

THROUGH MODELING THE PATHWAYS OF DISEASE AND MULTIPLE RISK FACTORS

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IMPROVING THE ACCURACY AND INTERPRETATION OF POLYGENIC RISK SCORE



ABSTRACT

Motivation

PRS has become a standard tool for quantifying the genetic risk of complex diseases.

- Traditional PRS typically only explains a limited amount of disease heritability.
- Despite several improvements to the PRS, the gap between PRS-explained variance and disease heritability remains significant.
- Minimax risk theory also implies that the existing PRS methods cannot be improved without additional information on the disease's biological mechanism.

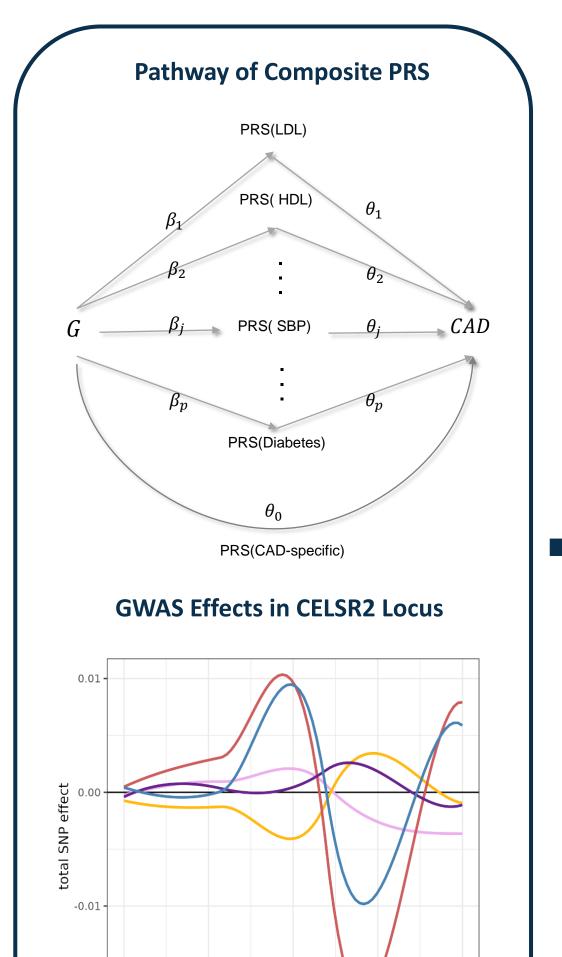
Method

- Genetic variants can influence a disease via the "genetic variants risk factors disease" pathway.
- Substantial portion of the genetic associations with complex diseases may be due to intermediary associations with risk factors.
- Using the pathway's information can theoretically increase the accuracy and interpretability of a PRS
- We build a composite PRS with direct and indirect genetic effects, which can increase the accuracy and interpretability of a PRS.

Conclusion

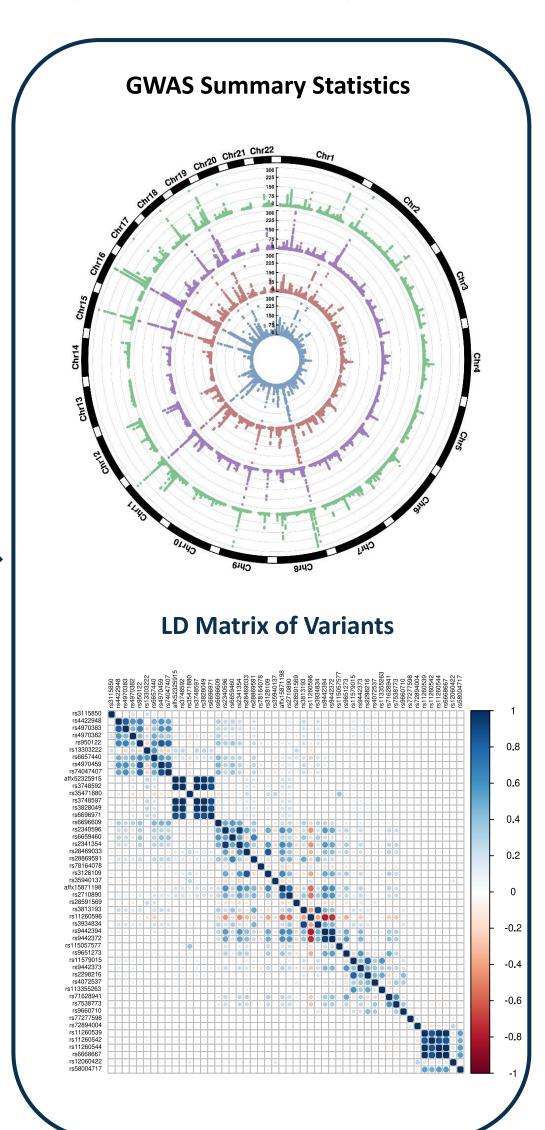
- Composite PRS is epidemiologically interpretable and can improve disease prediction accuracy.
- The significant improvement in prediction accuracy over a traditional PRS can be attributed to the leveraging of information on multiple risk factors for the disease of interest.
- Composite PRS also has a clear interpretation of risk factors affecting an outcome.
- We will apply the new composite PRS method to the prediction of cardiovascular disease outcomes in UK Biobank data and compare our method to existing alternatives.

