ML:Introduction

What is Machine Learning? Two definitions of Machine Learning are offered. Arthur Samuel described it as: "the field of study that gives computers the ability to learn

without being explicitly programmed." This is an older, informal definition. Tom Mitchell provides a more modern definition: "A computer program is said to learn from experience E with respect to some class of tasks T

and performance measure P, if its performance at tasks in T, as measured by P, improves with experience E."

E = the experience of playing many games of checkers

Example: playing checkers.

T = the task of playing checkers. P = the probability that the program will win the next game.

relationship between the input and the output.

supervised learning, OR

In general, any machine learning problem can be assigned to one of two broad classifications:

unsupervised learning.

Supervised Learning

Supervised learning problems are categorized into "regression" and "classification" problems. In a regression problem, we are trying to predict results within a continuous output, meaning that we are trying to map input variables to some continuous function. In a classification problem, we are instead trying to predict results in a discrete output. In other words, we are trying to map input variables into discrete categories. Here is a description on Math is Fun on Continuous and Discrete Data.

In supervised learning, we are given a data set and already know what our correct output should look like, having the idea that there is a

Example 1: Given data about the size of houses on the real estate market, try to predict their price. Price as a function of size is a continuous output, so this is a regression problem. We could turn this example into a classification problem by instead making our output about whether the house "sells for more or less than

the asking price." Here we are classifying the houses based on price into two discrete categories.

Example 2: (a) Regression - Given a picture of Male/Female, We have to predict his/her age on the basis of given picture.

(b) Classification - Given a picture of Male/Female, We have to predict Whether He/She is of High school, College, Graduate age. Another Example for Classification - Banks have to decide whether or not to give a loan to someone on the basis of his credit history.

Unsupervised learning, on the other hand, allows us to approach problems with little or no idea what our results should look like. We can derive structure from data where we don't necessarily know the effect of the variables.

We can derive this structure by clustering the data based on relationships among the variables in the data. With unsupervised learning there is no feedback based on the prediction results, i.e., there is no teacher to correct you.

Example:

number that are somehow similar or related by different variables, such as word frequency, sentence length, page count, and so on. Non-clustering: The "Cocktail Party Algorithm", which can find structure in messy data (such as the identification of individual voices and music from a mesh of sounds at a cocktail party (https://en.wikipedia.org/wiki/Cocktail party effect)). Here is an answer on Quora to enhance

your understanding.: https://www.quora.com/What-is-the-difference-between-supervised-and-unsupervised-learning-algorithms?

Clustering: Take a collection of 1000 essays written on the US Economy, and find a way to automatically group these essays into a small

Model Representation Recall that in regression problems, we are taking input variables and trying to fit the output onto a continuous expected result function.

Our hypothesis function has the general form:

ML:Linear Regression with One Variable

 $\hat{y} = h_{\theta}(x) = \theta_0 + \theta_1 x$

points of our training data set. In such a case the value of $J(\theta_0, \theta_1)$ will be 0.

function using our hypothesis with those specific theta parameters.

input x output y 0

7

7

8

For Enterprise

So for input of 1 to our hypothesis, y will be 4. This is off by 3. Note that we will be trying out various values of θ_0 and θ_1 to try to find values

1

2

3

Example:

This function is otherwise called the "Squared error function", or "Mean squared error". The mean is halved
$$\left(\frac{1}{2m}\right)$$
 as a convenience for the computation of the gradient descent, as the derivative term of the square function will cancel out the $\frac{1}{2}$ term.

Now we are able to concretely measure the accuracy of our predictor function against the correct results we have so that we can predict new results we don't have.

