Remote questions: https://course.netsec.inf.ethz.ch/questions

Crypto Refresher

Symmetric Cryptography, Asymmetric Cryptography, Hash Functions

Network Security AS 2020

15 September 2020

Adrian Perrig Markus Legner



Other Lectures about Cryptography

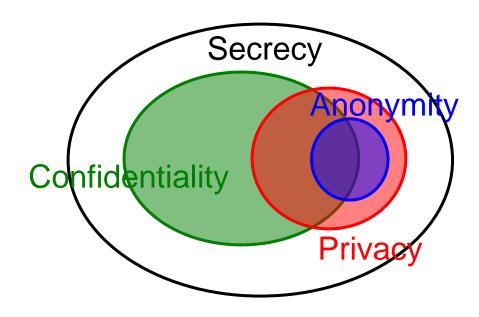
- Information Security (Prof. Dr. Srdjan Capkun, Prof. Dr. David Basin, Dr. Ralf Sasse)
 https://infsec.ethz.ch/education/as15_ss19/ss2020/infsec.html
- Applied Cryptography (Prof. Dr. Kenny Paterson)
 https://appliedcrypto.ethz.ch/education/lectures/appcry1.html

Secrecy, Confidentiality, Privacy, Anonymity

- Often considered synonymous, but are slightly different
- Secrecy
 - Keep data hidden from unintended receivers
 - "Alice and Bob use encrypted communication links to achieve secrecy"
- Confidentiality
 - Keep someone else's data secret
 - "Trent encrypts all user information to keep their client's information confidential in case of a file server compromise"
- Privacy
 - Keep data about a person secret
 - "To protect Alice's privacy, company XYZ did not disclose any personal information"

Secrecy, Confidentiality, Privacy, Anonymity

- Anonymity
 - Keep identity of a protocol participant secret
 - "To hide her identity to the web server, Alice uses The Onion Router (TOR) to communicate"



Network Security

Integrity, Authentication

- Sometimes used interchangeably, but they have different connotations
- Data integrity
 - Ensure data is "correct" (i.e., correct syntax & unchanged)
 - Prevents unauthorized or improper changes
 - "Trent always verifies the integrity of his database after restoring a backup, to ensure that no incorrect records exist"
- Entity authentication or identification
 - Verify the identity of another protocol participant
 - "Alice authenticates Bob each time they establish a secure connection"
- Data authentication
 - Ensure that data originates from claimed sender
 - "For every message Bob sends, Alice authenticates it to ensure that it originates from Bob"

Difference between Integrity and Authentication

- Integrity is often a property of local or stored data
 - For example, we want to ensure integrity for a database stored on disk, which emphasizes that we want to prevent unauthorized changes
 - Integrity emphasizes that data has not been changed
- Authentication used in network context, where entities communicate across a network
 - Two communicating hosts want to achieve data authentication to ensure data was not changed by network
 - Authentication emphasizes that data was created by a specific sender
 - Implies integrity, data unchanged in transit
 - Implies that identity of sender is verified

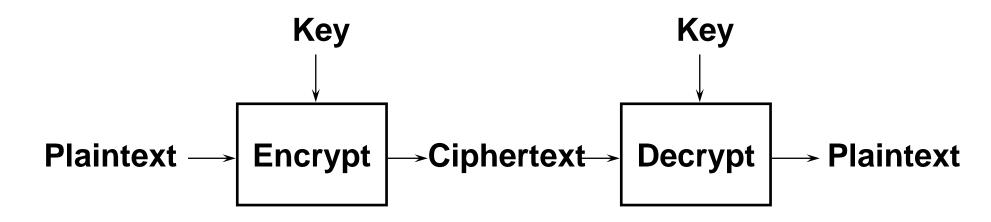
Basic Cryptographic Primitives

- Symmetric (shared-key, same-key)
 - Block cipher (pseudo-random permutation PRP)
 - Stream cipher (pseudo-random generators PRG)
 - Message authentication code (MAC)
- Asymmetric (public-private key)
 - Diffie–Hellman key agreement
 - Public-key encryption
 - Digital signature
- Others (unkeyed symmetric)
 - One-way function
 - Cryptographic hash function

