Boston University Department of Electrical and Computer Engineering

ENG EC 500 B1 (Ishwar) Introduction to Learning from Data

Matlab Exercise 2 Solution

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Due: 4pm Tue 3 Nov 2015 PHO440 box + Blackboard

Required reading: Your notes from lectures and additional notes on website on classification.

- Advise: This homework assignment requires a large amount of time and effort. We urge you to start right away. This assignment cannot be finished by staying up all night just before the deadline.
- This homework assignment requires programming in MATLAB. If you are new to MATLAB programming, please refer to the following link for a primer: http://www.math.ucsd.edu/~bdriver/21d-s99/matlab-primer.html
- You will be making two submissions: (1) A paper submission in the box outside PHO440. (2) An electronic submission of all your matlab code to blackboard (in a single zipped file appropriately named as described below).
- Paper submission: This must include all plots, figures, tables, numerical values, derivations, explanations (analysis of results and comments), and also printouts of all the matlab. m files that you either created anew or modified. Submit color printouts of figures and plots whenever appropriate. Color printers are available in PHO307 and PHO305. Be sure to annotate figures, plots, and tables appropriately: give them suitable *titles* to describe the content, label the *axes*, indicate *units* for each axis, and use a *legend* to indicate multiple curves in the plots. Please also explain each figure properly in your solution.
- Blackboard submission: All the matlab .m files (and only .m files) that you either create anew or modify must be appropriately named and placed into a single directory which should be zipped and uploaded into the course website. Your directory must be named as follows: <yourBUemailID>_matlab2. For example, if your BU email address is mary567@bu.edu you would submit a single directory named: mary567_matlab2.zip which contains all the matlab code (and only the code).
- File naming convention: Instructions for file names to use are provided for each problem. As a general rule, each file name must begin with your BU email ID, e.g., mary567_<filename>.m. The file name will typically contain the problem number and subpart, e.g., for problem 2.1b, the file name would be mary567_matlab2_1b.m. Note that the dot . in 2.1 is replaced with an underscore (this is important).

Problem 2.1 San Francisco Crime Prediction: (~1–2hrs run time)

In this problem we will work with a recent real-world dataset that can be downloaded from the following website: https://www.kaggle.com/c/sf-crime. This dataset is hosted by Kaggle as part of a competition for the machine learning community to use for fun and practice. The competition started at 8:51 pm on Tuesday 2 June 2015 UTC and ends at 11:59 pm, Monday 6 June 2016 UTC (370 total days). The dataset contains information about various incidents ranging from January 2003 to March 2015 derived from the San Francisco Police Department Crime Incident Reporting system. The raw data has been pre-processed into two MATLAB .mat files: data_SFcrime_train.mat and data_SFcrime_test.mat. Each incident contains the following attributes:

- Dates: The times at which the crimes occurred. We will only extract the "Hour" (in 24-hour format).
- Category: The type of crime. This is the class label and is only available for the training set.
- DayOfWeek: Weekday of crime: Sunday, Monday, Tuesday, etc.
- PdDistrict: Police department district.
- Address: Street address of crime. We are not going to use this attribute in this MATLAB exercise.
- X and Y: GPS coordinates (X = Longitude, Y = Latitude) of the crime location. We are not going to use this attribute in this MATLAB exercise. You can, however, use them to visualize the incidents on a map of San Francisco.
- (a) In this exercise we are going to make use of Hour (extracted from Date), DayOfWeek, and PdDistrict to build a classifier. We will treat all of them as *categorical* variables even though some of them like Hour and DayOfWeek have some quantitative and ordinal aspects to them. We will convert these three categorical variables into real-valued vectors as follows. The variable DayOfWeek will be represented as a 7-dimensional vector with "Sunday"= [1,0,0,0,0,0,0], "Monday"= [0,1,0,0,0,0,0], and so on. Similarly, the Hour variable will be represented as a 24-dimensional vector of zeros with a single one in the slot corresponding to the hour. The PdDistrict variable will likewise be a 10-dimensional vector of zeros with a single one in the slot corresponding to the police district (there are 10 police districts in the dataset). We will then concatenate all three of these vectors (Hour, DayOfWeek, PdDistrict) into one long binary feature vector of length 24 + 7 + 10 = 41. Perform these pre-processing steps for both the training and the test dataset.
 - (i) **Submit** your script for processing the categorical features with name <yourBUemailID>_matlab2_1a.m.
 - (ii) **Plot** three histograms (one for Hour, one for DayOfWeek, and one for PdDistrict) for all the incidents contained in the file data_SFcrime_train.mat.
 - (iii) Based on the incidents in data_SFcrime_train.mat, **find and report** the most likely hour of occurrence of each type of crime.
 - (iv) Based on the incidents in data_SFcrime_train.mat, find and report the most likely type of crime within each PdDistrict.

