = |S_1| = |S_2|$. The EMD between A and B is defined Earth Mover's distance Consider $S_1, S_2 \subseteq \mathbb{R}^3$ of equal

$$d_{EMD}(S_1, S_2) = \min_{\phi: S_1 \to S_2} \sum_{x \in S_1} ||x - \phi(x)||_2$$

where $\phi: S_1 \to S_2$ is a bijection.

A Point Set Generation Network for 3D Object Reconstruction from a Single Image, CVPR 2016



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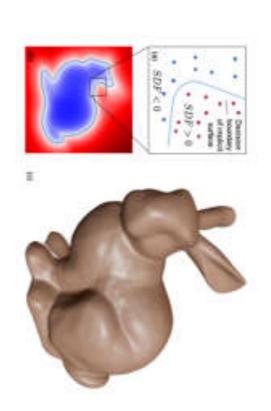
where $\phi: S_1 \to S_2$ is a bijection.

Sum of the closest distances Insensitive to sampling

Sum of the matched closest distances
Sensitive to sampling

Implicit Field

Implicit Shape



SDF

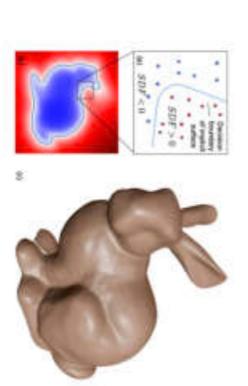
- Both an implicit geometry and surface representation
- Can convert into mesh
- Signed distance function, unsigned distance function, occupancy network

Signed Distance Function (SDF)

Interior: F(x, y, z) < 0Exterior: F(x, y, z) > 0Surface: F(x, y, z) = 0 (zero set, zero iso-surface)

Example implementation:

- SDF: F(x, y, z) = distance to the surface

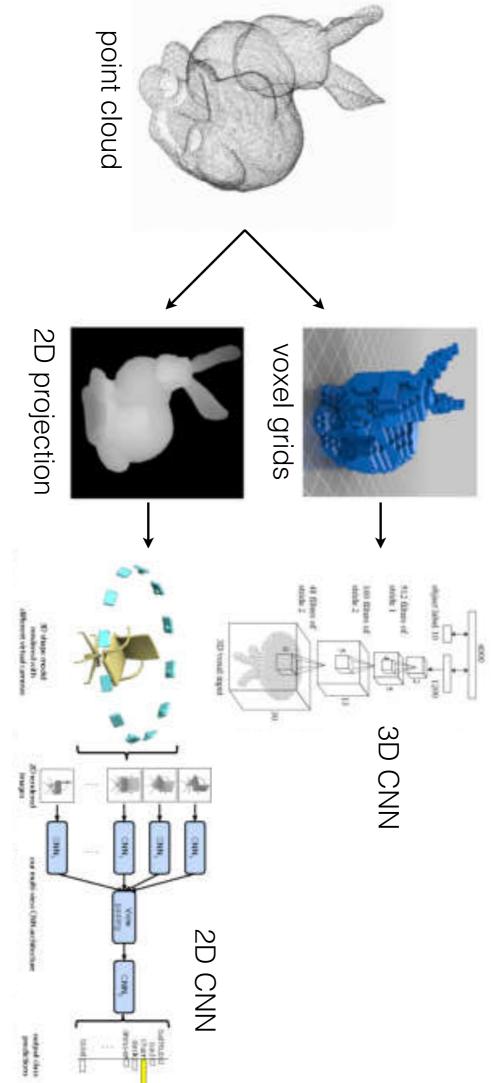


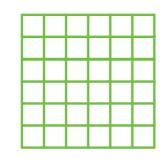
3D Deep Learning

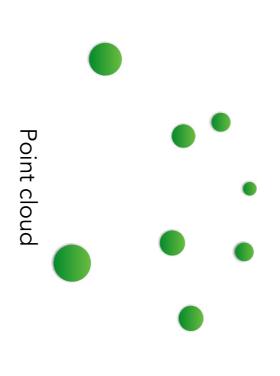
Outline

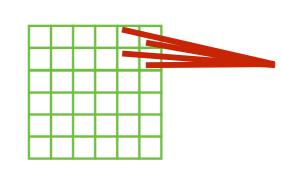
- Point Networks
- PointNet
- PointNet++
- Voxel Networks
- Networks for other representations
- SDF
- Mesh

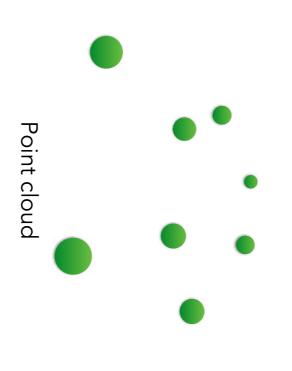
Straightforward Ways of Processing Point Clouds