If we try to think of it in visual terms, our training data set is scattered on the x-y plane. We are trying to make straight line (defined by $h_{\theta}(x)$)

average squared vertical distances of the scattered points from the line will be the least. In the best case, the line should pass through all the

which passes through this scattered set of data. Our objective is to get the best possible line. The best possible line will be such so that the

To break it apart, it is $\frac{1}{2}$ \bar{x} where \bar{x} is the mean of the squares of $h_{\theta}(x_i) = y_i$, or the difference between the predicted value and the actual

Imagine that we graph our hypothesis function based on its fields θ_0 and θ_1 (actually we are graphing the cost function as a function of the parameter estimates). This can be kind of confusing; we are moving up to a higher level of abstraction. We are not graphing x and y itself, but the parameter range of our hypothesis function and the cost resulting from selecting particular set of parameters.

We put θ_0 on the x axis and θ_1 on the y axis, with the cost function on the vertical z axis. The points on our graph will be the result of the cost

We will know that we have succeeded when our cost function is at the very bottom of the pits in our graph, i.e. when its value is the minimum.

The way we do this is by taking the derivative (the tangential line to a function) of our cost function. The slope of the tangent is the derivative at that point and it will give us a direction to move towards. We make steps down the cost function in the direction with the steepest descent, and the size of each step is determined by the parameter α , which is called the learning rate.

Gradient Descent for Linear Regression

 $\theta_i := \theta_i - \alpha$ [Slope of tangent aka derivative in j dimension][Slope of tangent aka derivative in j dimension]

 $\theta_0 := \theta_0 - \alpha \frac{1}{m} \sum_{i=1}^{m} (h_{\theta}(x_i) - y_i)$

 $\theta_1 := \theta_1 - \alpha \frac{1}{m} \sum_{i=1}^m \left((h_{\theta}(x_i) - y_i) x_i \right)$

Khan Academy has excellent Linear Algebra Tutorials (https://www.khanacademy.org/#linear-algebra)

Matrices and Vectors Matrices are 2-dimensional arrays: g h i

Matrices are usually denoted by uppercase names while vectors are lowercase. "Scalar" means that an object is a single value, not a vector or matrix. R refers to the set of scalar real numbers

 $\begin{bmatrix} a & b \\ c & d \end{bmatrix} + \begin{bmatrix} w & x \\ y & z \end{bmatrix} = \begin{bmatrix} a+w & b+x \\ c+y & d+z \end{bmatrix}$

 $\begin{bmatrix} a & b \\ c & d \end{bmatrix} * x = \begin{bmatrix} a * x & b * x \\ c * x & d * x \end{bmatrix}$

 $\begin{bmatrix} a & b \\ c & d \\ e & f \end{bmatrix} * \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} a * x + b * y \\ c * x + d * y \\ e * x + f * y \end{bmatrix}$

• R n refers to the set of n-dimensional vectors of real numbers

Addition and Scalar Multiplication

To add or subtract two matrices, their dimensions must be **the same**.

In scalar multiplication, we simply multiply every element by the scalar value:

ML:Linear Algebra Review

A vector is a matrix with one column and many rows:

- Matrix-Vector Multiplication We map the column of the vector onto each row of the matrix, multiplying each element and summing the result.
- An **m** x **n** matrix multiplied by an **n** x 1 vector results in an **m** x 1 vector.

Matrix-Matrix Multiplication

 $\begin{bmatrix} a & b \\ c & d \\ e & f \end{bmatrix} * \begin{bmatrix} w & x \\ y & z \end{bmatrix} = \begin{bmatrix} a*w+b*y & a*x+b*z \\ c*w+d*y & c*x+d*z \\ e*w+f*y & e*x+f*z \end{bmatrix}$

To multiply two matrices, the number of **columns** of the first matrix must equal the number of **rows** of the second matrix.

The **identity matrix**, when multiplied by any matrix of the same dimensions, results in the original matrix. It's just like multiplying numbers by 1. The identity matrix simply has 1's on the diagonal (upper left to lower right diagonal) and 0's elsewhere.

