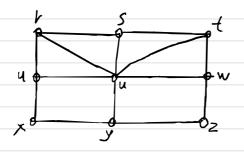
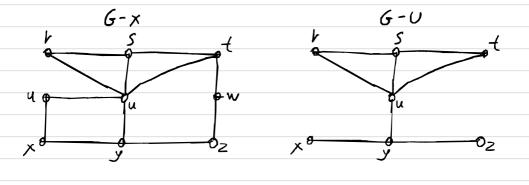
1.11. Let G be the graph of figure 1.20. Let X= {e, f} were e=re and f=uw, and let U= {u,w}. Draw the subgraphs G-x and G-U of G

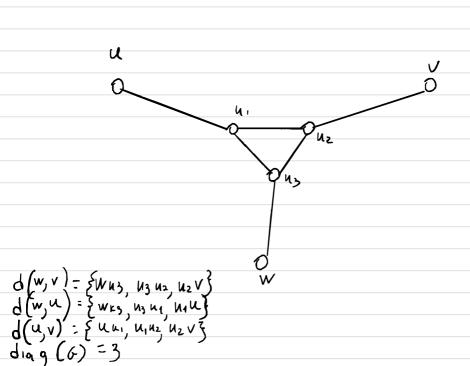


Solution 1.11



1.13

a) Give an example of an connected graph G containing three vertixes u, v, W such that d(u,v) = d(u,w) = d(v,w) = diam (6):3



b) Is there some relation between the number of vertixes and the diameter of a connected graph?

Draw all connected graphs of order s in which the distance between every two dinstinct vertices is odd. Explain why you know that you have drawn all such graphs.

Solvion

(a) dist(uv) 7.1 as G connected.

1) dist (u,v) is the length (no of edges) of the geodesic Path

(a) for any Path W, 2.1 |W| = |E(w)| 2.2 |E(w)| + 1 = |V(w)| 2.3 |W| = |V(w)| - 1

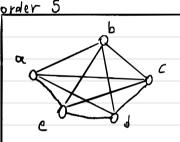
Braths may not have more vertexes than the total sum of vertexes in a graph

(4) Therefore from 2.3 and 3 we conclude for order s...

 $\forall u, v \in V(b)$ $\forall u,$

S) So from 4. We can see $\forall u, v \in V(G)...$ $d_{151}(u,v) = 1 \quad \forall \ d_{157}(v,v) = 3$

6) The graph where disi (u,v)=1 is trivial. Is the complete graph
of order 5



7 There is no graph of order 5 s.t + u, v & V(6), dist(u,v)=3

let a 6 of order 5 where dist(u,v) = 3 + u,v.

let the Path P= {11=1e, x, v}

· There is a parn u-x of length = 1

· Impossible

8) 15 There any That has dist (4, v) = 1 OR dist (4, v) = 3?

The complete graph of order 5 honors This criterion

ar least one

(g) We will show man such a graph does not exist.

Let 6 with |6| = 5 where $-\frac{1}{4} \sin(0, v) = 1 \text{ OR } \sin(0, v) = 3 \quad \forall \quad u, v \in V(6)$ $+\frac{1}{4} \sin(0, v) = 3 \quad \forall \quad u, v \in V(6)$

let Geodesic Path P U-V of size 3 P=(Vo=V, X, Y, U) X, Y & V (6)

Parn P (Vo = V, X, y, u) reveals parn V-y parn p has size 2

The only graph 6 of order 5 that honors this criterion is the Complete graph of order 5

1.17: To DURGHE OTO LETTURE IS.

1.19: Theorem 1.10 states that a graph & of order 3 or more is connected if and only if & contains two dinstinct vertices u, v

Such that G-u, G-v are connected.

Based on the one, one might suspect that the following statement is true...

True ...

Frey connected graph G of order 4 or more contains three dinstance Vertexes u, v and w such that G-u, G-v, G-w

Connected "

Is it true?

Solution

Not naving 3 disstance & V, w S. E. G. U, G.V, G.W commerced

 $V(6) = \{a, b, c, d\}$ $E(6) = \{(ab), (bc), (cd)\}$

Solution

6: a b c d

7: 0 0 0 0

Picu any for U, W, V

result modd be a not come (red 60)Ph of

Order > U