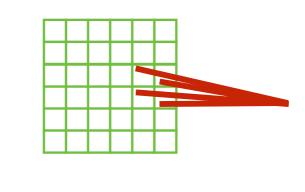


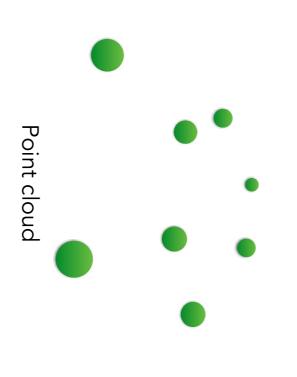


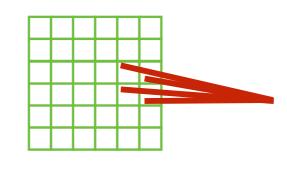


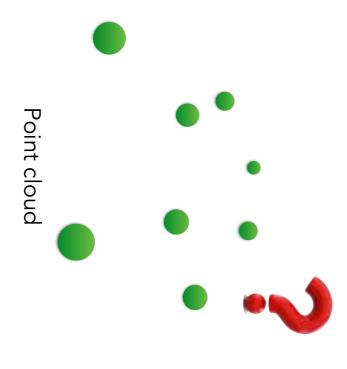












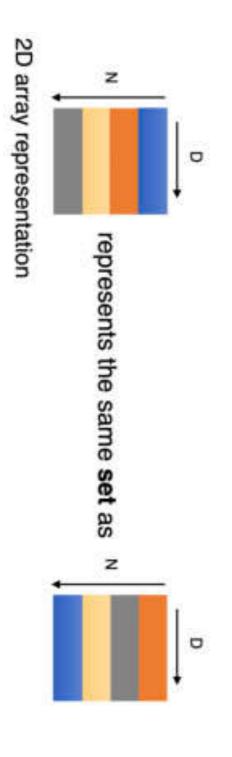
Unordered Inputs

Point cloud: N orderless points, each represented by a D dim coordinate



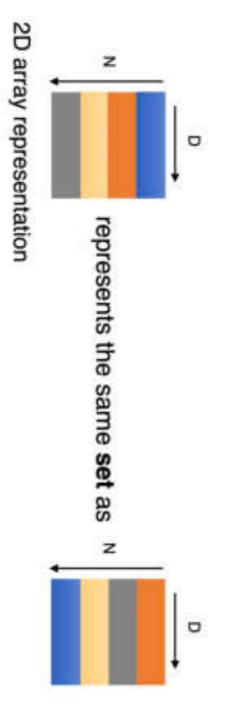
Unordered Inputs

Point cloud: N orderless points, each represented by a D dim coordinate



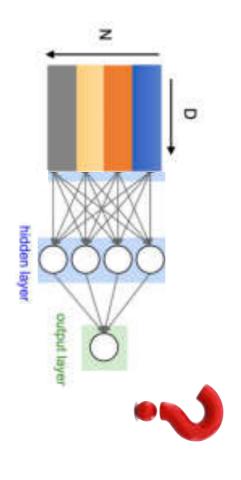
Desired Properties of a Point Cloud Network

Point cloud: N orderless points, each represented by a D dim coordinate

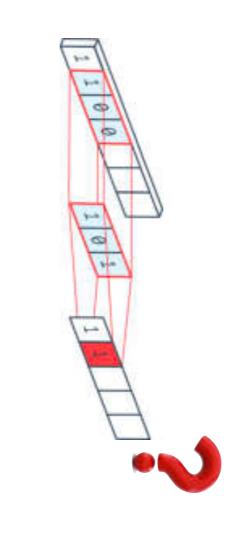


Deep net needs to be invariant to N! permutations

Permutation Invariance



Fully connected network



1D convolutional network

Permutation Invariance — Sorting?

lexsorted
$$(1,2,3) \qquad (1,1,1) \\ (1,1,1) \qquad (1,2,3) \qquad MLP \qquad (2,3,2) \qquad MLP \qquad (2,3,4) \qquad (2,3,4)$$

Not a good idea! Adding one point will change the order dramatically!

Permutation Invariance: Symmetric Function

$$f(x_1,x_2,...,x_n) \equiv f(x_{\pi_1},x_{\pi_2},...,x_{\pi_n}), x_i \in \mathbb{R}^D$$

Permutation Invariance: Symmetric Function

$$f(x_1,x_2,...,x_n) \equiv f(x_{\pi_1},x_{\pi_2},...,x_{\pi_n}), x_i \in \mathbb{R}^D$$

Examples:

$$f(x_1,x_2,...,x_n) = \max\{x_1,x_2,...,x_n\}$$
$$f(x_1,x_2,...,x_n) = x_1 + x_2 + ... + x_n$$

Permutation Invariance: Symmetric Function

$$f(x_1,x_2,...,x_n) \equiv f(x_{\pi_1},x_{\pi_2},...,x_{\pi_n}), x_i \in \mathbb{R}^D$$

Examples:

$$f(x_1,x_2,...,x_n) = \max\{x_1,x_2,...,x_n\}$$

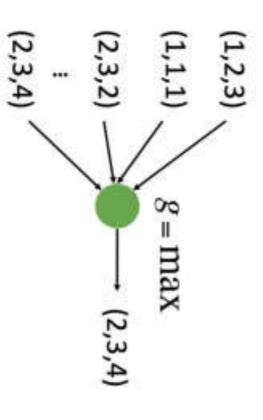
 $f(x_1,x_2,...,x_n) = x_1 + x_2 + ... + x_n$

:

How can we construct a universal family of symmetric functions by neural networks?

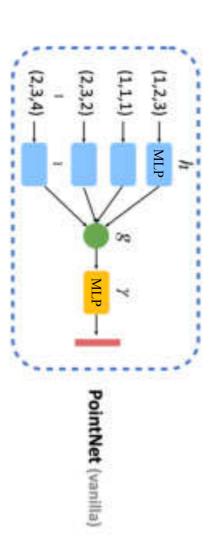
Construct Symmetric Functions by Neural Networks

Simplest form: directly aggregate all points with a symmetric operator gJust discovers simple extreme/aggregate properties of the geometry.



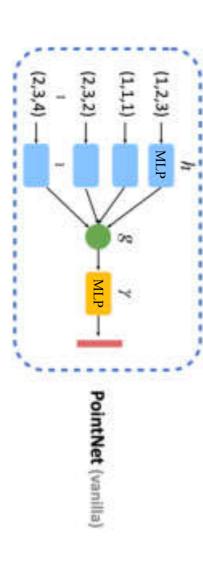
Construct Symmetric Functions by Neural Networks

$$f(x_1,x_2,...,x_n) = \gamma \circ g(h(x_1),...,h(x_n))$$
 is symmetric if g is symmetric

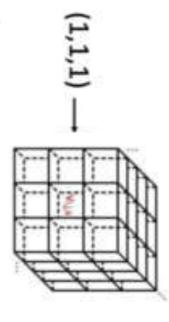


Construct Symmetric Functions by Neural Networks

$$f(x_1,x_2,...,x_n) = \gamma \circ g(h(x_1),...,h(x_n))$$
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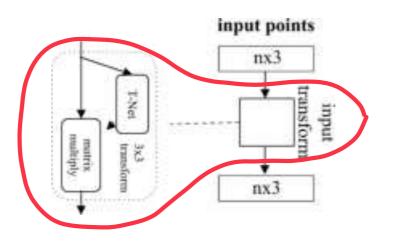
Reflection: assuming g is a max operation, construct a function h where geometric details get kept after applying g.