Step I: Construction of CAD Pathway

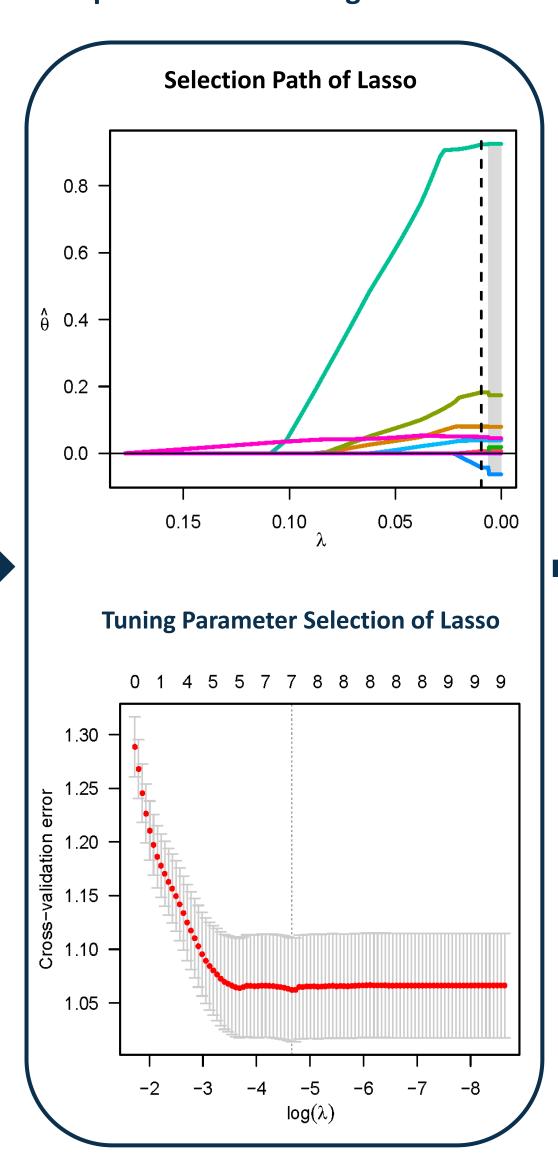


Chromosome 1 position (CELSR2 locus)

