Determinism in SLiM

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Introduction

I've been noticing some strange behaviour with my output when modelling two traits: certain values keep cropping up for the same seed, which indicates the deterministic nature of SLiM and the effect that each parameter has on affecting that determinism. In particular, the same pleiotropy values (which are the covariance values used in the variance-covariance matrix sigma used when pulling values for phenotypes 0 and 1 from a multivariate normal) result in the same phenotypes for trait 0. Below are some examples of this.

```
> slim_out[slim_out$mean0 == 0.030587500, ]
             mean0
                        var0
                                   mean1
                                               var1
                                                            COV
                                                                     pear
                                                                                seed
                                                                                         r delmu pleio
     100 0.0305875 0.0564421 -0.01489140 0.0281072 -0.02748320
                                                                -0.690012 929413209
                                                                                               0.000
     100 0.0305875 0.0564421 -0.01489140 0.0281072 -0.02748320 -0.690012 929413209 0e+00
                                                                                               0.000
1335 100 0.0305875 0.0564421 -0.01095120 0.0217330 -0.02021240 -0.577105 929413209 0e+00
                                                                                               0 0.125
1617\ 100\ 0.0305875\ 0.0564421\ -0.01095120\ 0.0217330\ -0.02021240\ -0.577105\ 929413209
                                                                                               0 0.125
3208 100 0.0305875 0.0564421 -0.00677167 0.0165729 -0.01249990 -0.408702 929413209 0e+00
                                                                                               0 0.250
3459 100 0.0305875 0.0564421 -0.00677167 0.0165729 -0.01249990 -0.408702 929413209 1e-08
                                                                                               0 0.250
5053 100 0.0305875 0.0564421
                              0.00239741 0.0113898
                                                     0.00441993
                                                                 0.174323 929413209 0e+00
                                                                                               0 0.500
5303 100 0.0305875 0.0564421
                              0.00239741 0.0113898
                                                     0.00441993
                                                                                               0 0.500
                                                                 0.174323 929413209 1e-08
```

What this says to me is that linkage between gene regions (r) from 0 to 1e-08 doesn't have any appreciable effect on the simulation to affect the determinism of the simulation at a certain seed, but 0.5 (which is my third level for linkage) does. Deleterious mutation has an effect on determinism when they are included (shown by all of the values listed here having the same delmu value). Interesting that mean0 remains the same for all of them, whereas mean1 changes between runs with different levels of pleiotropy. This could be related to how SLiM processes pulls from multivariate normal distributions somehow? The pulls may be sequential, with the second (from which mean1 is calculated) being dependent on the first. This would explain the result, as the pleiotropic effect which is affecting mean1's constituents (the individual mutation effects) but not mean0's is pulled after mean0 (or rather, the constituent effects of mean0) is already stored. I think this means that there's no reason to include 1e-08 as a treatment level, it should be replaced with a higher recombination rate, something like 1e-05? Will have to test. What is annoying about this is that for each level of r and deleterious mutations (which do affect mean0 at a given seed), they will have an identical mean0 for each level of pleio (which doesn't affect it!).

We'll look at another example for r = 0.5:

```
> slim_out[slim_out$mean0 == -0.000966824, ]
                mean0
                              var0
                                        mean1
                                                                                      r delmu pleio
                                                   var1
                                                                 cov pear
39
     100 -0.000966824 0.000233219 0.00814330 0.0165451 -0.00196434
                                                                       -1 929413209 0.5
                                                                                            0.000
1885 100 -0.000966824 0.000233219 0.00795858 0.0158030 -0.00191978
                                                                                            0 0.125
                                                                       -1 929413209 0.5
3735 100 -0.000966824 0.000233219 0.00764301 0.0145747 -0.00184366
                                                                       -1 929413209 0.5
                                                                                            0 0.250
5582 100 -0.000966824 0.000233219 0.00656890 0.0107660 -0.00158456
                                                                       -1 929413209 0.5
                                                                                            0 0.500
```

Because this r value (0.5) results in a different mean than the other levels for the same generation and seed, clearly it does have an effect on the determinism of the simulation. This particular mean value appears 4 times, one for each level of pleiotropy, indicating the same thing as before: each level of pleiotropy has an effect on the determinism of mean but not mean 0.