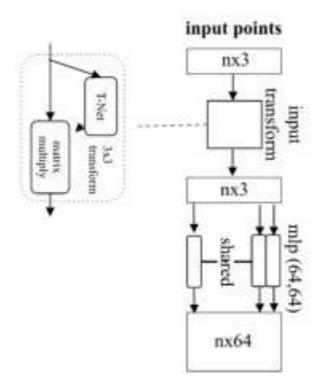


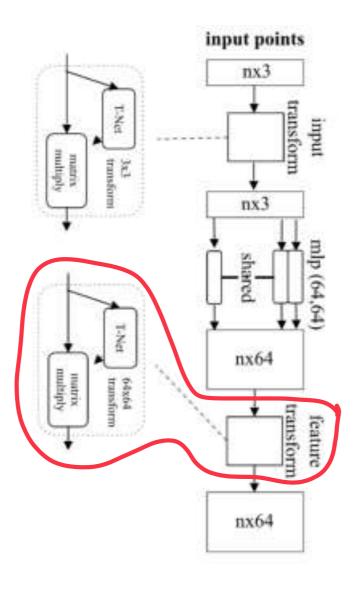
Spatial Hashing Function

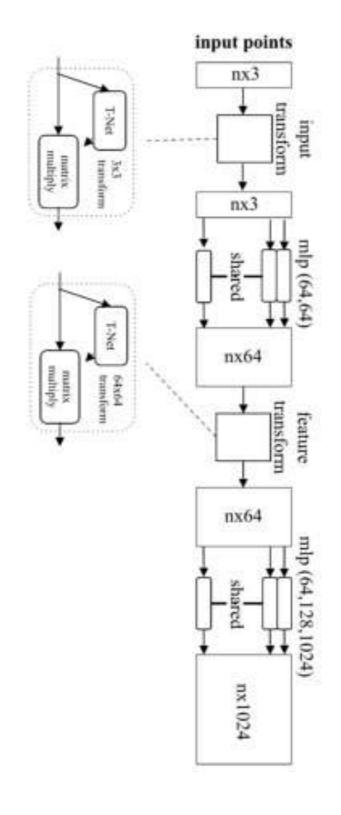
input points

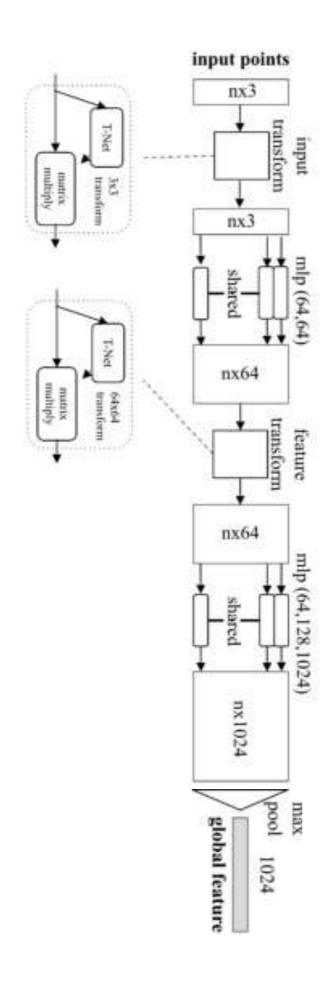
nx3

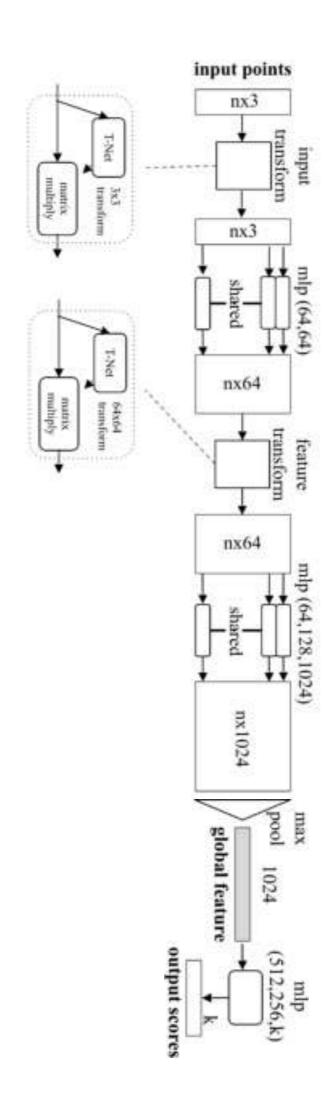




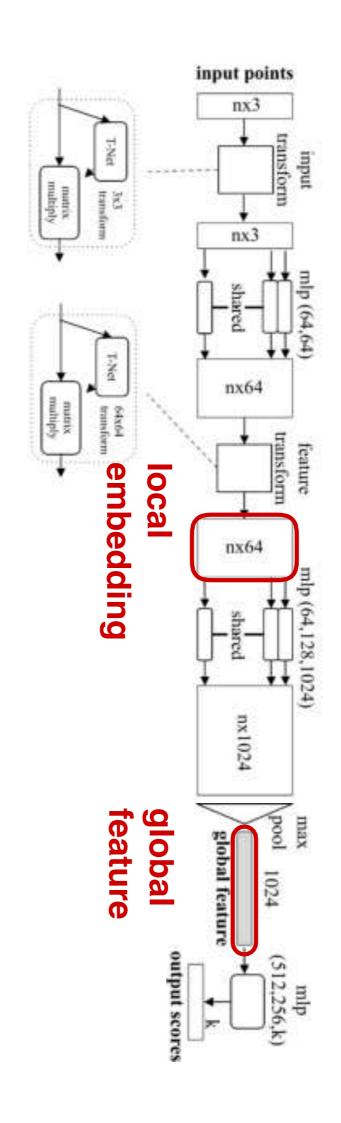




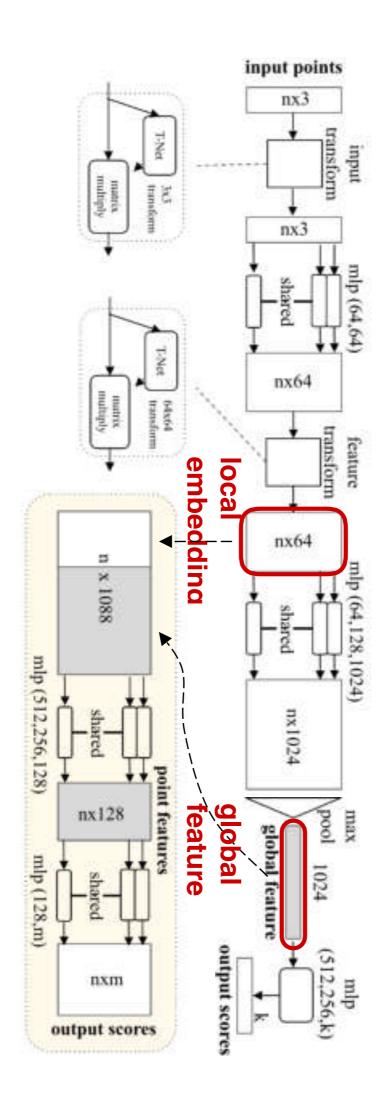




Extension to Segmentation

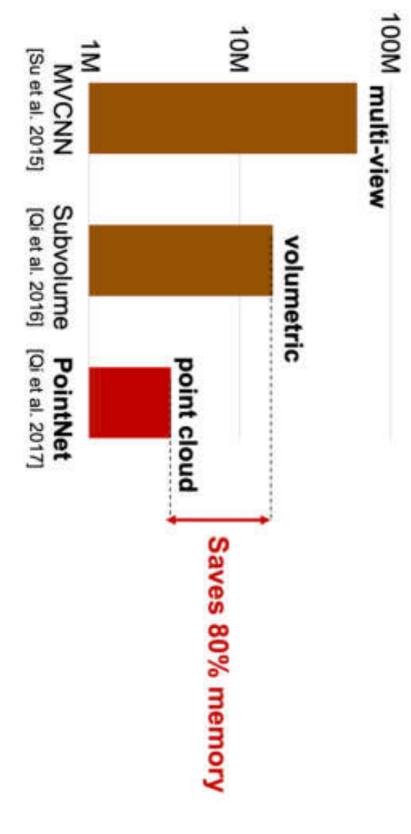


Extension to Segmentation

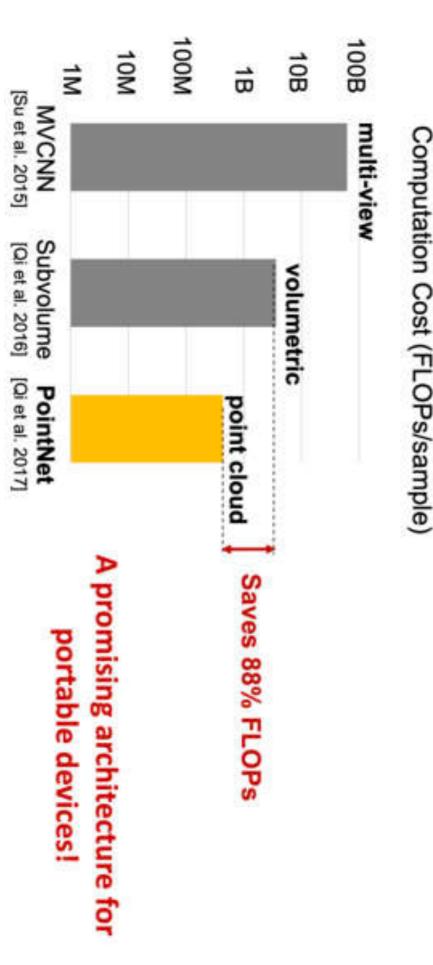


PointNet is Light-Weight and Fast





PointNet is Light-Weight and Fast