Visualization aid: For the purpose of visualization, we have provided you with a map visualization tool: plot_google_map.m. If you discover any interesting patterns or create any informative figures for visualization, please include them in your report.

(b) ℓ_2 -regularized multi-class logistic regression classifier: Now each incident is represented as a 41-dimensional vector \mathbf{x}_i whose elements are either 0 or 1 (viewed as real numbers). Write a MATLAB script to implement the gradient descent algorithm to learn the parameters $\theta := \{\mathbf{w}_1, \dots, \mathbf{w}_m\}$ of an ℓ_2 -regularized multi-class logistic regression. Recall that the negative log-likelihood function of logistic regression for m classes and its gradients are given by:

$$NLL(\theta) = \sum_{j=1}^{n} \ln \left(\sum_{k=1}^{m} e^{\mathbf{w}_{k}^{\mathsf{T}} \mathbf{x}_{j}} \right) - \sum_{k=1}^{m} \mathbf{w}_{k}^{\mathsf{T}} \left(\sum_{j=1}^{n} 1(y_{j} = k) \mathbf{x}_{j} \right)$$
$$\nabla_{\mathbf{w}_{y}} NLL(\theta) = \sum_{j=1}^{n} \left(\frac{e^{\mathbf{w}_{y}^{\mathsf{T}} \mathbf{x}_{j}}}{\sum_{k=1}^{m} e^{\mathbf{w}_{k}^{\mathsf{T}} \mathbf{x}_{j}}} - 1(y_{j} = y) \right) \mathbf{x}_{j}, \quad y = 1, \dots, m.$$

The ℓ_2 -regularized objective function to be minimized and its gradients are given by:

$$f(\theta) := \text{NLL}(\theta) + \frac{\lambda}{2} \sum_{k=1}^{m} ||\mathbf{w}_k||_2^2, \quad \lambda > 0,$$

$$\nabla_{\mathbf{w}_{y}} f(\theta) = \nabla_{\mathbf{w}_{y}} \text{NLL}(\theta) + \lambda \mathbf{w}_{y}, \quad y = 1, \dots, m.$$

The pseudocode of the gradient descent algorithm appears below.

Initialize: $\theta_0 := \{\mathbf{w}_1^{(0)}, \dots, \mathbf{w}_m^{(0)}\}$

For $t = 1, 2, ..., t_{max}$, do:

Evaluate gradients: $\nabla_{\mathbf{w}_k} f(\theta_t), k = 1, \dots, m$ Update weights: $\mathbf{w}_k^{(t+1)} = \mathbf{w}_k^{(t)} - \eta_t \nabla_{\mathbf{w}_v} f(\theta_t), k = 1, \dots, m$

Endfor

Choose a fixed step size η (recommended: 10^{-5}) and initialize all \mathbf{w}_k 's to be zero. We recommend using $\lambda = 1000$. Use the first 60% of data samples in data_SFcrime_train.mat as your training set and the remaining 40% as the "test" set.

- (i) **Plot** the value of the objective function $f(\theta_t)$ (y-axis) against the number of iterations t (x-axis) for $t = 1, 2, \dots, t_{\text{max}} = 1000$.
- (ii) **Plot** the test *logloss* and the test CCR versus the number of iterations respectively. The *logloss* on the "test" set is defined as:

logloss =
$$-\frac{1}{n_{\text{test}}} \sum_{j=1}^{n_{\text{test}}} \log p(y_j | \mathbf{x}_j, \theta)$$

where \mathbf{x}_j is the test data point and y_j is its ground truth label, and $p(y|\mathbf{x},\theta) = \frac{e^{\mathbf{w}_y^\mathsf{T}\mathbf{x}}}{\sum_{i=1}^m e^{\mathbf{w}_k^\mathsf{T}\mathbf{x}}}$. In order to avoid taking the label, $e^{\mathbf{x}_j}$ to avoid taking the logarithm of extremely small numbers, any value $p(y_i|\mathbf{x}_i,\theta)$ that is smaller than 10^{-10} should be treated as 10^{-10} .