Symmetric Cryptography

Symmetric Encryption Primitives

- Encryption key = decryption key
- Encryption: E_{κ} (plaintext) = ciphertext
- Decryption: D_{K} (ciphertext) = plaintext
- We write {plaintext}_K for E_K(plaintext)



Stream Ciphers

- One-time pad
 - Use unique random keystream for each message
 - Is this secure? **Yes.**
 - Is this secure if we re-use keystream? No.
- Stream ciphers use pseudo-random generator (PRG) to generate keystream from seed
 - Encryption: use shared key k and initialization vector IV for the seed ciphertext = plaintext

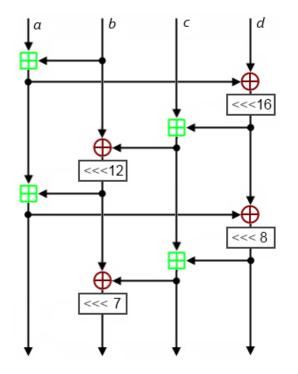
 PRG(k, IV)
 - Send IV, ciphertext
- Example: AES in CTR mode

ChaCha Stream Cipher

- Dan Bernstein designed ChaCha in 2008 (adaptation of earlier Salsa stream cipher)
- Used in TLS 1.3 and Wireguard VPN
- Structure: 128-bit constant, a 256-bit key, a 64-bit counter (Position), and a 64-bit nonce, arranged as a 4 × 4 matrix of 32-bit words
- Quarter round function illustrates cipher structure using addition, xor, and rotate
- High speed: around 4 cycles per byte

Initial state of ChaCha

Cons	Cons	Cons	Cons
Key	Key	Key	Key
Key	Key	Key	Key
Pos	Pos	Nonce	Nonce



Stream Cipher Vulnerabilities

- Keystream reuse attack
 - Enormous security vulnerability if same keystream used to encrypt two different messages
 - $c1 = p1 \oplus k$, $c2 = p2 \oplus k$
 - c1 ⊕ c2 = p1 ⊕ p2 (which is easy to analyze, because the unknown key is removed!)
 - c1 = p1 ⊕ PRG(K, IV), where IV = initialization vector, make sure IV is never used twice!
- Ciphertext modification attack
 - Alteration of ciphertext will alter corresponding values in plaintext after decryption
 - Example, encrypt a single bit: c = p ⊕ k, for p=1, k=0, thus c=1
 - If attacker changes c to 0 during transmission, decrypted value is changed to 0! p = c ⊕ k, if c=0, k=0, then p=0
 - To defend, need to ensure authenticity of ciphertext

Block Ciphers

- Block cipher is a pseudo-random permutation (PRP), each key defines a one-to-one mapping of input block to output block
 - Substitution cipher with large block size
- Encrypt each block separately
- Examples: DES, Rijndael (=AES)

Advanced Encryption Standard: AES

- Officially adopted for US government work, but voluntarily adopted by private sector
- Winning cipher was Rijndael (pronounced Rhine-doll)
 - Belgian designers: Joan Daemen & Vincent Rijmen
- Adopted by NIST in November 2001
- {128, 192, 256}-bit key size
- High-speed cipher
 - Using native AESni instructions on Intel and AMD CPUs, 128-bit AES encryption requires only 30 clock cycles (~10 ns)
 - ~7x faster than loading a byte from DRAM!
 - Illustration: light travels 3 m in 10 ns

Block-Cipher Modes of Operation

- Block cipher modes of operation
 - ECB: Electronic code book
 - CBC: Cipher block chaining
 - CFB: Cipher feedback
 - OFB: Output feedback
 - CTR: Counter mode
 - GCM: Galois Counter Mode:

encryption and authentication in a single pass!