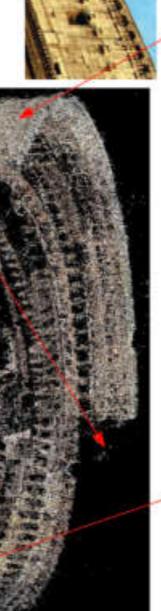


Robustness to Data Corruption

- Many challenges
- Resolution
- Occlusion
- Noise
- Registration

Noise→Poor detail reproduction

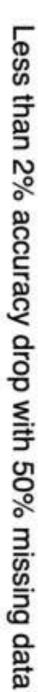
Low resolution further obscures detail

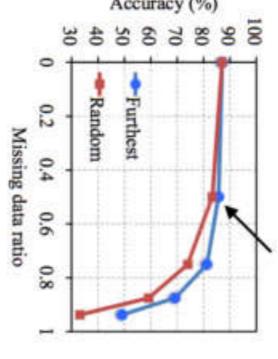




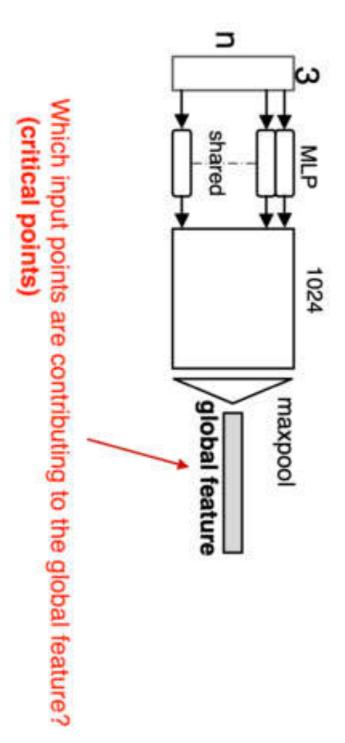
Occlusion→ Interiors not captured

Robustness to Data Corruption



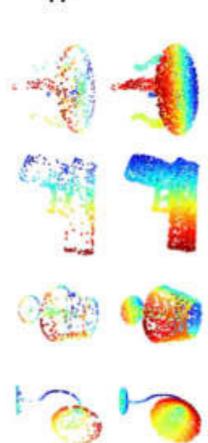


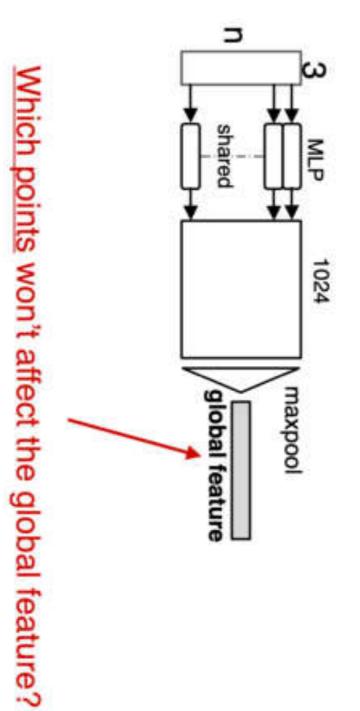
classification accuracy (%) dataset: ModelNet40; metric: 40-class