(c) (Bonus) Cross-validate the regularization parameter λ using all the data in data_SFcrime_train.mat. **Report** the best value of λ . **Predict** the labels for the **real** test data points in data_SFcrime_test.mat (the ground truth labels for the real test data have been withheld by the competition). Submit your results to the original competition website and find out and **report** the real test error from the website. Report the strategy that you used and your results on the leader board of the competition. Attach screen-shots of your submission to the website and the leaderboard.

Solution:

- (a) (i) Please see the example script provided.
 - (ii) The three histograms for all the incidents contained in the data file data_SFcrime_train.mat are summarized in Figure 1.
 - (iii) For each type of crime, the most likely hours are summarized in Table 1:
 - (iv) Within each PdDistrict, information about the most likely type of crime is summarized in Table 2

This question outlines the typical first steps that one should take when dealing with a dataset "from the wild". It is a good practice to start by quickly checking some characteristics of each attribute. By doing so, you can get some insight into each attribute. You can also get a rough understanding of how informative each attribute is.

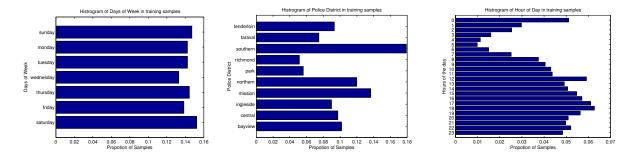


Figure 1: Histrograms for Hour, DayOfWeek, and PdDistrict for all the incidents contained in the data file data_SFcrime_train.mat for Problem 2.1(a). The histogram for DayOfWeek shows that the frequency of occurrence of an incident is roughly uniform over all days of the week and is slightly higher during weekends. The histrogram for PdDistrict shows that the southern district has significantly more crimes (reported) than others. The histrogram for the hour of day shows that the frequency of incidents peaks at noon and in the late afternoon, and is low early in the morning.

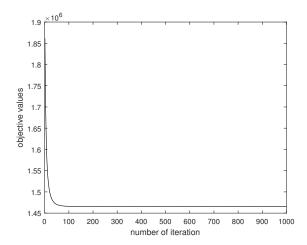


Figure 2: The value of the objective function plotted against the number of iterations for Problem 2.1(b)(i). The objective function converges after about 200 iterations. Your solution should be roughly the same if you use all the recommended settings.

- (b) (i) The value of the objective function against the number of iterations is summarized in Figure 2.
 - (ii) The test logloss and test CCR values plotted against the number of iterations are summarized in Figure 3.

Type of Crime	Most Likely Hour
'ARSON'	0
'ASSAULT'	0
'BAD CHECKS'	12
'BRIBERY'	17
'BURGLARY'	17
'DISORDERLY CONDUCT'	6
'DRIVING UNDER THE INFLUENCE'	0
'DRUG/NARCOTIC'	14
'DRUNKENNESS'	0
'EMBEZZLEMENT'	0
'EXTORTION'	0
'FAMILY OFFENSES'	15
'FORGERY/COUNTERFEITING'	0
'FRAUD'	0
'GAMBLING'	13
'KIDNAPPING'	0
'LARCENY/THEFT'	18
'LIQUOR LAWS'	17
'LOITERING'	17
'MISSING PERSON'	8
'NON-CRIMINAL'	12
'OTHER OFFENSES'	17
'PORNOGRAPHY/OBSCENE MAT'	14
'PROSTITUTION'	22
'RECOVERED VEHICLE'	12
'ROBBERY'	21
'RUNAWAY'	18
'SECONDARY CODES'	12
'SEX OFFENSES FORCIBLE'	0
'SEX OFFENSES NON FORCIBLE'	0
'STOLEN PROPERTY'	16
'SUICIDE'	18
'SUSPICIOUS OCC'	12
'TREA'	5
'TRESPASS'	6
'VANDALISM'	18
'VEHICLE THEFT'	18
'WARRANTS'	17
'WEAPON LAWS'	0

Table 1: Solution to Problem 2.1(a)(iii). The most likely hour for each type of incident based on the samples in the data file data_SFcrime_train.mat.

