

1 Session-aware Recommendation: A Surprising Quest 2 for the State-of-the-art

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6 **Abstract**

7 Recommender systems are designed to help users in situations of informa-
8 tion overload. In recent years we observed increased interest in session-based
9 recommendation scenarios, where the problem is to make item suggestions
10 to users based only on interactions observed in an ongoing session, e.g., on
11 an e-commerce site. However, in cases where interactions from previous
12 user sessions are also available, the recommendations can be personalized
13 according to the users' long-term preferences, a process called *session-aware*
14 recommendation. Today, research in this area is scattered, and many works
15 only compare a newly proposed *session-aware* with existing *session-based*
16 models. This makes it challenging to understand what represents the state-
17 of-the-art. To close this research gap, we benchmarked recent session-aware
18 algorithms against each other and against a number of session-based recom-
19 mendation algorithms along with heuristic extensions thereof. Our compar-
20 ison, to some surprise, revealed that (i) simple techniques based on nearest
21 neighbors consistently outperform recent neural techniques and that (ii) ses-
22 sion-aware models were mostly not better than approaches that do *not* use
23 long-term preference information. Our work therefore points to potential

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24 methodological issues where new methods are compared to weak baselines,
25 and it also indicates that there remains a huge potential for more sophisti-
26 cated session-aware recommendation algorithms.

27 *Keywords:*

28 Session-aware Recommendation, Evaluation, Reproducibility

29 1. Introduction

30 Recommender systems (RS) can nowadays be found on many modern
31 e-commerce and media streaming sites, where they help users find items of
32 interest in situations of information overload. One reason for the success
33 of RS lies in their ability to personalize the item suggestions based on the
34 preferences and observed past behavior of the individual users. Historically,
35 researchers have therefore strongly focused on situations where only informa-
36 tion about long-term user preferences is available, e.g., in the form of item
37 ratings. Only in recent years, more focus was put on the problem of *session-*
38 *based* recommendation, where the system has to deal with anonymous users
39 and therefore can base its recommendations only on a small number of in-
40 teractions that are observed in the ongoing session.

41 Due to the practical relevance of this problem, a variety of technical ap-
42 proaches to session-based recommendation were proposed in the past few
43 years, in particular ones based on deep learning (neural) techniques, see
44 [28, 47]. Implicitly, these methods try to make recommendations by guessing
45 the user’s short-term intent or situational context only from the currently ob-
46 served interactions. However, while it is well known that the current intents
47 and context may strongly determine which items are relevant in the given

48 situation [18], information about long-term preferences of users, if available,
49 should not be ignored. In particular, the consideration of such information
50 allows us to make session-based recommendations that are *personalized* ac-
51 cording to long-term preferences, a process which is also called *session-aware*
52 recommendation [35].

53 Session-aware recommendation problems are recently receiving increased
54 interest. Today, the research literature is however still scattered, which makes
55 it difficult to understand what represents the state-of-the-art in this area.
56 One particular problem in that context is that existing works do not use a
57 consistent set of baseline algorithms in their performance comparisons. Some
58 works, for example, mainly compare session-*aware* models with session-*based*
59 ones, i.e., with algorithms that do not consider long-term preference informa-
60 tion, e.g., GRU4REC [15]. Several other works use *sequential* recommendation
61 algorithms, e.g., FOSSIL [13], as a baseline. These are algorithms that con-
62 sider the sequence of the events but are usually designed for settings where
63 the input is a time-stamped user-item rating matrix and not a sequential
64 log of observed interactions. Only in a few works, previous session-aware
65 algorithms are considered in the evaluations. One example is the method
66 by Phuong et al. [34], which uses the HGRU4REC method [36] as a baseline.
67 Finally, almost all works include some trivial baselines, e.g., the recommen-
68 dation of popular items in a session.

69 With this work, our goal is to close the research gap regarding the state-
70 of-the-art in session-aware recommendation. For this purpose, we have con-
71 ducted extensive experimental evaluations in which we compared five re-
72 cent neural models for session-*aware* recommendation with (i) a set of ex-

73 isting neural and non-neural approaches to session-*based* recommendation,
 74 and (ii) heuristic extensions of the session-based techniques that, e.g., make
 75 use of reminders [20] or consider interactions that were observed immedi-
 76 ately before the ongoing session. Regarding the baseline techniques, we in
 77 particular considered methods based on nearest neighbors techniques, which
 78 previously proved to be very competitive in session-based recommendation
 79 scenarios [29]. All investigated techniques were compared by extending the
 80 evaluation framework shared in [27]. For reproducibility purposes, we share
 81 all data and code used in the experiments online¹, including the code for data
 82 preprocessing, hyperparameter optimization, and measuring.

