

# Lista 6

①

$$n = 100$$

$$\sigma(x) = 16$$

$$X \sim N(x, \mu=100, \sigma^2=16)$$

$$P(X > 95) = P\left(\frac{X-100}{4} > \frac{95-100}{4}\right) = P(Z > -1.25) = .89$$

$$P(X \leq 95) = 1 - P(X > 95) = 1 - .8944 = .1056$$

La Ganancia Esperada

$$P(X > 95) \times 25 + P(X \leq 95) \times 10$$

$$= (.8944)(25) + .1056(10) = 23.4$$

②

X = Valulas con Presion de activacion

$$X \sim N(x, 26, 4), z_1 = \frac{20-26}{4} = -1.5, z_2 = \frac{32-26}{4} = 1.5$$

$$P(20 \leq X \leq 32) = P(-1.5 \leq Z \leq 1.5) = .8664$$

③

$$D \sim N(x, \mu=4, \sigma^2=.01)$$

Para ganar .5 se debe

$$.05 < |D-4| < .08 \rightarrow \text{Desarrollando } ||$$

$$D-4 > .05 = 4.05 \quad D-4 < .08 = 3.92$$

$$-D+4 > .05 = 3.95 \quad -D+4 < .08 = 3.92$$

$$D > 4.05 \quad D < 3.95$$

$$P(X=0.5) = P(.05 < |D-4| < .08) = P(4.05 < D < 4.08) + P(3.92 < D < 3.95)$$

$$= P\left[\frac{4.05-4}{.1} < z < \frac{4.08-4}{.1}\right] + P\left[\frac{3.92-4}{.1} < z < \frac{3.95-4}{.1}\right]$$

$$= P(.5 < z < .8) + P(-.8 < z < -.5) \\ (.00967 + .00967) = .01934$$

Para ganancia = 2

$$P(x=1) = P(10-4 > .08) = (0-4) > .08 \\ \left. \begin{array}{l} 0-4 > .08 = 4.08 \\ -0+4 > .08 \end{array} \right\} 0 < 3.92$$

$$P(10-4 > .08) = P(0 > 4.08) + P(0 < 3.92)$$

$$= P\left(\frac{4.08-4}{.1}\right) + P\left(\frac{3.92-4}{.1}\right)$$

$$P(z > .8) + P(z < -.8) = .2119 + .2119 = .4238$$

$$E(x) = \sum(x)P(x) = 1(.4238) + (-5)(.01934) = .5205$$

(4)

$$x \sim N(\mu, \sigma)$$

$$P(x \leq c) = 2P(x > c) = 2(1 - P(x \leq c))$$

$$P(x \leq c) + 2P(x \leq c) = 2$$

$$P(x \leq c) = \frac{2}{3}$$

$$P\left(\frac{x-\mu}{\sigma} \leq \frac{c-\mu}{\sigma}\right) = \frac{2}{3}, P\left(z \leq \frac{c-\mu}{\sigma}\right) = .66$$

entonces la acumulada es .66

$$\frac{c-\mu}{\sigma} = .43$$

$$c = .43\sigma + \mu$$

5

$X = \text{Diametro del cable}$

$$X \sim N(\mu, \sigma, .0004)$$

Este se considera defectuoso si  $|X - \mu| > .025$   
 Probabilidad que sea defectuoso