PdDistrict	Most Likely Crime
'bayview'	'OTHER OFFENSES'
'central'	'LARCENY/THEFT'
'ingleside'	'OTHER OFFENSES'
'mission'	'OTHER OFFENSES'
'northern'	'LARCENY/THEFT'
'park'	'LARCENY/THEFT'
'richmond'	'LARCENY/THEFT'
'southern'	'LARCENY/THEFT'
'taraval'	'LARCENY/THEFT'
'tenderloin'	'DRUG/NARCOTIC'

Table 2: Solution to Problem 2.1(a)(iv). The most likely type of crime within each PdDistrict based on the samples in the data file data_SFcrime_train.mat.

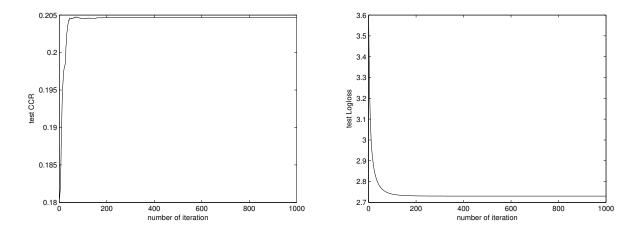


Figure 3: The test logloss and test CCR values plotted against the number of iterations for Problem 2.1(b)(ii). Your solution should be roughly the same if you use all the recommended settings.

Problem 2.2 SVM Classifier for Text Documents: (~1–2hrs run time)

In this problem we will use SVMs to classify documents in the 20 Newsgroup dataset which we have encountered before in Matlab Exercise 1.2. The dataset provided in data_20news.zip contains the following files:

- 1. vocabulary.txt: a list of all the words that can appear in the documents. The line number is the Word_ID.
- 2. newsgrouplabels.txt: the names of the 20 classes. The line number is the label_ID.
- 3. train.label and test.label: the labels of all the training and test documents.
- 4. train.data and test.data: files containing words along with their counts appearing in training and test documents. Each line in the files is of the form: "Document_ID, Word_ID, word count". Word count is the number of times the word: Word_ID appears in document: Document_ID.
- 5. stoplist.txt: a list of commonly used "stop words" such as "the", "is", "on", etc.

For this problem, we will **remove** all the stop words from the original documents. We represent the j-th document as a **word-frequency vector** $\mathbf{x}_j \in \mathbb{R}^W$ over the entire vocabulary of size W: $\mathbf{x}_{w,j} = n_{w,j}/n_j$ where $n_{w,j}$ is the number times word w appears in document j and n_j is the total number of words in document j. We will use the following built-in MATLAB implementations for SVM training and testing: symtrain and symclassify.

Binary Classification:

- (a) Train a *binary* SVM classifier using the linear kernel to distinguish between the following two classes: *alt.atheism* (class 1) and *talk.religion.misc* (class 20). Here the so-called "boxconstraint" parameter C is unspecified and needs to be determined via cross-validation. This is typically done through an exhaustive grid-search. Create one 5-fold cross-validation (CV) partitioning by splitting the training data into 5 equal-sized disjoint parts uniformly at random. Then for different choices of C's in the range $2^{-5}, 2^{-4}, \ldots, 2^{15}$, calculate the CV-CCR. For one value of C, the CV-CCR is calculated by first successively training on 4 out of the 5 folds and testing on the remaining one to obtain a CCR value, and then averaging the 5 CCR values (one CCR for each test fold).
 - (i) **Plot** of the CV-CCR (y-axis) as function of C (x-axis, use log-scale).
 - (ii) **Report** the best C^* , i.e., the value of C that achieves the maximum CCR.
 - (iii) Use C^* to train a linear SVM classifier on all the training data, and test it on the test dataset. **Report** the test CCR.
 - (iv) **Submit** your script with name <yourBUemailID>_matlab2_2a.m.

Recommendations: Set 'autoscale' to be 'false' so that symtrain does not automatically re-scale each feature dimension. For the 'boxconstraint' in MATLAB, set it to be a vector C * ones(n, 1) where n is the number of training samples.