83 The results of our investigations are more than surprising. In the major-
 84 ity of cases, and on all four considered datasets, heuristic extensions of exist-
 85 ing *session-based* algorithms were the best-performing techniques. In many
 86 cases, even plain session-based techniques, and in particular ones based on
 87 nearest-neighbor techniques, outperform recent session-aware models even
 88 though they do not consider the available long-term preference information
 89 for personalization. With our work, we therefore provide new baselines that
 90 should be considered in future works on session-aware recommendation. On
 91 a more general level, our observations also point to potential methodologi-
 92 cal issues, where new models are compared to baselines that are either not
 93 properly optimized, that do not leverage all available information, or that are
 94 rather weak for the given task. Similar observations were previously made in
 95 the field of information retrieval and in other areas of recommender systems

¹[https://www.dropbox.com/sh/gp1xnm4rsn777fp/AABxfe_Q7aH2q0rPzAbndMCSa?](https://www.dropbox.com/sh/gp1xnm4rsn777fp/AABxfe_Q7aH2q0rPzAbndMCSa?dl=0)
 dl=0

96 [3, 7, 49].

97 On a more positive note, our evaluations suggest that there is a huge po-
98 tential to be tapped by more sophisticated (neural) algorithms that combine
99 short-term and long-term preference signals for session-aware recommenda-
100 tion. An important prerequisite for progress in this area however lies in an
101 increased level of reproducibility of published research. A side observation
102 of our research is that despite some positive developments in recent years,
103 where researchers increasingly share their code on public repositories, it in
104 many cases still remains challenging to reproduce existing works.

105 The paper is organized as follows. In Section 2, we discuss relevant previ-
106 ous works. Section 3 describes our research methodology in more detail with
107 respect to the compared algorithms, the evaluation protocol, and the perfor-
108 mance measures. The results of our experiments are reported in Section 4,
109 and we discuss research implications and future works in Section 5.

110 2. Previous Work

111 Historically, recommender systems research focused strongly on the prob-
112 lem of rating prediction given a user-item rating matrix, a setting which is
113 also known as the “matrix completion” problem [39]. In this original collab-
114 orative filtering problem setting, the order of the ratings or the time when
115 they were provided were not considered in the algorithms. Soon, however,
116 it turned out that these aspects can matter, leading to the development of
117 *time-aware* recommender systems [5], e.g., in the form of the *timeSVD++*
118 algorithm as used in the Netflix Prize [24].

119 Ten years after the Netflix Prize, the focus of research has mostly shifted

120 from rating prediction to settings where mainly implicit feedback signals by
 121 users (e.g., purchase or item-view events) are available. Moreover, instead of
 122 considering the user-item matrix as the main input, recent research more of-
 123 ten focuses on settings where the main input to a recommendation algorithm
 124 are sequential logs of recorded user interactions. The family of approaches
 125 that relies on such types of inputs are referred to as *sequence-aware* recom-
 126 mender systems [35].

127 Within this class of sequence-aware recommender systems, we can differ-
 128 entiate between three main categories of problem settings and algorithmic
 129 approaches.

- 130 • *Sequential Recommender Systems:* Unlike the other types of sequence-
 131 aware approaches discussed here, these systems are rooted in the tra-
 132 dition of relying on a user-item rating matrix as an input. The partic-
 133 ularity of such systems is that the sequence of events is first extracted
 134 from the time-stamped rating matrix, and the goal then usually is to
 135 predict the immediate next user action (e.g., the next Point-of-Interest
 136 that a user will visit), given the entire preference profile of the user.
- 137 • *Session-based Recommender Systems:* The input to these systems are
 138 time-ordered logs of recorded user interactions, where the interactions
 139 are grouped into *anonymous sessions*. Such a session could, for exam-
 140 ple, correspond to a listening session on a music service, or a shopping
 141 session on an e-commerce site. One particularity of such approaches is
 142 that users are not tracked across sessions, which is a common problem
 143 on websites that deal with first-time users or users that are not logged
 144 in. The prediction task in this setting is to predict the next user action,



Figure 1: Comparison of session-based and session-aware recommendation problems. Different colors indicate different users.

given only the interactions of the current session. Today, session-based recommendation is a highly active research area due to its practical relevance.

- *Session-aware Recommender Systems:* This category is also referred to as *personalized session-based recommender systems*. It is similar to session-based recommendation in that the user actions are grouped into sessions. Also the prediction goal is identical. However, in this problem setting, users are not anonymous, i.e., it is possible to leverage information about past user sessions when predicting the next interaction for the current session.

Figure 1 illustrates the differences between *session-based* and *session-*

156 *aware* recommendation scenarios.² In both problem settings, the recom-
 157 mendation problem consists of predicting which action a user will do next in
 158 an ongoing session. In an e-commerce setting, for example, the problem is
 159 to predict which items are relevant for the user, given the last few observed
 160 interactions in an ongoing shopping session. The difference between the two
 161 scenarios however is that in one case we have long-term preference informa-
 162 tion about the user (session-aware recommendation), whereas in the other
 163 case such information is not available. Technically, this usually means that
 164 in session-aware scenarios we have user identifiers attached to the past usage
 165 sessions in the training data. In Figure 1, we indicate sessions by different
 166 users with different colors.

167 Unfortunately, the terminology in the literature is not entirely consistent.
 168 In this work, we will therefore use the categorization and terminology as
 169 described above to avoid confusion. Next, we review the main technical
 170 approaches in each category.

