

# Midterm 1 practice

## UCLA: Math 170A, Fall 2017

*Instructor:* Noah White

*Date:*

*Version:* practice

- This exam has 5 questions, for a total of 20 points.
- Please print your working and answers neatly.
- Write your solutions in the space provided showing working.
- All final answers should be exact values. Decimal approximations will not be given credit.
- Indicate your final answer clearly.
- Full points will only be awarded for solutions with correct working.
- You may write on the reverse of a page or on the blank pages found at the back of the booklet however these will not be graded unless very clearly indicated.
- Non programmable and non graphing calculators are allowed.

Name: \_\_\_\_\_

ID number: \_\_\_\_\_

Question	Points	Score
1	5	
2	5	
3	5	
4	5	
5	0	
Total:	20	

1. Let  $A, B, C$  be events in some probability space. Find expressions for the following events in terms of  $A, B, C$  and set operations (e.g.  $\cap, \cup, ^c$ ).
  - (a) (1 point) Only  $A$  occurs.
  - (b) (1 point) Both  $A$  and  $B$  but not  $C$  occur.
  - (c) (1 point) At least one event occurs.
  - (d) (1 point) One and no more occurs.
  - (e) (1 point) Not more than two occur.
2. There is a box with  $r$  red balls and  $b$  blue balls, where  $r, b \geq 4$ . Three balls are drawn without replacement. For  $i = 1, 2, 3$ , let  $A_i$  be the event that the  $i$ -th ball is blue. Let  $B$  be the event that all three balls are blue.
  - (a) (1 point) Find  $\mathbb{P}(A_1)$ .
  - (b) (1 point) Find  $\mathbb{P}(A_3)$ .
  - (c) (1 point) Find  $\mathbb{P}(B)$ .
  - (d) (2 points) Mark each of the following as True or False. Do not provide justification. One point for each correct answer + one point if all your answers are correct (i.e. if you aren't sure of one, it might be better to leave it blank).
    - TRUE FALSE  $A_1$  and  $A_2$  are independent.
    - TRUE FALSE  $A_1, A_2$  and  $A_3$  are independent.
    - TRUE FALSE  $A_1$  and  $B$  are independent.
3. (5 points) Suppose that each student in a class of 40 students has birthday occurring on each day of the year with equal probability and independently of the other students. What is the probability that there are no shared birthdays?
4. (5 points) There are three museums in a town. Each is open with probability 0.4 and closed with probability 0.6 independently of the other museums. Two of the museums are located on the street A and one on the street B. A tourist chooses either street A or street B with equal probability and walks down the whole length of the street he chose. He will enter every **open** museum he encounters on his way. Given that he entered exactly one museum, what is the probability he chose to walk down the street A?
5. (0 points) *Bonus\** If you have  $n$  lines in the plane  $\mathbb{R}^2$  that only intersect in pairs (i.e. there is no point where 3 or more lines intersect simultaneously), how many regions do these lines divide the plane into?  
*\*The real exam will not have a bonus question. This is maybe too hard for an exam and maybe slightly outside the scope of the course, so it is just a question to entertain those of you who are curious. Show me your solutions.*

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