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# Thompson sampling for duelling bandits

Large-scale Online Learning and Decision Making Wednesday 19th September 2012 Cumberland Lodge, Windsor, UK

#### Overview

- Motivation
- The Duelling Bandits Problem
- The Algorithm
- Progress and Future Work

#### Motivation

### Touch Clarity

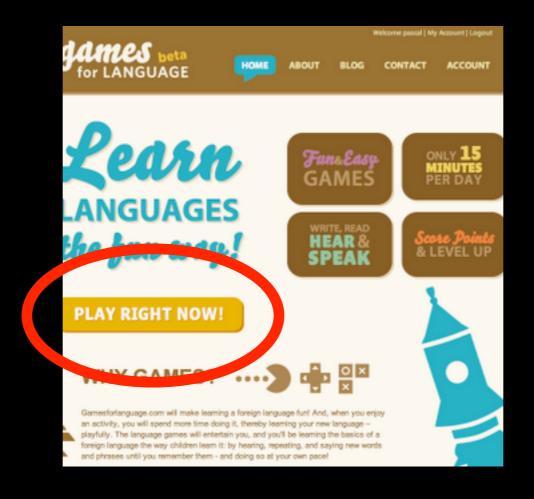
Years pass...

Myna mynaweb.com



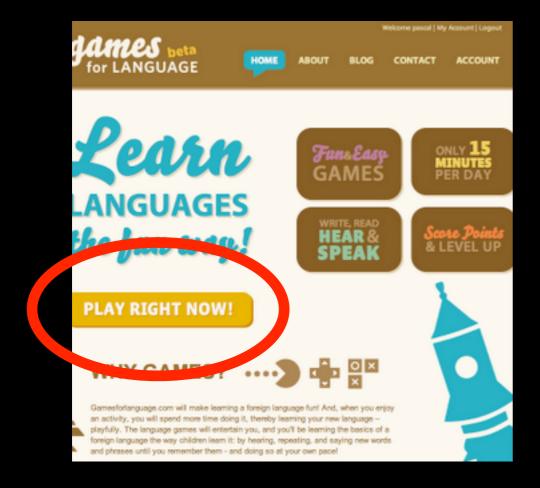


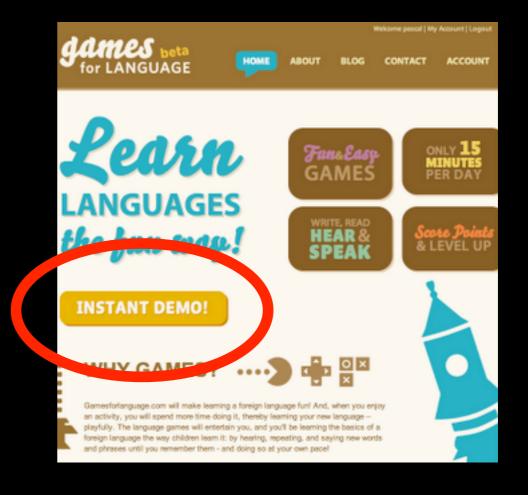


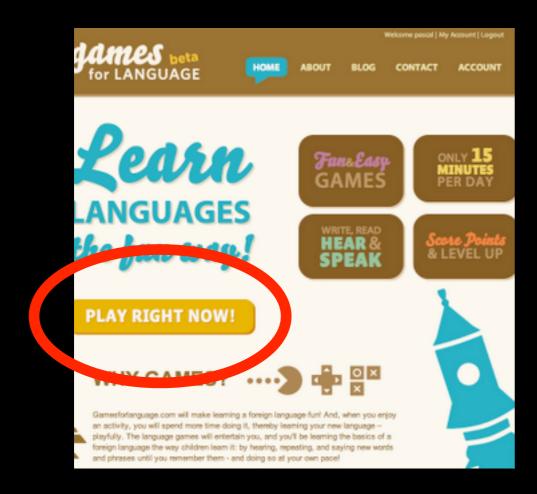












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### hypothesis testing?

### hypoilissis resting?

### modern banditry!

## problem: delayed rewards

# solution: thompson sampling

## problem: non-stationary rewards

stationary preferences are a more reasonable assumption

# this is the duelling bandits problem

we receive not absolute rewards but partial preferences between 2 or more arms

e.g. arms 2 and 4 are preferred over 1, 3, and 5

solution: solve duelling bandits + thompson sampling

starting place: pairwise preferences between arms

 $Pr(arm_i > arm_j)$ 

### beta prior

 $Pr(arm_i > arm_j) \sim Beta(a_{ij}, b_{ij})$ 

defines (probabilistic) partial ordering over arms

$$Pr(arm_1 > arm_2) = 0.7$$
  
 $Pr(arm_1 > arm_3) = 0.4$ 

$$Pr(arm_2 > arm_1) = 0.3$$

• • •

## note: transitivity not enforced

we can sample a partial ordering, but how do we then sample an arm?

# partial orderings define a Markov chain

can sample from the stationary distribution of the chain!

### Algorithm Sketch

- Sample transition matrix from Beta priors
- Calculate stationary distribution (e.g. power iterations)
- Sample from stationary distribution
- Update priors in the usual way

results?

#### Future Work

- We can sample multiple choices at once
- We can handle multiple arms being rewarded at once
- Therefore, extension to ranking problems seems straightforward

thanks!

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