171 *Sequential Recommendation Approaches.* The first comparably simple ap-
 172 proaches in this category were based on Markov models, e.g., [32]. Later
 173 on, more sophisticated approaches emerged which, for example, combined
 174 the advantages of matrix factorization techniques with sequence modeling
 175 approaches. Rendle et al. [38] proposed the Factorized Personalized Markov
 176 Chain (FPMC) approach as an early method for next-basket recommenda-
 177 tion in e-commerce settings, where user interactions are represented as a

²Remember that sequential problems, which are not based on the concept of a session, are not in the scope of this work.

178 three dimensional tensor (user, current item, next-item). Kabbur et al. [22]
 179 later proposed FISM, a method based on an item-item factorization. FISM
 180 was then combined with factorized Markov chains to incorporate sequential
 181 information into the FOSSIL model [12].

182 In recent years, several sequential recommender systems based on neural
 183 networks were developed. Kang and McAuley [23], for example, proposed
 184 SASREC (self-attention based sequential model), a method that allows to
 185 capture long-term semantics like an RNN. However, through the use of an
 186 attention mechanism, it focuses only on a smaller set of interactions to make
 187 the item predictions. In the CASER method, Tang and Wang [45] embedded
 188 a sequence of recent items into latent spaces as an “image” in time, and
 189 proposed to learn sequential patterns as local features of the image with
 190 the help of convolutional filters. Most recently, Sun et al. [43] proposed
 191 BERT4REC, which employs a deep bidirectional self-attention mechanism to
 192 model user behavior sequences.

193 In this work, we do not consider this class of algorithms in our perfor-
 194 mance comparison because these methods, in their original designs, do not
 195 consider the concept of a session in the input data. While it is in principle
 196 possible to apply these methods in a particular way for session-based recom-
 197 mendation problems, a previous evaluation shows that sequential approaches
 198 are often not competitive with techniques that were specifically designed for
 199 the problem setting. Specifically, the evaluation presented in [27] included
 200 a number of sequential approaches, namely FPMC, MC, SMF, BPR-MF, FISM,
 201 and FOSSIL.³ Their findings showed that (*i*) these approaches either are gen-

³FPMC: Factorized Personalized Markov Chains [38], MC: Markov Chains [32], SMF:

erally not competitive in this setting or only lead to competitive results in a few specific cases and (ii) that nearest neighbor recommenders outperform them in terms of prediction accuracy.

Session-based Recommendation Approaches. While there exist some earlier works on session-based recommendation, e.g., in the context of website navigation support and e-commerce [31, 42], research on this topic started to grow only in the mid-2010s. These developments were particularly spurred by the release of datasets in the context of machine learning competitions, e.g., at ACM RecSys 2015. At around the same time, deep learning methods were increasingly applied for recommendation problems in general. The first deep learning approach to session-based recommendation was GRU4REC [15], which is based on Recurrent Neural Networks. Later on, various other types of neural architectures were explored, including attention mechanisms, convolutional neural networks, graph neural networks or hybrid architectures, see [47] for an overview.

Recent work however indicates that in many cases much simpler methods can achieve similar or even higher performance levels than today’s deep learning models. Most recently, Ludewig et al. [29] benchmarked several of the mentioned neural methods against conceptually simpler session-based algorithms which, for example, rely on nearest-neighbor techniques. Quite interestingly, their analyses and similar previous works [8, 27] not only show

Session-based Matrix Factorization [27], BPR-MF: Bayesian Personalized Ranking [37], FISM: Factored Item Similarity Models [22], FOSSIL: FactOrized Sequential Prediction with Item SIilarity ModeLs [12].

223 the strong performance of conceptually simple techniques, but also revealed
224 that two of the earlier neural methods, GRU4REC and NARM, often perform
225 better than more recent complex techniques. In the performance comparison
226 in this present work on session-aware recommendation, we include several
227 techniques for session-based recommendation as baselines. This allows us to
228 assess the added value of considering long-term preference information com-
229 pared to a situation where such information is not available or not leveraged.

230 *Session-aware Recommendation Approaches.* The literature on session-aware
231 recommendation is still quite sparse. An early approach is discussed in [20].
232 One main goal of their work was to understand the relative importance of
233 short-term user intents when visiting an e-commerce site compared to the
234 long-term preference model. Their analyses, which were based on a large but
235 private e-commerce dataset, emphasized the importance of considering the
236 most recent observed user behavior when recommending. Furthermore, it
237 also turned out that *reminding* users of items that they have viewed before
238 can be beneficial, both in terms of accuracy measures and business metrics.

239 While the work in [20] relied on deep learning for the final predictions in
240 one of their models, the core of the proposed technical approach was based
241 on feature engineering and the use of side information about the items to
242 recommend. One of the earliest “pure” deep learning techniques for session-
243 aware recommendation was proposed by [36]. Technically, the authors based
244 their work on GRU4REC, and they used a second, parallel GRU layer to model
245 information across sessions, resulting in a model called HGRU4REC. Their
246 analyses showed that incorporating long-term preferences can be beneficial,
247 i.e., HGRU4REC was outperforming an early version of GRU4REC in their

248 experiments.