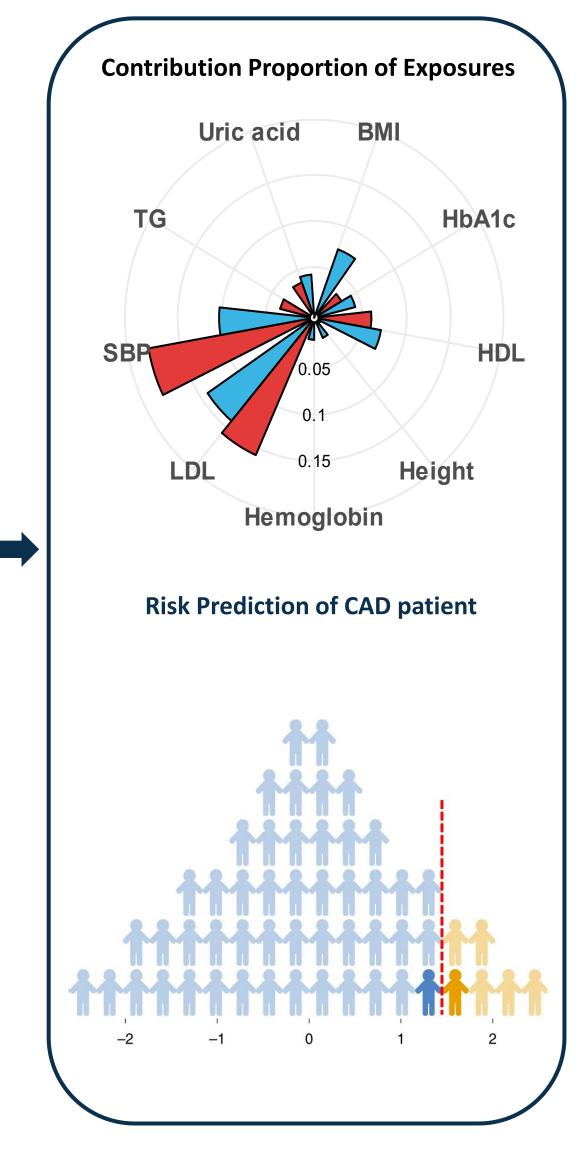
Step II: Estimation of Exposure PRS

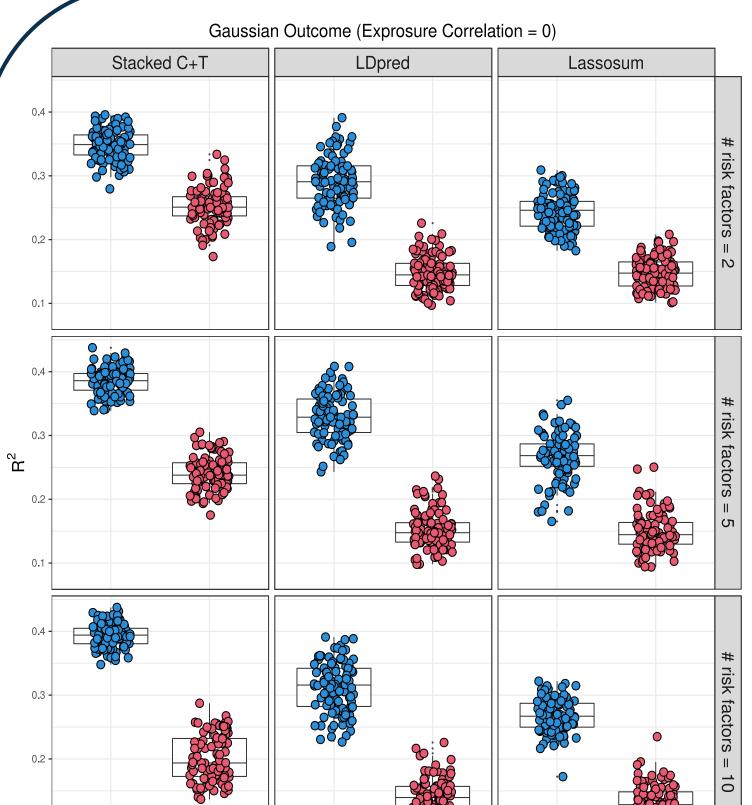


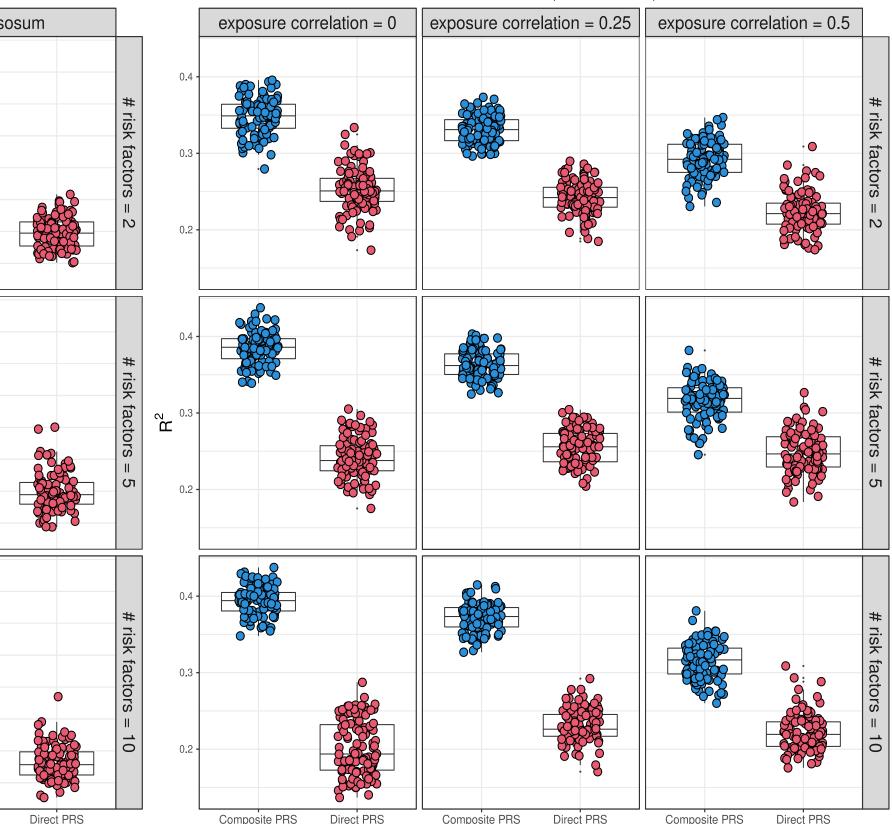
Step III: Selection of Significant PRS



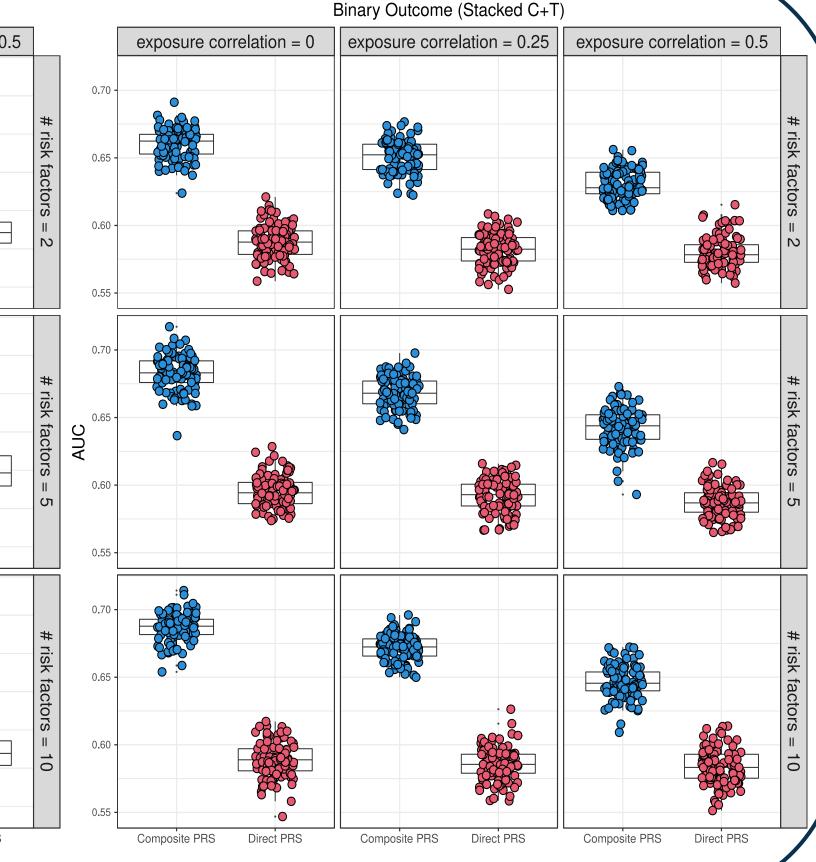
Step IV: Inference of Composite PRS







Gaussian Outcome (Stacked C+T)



Model

- $x_{i1}, ..., x_{ip}$ are p exposures and y_i is an outcome.
- The model for x_{ij} is

$$x_{ij} = \eta_{ij} + u_{ij},$$

where $\eta_{ij} = \sum_{s=1}^{m} g_{is} \beta_{js}$ is the PRS for x_{ij} .

- The model of y_i is

$$y_i = \eta_{i0}\theta_0 + \sum_{j=1}^p x_{ij}\theta_j + \mathbf{W}_i^{\mathsf{T}} \mathbf{\gamma} + u_{i0}$$
$$= \sum_{j=0}^p \eta_{ij}\theta_j + \mathbf{W}_i^{\mathsf{T}} \mathbf{\gamma} + u_j^*$$

where \mathbf{W}_i is a vector of covariate.