(b) Train a binary SVM classifier using the RBF kernel to distinguish between the alt.atheism and talk.religion.misc classes. Here you will have to determine two free parameters: the "boxconstraint" C and the "rbf-sigma". You should choose the best pair of parameters through an exhaustive search on a 2-D grid. As described in part (a), create a 5-fold cross-validation partitioning and calculate the CV-CCR for all combinations of values of the boxconstraint (values: $2^{-5}, 2^{-4}, \ldots, 2^{15}$) and rbf-sigma (values: $2^{-13}, 2^{-13}, \ldots, 2^3$).

- (i) **Plot** the CV-CCRs as a function of the boxconstraint (*x*-axis) and the rbf-sigma (*y*-axis) using a 2-D contour plot. Use a log-scale for both the boxconstraint and rbf-sigma. Remember to include the colorbar in your figure.
- (ii) **Report** the best (boxconstraint, rbf-sigma) pair.
- (iii) Use the best pair of parameters that you found in the previous part to train an RBF kernel SVM classifier on the entire training set and test it on the test dataset. **Report** the test CCR.
- (iv) **Submit** your script with name <yourBUemailID>_matlab2_2b.m.

Useful MATLAB functions: cvpartition, contour, colorbar.

Recommendations: Set 'autoscale' to be 'false'. For the 'boxconstraint' in MATLAB, set it to be a vector C * ones(n, 1) where n is the number of training samples. Be patient; it might take a long time.

(c) We will now train a *binary* SVM (using a linear kernel) to separate class #17 (positive samples) from the remaining classes (the remaining 19 classes taken together are the negative samples). One practical issue here is that the number of samples in the positive class is far less than the number of samples in the negative class, i.e., the dataset is inherently unbalanced. Recall from class that the SVM solution can be reformulated as the unconstrained minimizer of the following objective function:

$$\min_{\mathbf{w},b} \left[\frac{1}{2} ||\mathbf{w}||_{2}^{2} + C_{+} \sum_{j:y_{j}="+"} \left(1 - y_{j}(\mathbf{w}^{\top}\mathbf{x}_{j} + b) \right)_{+} + C_{-} \sum_{j:y_{j}="-"} \left(1 - y_{j}(\mathbf{w}^{\top}\mathbf{x}_{j} + b) \right)_{+} \right]$$

As discussed in the class, the training objective function will be dominated by samples from the negative class if we follow the standard setting where $C_+ = C_- = C$. A commonly used practical strategy to mitigate this problem is to set different penalties C_+ and C_- for different classes. Specifically, $C_+ = n \times C/n_+$ and $C_- = n \times C/n_-$, where n_+ and n_- are number of positive and negative samples and $n = n_+ + n_-$ is the total number of training samples. Use this strategy and the same setting as in part (a), i.e., use a linear kernel and set autoscale = false. **Report** the same results as required in part (a). **In addition, report** the 2×2 confusion matrix of test data. **Comment on** what you observe about the confusion matrix.

Useful facts: if you set the 'boxconstraint' to be a *scalar* in symtrain, then C_+ and C_- are automatically scaled as described above by default. Parts (c) and (d) can be run together to save time.

- (d) The CCR in part (c) might not be a good performance metric since the dataset is highly unbalanced. For the same setting as part (c):
 - (i) **Plot** the cross-validation **precision**, **recall**, and **F-score** as functions of the regularization (penalty) parameter *C* (on the same plot).
 - (ii) **Report** the best values of C in terms of both **recall** and **F-score**. Also **report** the confusion matrices associated with these two best values of C.

One-versus-one (OVO) multi-class classification: We will next build a multi-class SVM classifier using the following strategy: Train m(m-1)/2 binary SVMs for all the class pairs. At test time, apply all these m(m-1)/2 binary SVMs to the test sample and predict the label as the one with the most votes.

- (e) Apply OVO to the entire 20 News Group dataset using the linear kernel with the *default* regularization parameter *C* in MATLAB.
 - (i) **Report** the overall CCR.
 - (ii) **Report** your training and test times (use MATLAB functions tic, toc for this part).