249 In the same year, Ruocco et al. [40] proposed the IIRNN model. Like
250 HGRU4REC, this model uses an RNN architecture and extends a session-
251 based technique to model inter-session and intra-session information. Like
252 in the case of HGRU4REC, the authors investigate the value of considering
253 long-term preference information by comparing their method to session-based
254 techniques. RNNs were later on also used in the NSAR model [33] to encode
255 session patterns in combination with user embeddings to represent long-term
256 user preferences across sessions. In their experiments, the authors not only
257 compare their model to session-based techniques, but also to HGRU4REC as
258 a representative of a session-aware approach.

259 A number of neural architectures other than RNNs were proposed in
260 recent years. Hu et al. [17], for example, combine the inter-session and intra-
261 session context with a joint context encoder for item prediction in the NCSF
262 approach. In the SHAN model [50], in contrast, the authors leverage a two-
263 layer hierarchical attention network to model short-term and long-term user
264 interests. In the SWIWO [16] approach, the authors were inspired by language
265 modeling approaches like *word2vec*, where the underlying idea is that items
266 can be seen as words, hence, predicting a relevant word based on context
267 information is equivalent to recommending a relevant item in an ongoing
268 session. Finally, Cai and Hu [4] proposed the SAMR method, which leverages
269 a topic-based probabilistic model to define the users’ listening behavior.

270 Unlike most previous works, which compare a newly-proposed session-
271 aware model with previous session-based ones, our work compares session-
272 aware methods against each other. Furthermore, we benchmark several of

273 these recent session-aware methods with (i) existing session-based techniques
274 and (ii) extended versions of them that also consider long-term preference
275 information. We describe our research methodology next.

276 3. Research Methodology

277 In this section, we describe which algorithms we selected for inclusion
278 in our comparison. Moreover, we provide details about the experimental
279 configuration in terms of the evaluation protocol and the used datasets. As
280 mentioned, all datasets and the code used in the experiments are shared
281 online to ensure reproducibility.

282 3.1. Compared Algorithms

283 In our experiments, we compare neural session-aware algorithms with a
284 number of baselines. Details about the algorithms are provided next.

285 3.1.1. Neural Session-Aware Algorithms

286 We identified five recent neural approaches, which we integrated into our
287 evaluation framework using the source provided by the authors: HGRU4REC,
288 IIRNN, SHAN, NCSF, and NSAR.

- 289 • HGRU4REC: This method [36] is based on the GRU4REC algorithm.
290 To model the interactions of a user within a session, it utilizes RNNs
291 based on a single GRU layer. By adding an extra GRU layer, it models
292 information across user sessions. The user-level GRU initializes the
293 hidden state of the session-level GRU and optionally propagates the
294 user representation in the input to the session-level GRU to personalize
295 its recommendations.

- 296 • IIRNN: This method [40] extends a session-based recommender built

297 on RNN, called intra-session RNN, by using a second RNN that is

298 called inter-session RNN. The intra-session RNN is the same as in the

299 GRU4REC model. The inter-session RNN learns from the user’s recent

300 sessions and feeds the information to the intra-session RNN. At the

301 beginning of every session, the final output of the inter-session RNN

302 initializes the hidden state of the intra-session RNN.
- 303 • SHAN: This model [50] uses a two-layer hierarchical attention network

304 to learn a hybrid representation for each user that combines the long-

305 term and short-term preferences. It first embeds sparse user and item

306 inputs into low-dimensional dense vectors. The long-term user rep-

307 resentation is a weighted sum over the embeddings of items in the

308 long-term item set. By learning the weights, the first attention layer

309 learns user long-term preferences. The second attention layer returns

310 the final user representation by combining the long-term user model

311 and the embeddings of the items in the short-term item set.
- 312 • NCSF: This session-aware neural method [17] has three components:

313 (i) the historical session encoder to represent the inter-session context,

314 (ii) the current session encoder to represent the intra-session context,

315 and (iii) the joint context encoder to integrate the information of the

316 intra-session context and the inter-session context for item prediction.
- 317 • NSAR: This method [34] utilizes RNNs to encode session patterns

318 (short-term user preferences) and user embeddings to represent long-

319 term user preferences across sessions. It supports different ways of

320 integrating user long-term preferences with the session patterns, where
321 user embeddings can either be integrated with the input or the output
322 of the session RNNs. Moreover, with the help of a gating mechanism,
323 the contribution of each component can be fixed or adaptive.

324 To avoid a bias in the algorithm selection, we applied the following pro-
325 cedure to identify algorithms for inclusion in our experiments. An initial set
326 of candidate works was retrieved through a search on Google Scholar using
327 search terms like “session-aware recommendation” or “personalized session-
328 based recommendation”. We inspected the returned results to see if the pa-
329 pers fulfilled our inclusion criteria. Besides being actually a work on session-
330 aware recommendation according to the above definition, we required that
331 the source code of the method was publicly available and could be integrated
332 into our Python-based evaluation framework⁴. Moreover, we only considered
333 papers that had undergone a peer review process, i.e., we did not include
334 non-reviewed preprints. Finally, we included only works that did not con-
335 sider side information about the items. As a result of this last constraint, we
336 did not include works like [44] for the domain of news recommendation.