Stream cipher: plaintext is XORed with keystream generated from secret key and initialization vector (IV)

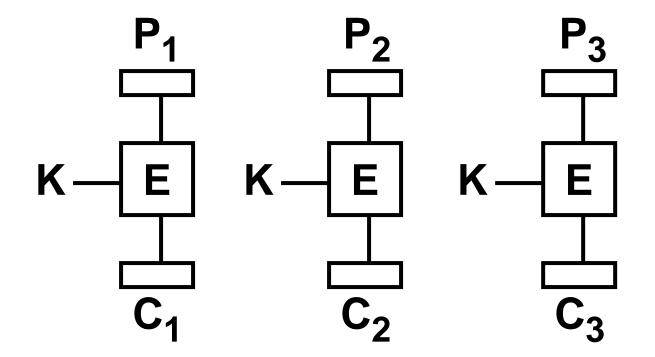
Block cipher in a stream

cipher mode

Electronic Code Book (ECB)

- Natural approach for encryption: given a message M, split M up into blocks of size b bits (where b = input size of block cipher)
- Ciphertext = $\{M_1\}_K \{M_2\}_K \dots \{M_n\}_K$
- This approach is called Electronic Code Book mode (ECB mode)
- Advantages
 - Simple to compute
- Disadvantages
 - Same plaintext always corresponds to same ciphertext
 - Traffic analysis yields which ciphertext blocks are equal → know which plaintext blocks are equal
 - Adversary may be able to guess part of plaintext, can decrypt parts of a message if same ciphertext block occurs
 - Adversary can replace blocks with other blocks

ECB Mode



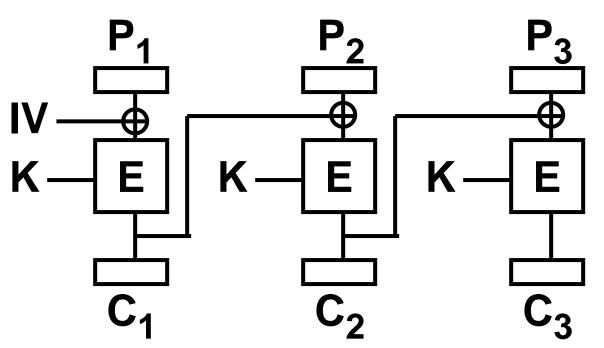
Desired Properties

- Semantic security: if adversary had to guess value of a single plaintext bit, can guess at best at random
 - Even if we keep encrypting a 1-bit message with skewed distribution (e.g., a fire alarm message, which almost always carries the same plaintext bit), attacker cannot guess value of plaintext given ciphertext
- Adversary cannot cut-and-paste blocks of ciphertext, otherwise complete message garbled

Cipher Block Chaining (CBC)

- Cj = { Pj ⊕ Cj-1 }K
- C0 = IV called initialization vector

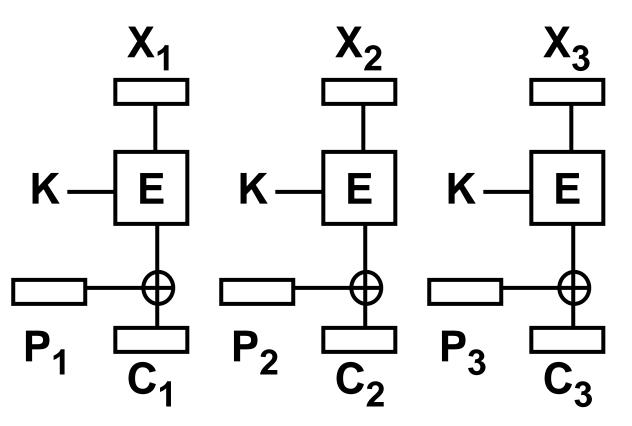
- Advantages
 - Semantic security
- Disadvantages
 - Altered ciphertext only influences two blocks
 - Not secure for variable-sized messages!
 - However, self-synchronizing can be an advantage too!



