

$$\frac{\partial u}{\partial t} = -c \frac{\partial u}{\partial x} + c \frac{\partial^2 u}{\partial x^2} \frac{(\Delta x)}{2!} (1 - CFL)$$

Assume solution is summation of terms like $(A_k e^{jkx}) e^{\alpha t}$

$$\alpha(A_k e^{jkx}) e^{\alpha t} = -cjk(A_k e^{jkx}) e^{\alpha t} + c(jk)^2 (A_k e^{jkx}) e^{\alpha t} \frac{(\Delta x)}{2!} (1 - CFL)$$

$$\alpha = -cjk - ck^2 \frac{(\Delta x)}{2!} (1 - CFL)$$

Error in Lecture (at 18:50 mark): Missing “t” (Hat tip to Hussein Mariner for this catch)

$$u(x, t) = A_k e^{jk(x-ct)} e^{-(1-CFL)(ck^2)\Delta x \textcolor{red}{t}/2}$$