337 In Table 3.1.1, we show to which baselines the selected neural approaches
338 were compared in their original publications. Note that in this table only the
339 last two rows, HGRU4REC and SWIWO represent session-aware techniques.
340 Our analysis furthermore shows that researchers use a variety of baselines in
341 their experiments, which contributes to the difficulty of understanding what

⁴For example, the code used in [4] is not publicly available, and the method in [16] is written in MATLAB.

342 represents the state-of-the-art.

343 3.1.2. Neural and Non-Neural Session-based Baselines

344 We selected the baselines according to the results of [29]. Note that while
345 GRU4REC and NARM are not the most recent neural methods, the analysis
346 in [29] showed that they are highly competitive among the neural models for
347 different datasets.

- 348 • GRU4REC: This neural model [15] employs RNNs based on Gated Re-
349 current Units (GRU) for the session-based recommendation task. It
350 introduces several modifications, including a ranking loss function, to
351 classic RNNs to adapt it for the recommendation task in the session-
352 based setting. The authors later on improved the model with an al-
353 ternative loss function and by applying further refinements, [14]. We
354 include the latest version of GRU4REC in our experiments.
- 355 • NARM: This model [26] extends GRU4REC. It utilizes a hybrid en-
356 coder with an attention mechanism to model the sequential behavior
357 of users and capture their main intent of the current session. A bi-
358 linear matching scheme is used to compute the recommendation scores
359 of each candidate item based on a unified session representation.
- 360 • SR: The *Sequential Rules* method, proposed in [27], extends the simple
361 *Association Rules* technique (also from [27]) and counts pairwise item
362 co-occurrences in the training sessions. It considers the order of the
363 items in a session as well as the distance between them when scoring
364 the items.

Table 1: Overview of the baseline techniques that each neural session-aware approach was originally compared to. The methods are ordered chronologically by the date of publication. The marks (**X**) indicate which baselines were used in the comparison.

	Method				
	HGRU4REC	IIRNN	SHAN	NCSF	NSAR
Baseline	MR	X			
	POP	X	X	X	
	PPOP	X			
	IKNN	X		X	
	BPR-MF	X	X		X
	FPMC		X	X	
	FOSSIL		X		
	GRU4REC	X	X	X	X
	GRU4REC2			X	X
	BPR-GRU4REC2				X
	HRM		X		
	CASER				X
	HGRU4REC				X
	SWIWO			X	

MR: most recent interacted item; POP: most popular item in the dataset;
PPOP: most popular item for the user; IKNN: Item-based kNN [15];
BPR-MF: Bayesian Personalized Ranking [37]; FPMC: Factorized
Personalized Markov Chains [38]; FOSSIL: FactOrized Sequential
Prediction with Item SIMilarity ModeLS [12]; GRU4REC: [15];
GRU4REC2: the improved version of the GRU4REC model [14];
HRM: Hierarchical Representation Model [46]; CASER: Convolutional
Sequence Embedding Recommendation Model [45]; BPR-GRU4REC2:
a baseline proposed in [34] that merges the rankings returned by
BPR-MF and GRU4REC2 following the proposed framework in [18] for
session-aware setting; HGRU4REC: [36]; SWIWO: [16].

- 365 • VSKNN: This nearest-neighbor baseline for session-based recommenda-
 366 tion was proposed in [27], and it is based on the SKNN method [19].
 367 It first finds past sessions that contain the same items as the current
 368 session. The recommendation list is then generated using items that
 369 occur in the most similar sessions. This method considers the order
 370 of the items while computing both session similarities and item scores.
 371 Moreover, it applies the Inverse-Document-Frequency (IDF) weighting
 372 scheme to put more emphasis on less popular items.
- 373 • STAN: The *Sequence and Time Aware Neighborhood* method was pro-
 374 posed in [8]. It improves SKNN by considering three additional factors
 375 for making recommendations: (i) the recency of an item in the current
 376 session, (ii) the recency of a past session w.r.t. the current session, and
 377 (iii) the distance of a recommendable item w.r.t. a shared item in the
 378 neighboring sessions.
- 379 • VSTAN: This nearest-neighbor session-based recommendation algorithm
 380 combines all the extensions to SKNN from STAN and VSKNN in a single
 381 approach; proposed in [29].

382 3.1.3. *Extensions of Session-based Baselines*

383 We experimented with three simple ways of extending session-based al-
 384 gorithms in a way that they consider past preference information.

- 385 • EXTEND – *Extending the current session with recent interactions*: In
 386 case there is little information available about the ongoing session, e.g.,
 387 when only a few first clicks are recorded, we extend the current session
 388 with interactions that we observed in the previous sessions of the user.