Counter Mode (CTR)

- X1 = IV called initialization vector
- Xj = X1 + i 1
- **■** Cj = { Xj }K ⊕ Pj

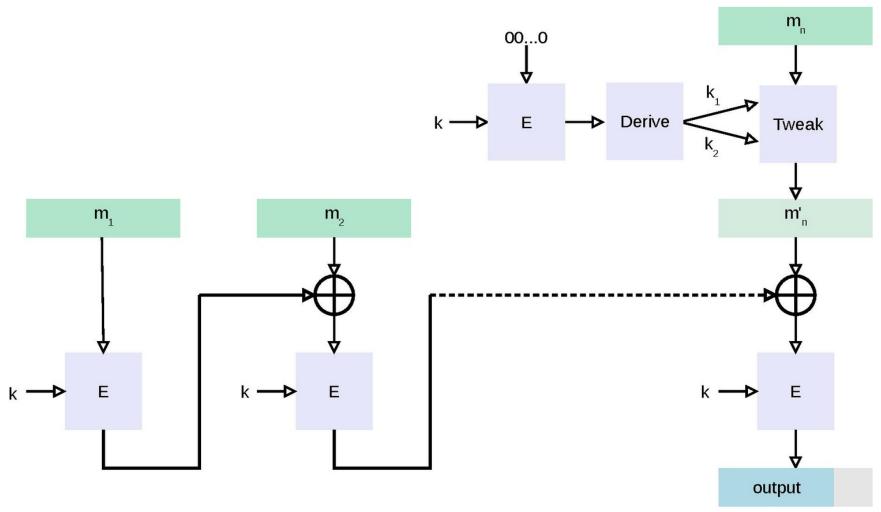
- Advantages
 - Semantic security
- Disadvantages
 - Altered ciphertext only influences single block
 - Same vulnerabilities as any stream cipher



Message Authentication Codes

- Message authentication codes (MAC) provide a "cryptographic checksum" for authentication, integrity
 - Write MAC(K, M), or MAC_K(M) (K is a shared symmetric key)
 - Intuition: MAC for a specific message can only be calculated when knowing the key K
- Use
 - A and B share symmetric key K_{AB}
 - A \rightarrow B: M, MAC(K_{AB} , M)
- Hash-based MAC: **HMAC**
 - Example based on SHA256:
 - HMAC-SHA256(K, M)=SHA256(K ⊕ opad || SHA256(K ⊕ ipad || M))
 - ipad = 3636..36, opad = 5C5C..5C
- Block-cipher based MAC: **CMAC**
- Other MAC algorithms: Carter-Wegman MAC, Galois MAC

Cipher-based Message Authentication Code (CMAC)