Original Shape:

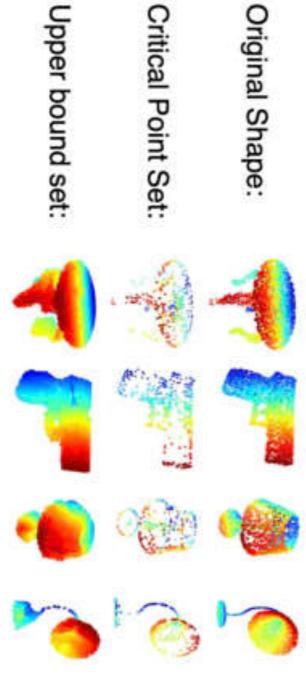
Critical Point Set:





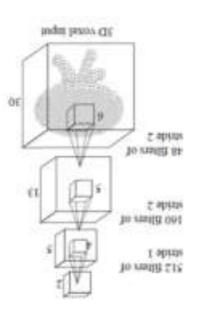
Original Shape:

Critical Point Set:



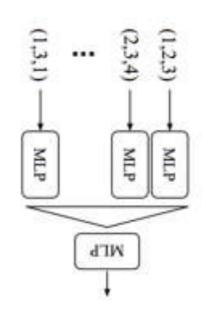
Limitation of PointNet

Hierarchical feature learning Multiple levels of abstraction



3D CNN (Wu et al.)

Global feature learning Either one point or all points



PointNet (vanilla) (Qi et al.)

- No local context for each point
- Global feature depends on absolute coordinate. Hard to generalize to unseen scene configurations!

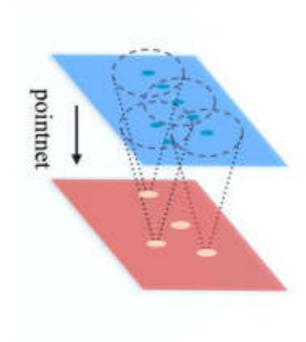
Outline

- Point Networks
- PointNet
- PointNet++
- Voxel Networks
- Networks for other representations
- SDF
- Mesh

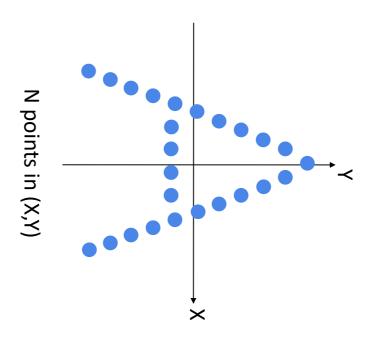
PointNet++

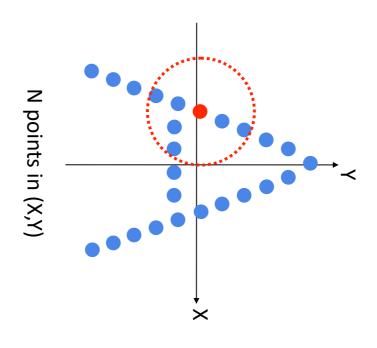
Basic idea: Recursively apply pointnet at local regions.

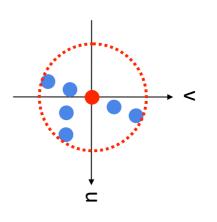
- √ Hierarchical feature learning
- ✓ Local translation invariance
- ✓ Permutation invariance



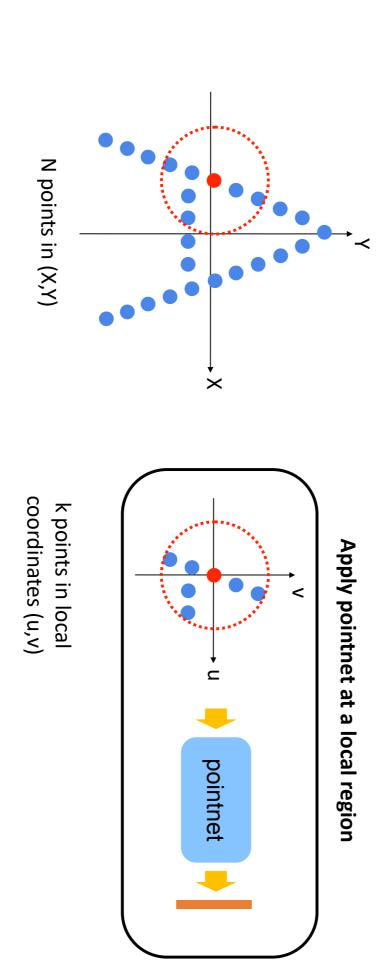
Charles R. Qi, Li Yi, Hao Su, Leonidas Guibas. PointNet++: Deep Hierarchical Feature Learning on Point Sets in a Metric Space (NIPS'17)