- 389 • BOOST – *Emphasizing previously seen items*: In some domains, re-
 390 peated interactions with already seen or consumed items are not un-
 391 common. We apply a simple “boosting” approach to slightly increase
 392 the scores computed by an underlying algorithm in case an item has
 393 appeared previously in the interaction history.
- 394 • REMIND – *Applying reminding techniques*: In [20], the authors pro-
 395 posed a number of “reminder” techniques to emphasize items the user
 396 has seen before. The general approach is to determine and score a
 397 set of candidate items that the current user has interacted with in the
 398 past. We considered different strategies that were inspired by [20] in
 399 our evaluations.

400 EXTEND. We implemented this strategy as follows. First, we choose a value
 401 for the “desired session length” d , which is a hyperparameter to be determined
 402 on the validation set. In case an ongoing session has fewer interactions than
 403 d , we extend the current session with previous interactions from the same
 404 user until the session length d is reached or no more previous interactions
 405 exist. The extension is done by simply prepending the elements of previous
 406 interactions to the current session in the order they appeared in the log.

407 BOOST. This simple approach can in principle be applied to any algorithm
 408 that returns scores. Methods like SR and VSKNN, for example, return scores
 409 based on item co-occurrences and the positions of the co-occurring items,
 410 as described in [27]. In our experiments, we used a hyperparameter b as
 411 a boost factor. Technically, we look up each item that is recommended by
 412 the underlying method and check if it occurred in the interaction history of

413 the current user at least once. In case the item appeared previously in the
 414 history, we increase the original score by b %.

415 REMIND. Different reminding strategies were proposed in [20]. In our exper-
 416 iments, we tested a number of alternative ways to select and score items to
 417 consider as reminders. In all of them, the reminder list is created by adding
 418 items of the user’s last p sessions, which is a hyperparameter to be deter-
 419 mined on the validation set. The assumption is that very old sessions at
 420 some stage might become irrelevant and should not be considered anymore.
 421 The following reminder strategies are the best performing ones according to
 422 our experiments.

423 *Interaction Recency.* In this strategy, we use a decay function to score
 424 reminder items, i.e., items in the interaction history of the user, based on the
 425 time of the user’s last interaction with them:

$$\text{IRecScore}(i) = T_c / (T_c - T_i) \quad (1)$$

426 Here, T_c is the timestamp of the current session, and T_i is the timestamp
 427 of the last interaction of the user with the item i .

428 *Session Similarity.* In this strategy, the items of the last P sessions of
 429 the user are scored based on the similarity score(s) of the current session
 430 and the previous session(s) that they belong to. This strategy is based on a
 431 nearest-neighbor recommendation method to calculate the similarity scores
 432 between sessions:

$$\text{SSimScore}(i) = \sum_{p=1}^P \text{Sim}(S_c, S_p) \cdot 1_p(i) \quad (2)$$

433 Here, S_c denotes the current session, and S_p denotes a session in the set
 434 of the last P past sessions of the user. Sim is the similarity function of the
 435 nearest-neighbor algorithm, and the indicator function $1_p(i)$ returns 1 if the
 436 session p contains item i and 0 otherwise.

437 In our present work, we used a *hybrid* approach to combine aspects of
 438 interaction recency (IRec), session similarity (SSim), and the item’s rele-
 439 vance score (RelScore), as determined by a recommendation algorithm, in
 440 a weighted approach. The overall ranking score for an item i is therefore
 441 defined as

$$\text{OverallScore}(i) = W1 \times \text{RelScore}(i) + W2 \times \text{IRecScore}(i) + W3 \times \text{SSimScore}(i) \quad (3)$$

442 Here, $W1$, $W2$, and $W3$ are hyperparameters to tune, and the individual
 443 scores are normalized before they are combined. Note that for algorithms
 444 that are not based on nearest-neighbors, we do not compute a SSimScore
 445 value, and we thus set $W3$ to 0.

446 3.2. Datasets

447 We conducted our evaluations on four public datasets from three different
 448 domains: e-commerce, social networks and music.

- 449 • *RETAIL*: A dataset published by the e-commerce personalization com-
 450 pany *Retail Rocket*. It covers user interactions with a real-world e-
 451 commerce website over 4.5 months.
- 452 • *XING*: A dataset published in the context of the ACM RecSys 2016
 453 Challenge that contains interactions of job postings on a career-oriented

454 social networking site, *XING*, from about three months. It contains
 455 a fraction of *XING* users and job postings, and the data is enriched
 456 with artificial users for privacy reasons. The interactions include four
 457 types of actions: *click*, *bookmark*, *reply*, and *delete*. We filtered out all
 458 interactions of type *delete* from the dataset for our evaluation, as done
 459 in [36], because they are considered as negative interactions.

- 460 • *COSMETICS*: An e-commerce dataset containing the event history
 461 of a cosmetics shop for five months.⁵ The interactions include four
 462 types of actions: *click*, *view*, *add-to-cart*, *remove-from-cart*, *purchase*.
 463 Since the methods examined in our work are not designed to consider
 464 multiple types of actions, we only used the interactions of one type
 465 (*item views*) for our evaluation, as was done also in various previous
 466 works [15, 26]. Furthermore, we randomly sampled 10% of the users
 467 of this large dataset because of scalability issues of some of the neural
 468 methods.