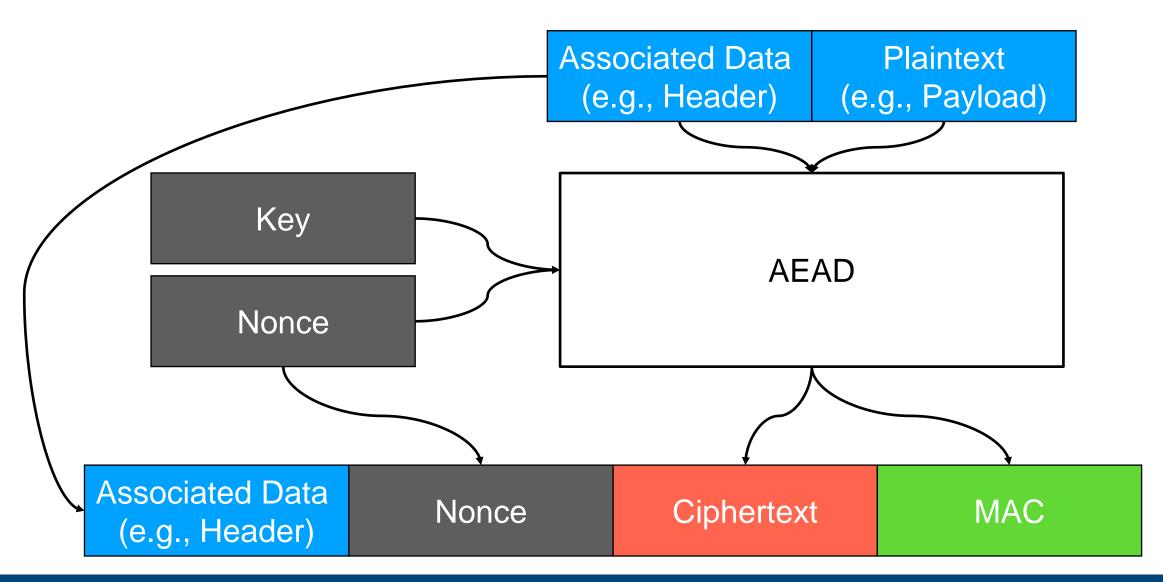


Graphic from https://en.wikipedia.org/wiki/One-key_MAC

Authenticated Encryption with Associated Data

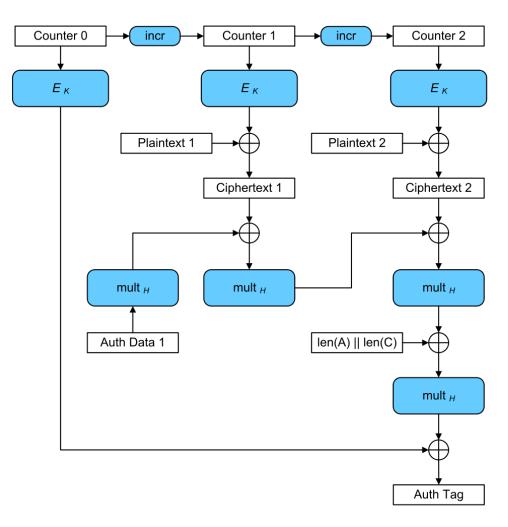
- Two Goals:
 - Encrypt message
 - Authenticate ciphertext and associated data
- Combines encryption and authentication in a secure manner
 - Uses form of "Encrypt and MAC" approach
 - Avoids issues with "MAC then Encrypt" (e.g., Lucky13 attack on TLS)
 - Ready-to-use cryptographic primitive

Authenticated Encryption with Associated Data



Galois Counter Mode (GCM)

- AEAD based on
 - Block cipher in CTR mode
 - Galois MAC
- Today mostly used with the AES block cipher → AES-GCM



Graphic from https://en.wikipedia.org/wiki/Galois/Counter_Mode

Asymmetric Cryptography

Asymmetric Primitive: Diffie-Hellman

- Public values: large prime *p*, generator *g*
- Alice has secret value a, Bob has secret b
- A \rightarrow B: $g^a \pmod{p}$
- B \rightarrow A: $g^b \pmod{p}$
- Bob computes $(g^a)^b = g^{ab} \pmod{p}$
- Alice computes $(g^b)^a = g^{ab} \pmod{p}$
- Eve *cannot* compute g^{ab} (mod p)

Example

- *a*=3, *b*=6, *g*=2, *p*=11
- A \rightarrow B: $g^a \pmod{p} = 2^3 \pmod{11} = 8$
- B → A: $g^b \pmod{p} = 2^6 \pmod{11}$

$$= 64 \pmod{11} = 9$$

■ Bob computes $(g^a)^b \pmod{p} = 8^6 \pmod{11}$

$$= 262144 \pmod{11} = 3$$

■ Alice computes $(g^b)^a \pmod{p} = 9^3 \pmod{11}$

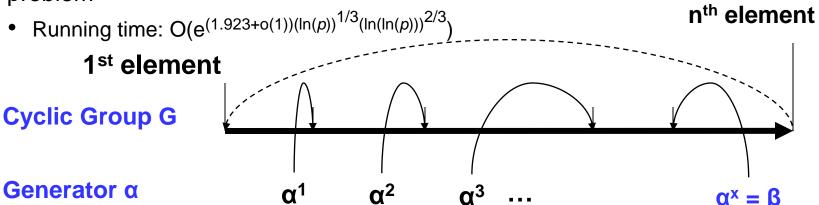
$$= 729 \pmod{11} = 3$$

Discrete Logarithm Problem

- Public values: large prime *p*, generator *g*
- \blacksquare $g^a \mod p = x$
- Discrete logarithm problem: given x, g, and p, find a
- Table *g*=2, *p*=11