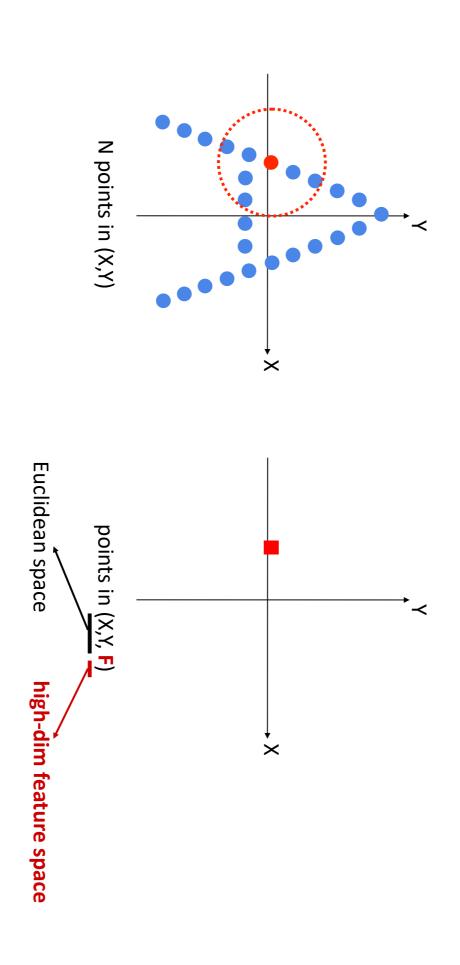


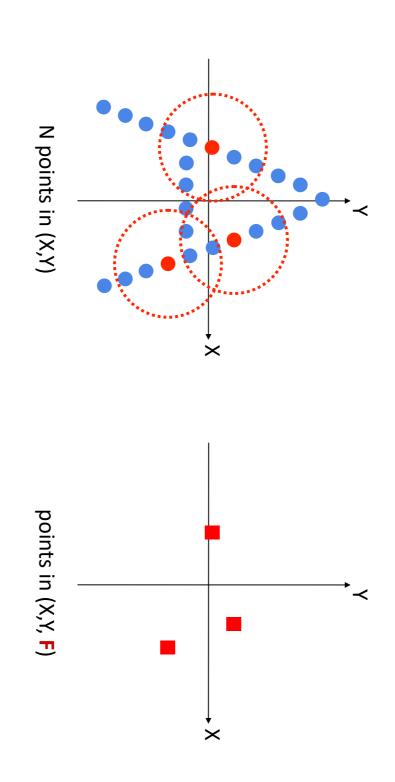


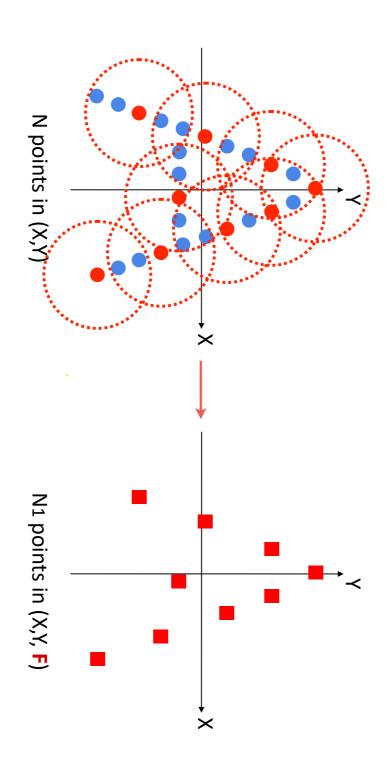


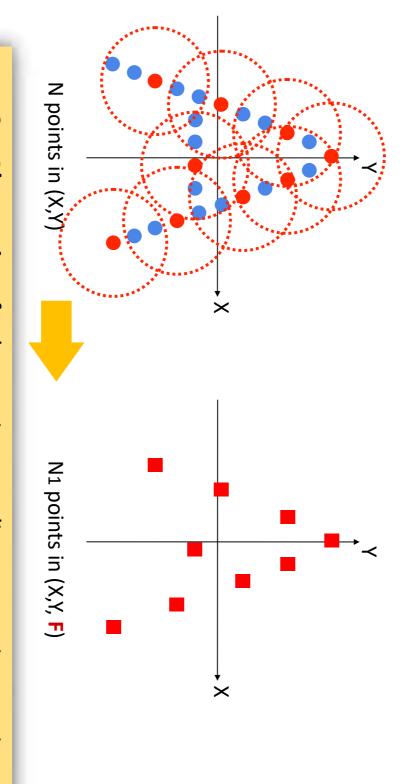
k points in local coordinates (u,v)





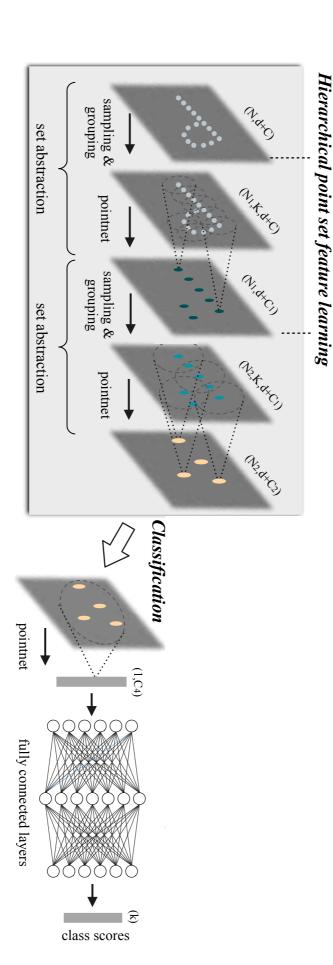




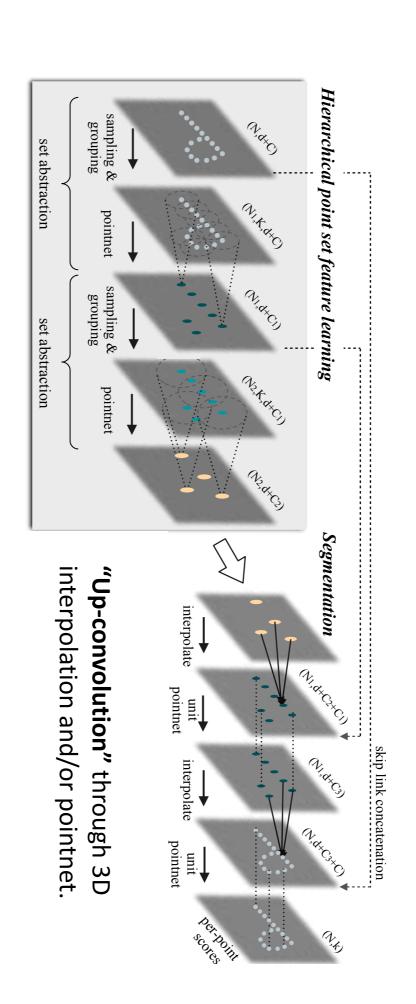


Set Abstraction: farthest point sampling + grouping + pointnet

PointNet++ for Classification



PointNet++ for Segmentation



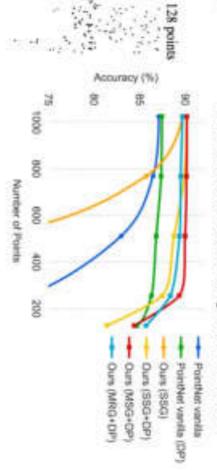
PointNet++: Classificiation

assification	Table 1: MNIST digit classification
0.51	Ours
0.78	PointNet [20]
1.30	PointNet (vanilla) [20]
0.47	Network in Network [13]
0.80	LeNet5 [11]
1.60	Multi-layer perceptron [24]
Error rate (%)	Method