- (iii) Report the confusion matrix of the test set.
- (iv) **Submit** your script with name <yourBUemailID>_matlab2_2e.m
- (f) Apply OVO to the entire 20 News Group data using the rbf kernel with the *default* regularization parameters C, σ in MATLAB.
 - (i) **Report** the overall CCR.
 - (ii) **Report** your training and test times (use MATLAB functions tic, toc).
 - (iii) **Report** the confusion matrix of the test set.
 - (iv) **Submit** your script with name <yourBUemailID>_matlab2_2f.m

Solution:

(a) (i) Figure 4 summarizes the cross-validation CCRs as a function of the regularization parameter *C* ('boxconstraint' in MATLAB's built-in function). Your figure might look a bit different since the cross-validation partitioning is created randomly. It should, however, follow a similar trend. For many datasets, this range of *C* is a good choice to start with.

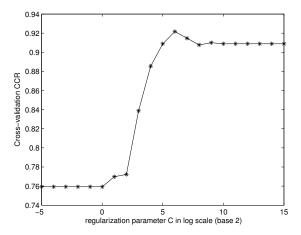


Figure 4: The Cross Validation-CCR as function of the 'boxconstraint' C (regularization parameter) in linear SVM for binary document classification. This is the solution plot for Problem 2.2(a)(i). 5-fold cross validation is used to produce the results.

- (ii) In the example run shown in Figure 4, the optimal $C^* = 64$.
- (iii) Using $C^* = 64$ as the regularization parameter and a linear SVM trained on the entire training set, the test CCR is 80.32%.
- (iv) Please see the example script provided.
- (b) (i) Figure 5 summarizes the cross-validation CCRs as a function of the regularization parameter and the RBF kernel parameter 'rbf-sig'. Your figure might look a bit different since the *k*-fold partitioning is created randomly, but it should follow a similar pattern. In Figure 6, we also include other types of plots in order to better illustrate the CV-CCR surface.
 - (ii) In the example run shown in Figure 5, the best combination of the tuning parameters are: 'boxconstraint'= 4096 and 'rbf-sig'= 4.

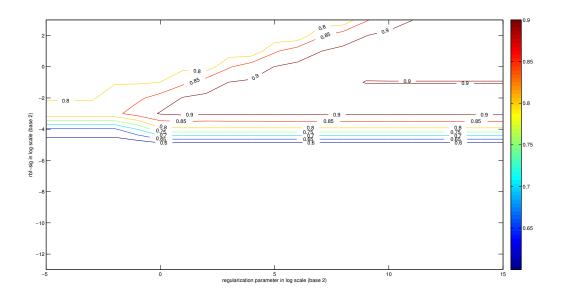


Figure 5: 2-D contour plot of the cross-validation-CCR plotted as a function of C and the 'rbf-sigma' in RBF-kernel SVM for binary document classification. This is the solution plot for Problem 2.2(b)(i). 5-fold cross validation is used to produce the results.

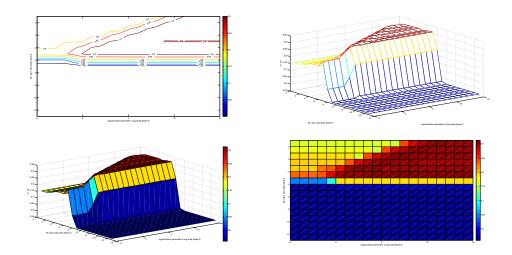


Figure 6: The cross-validation-CCR as function of C and the 'rbf-sigma' in RBF-kernel SVM for binary document classification. Top-left: 2-D contour plot, top-right: 3-D mesh plot, bottom-left: 3-D surf plot, and bottom-right: 2-D pseudo-color plot. These plots illustrate the solution to Problem 2.2(b)(i). 5-fold cross validation is used to produce the results.

- (iii) Using the optimal combination of tuning parameters, the test CCR for binary rbf-kernel SVM is 80.32%. (Note: it is only coincidental (for this dataset) that it matches the performance of the linear SVM. This is not always the case.)
- (iv) Please see the example script provided.
- (c) (i) Figure 7 summarizes the cross-validation CCR as a function of the regularization parameter for

separating class 17 from the rest. Yoir figure might look a bit different since the 5-fold CV-partitioning is created randomly. It should, however, follow a similar pattern.