$$X - \mu > .025$$

$$-X + \mu > .025 \quad \Rightarrow \quad X - \mu < -.025$$

$$P(|X - \mu| > .025) = P(X - \mu > .025) + P(X - \mu < -.025)$$

$$Z = \frac{.025}{.02} = 1.25 \quad Z = \frac{-.025}{.02} = -1.25$$

$$= (Z > 1.25) + (Z < -1.25)$$

$$= .1056 + .1056 = .2112$$

6

$X = \text{Daño a la carga}$

$$X \sim N(\mu, \sigma^2 = (30)^2)$$

$$Z = \frac{100 - 200}{30}$$

$$P(X < 100) = \Phi(-3.3) = .0004$$

$$X \sim B(X, .0004)$$

$$P(X > 1) = 1 - P(X = 0)$$

$$= 1 - \binom{5}{0} (.0004)^0 (1 - .0004)^5$$

$$(1 - .0004) = .9996 \quad .9996^5 = .998001 \quad 1 - .998001 = .001998400$$

7)  $x$

$$z_1 = \frac{14.7 - 15}{.2} = -1.5 \quad z_2 = \frac{15.1 - 15}{.2} = .5$$

$$P(x \leq 14.7) = \Phi(-1.5) = .069146$$

$$P(x \leq 15.1) = \Phi(.5) = .69146$$

$$P(14.7 \leq x \leq 15.1) = .69146 - .069146 = .62231$$

b) 25 millos por galon

14.8 — 25 millos  
370

$$z = \frac{14.8 - 15}{.2} = -1$$

$$1 - P(x \leq 14.8) = 1 - \Phi(-1) = 1 - .15866 = .84134$$

8)  $x = \text{Peso Paquete} + z$   
 $x \sim N(\mu = 10, \sigma^2 = 4)$

$$P(x \leq C-1) = .99$$

$$z = \frac{C-10}{2} =$$

$$P\left(2 \leq \frac{C-10}{2}\right) = P\left(z \leq \frac{C-10}{2}\right) = .99 \quad C = 2(z) + 10$$

$$\frac{C-10}{2} = 2.3 \quad C = 14.6$$

9

$$P(X < 9.671) = .05 \quad P(X > 10.256) = .10$$

$$P\left(Z < \frac{9.671 - \mu}{\sigma}\right) = .05 \quad P\left(Z > \frac{10.256 - \mu}{\sigma}\right) = .10$$

al buscar en la tabla los valores de .05 y .10

$$\frac{9.671 - \mu}{\sigma} = -1.645 \quad \text{y} \quad \frac{10.256 - \mu}{\sigma} = 1.28$$

$$9.671 - \mu = -1.645\sigma \quad \text{Restando ② de ①}$$

$$10.256 - \mu = 1.28\sigma \quad \text{--- ②} \quad - .585 = -2.925\sigma$$

$$\text{Sustituyendo en ①} \quad \sigma = \frac{.585}{2.925} = .2$$

$$9.671 + 1.645(-.02) = \mu = 10$$

10

$$\sigma = 400 \quad \sigma^2 = (40 \text{ hrs})^2$$

$$P(X > 750) = 1 - P(X \leq 750)$$

$$Z = \frac{750 - 800}{\sqrt{400}} = -.625$$

$$P(Z > -0.625) = 1 - .2643 = .7357$$

⑪  $x = \text{Paginas de texto}$

$$\sigma^2 = (15)^2$$

$$P(x \leq 100) = P(z \leq \frac{100 - 90}{15}) = \Phi(1.666) = .768$$

$$P(80 \leq x \leq 110) = \frac{80 - 90}{15} \leq z \leq \frac{110 - 90}{15}$$

$$= \Phi(-.666) - \Phi(1.33) = .687$$

⑫  $Y = \mu$   
 $\mu$

$$\mu = 19.9$$

$$\sigma^2 = (3.2)^2$$

$$x = \mu$$

$$\mu = 20.7$$

$$\sigma^2 = (1.56)^2$$

$$x \sim N(\mu = 20.7, \sigma^2 = 11.56^2)$$

$$Y \sim N(\mu = 19.9, \sigma^2 = (3.2)^2)$$

$$P(Y > x) = P(x - Y < 0)$$

$$x - Y \sim N(\mu = 20.7 - 19.9,$$

$$\sigma^2 = 11.56 + 10.24)$$

$$P\left(\frac{x - \mu - .8}{4.66} < \frac{0 - .08}{4.66}\right) = P(z < -.171324)$$

$$\sigma = \sqrt{11.56 + 10.24} = 4.66$$

$$P(z > .1713) = 1 - \Phi(.171324) = .4325$$

⑬  $x = \text{longitud 1-esimo componente}$

$$x \sim N(\mu = 2, \sigma^2 = (.02)^2)$$

$$P(5.7 \leq x \leq 6.3) = P\left(\frac{5.7 - 3(2)}{\sqrt{.12}} \leq z \leq \frac{6.3 - 6}{\sqrt{.12}}\right) =$$

$$P(-.86 \leq z \leq .86) = .6102 \times 100 = 61\%$$