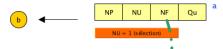
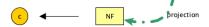
## Algèbre Relationnelle

- (1)  $\pi_{NU,NomU,Ville}(U)$  ou U
- (2)  $\sigma_{Ville='Londres'}(U)$
- (3) Solution complète :  $\pi_{NF}(\sigma_{NU=1 \land NP=1}(PUF))$

$$a \leftarrow \sigma_{NP=1}(PUF)$$
  
$$b \leftarrow \sigma_{NU=1}(a)$$
  
$$c \leftarrow \pi_{NF}(b)$$





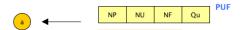


(4) Solution complète :  $\pi_{NomP,Couleur}(P \bowtie_{NP=NP} \sigma_{NF=1}(PUF))$ 

$$a \leftarrow \sigma_{NF=1}(PUF)$$

$$b \leftarrow P \bowtie_{NP=NP} (a)$$

$$c \leftarrow \pi_{NomP,Couleur}(b)$$





(5) Solution complète :  $\pi_{NF}(\sigma_{NU=1}(PUF) \bowtie_{NP=NP} \sigma_{Couleur='Rouge'}(P))$ 

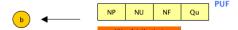
$$a \leftarrow \sigma_{Couleur='Rouge'}(P)$$
  

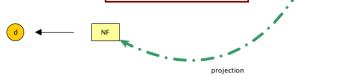
$$b \leftarrow \sigma_{NU=1}(PUF)$$
  

$$c \leftarrow b \bowtie_{NP=NP} a$$
  

$$d \leftarrow \pi_{NF}(c)$$







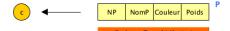
(6) Solution complète :  $\pi_{NomF}(F*PUF*\sigma_{Couleur='Rouge'}(P)*\pi_{NU}(\sigma_{Ville='Londres' \lor Ville='Paris'}(U)))$ 

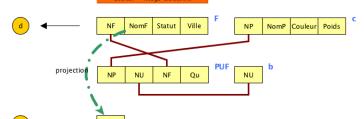
$$a \leftarrow \sigma_{Ville='Londres' \lor Ville='Paris'}(U)$$
  
$$b \leftarrow \pi_{NU}(a)$$
  
$$c \leftarrow \sigma_{Couleur='Rouge'}(P)$$

$$\begin{aligned} c &\leftarrow \sigma_{Couleur='Rouge'}(P) \\ d &\leftarrow F * PUF * c * b \end{aligned}$$

$$e \leftarrow \pi_d$$

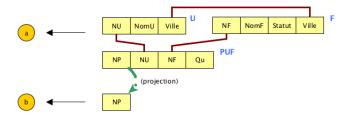






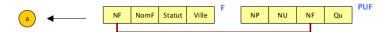
(7) Solution complète :  $\pi_{NP}(PUF * F * U)$ 

$$a \leftarrow PUF * F * U$$
$$b \leftarrow \pi_{NP}(a)$$



ou autre solution :  $\pi_{NP}((PUF \bowtie_{NF=NF} F) \bowtie_{NU=NU \land Ville=Ville} U)$ 

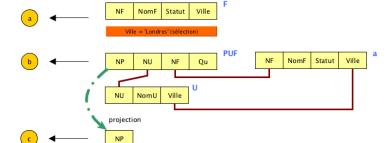
$$a \leftarrow PUF \bowtie_{NF=NF} F$$
  
$$b \leftarrow a \bowtie_{NU=NU \land Ville=Ville} (U)$$





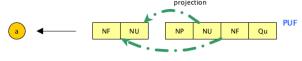
(8) Solution complète :  $\pi_{NP}(PUF * \sigma_{Ville='Londres'}(F) * U)$ 

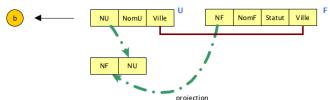
$$a \leftarrow \sigma_{Ville='Londres'}(F)$$
  
$$b \leftarrow PUF * a * U$$
  
$$c \leftarrow \pi_{NP}(b)$$



(9) Solution complète :  $\pi_{NU}(\pi_{NF,NU}(PUF) - \pi_{NF,NU}(U * F))$ 

$$a \leftarrow \pi_{NF,NU}(PUF)$$
  
$$b \leftarrow \pi_{NF,NU}(U * F)$$
  
$$c \leftarrow \pi_{NU}(a - b)$$





(10) Solution complète :  $\pi_{NF}(\sigma_{NU=1}(PUF)) \cap \pi_{NF}(\sigma_{NU=2}(PUF))$ 

$$a \leftarrow \sigma_{NU=2}(PUF) \\ b \leftarrow \pi_{NF}(a)$$

$$c \leftarrow \sigma_{NU=1}(PUF)$$

$$d \leftarrow \pi_{NF}(c)$$

$$e \leftarrow d \cap b$$

(11) Solution complète :  $\pi_{NU}(\pi_{NP}(\sigma_{NF=3}(PUF))) \bowtie_{NP=NP} PUF)$ 

$$a \leftarrow \sigma_{NU=2}(PUF)$$

$$b \leftarrow \pi_{NP}(a)$$

$$c \leftarrow b \bowtie_{NP=NP} PUF$$

$$d \leftarrow \pi_{NU}(c)$$

(12) Solution complète :  $\pi_{NP}(P) - \pi_{NP}(\sigma_{Poids>P2}(P \times \alpha_{Poids:P2}(\pi_{Poids}(P))))$ 

$$a \leftarrow \pi_{Poids}(P)$$

$$b \leftarrow P \times \alpha_{Poids:P2}(a)$$

$$c \leftarrow \sigma_{Poids \geq P2}(b)$$

$$d \leftarrow \pi_{NP}(c)$$

$$e \leftarrow \pi_{NP}(P)$$

$$f \leftarrow e - d$$