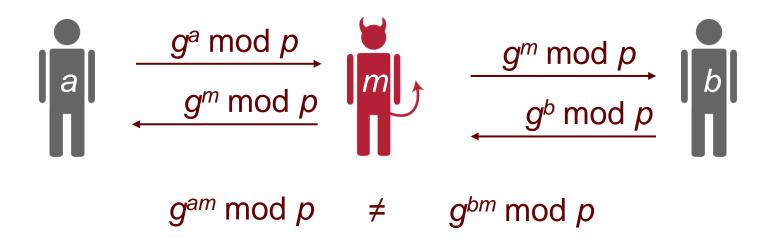
а	1	2	3	4	5	6	7	8	9	10
X	2	4	8	5	10	9	7	3	6	1

Number field sieve is fastest algorithm known today to solve discrete logarithm problem



Problem: Man-in-the-Middle Attack

- Public values: large prime p, generator g
- Problem: in Man-in-the-Middle attack, Mallory impersonates Alice to Bob and Bob to Alice



Asymmetric Primitive: RSA

- Invented by Rivest, Shamir, Adleman 1978
- Let *p*, *q* be large secret primes
- Pick e, compute d so $ed \equiv 1 \mod \phi(pq)$
 - Public key: N=pq, e
 - Private key: p, q, d
- Signature generation of message M $\Sigma = M^d \mod N$
- Signature verification:

$$\Sigma^{e} = M^{ed} = M^{1 + K\phi(pq)} = M \pmod{N}$$

Example

- $p=3, q=7, N=21, \phi(pq)=12, e=5, d=5$
- $\phi(pq) = (3-1)^*(7-1) = 2^*6 = 12$
- **■** *e*=5
 - Want d such that $ed \equiv 1 \mod \phi(pq) = 1 \mod 12$
 - Pick *d*=5
- M=2
 - Signature $\Sigma = M^d \mod N = 2^5 \mod 21 = 11$
 - Signature verification:

$$\Sigma^e = (M^d)^e \mod 21 = 11^5 \mod 21$$

= 161051 mod 21 = 2

■ Could also pick *e*=7, *d*=7...

Encrypted Key Exchange (EKE) DH Protocol

- A, B share password P, want to authenticate each other and establish a shared secret key
- K = H(P), A picks random a, B picks random b
- 1: A \rightarrow B: $\{g^a\}_K$
- $\blacksquare \mathcal{K} = H(g^{ab})$
- 2: B \rightarrow A: $\{g^b\}_K$, $\{N_B\}_{K'}$
- 3: A \rightarrow B: { N_A , N_B }_{K'}
- 4: B \rightarrow A: $\{N_A\}_K$
- Dictionary attacks? (Enables verification by attacker if a given password was correct or not.)

Difference between Authentication and Signature

- Authentication enables the receiver to verify origin, but receiver cannot convince a third party of origin
- Signature enables the receiver to verify origin, and receiver can convince third party of origin as well
- Signature also provides authentication

Comparison Symmetric vs Asymmetric Crypto

Symmetric crypto

- Need shared secret key
- 128 bit key for high security (year 2020)
- ~100,000,000 ops/s on 5GHz processor
- 10x speedup in HW

Asymmetric crypto

- Need authentic public key
 → public-key infrastructures (PKIs)
- 3072 bit key (RSA), 384 bit key (EC) for high security (year 2020)
- ~1000 signatures/s~10000 verify/s (RSA) on 5GHz processor
- Limited speedup in HW

Hash Functions

Cryptographic Hash Functions

- Maps arbitrary-length input into finite length output
- Properties of a secure (cryptographic) hash function
 - One-way: Given y = H(x), cannot find x' s.t. H(x') = y
 - Weak collision resistance: Given x, cannot find $x' \neq x$ s.t. H(x) = H(x')
 - Strong collision resistance: Cannot find x ≠ x' s.t. H(x) = H(x')
- Example: MD5, SHA-1, SHA-2, SHA-3, Poly1305
 - MD5 and SHA-1 have been broken to some extent

