

Math 3B: Lecture 2

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September 26, 2016

Last time

Last time, we spoke about

- The syllabus

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- Problem sets, homework, and quizzes

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- Differentiation of common functions
- Product rule
- Chain rule

Quiz tomorrow

- First quiz tomorrow and Thursday.

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- Have a look at the graphing questions!

Graphing using calculus: Why?

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- Understand functions qualitatively

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- Building intuition
- Understand functions qualitatively
- Better understanding of derivatives

Building intuition

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- $P(t) = \frac{Mt}{t+1}$ for some large number M
- $P(t) = \frac{Mt}{t+e^t}$

The ingredients

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- The regions of increase/decrease of the first derivative

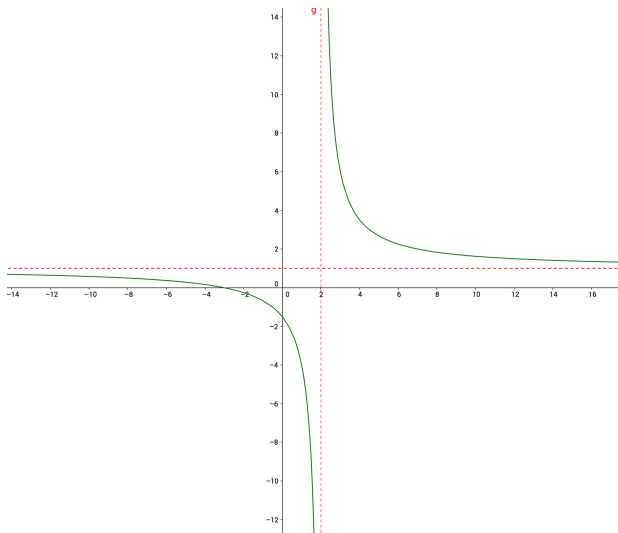
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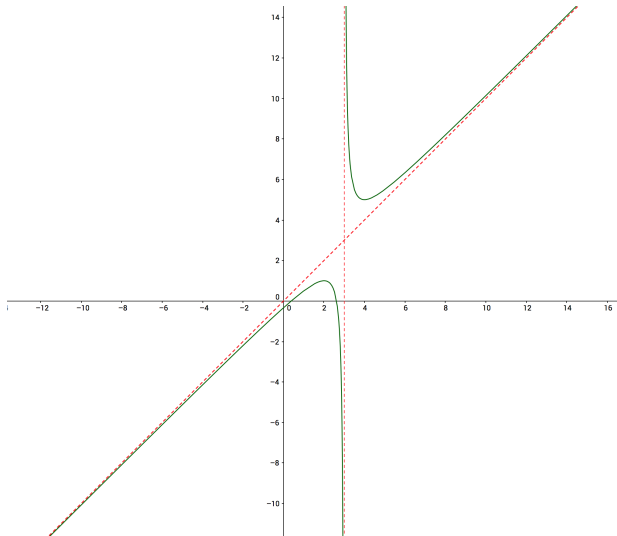
- The x and y intercepts
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- The regions of increase/decrease of the first derivative
- The regions of increase/decrease of the second derivative

Asymptotes

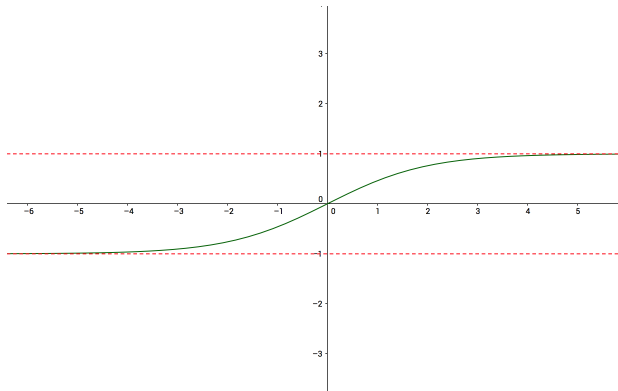
An **asymptote** is a line which the function approaches. Some examples:



