

Proof of Warlock DPS Equations

by Deadlord

Legend

D = Total DPS over the fight

T = Fight length in seconds

R_j = Raw damage of the j^{th} shadow bolt, $j \in \{1, \dots, N\}$

N = Number of shadow bolts cast

Total DPS Equation

First note that if there is no life tapping needed for the fight, we have

$$N = \left\lfloor \frac{T}{2.5} \right\rfloor$$

and the total damage over time will be the sum of all the random damage from each cast

$$D = \sum_{j=1}^N R_j$$

and each damage draw is

$$R_j = \left(B_j + \frac{3}{3.5}s \right) H_j (2C_j + 1)$$

where B_j is the random base damage of the j^{th} cast, s is the spell power of the caster, H_j is the binary outcome of the spell hit occurring with probability $\min\{0.83 + p, 0.99\}$ where p is the caster's hit chance, and C_j is likewise the binary event of a critical strike occurring with probability equal to the caster's crit chance.

Technically, the value of B_j is drawn uniformly, but the true distribution for the sum of these is difficult to work with so I'll approximate D as Normal in the limit of large N .

Extending to Life Tap

Longer fights require Life Tap, even with the use of Demonic Runes or Mana Potions. In this case, we have

$$N = \left\lfloor \frac{T - L}{2.5} \right\rfloor$$

where L is the time spent life tapping. If we have M total life taps during the fight, then

$$L = 1.5M$$

by the Global Cooldown (GCD).

Expected Value

$$\begin{aligned}\mathbb{E}[R_j] &= E\left[\left(B_j + \frac{3}{3.5}s\right) H_j (2C_j + 1)\right] = \left(\mathbb{E}[B_j] + \frac{3}{3.5}s\right) \mathbb{E}[H_j] (2\mathbb{E}[C_j] + 1) \\ &= \left(\frac{a_j^k + b_j^k}{2} + \frac{3}{3.5}s\right) p (2q + 1)\end{aligned}$$

where a_j^k is the lower bound of the base shadow bolt damage of rank k on the j^{th} cast. Likewise, b_j^k is this upper bound.