Attack Complexity: One-Wayness

- Assume secure hash function with n-bit output
- One-wayness: given output y, how many operations does it take to find any x, such that H(x) = y?
 - Assumption: best attack is random search
 - For each trial x, probability that output is y is 2⁻ⁿ
 - P[find x after m trials]=1-(1-2⁻ⁿ)^m
 - Rule of thumb: find x after 2ⁿ⁻¹ trials on average

Attack Complexity: Weak Collision Resistence

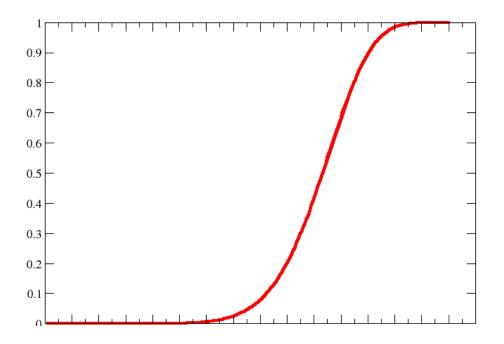
- Weak collision resistance (or second pre-image collision resistance): given input x, how many operations does it take to find another x' ≠ x, s.t. H(x) = H(x')?
 - Assumption: best attack is random search
 - For each trial x', probability that output is equal is 2⁻ⁿ
 - P[find x after m trials]=1-(1-2-n)m
 - Rule of thumb: find x' after 2ⁿ⁻¹ trials on average

Attack Complexity: Strong Colllision Resistence

- Strong collision resistance: how many operations does it take to find x and x', s.t. x' ≠ x and H(x) = H(x')?
 - Assumption: best attack is random search
 - Algorithm picks random x', checks whether H(x') matches any other output value previously seen
 - P[find col after m trials]= $1-(1-1/2^n)(1-2/2^n)(1-3/2^n)...(1-(m+1)/2^n)$
 - Rule of thumb: find collision after 2^{n/2} trials on average
 - (1.17*2^{n/2} to be a bit more precise)

Birthday Paradox

- How many people need to be in a room to have a probability > 50% that at least two people have the same birthday?
- Answer: approximately 1.17*365^{1/2} ~ 22.4



Lack of Collision Resistance

- How good is life without collision insurance?
- No real effect on most protocols
 - SSL, IPsec, SSH, etc. use MD5 in three ways
 - Key expansion
 - HMAC
 - Signatures
 - In most use cases, not affected by collisions
- What about PKI certificates?
 - Register certificate for <u>www.something.com</u> and use certificate for <u>www.bank.com</u> if H(Cert www.something.com) = H(Cert www.bank.com)
 - Countermeasure?

One-Way Hash Chains

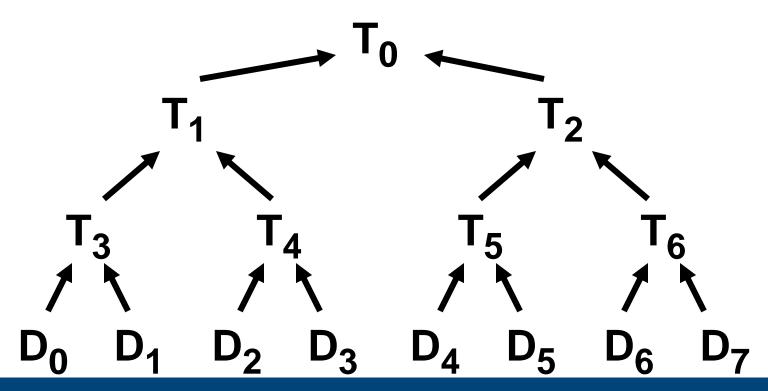
- Versatile cryptographic primitive
- Construction
 - Pick random r_N and public one-way function F
 - $r_i = F(r_{i+1})$
 - Secret value: r_N, public value r₀

$$r_0 \stackrel{F}{\longleftarrow} r_1 \stackrel{F}{\longleftarrow} r_2 \stackrel{F}{\longleftarrow} r_3 \stackrel{F}{\longleftarrow} r_4$$