- 469 • *LASTFM*: A music dataset that contains the entire listening history of
 470 almost 1,000 users during five years. The dataset was retrieved from
 471 the online music service *Last.fm*⁶.

472 For each dataset, we first partitioned the log into sessions by applying a
 473 commonly used 30-minute user inactivity threshold⁷. We kept multiple inter-

⁵<https://www.kaggle.com/mkechinov/ecommerce-events-history-in-cosmetics-shop>

⁶<https://www.last.fm/>

⁷The COSMETICS dataset already contains session IDs, but we noticed that there were large inactivity thresholds and some of the original sessions spanned several days.

actions with the same item in one session because repeated recommendations can help as reminders [20, 25]. Many previous works on session-aware recommendation use a single training-test split of the whole dataset or a sample of it for evaluation. Evaluating on only one split of data is risky because of possible random effects. We therefore split each dataset into five contiguous subsets by time and averaged the results across slices as done in [29]. To have about the same number of events for each slice, we skipped the first 500 days of the LASTFM dataset.

Following common practice in the field, we then further pre-processed each slice as follows. We first removed items with less than five interactions in the slice. Then, we removed sessions that contain only one event. For the LASTFM dataset, we also removed sessions with more than 20 events⁸. Finally, we filtered out users with less than three sessions. Table 2 shows the average characteristics of the slices for each dataset after the pre-preprocessing phase.

Table 2: Characteristics of the datasets. The values are averaged over all five slices.

	Events	Users	Sessions	Items	Sessions per User	Actions per Session
RETAIL	45,378	1,400	7,198	10,424	5.15	6.28
XING	333,625	13,533	59,318	61,006	4.38	5.62
COSMETICS	81,159	1,821	9,826	17,790	5.39	8.24
LASTFM	750,276	658	94,818	107,134	144.61	7.92

⁸The dataset contains a number of very long sessions with dozens of listening events, and the probability that users *actively* listened to tracks for many hours seems low. Therefore, we only considered the first 20 elements, which corresponds to a listening session about 1.5 hours for the case of pop music, see also [33, 40] for similar approaches.

489 *3.3. Evaluation Protocol and Metrics*

490 *Creation of Training, Validation, and Test Splits.* Since we are given user-
491 IDs for the sessions, we are able to apply a user-wise data splitting approach.
492 Specifically, like in [11, 33, 34, 36, 48], we use the last session of each user as
493 test data. The second-to-last session is used as validation data to tune the
494 parameters in our experiments, see also [33, 34, 48]. The remaining sessions
495 are considered as training data. This splitting approach allows us to assess
496 the performance both for users with shorter and longer interaction histories.
497 We finally filter out the items from the validation and test sets of each of the
498 five slices that did not appear in the training set of that slice.

499 *Target Item Selection.* We apply a procedure that is commonly used also in
500 session-based recommendation, e.g., in [15] and many other works. Specifi-
501 cally, we iteratively reveal each item after the other in the test session and
502 do the evaluation after each item⁹.

503 We apply this approach as it reflects the most realistic user behavior in
504 a session. Following previous works [27, 28, 29], we consider two evaluation
505 scenarios. In one case, we only consider the immediate next item in the test
506 session as a ground truth. In the other, more realistic case, all upcoming
507 items in the test session are considered relevant.

⁹In the implementation of the NCSF method, we found that the authors use a *context window*, which includes items *before and after* a given target item t to make the prediction. In reality, however, we cannot know which items will appear after t . As we could not resolve this issue with the authors, we used an implementation that only uses items appearing *before* the target item as the context.

508 *Accuracy Metrics.* We use standard classification and ranking measures to
 509 evaluate the performance of the recommendation algorithms. We measure
 510 the performance in two different ways, as done in [29], according to the target
 511 item selection approach. First, when we consider only the immediate next
 512 item as the target item, the used metrics are the Hit Rate (HR) and Mean
 513 Reciprocal Rank (MRR). Second, when all items of the current session are
 514 assumed to be relevant to the user, we consider all the remaining items of an
 515 ongoing session as the target item. In this case, the used accuracy metrics
 516 are Precision, Recall, and Mean Average Precision (MAP).

517 *Coverage and Popularity Bias Metrics.* It is well known that factors other
 518 than accuracy can impact the effectiveness of a recommendation algorithm
 519 in practice [41]. In this work, we consider *coverage* and the tendency of
 520 an algorithm to focus on popular items (*popularity bias*) as relevant factors.
 521 *Coverage* tells us how many items actually ever appear in the top-n lists
 522 of users. This measure, which is also known as “aggregate diversity” [1],
 523 gives us some indication of how strongly personalized the recommendations
 524 of an algorithm are. A strong popularity bias, on the other hand, indicates
 525 that an algorithm is not focusing much on the long-tail of the item catalog,
 526 which, however, can be desirable in practice. We calculate the *popularity*
 527 *bias* as done in [27]. Specifically, we average the popularity scores of all
 528 recommended items. These popularity scores are computed by counting how
 529 often each item appears in the training set. To bound their values between
 530 0 and 1, we apply min-max normalization.