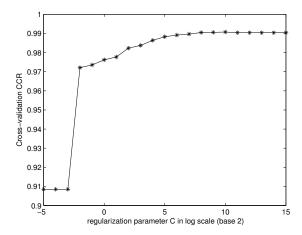


Figure 7: The cross-validation-CCR as function of the 'boxconstraint' C (regularization parameter) in linear SVM for binary document classification. The positive class is the 17-th class. The negative class is the union of all the remaining 19 classes. This is the solution plot for Problem 2.2(c)(i). 5-fold cross validation is used to produce the results.

- (ii) In the example run illustrated in Figure 7, the optimal choice of the regularization parameter is $C^* = 1024$. Your result could be different since the 5-fold CV-partitioning is created randomly, but it should be somewhat similar.
- (iii) The test CCR using $C^* = 1024$ is 97.14%.
- (iv) Please see the example script provided.
- (v) The confusion matrix of the test set is illustrated in Table 3.

	Truth '-'	Truth '+'
Decision '-'	7049	123
Decision '+'	91	241

Table 3: Confusion matrix of test set using $C^* = 1024$ and a linear SVM trained on the entire training set. The positive class is class-17 in this example. The negative class is the union of all the remaining 19 classes. The overall CCR is high, but the positive class is poorly classified.

From the confusion table it is clear that while the overall test CCR is good, the classification performance for the positive samples is poor. The setting of this binary classification problem is unbalanced, i.e., the number of negative samples is much higher than the number of positive samples. One should, therefore, consider using performance metrics other than CCR in order to choose the best tuning parameter(s).

(d) (i) Figure 8 summarizes the cross-validation metrics (Precision, Recall, and F-score) as functions of the regularization parameter for separating class 17 from the rest. Your figure might look a bit different since the *k*-fold partitioning is created randomly. It should, however, follow a similar pattern.

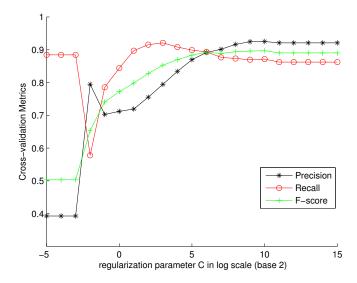


Figure 8: The cross-validation precision, recall, and F-score as functions of the regularization parameter C. This is the solution plot for Problem 2.2(d)(i). The positive class is class-17 and the negative class is the union of all the remaining 19 categories. 5-fold cross validation is used to produce the results.

(ii) For recall, $C^* = 8$. Using recall as the performance metric we have the following test confusion matrix (Table 4):

	Truth '-'	Truth '+'
Decision '-'	6959	66
Decision '+'	181	298

Table 4: Confusion matrix of the test set using $C^* = 8$ and a linear SVM trained on the entire training set. Here, 'recall' is used as the performance metric. The positive class is class-17 in this example. The negative class is the union of all the remaining 19 classes.

For F-score, $C^* = 512$. For F-score as the performance metric, the test confusion matrix is shown in Table 5.

	Truth '-'	Truth '+'
Decision '-'	7044	119
Decision '+'	96	245

Table 5: Confusion matrix of the test set using $C^* = 512$ and a linear SVM trained on the entire training set. Here, F-score is used as the performance metric. The positive class is class-17 in this example. The negative class is the union of all the remaining 19 classes.

By comparing Table 3, Table 4, and Table 5, one can see how CCR, recall, and F-score can help select the regularization parameters.

- (e) (i) The overall test CCR using one-vs-one strategy is: 30.82%.
 - (ii) The training and test times depend on the platforms and implementations. For a test run on a

single Windows laptop with Intel i7-5600 CPU and 16G memory, the training time is about 65.6 seconds and the test time about 61.1 seconds.

(iii) The confusion matrix appears in Table 6.