- Properties
 - Use in reverse order of construction: r₀ , r₁ ... r_N
 - Infeasible to derive r_i from r_j (j<i)
 - Efficiently authenticate r_i using r_i (j<i): $r_i = F^{i-j}(r_i)$
 - Robust to missing values

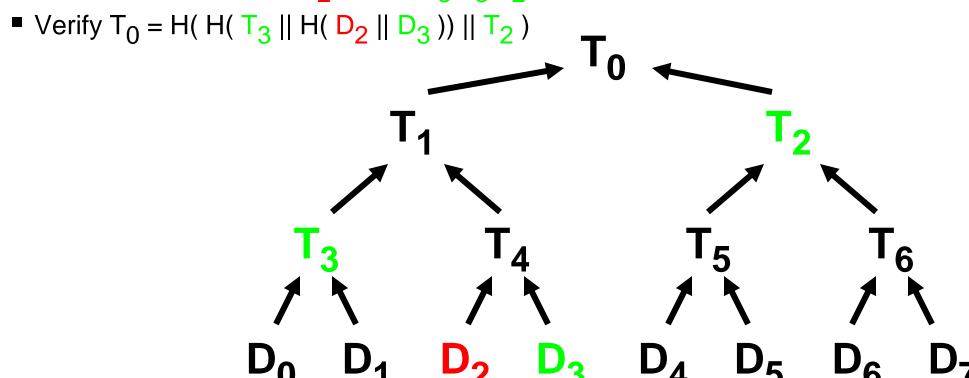
Merkle Hash Trees

- Authenticate a sequence of data values D₀ , D₁ , ..., D_N
- Construct binary tree over data values



Merkle Hash Trees

- Verifier knows T₀
- How can verifier authenticate leaf D_i?
- Solution: recompute T₀ using D_i
- Example authenticate D₂, send D₃ T₃ T₂



Selecting Cryptographic Key Lengths

Useful resources

- https://www.keylength.com
- https://en.wikipedia.org/wiki/Key_size

Method	Date	Symmetric	Factoring Modulus	Discrete Logarithm Key Group		Elliptic Curve	Hash
[1] Lenstra / Verheul	2037	99	2986 2464	175	2986	186	197
[2] Lenstra Updated 🕜	2032	90	2278 3034	179	2278	179	179
[3] ECRYPT II	2031 - 2040	128	3248	256	3248	256	256
[4] NIST	2016 - 2030 & beyond	128	3072	256	3072	256	256
[5] ANSSI	> 2030	128	3072	200	3072	256	256
[6] IAD-NSA	-	256	3072	-	-	384	384
[7] RFC3766 @	-	123	2986	246	2986	231	-
[8] BSI	> 2022	128	3000	250	3000	250	256

Powers of Two Conversion & Useful Units

- $2^{n} = 10^{m}$ $m \sim (n/10) * 3$ $n \sim (m/3) * 10$
- Fast conversion trick:
 - $2^{10} \sim 10^3$, $2^{20} \sim 10^6$, $2^{30} \sim 10^9$
 - $2^0 = 1$, $2^1 = 2$, $2^2 = 4$, $2^3 = 8$, $2^4 = 16$, $2^5 = 32$, $2^6 = 64$, 128, 256, 512, 1024
- Seconds per day ~2¹⁶, seconds per year ~2²⁵
- Schneier's Applied Cryptography, p18
 - Probability to get hit by lightning per day (10⁻¹⁰, 2⁻³³)
 - Number of atoms on earth (10⁵¹, 2¹⁷⁰)
 - Number of atoms in the universe (10⁷⁷, 2²⁶⁵)
 - Time until next ice age (14,000, 2¹⁴ years)
 - Duration until sun goes nova (10⁹, 2³⁰ years)
 - Age of the Universe (10¹⁰, 2³³ years)