roller coaster tycoon 2

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1 Formulation

1.1 Assumptions

- The terminology 'smooth' was used to describe the transition between pieces of track. It is assumed that this means they are both at the same location in space, meaning there will be no gaps, and that their gradient will be the same at the point of intersection, so that there is no sudden change gradient.

- it will be assumed that the gradient of the start and end sections of track is 0 as this was not specified.

1.2 Observations

- The track is divided into 3 segments. The first segment's start is partially undefined, say $(x,)$, and ended at $(0, 80)$, and was referred to as the "first" segment. The "middle" segment started at $(0, 80)$, and continued to $(150, 30)$. The final section stared at $(150, 30)$, and continued for an undefined length, say until $(x, 30)$.
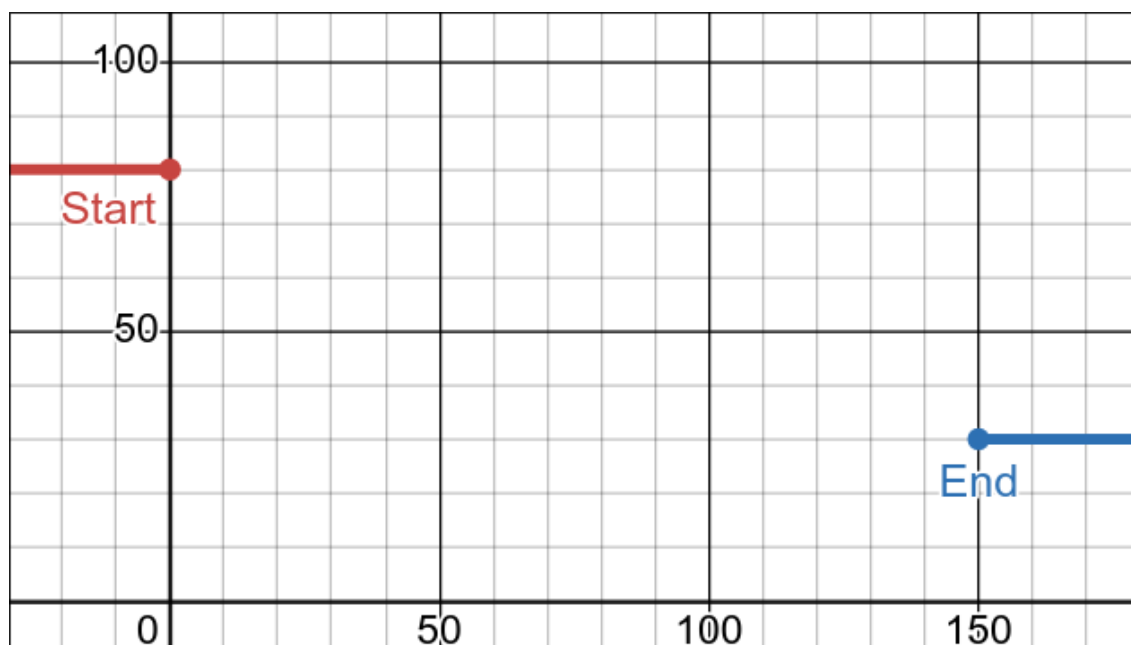

Figure 1: The proposed start and end sections of the track

- The roller coaster could be faithfully modelled in 2D to simplify calculations as the width of the track and much of its geometry were not relevant in this case and we were not provided with specifications regarding the width available.

- The task sheet defined the success criteria as causing the maximum amount of exhilaration, caused by "swift changes in direction, height and steepness".

- It was required that the track be constructed of at least 3 types of functions or more. These must be considered when it came to choosing the shape of the track.

1.3 Translation of aspects to Mathematical concepts and techniques

- Since the roller coaster had been assumed to be 2D, it's track could be represented on the Cartesian plane. This allowed us to use desmos to graph its track and perform calculations by letting 1 unit be 1 meter.

- The derivative function of modelled section of track could be used to determine the gradient at that point and therefore be used to determine if the track exceeded the specified "Maximum Slope for safety" requirement provided by the task sheet.

- "Swift changes in direction, height and steepness" could be translated to swift changes in the y−axis, and gradient. However, there was a maximum gradient specified that must be considered.

- In order to achieve as much of a thrill as possible, the maximum slope should be reached whenever possible and appropriate.

- Cubic in general form

2 Solve

2.1 Modeling in Desmos

- The cubic function was considered as the beginning of the coaster as

- Considering that the starting points for the middle section were already 80m in the air, it was determined that climbing further was futile as there was already sufficient height for the maximum gradient to be reached for a reasonable duration and the anticipation had already been built during the climb to the beginning of the middle section.

- The community made desmos project "Cubic through four points" allowed for a cubic to be constructed via dragging points in the desmos UI. This allowed for the creation of a viable function through trial and error. `https://www.desmos.com/calculator/r0slnoidco`

- By defining the cubic generated as $f(x)$, desmos could generate the derivative function, $f'(x)$, automatically. Therefore by checking $f'(x)$ for intercepts with y=-2, it could be determined whether the generated cubic exceeded the maximum gradient.

- Clearly the first point will be $(80, 0)$ to connect with the start of the first segment. However we required for $f'(0) = 0$ so the gradient so that the middle segment could smoothly connect to the first segment. By differentiating the general form of a cubic, it was found that $f'(x) = 3ax^2 + 2bx + c$. The only part of the equation that did not have a coefficient of x^n is c, therefore c must be equal to 0 for $f'(0) = 0$. orgsa

3 Evaluate and Verify