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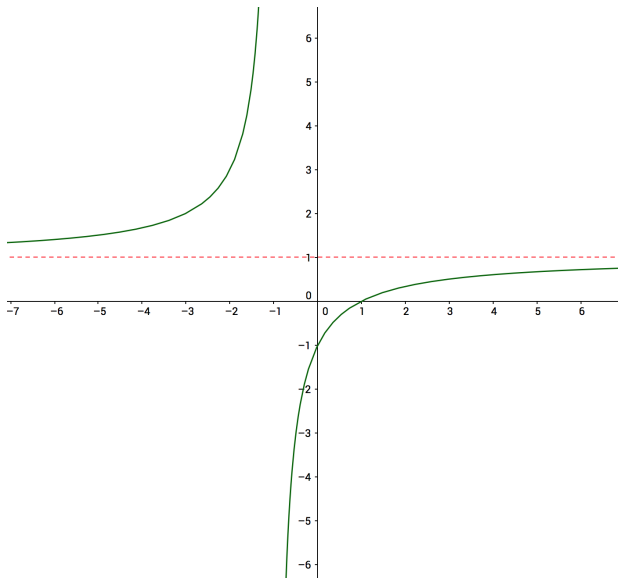
- Calculate $\lim_{x \rightarrow \infty} f(x)$
- Calculate $\lim_{x \rightarrow -\infty} f(x)$

Example

Say $f(x) = \frac{x-1}{1+x}$. In this case

$$\lim_{x \rightarrow \pm\infty} \frac{x-1}{x+1} = 1$$

Finding horizontal asymptotes



Finding verticle asymptotes

Verticle asymptotes happen when a function "blows up", or goes to infinity as it approaches a finite number. I.e. Is there a real number a so that

$$\lim_{x \rightarrow a^+} f(x) = \pm\infty$$

or

$$\lim_{x \rightarrow a^-} f(x) = \pm\infty$$

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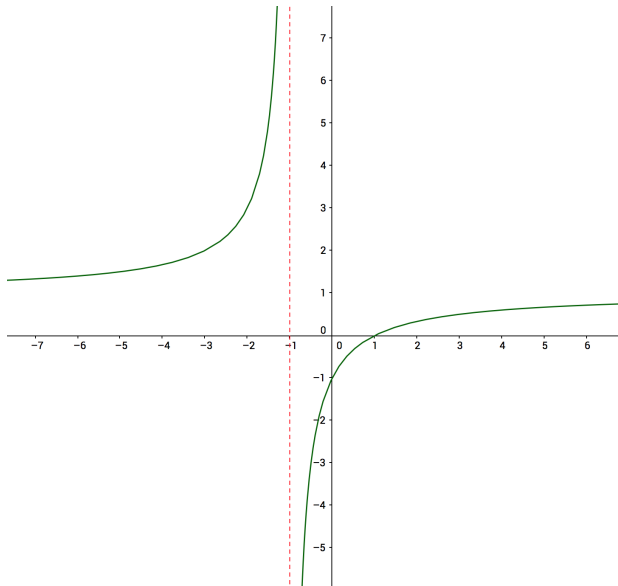
$$\lim_{x \rightarrow a^-} f(x) = \pm\infty$$

Example

$f(x) = \frac{x-1}{1+x}$, we have

$$\lim_{x \rightarrow -1^+} \frac{x-1}{1+x} = -\infty \quad \text{and} \quad \lim_{x \rightarrow -1^-} \frac{x-1}{1+x} = \infty$$

Finding verticle asymptotes

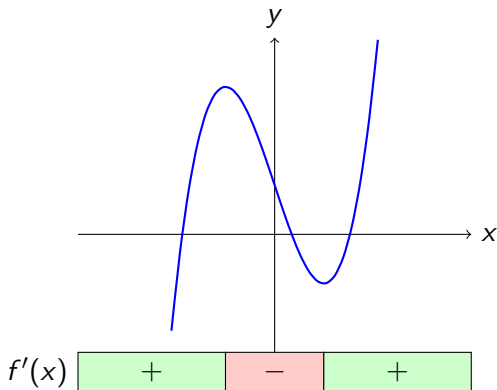


Finding slanted asymptotes

Lets come back to this...

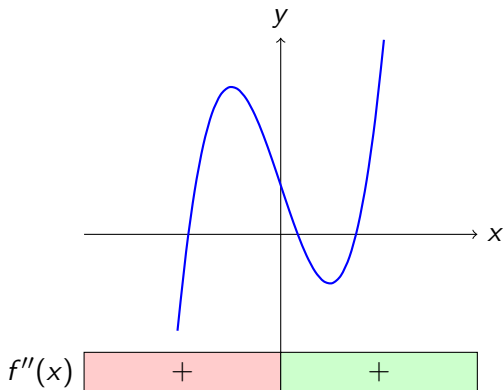
The first derivative

The first derivative tells us **is the function going up or down?**



The second derivative

The second derivative tells us **is the function concave up or down?**



Example time

... On the board.