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Class	200	
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CIGORILE	71999	
	20017	10.00
	20001100110	
	20001100110	

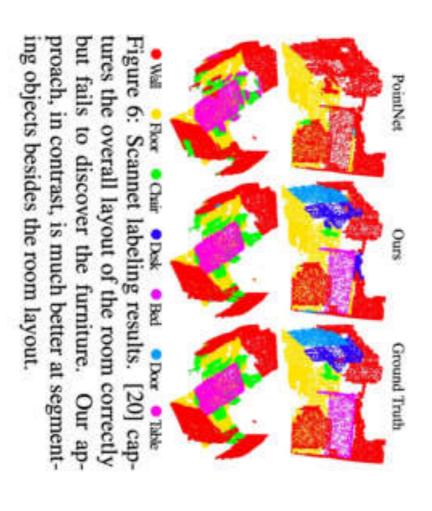
Ours pc Ours (with normal) pc	PointNet [20] pc	[20]			Method Input
90.7 91.9	89.2	87.2	90.1	89.2	Accuracy (%)

Table 2: ModelNet40 shape classification.



256 points

PointNet++: Segmentation

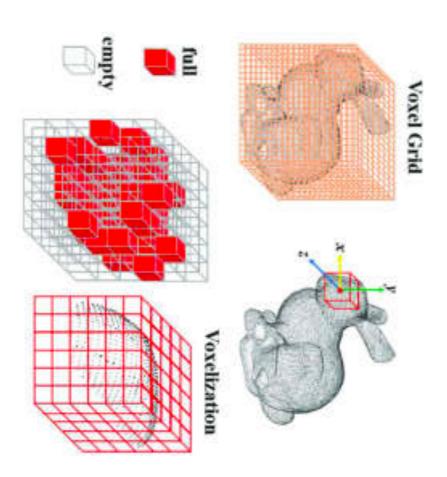


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- Voxel Networks
- Networks for other representations
- SDF
- Mesh

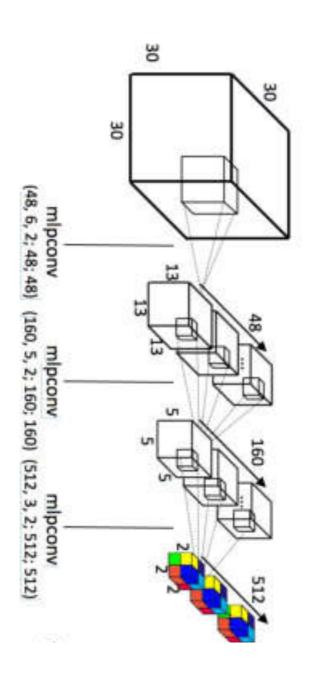
Voxelization

Represent the occupancy of regular 3D grids

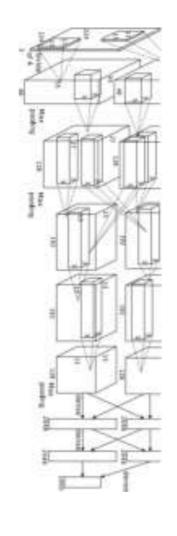


3D CNN on Volumetric Data

3D convolution uses 4D kernels



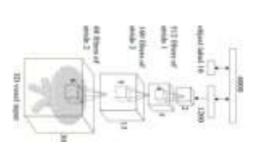
Complexity Issue



AlexNet, 2012

Input resolution: 224x224

224x224=50176

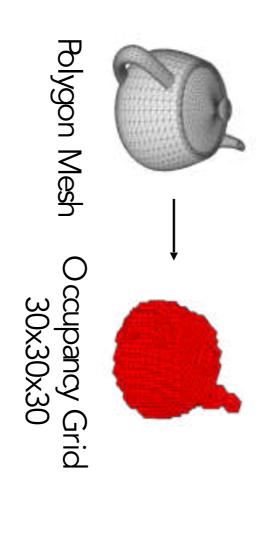


3DShapeNets, 2015

Input resolution: 30x30x30

224×224=27000

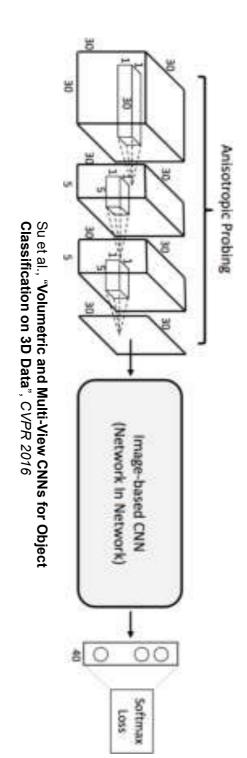
Complexity Issue



Information loss in voxelization

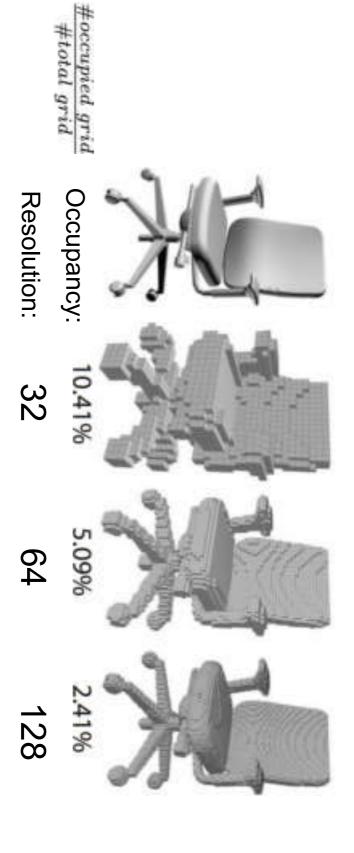
One Idea: Learn to Project

Idea: "X-ray" rendering + Image (2D) CNNs very low #param, very low computation



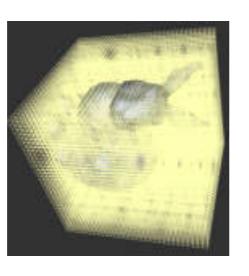
Many other works in autonomous driving use **bird's eye view** for object detection