We multiply two matrices by breaking it into several vector multiplications and concatenating the result

An m x n matrix multiplied by an n x o matrix results in an m x o matrix. In the above example, a 3 x 2 matrix times a 2 x 2 matrix resulted in

 $A = \begin{bmatrix} a & b \\ c & d \\ e & f \end{bmatrix}$

Unsupervised Learning

Linear regression with one variable is also known as "univariate linear regression." Univariate linear regression is used when you want to predict a single output value y from a single input value x. We're doing supervised learning here, so that means we already have an idea about what the input/output cause and effect should be.

The Hypothesis Function

Suppose we have the following set of training data:

Note that this is like the equation of a straight line. We give to $h_{\theta}(x)$ values for θ_0 and θ_1 to get our estimated output \hat{y} . In other words, we are trying to create a function called h_{θ} that is trying to map our input data (the x's) to our output data (the y's).

average) of all the results of the hypothesis with inputs from x's compared to the actual output y's. $J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^{m} (\hat{y}_i - y_i)^2 = \frac{1}{2m} \sum_{i=1}^{m} (h_{\theta}(x_i) - y_i)^2$

We can measure the accuracy of our hypothesis function by using a cost function. This takes an average (actually a fancier version of an

Now we can make a random guess about our h_{θ} function: $\theta_0 = 2$ and $\theta_1 = 2$. The hypothesis function becomes $h_{\theta}(x) = 2 + 2x$.

which provide the best possible "fit" or the most representative "straight line" through the data points mapped on the x-y plane.

The gradient descent algorithm is: repeat until convergence: $\theta_j := \theta_j - \alpha \, \tfrac{\eth}{\eth \, \theta_i} \, J(\theta_0, \theta_1)$

When specifically applied to the case of linear regression, a new form of the gradient descent equation can be derived. We can substitute our actual cost function and our actual hypothesis function and modify the equation to (the derivation of the formulas are out of the scope of this course, but a really great one can be found here):

where m is the size of the training set, θ_0 a constant that will be changing simultaneously with θ_1 and x_i , y_i are values of the given training

Note that we have separated out the two cases for θ_j into separate equations for θ_0 and θ_1 ; and that for θ_1 we are multiplying x_i at the end

The above matrix has four rows and three columns, so it is a 4 x 3 matrix.

 A vector with 'n' rows is referred to as an 'n'-dimensional vector v_i refers to the element in the ith row of the vector.

Addition and subtraction are element-wise, so you simply add or subtract each corresponding element:

• In general, all our vectors and matrices will be 1-indexed. Note that for some programming languages, the arrays are 0-indexed.

- The result is a vector. The vector must be the second term of the multiplication. The number of columns of the matrix must equal the number of rows of the vector.

a 3 x 2 matrix.

- Inverse and Transpose
- The transposition of a matrix is like rotating the matrix 90° in clockwise direction and then reversing it. We can compute transposition of matrices in matlab with the transpose(A) function or A':

Matrix Multiplication Properties

The **inverse** of a matrix A is denoted A-1. Multiplying by the inverse results in the identity matrix.

When multiplying the identity matrix after some matrix (A∗I), the square identity matrix should match the other matrix's **columns**. When multiplying the identity matrix before some other matrix (I*A), the square identity matrix should match the other matrix's **rows**.

Not commutative. A*B≠B*A

 $A^T = \begin{bmatrix} a & c & e \\ b & d & f \end{bmatrix}$

In other words:

repeat until convergence: {

set (data).

where

j=0,1 represents the feature index number.

Intuitively, this could be thought of as:

repeat until convergence:

So vectors are a subset of matrices. The above vector is a 4 x 1 matrix. Notation and terms: ullet A_{ij} refers to the element in the ith row and jth column of matrix ${\bf A}$.

Associative. (A*B)*C=A*(B*C)

A non square matrix does not have an inverse matrix. We can compute inverses of matrices in octave with the pinv(A) function [1] and in matlab with the inv(A) function. Matrices that don't have an inverse are singular or degenerate.

 $A_{ij} = A_{ji}^T$