PRS Estimation

- Let **G** is the sample matrix of G_i , \mathbf{x}_j is the sample vector of x_{ij} . Then

$$\widehat{b}_{\mathbf{j}} = (\widehat{b}_{1\mathbf{j}}, \dots, \widehat{b}_{m\mathbf{j}})^{\mathsf{T}} = \widehat{\mathbf{D}}^{-1} \mathbf{G}^{\mathsf{T}} \mathbf{x}_{\mathbf{j}} / n$$

where $\widehat{\mathbf{D}}$ is the diagonal variance matrix of \mathbf{G} .

- PRS methods estimate the effect size β by

$$\widehat{b}_{j} = \mathbf{D}^{-\frac{1}{2}} \mathbf{R} \mathbf{D}^{\frac{1}{2}} \beta_{j} + \boldsymbol{\epsilon}_{j},$$

where

$$\epsilon_{\rm j} \sim \mathcal{N}\left(0, \sigma_{u_{\rm j}u_{\rm j}}^2 \mathbf{D}^{-\frac{1}{2}} \mathbf{R} \mathbf{D}^{-1\frac{1}{2}}\right).$$

- The PRS estimate of x_i is $\widehat{\boldsymbol{\eta}}_j = \mathbf{G}_i^{\mathsf{T}} \widehat{\boldsymbol{\beta}}_j.$

Coefficient Selection

- Suppose we have obtained the estimated PRS $\widehat{\boldsymbol{\eta}}_0, \widehat{\boldsymbol{\eta}}_1, ..., \widehat{\boldsymbol{\eta}}_p$.
- For normalization, we reweight each PRS by $\widehat{\boldsymbol{\eta}}_j = \frac{\widehat{\boldsymbol{\eta}}_j}{se(\widehat{\boldsymbol{\eta}}_i)}.$
- We apply a penalized likelihood to estimate $\boldsymbol{\vartheta} = \left(\theta_0, \theta_1, \dots, \theta_p, \boldsymbol{\gamma}^{\mathsf{T}}\right)^{\mathsf{T}}$:

$$\widehat{\boldsymbol{\vartheta}} = \operatorname{argmin} \left\{ \sum_{i=1}^{n} -\log(l_i(\boldsymbol{\vartheta})) + \sum_{i=1}^{p} \lambda_i |\vartheta_i| \right\},\,$$

where $l_i(\vartheta)$ is the likelihood function.

Inference

- The variant weights of the novel composite PRS is

$$\widehat{\boldsymbol{\beta}}_{com} = \sum_{j=0}^{p} \widehat{\boldsymbol{\beta}}_{j} \, \widehat{\theta}_{j}$$

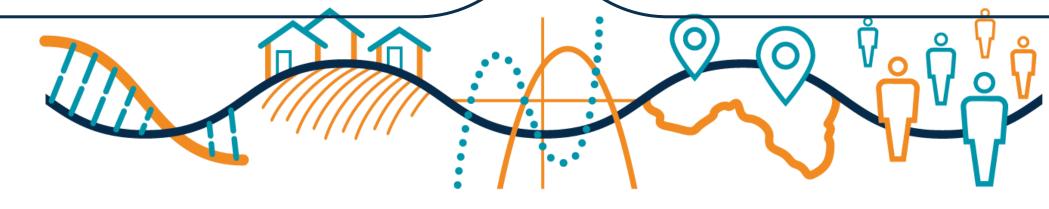
The risk prediction of y_i is yielded by the conditional probability

$$p(y_i|\mathbf{G}_i, \mathbf{W}_i) = \frac{\exp(\mathbf{G}_i^{\mathsf{T}}\widehat{\boldsymbol{\beta}}_{com} + \mathbf{W}_i^{\mathsf{T}}\widehat{\boldsymbol{\gamma}})}{\exp(\mathbf{G}_i^{\mathsf{T}}\widehat{\boldsymbol{\beta}}_{com} + \mathbf{W}_i^{\mathsf{T}}\widehat{\boldsymbol{\gamma}}) + 1}.$$

The contribution of each exposures can be model by the Pratt index:

$$PI(\mathbf{x}_j) = \hat{\theta}_j \times \hat{r}_j$$

where \hat{r}_j is the marginal regression coefficient between $\widehat{\boldsymbol{\eta}_j}$ and \mathbf{y} .



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