We'll look at a different deleterious mutation rate and see what happens:

```
> slim_out[slim_out$mean0 == 0.005640700, ]
     gen
             mean0
                                  mean1
                                             var1
                                                                 pear
                                                                           seed
                                                                                      delmu pleio
    100 0.0056407 0.013333 -0.00706205 0.0263014 0.0111262 0.594147 929413209 1e-08
                                                                                        0.1 0.000
516
2208 100 0.0056407 0.013333 -0.00630157 0.0288585 0.0127055 0.647729 929413209 0e+00
                                                                                        0.1 0.125
2451 100 0.0056407 0.013333 -0.00630157 0.0288585 0.0127055 0.647729 929413209 1e-08
                                                                                        0.1 0.125
3796 100 0.0056407 0.013333 -0.00542762 0.0308773 0.0141061 0.695224 929413209
                                                                                        0.1 0.250
4057 100 0.0056407 0.013333 -0.00542762 0.0308773 0.0141061 0.695224 929413209 1e-08
                                                                                        0.1 0.250
5583 100 0.0056407 0.013333 -0.00329556 0.0326949 0.0163020 0.780799 929413209 0e+00
                                                                                        0.1 0.500
5838 100 0.0056407 0.013333 -0.00329556 0.0326949 0.0163020 0.780799 929413209 1e-08
                                                                                        0.1 0.500
```

Only 7 values here: for whatever reason, with 0 pleiotropy, no linkage (r) does have an effect on determinism of mean1 compared to 1e-08 linkage. The rest is pretty much the same as before though - same seed, same generation, same mean0 with mean1 differing between pleiotropy values.

Now lets confirm this with a different seed:

```
> slim_out[slim_out$mean0 == -0.052997300, ]
      gen
               mean0
                         var0
                                      mean1
                                                  var1
                                                                         pear
                                                                                   seed
                                                                                              delmu pleio
21763 100 -0.0529973 0.053311
                               0.005995120 0.01165690 -0.01222490 -0.490394 676365814 0e+00
                                                                                                0.1 0.000
22015 100 -0.0529973 0.053311
                               0.005995120 0.01165690 -0.01222490 -0.490394 676365814 1e-08
                                                                                                0.1 0.000
23640 100 -0.0529973 0.053311 -0.000676563 0.00927547 -0.00546512 -0.245767 676365814 0e+00
                                                                                                0.1 0.125
23901 100 -0.0529973 0.053311 -0.000676563 0.00927547 -0.00546512 -0.245767 676365814 1e-08
                                                                                                0.1 0.125
25511 100 -0.0529973 0.053311 -0.007444570 0.00834192
                                                        0.00149107
                                                                    0.070706 676365814 0e+00
                                                                                                0.1 0.250
25781 100 -0.0529973 0.053311 -0.007444570 0.00834192
                                                        0.00149107
                                                                     0.070706 676365814 1e-08
                                                                                                0.1 0.250
27312 100 -0.0529973 0.053311 -0.021306700 0.01148340
                                                        0.01606850
                                                                     0.649428 676365814 0e+00
                                                                                                0.1 0.500
27572 100 -0.0529973 0.053311 -0.021306700 0.01148340
                                                        0.01606850
                                                                     0.649428 676365814 1e-08
                                                                                                0.1 0.500
```

Once again, 8 different results each with the same mean0, showing no effect of r=0 vs 1e-08 on the deterministic nature of SLiM affecting mean0, and also 4 results showing pleio only affecting mean1. So this isn't just one seed.

Conclusion

The pleiotropy value appears to affect only mean1, implying values are pulled sequentially from the rmvnorm() function in SLiM, dependent on the first value (which is averaged to give mean0). The result of this is that for any given combination of r and delmu treatments, mean0 is the exact same for every single level of pleio, invalidating any comparisons between mean0 and mean1, or var0 and var1; basically any look into covariance or correlation as a result of pleio doesn't make any sense because all the seeds with a given parameter set (minus pleio) give the same values for mean0 regardless of pleio. On the bright side, this has shown that I should choose a different level for r in future. I guess this means I should randomise pleiotropic effects per mutation and stop looking at its individual effects, because clearly that doesn't make any sense.