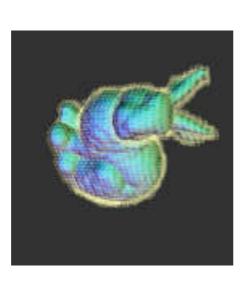
More Principled: Sparsity of 3D Shapes



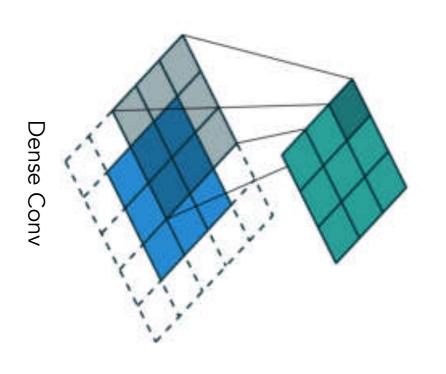
Store only the Occupied Grids

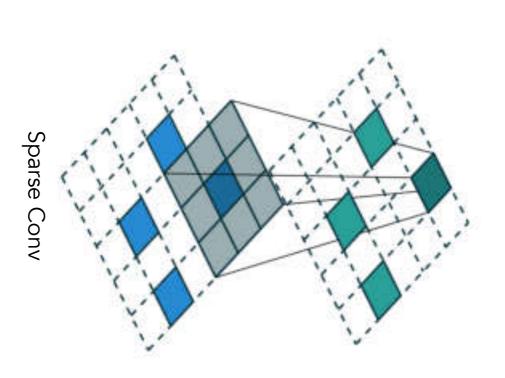
- Store the sparse surface signals
- Constrain the computation near the surface



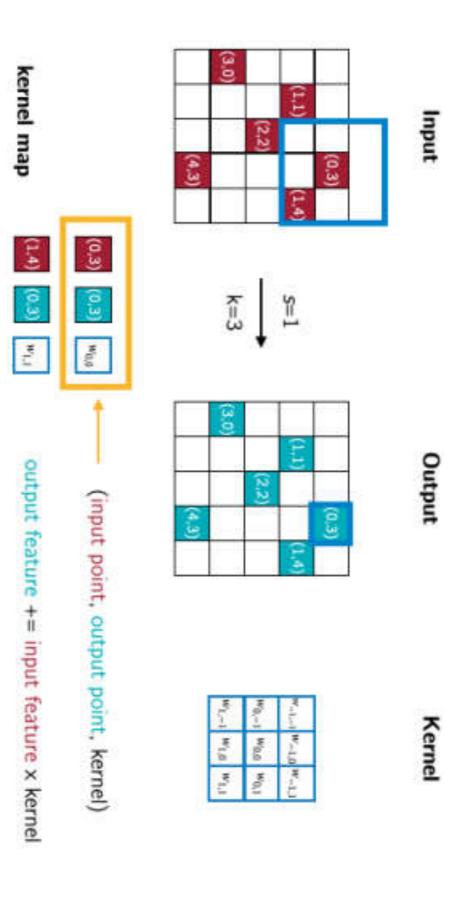


Sparse Convolution





Sparse Convolution



Implementation

- SparseConvNet
- https://github.com/facebookresearch/ SparseConvNet
- Uses ResNet architecture
- Takes time to train
- MinkowskiEngine
- TorchSparse
- Tensorflow3D

Summary of Sparse Conv

Pros:

- A way higher efficiency than dense conv
- Regular grid that supports indexing
- Similarly expressive compared to 2D Conv
- Translation equivariance similar to 2D Conv

Cons:

Discretization error

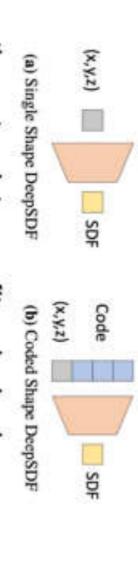
Sparse Conv vs. Point Cloud Networks

- Sparse Conv:
- +: Kernels are spatial anisotropic
- +: More efficient for indexing and neighbor query
- +: suitable for large-scale scenes
- -: limited resolutions
- Point cloud networks:
- +: high resolution
- +: easier to use and can be the first choice for a quick try
- -: slightly lower performance
- -: slower if performing FPS and ball query

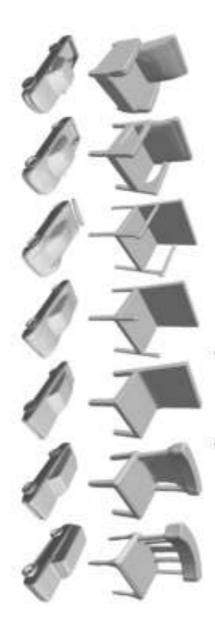
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Deep SDF

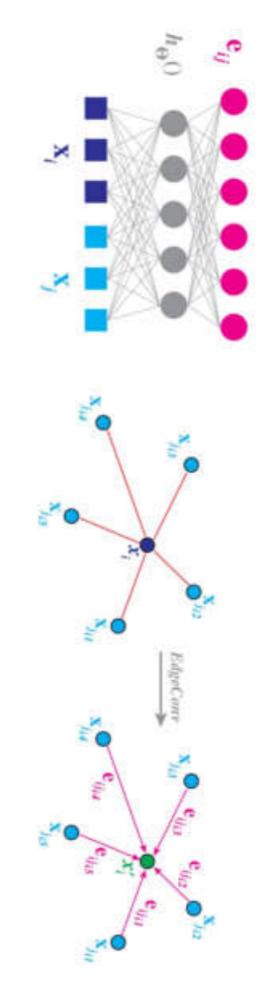


- (a) use the network to overfit a single shape
- network can be used for multiple shapes (b) use a latent code to represent a shape, so that the



Park et al., "DeepSDF: Learning continuous signed distance functions for shape representation.", CVPR 2019

Convolution on Mesh/Graph



Message passing: The output of EdgeConv at the i-th vertex is thus given by

$$\mathbf{x}_{i}' = \prod_{j:(i,j)\in\mathcal{E}} h_{\mathbf{\Theta}}(\mathbf{x}_{i}, \mathbf{x}_{j}). \tag{1}$$

Wang, et.al., Dynamic Graph CNN for Learning on Point Clouds, ToG 2019

Thank you!