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
1	68	0	0	0	0	0	0	2	1	4	0	1	0	3	0	6	1	7	1	17
2	0	46	10	7	0	9	1	1	0	1	0	1	1	0	4	0	0	0	0	0
3	0	4	121	8	2	14	0	1	0	0	0	1	0	0	0	1	0	0	0	0
4	0	1	15	100	20	0	30	0	0	0	0	0	1	0	0	0	0	0	0	0
5	0	1	4	1	68	0	5	0	0	0	0	1	2	0	1	0	0	0	0	0
6	0	0	7	0	0	28	0	0	0	0	0	0	0	1	0	0	0	0	0	0
7	0	1	1	2	2	0	72	2	1	2	1	0	1	2	0	0	2	0	0	0
8	0	0	0	0	0	0	3	58	3	0	0	0	0	1	0	0	0	0	0	0
9	0	0	0	0	0	0	0	0	110	0	0	0	0	0	0	0	0	0	0	0
10	0	0	1	1	0	0	0	2	1	222	44	0	0	1	1	0	0	3	1	0
11	0	0	0	1	1	0	0	0	0	7	183	0	0	0	0	0	0	0	0	0
12	1	0	1	0	0	3	1	0	0	0	0	85	2	0	0	0	1	0	0	0
13	174	331	215	269	282	331	261	297	253	134	155	206	378	252	214	242	43	203	94	118
14	9	1	2	1	3	0	3	10	12	10	3	7	2	123	6	6	3	8	14	11
15	2	1	1	0	1	4	1	1	0	0	1	0	2	0	147	2	0	0	0	0
16	25	0	0	0	0	0	0	0	0	0	1	0	0	2	0	106	0	0	0	27
17	37	3	13	2	4	1	5	21	16	17	11	93	4	7	19	35	314	115	166	65
18	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	39	0	0
19	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	33	0
20	2	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	1	0	13

Table 6: Confusion matrix of the OVO multi-class SVM classifier (with a linear kernel) on the 20 Newsgroup dataset (Problem 2.2(e)(iii)). Columns represent the ground truth and the rows the decisions. The default regularization parameter in MATLAB symtrain was used to generate this table.

- (iv) Please see the example script provided.
- (f) (i) The overall test CCR is 31.41%. Note that if we cross-validate the 'rbf-sig' parameter rather than using the default parameter, the CCR can be further improved.
 - (ii) The training and test times depend on the platform, device, and the implementation. For a test run on a single Windows laptop with Intel i7-5600 CPU and 16G memory, the training time is about 78.7 seconds and the test time is about 147.6 seconds.
 - (iii) The confusion matrix is shown in Table 7.
 - (iv) Please see the example script provided.

One should note that for parts (e) and (f), the regularization parameter for each binary classifier can be selected using cross-validation as in parts (a) and (b). In order to simplify the procedure, we omitted this step from the assignment.

	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
1	56	0	0	0	0	0	0	1	1	2	0	0	0	2	0	13	0	3	1	12
2	2	136	38	18	4	30	2	1	0	0	0	6	4	1	3	2	1	0	1	2
3	0	4	131	7	2	15	0	1	0	0	0	1	0	0	0	1	0	0	0	0
4	0	2	23	133	30	2	41	0	0	0	0	0	3	0	0	0	0	0	0	0
5	0	1	3	0	71	0	9	0	0	0	0	0	3	0	1	0	0	0	0	0
6	0	0	7	0	1	82	0	1	0	0	0	0	0	1	0	0	0	0	0	0
7	0	1	0	2	2	3	110	1	1	2	1	0	1	4	0	0	2	0	0	0
8	0	0	0	0	0	0	5	56	1	0	0	0	0	0	0	0	1	0	0	0
9	0	0	0	0	0	0	0	0	118	0	0	0	0	0	0	0	0	0	0	0
10	0	0	1	1	0	0	1	1	0	107	13	0	0	1	0	0	0	2	0	0
11	0	0	0	1	1	0	0	0	0	15	179	0	0	0	0	0	0	0	0	0
12	1	1	1	1	0	4	1	0	0	0	0	87	2	0	0	0	1	0	0	0
13	6	106	58	140	132	120	115	67	18	27	19	19	188	37	15	25	5	5	4	5
14	88	88	71	53	76	76	45	113	127	122	54	73	108	327	162	110	12	48	37	62
15	1	2	1	2	1	5	2	0	0	0	1	0	0	0	95	1	0	0	0	0
16	20	0	0	0	0	0	0	0	0	0	1	0	0	2	0	76	0	0	0	23
17	142	48	57	34	63	53	51	153	131	122	131	209	84	18	116	170	342	294	239	135
18	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	24	0	0
19	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	27	0
20	2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	12

Table 7: Confusion matrix of the OVO multi-class SVM classifier (with an rbf kernel) on the 20 Newsgroup dataset (Problem 2.2(f)(iii)). Columns represent the ground truth and the rows the decisions. The default tuning parameters in MATLAB symtrain were used.