Math 3B: Lecture 4

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October 6, 2017

Last time

Last time, we spoke about

- Graphing using calculus

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- Slanted asymptotes

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- Slanted asymptotes
- Examples

Functions

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Definition (Global maximum)

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Global Maximums and minimums

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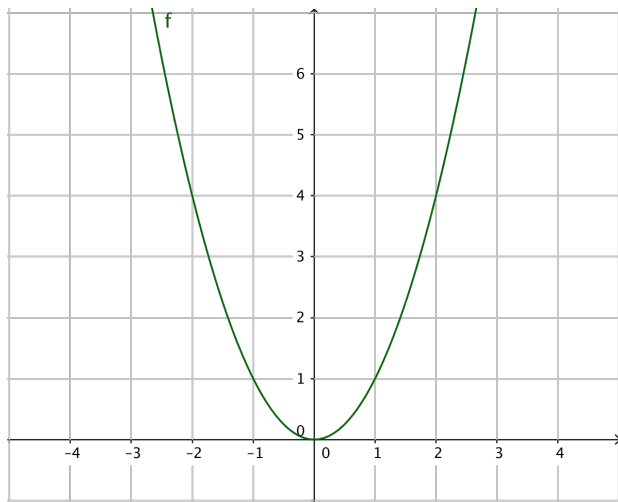$$f(x) \leq f(a) \quad \text{for all } x \in D$$

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Example of a global minimum

$f : \mathbb{R} \longrightarrow \mathbb{R}; x \mapsto x^2$ has a min at $x = 0$

Example of a global maximum

$f : (-\infty, 0\,] \longrightarrow \mathbb{R}; f(x) = x^3$ has a max at $x = 0$