531 *Computational Complexity.* Training deep learning models is often consid-
 532 ered computationally demanding. Nearest-neighbor techniques, on the other

533 hand, have no model-building phase, but the search for neighbors can, de-
 534 pending on the implementation, be computationally complex at run time.
 535 In our experiments, we therefore use the recency-based sampling approach
 536 proposed in [19] for all session-based nearest-neighbor approaches. To com-
 537 pare the computational complexity of the various methods, we measured the
 538 time that is needed by each algorithm, both for the training and the pre-
 539 diction phases. All these measurements were made on the same physical
 540 machine, which was exclusively used for the time measurements. The ma-
 541 chine is equipped with a Nvidia Titan Xp GPU and an Intel i7-3820 CPU.
 542 The neural models used the GPU whereas the non-neural techniques only
 543 used the CPU.

544 *Hyperparameter Optimization.* To obtain reliable results, we systematically
 545 and automatically tuned the hyperparameters for each algorithm and dataset.
 546 Technically, we applied a random hyperparameter optimization procedure
 547 with 100 iterations to optimize MRR@20 as done, e.g., in [27]¹⁰. For NARM,
 548 we however only ran 50 iterations as this method has a smaller set of hyper-
 549 parameters. For SHAN, we only ran 9 hyperparameter configurations since
 550 they cover all possible value combinations according to the original paper¹¹.
 551 For each dataset, we used the slice with the most number of events to tune
 552 hyperparameters.

¹⁰We also tried MAP@20 as the optimization target for some approaches, but this did not lead to a different ranking of the algorithms in terms of accuracy.

¹¹We unsuccessfully contacted the authors regarding the hyperparameter spaces.

553 4. Results

554 Tables 3–6 show the results of our performance comparison of neural and
555 non-neural methods, ordered by the values obtained for the MAP@20 metric.
556 Here, we correspondingly report the values obtained by applying a cut-off
557 threshold of 20. We performed additional experiments using alternative cut-
558 off lengths (5 and 10). The rankings of the algorithms for those other cut-off
559 values were generally in line with those observed at list length 20. Non-neural
560 methods are highlighted with a light gray background in the tables. Neural
561 session-*based* methods have a gray background. Session-*aware* techniques
562 finally have a dark gray background.

563 Note that we do not report all possible combinations of the proposed
564 extensions discussed in Section 3.1.3 for the sake of conciseness. We use the
565 following naming scheme for the different algorithm variants.

- 566 • REMIND: We denote algorithm variants that were extended with the
567 reminder technique with the postfix “_R”. Note that it is not meaning-
568 ful to incorporate the reminder extensions to session-*aware* methods, as
569 these models should already be able to implicitly leverage the long-term
570 preference information.
- 571 • EXTEND and BOOST: We report the effects of these extensions for the
572 non-neural methods¹², and we denote the extended method by append-

¹²In principle, these mechanisms can also be applied to the neural session-based methods. Initial experiments with the EXTEND extension for GRU4REC and NARM however did not lead to performance gains. Note also that the adaptation of existing neural session-based methods is not the main focus of our work.

573 ing the postfix “_E” (extend) and “_B” (boost) to the algorithm name,
 574 e.g., SR_B, VSKNN_EB. These extensions can also be combined with
 575 the reminder technique, e.g., VSKNN_EBR. For the SR method, only
 576 boosting was applied because extending the session is not applicable
 577 for this algorithm, which by design only considers the last interaction
 578 in a session.

579 For the sake of clarity, for each model and dataset, we report *(i)* the
 580 combination of the extensions that led to the best performance according to
 581 MAP@20 and *(ii)* the results of the original models without extensions. In
 582 case the original model had better performance than the extended ones, we
 583 only report the results for the original model.

584 In our analysis, we focus on the performance comparison of non-neural
 585 methods and neural session-aware recommendation techniques. Therefore,
 586 in Table 3 to Table 6, the highest obtained values among algorithms of these
 587 two families are printed in bold. Moreover, we underline the highest value
 588 that is obtained by the other family of algorithms. Stars indicate significant
 589 differences ($p < 0.05$) according to a Kruskal–Wallis test between all the mod-
 590 els and a Wilcoxon signed-rank test between the best-performing techniques
 591 from either category (non-neural or neural session-aware recommendation
 592 methods).

593 4.1. Accuracy Results

594 We can summarize the accuracy results for the individual datasets as
 595 follows.

Table 3: Results of the performance comparison on the RETAIL dataset with the focus on the comparison of **simple (non-neural)** methods and **neural session-aware** ones. The best results for each metric are highlighted in bold font. The next best results for algorithms from the other category (either simple methods or session-aware ones) are underlined. Non-neural methods are highlighted in light gray, session-based ones in gray and neural session-aware ones in dark gray.

Metrics	MAP@20	P@20	R@20	HR@20	MRR@20	COV@20	POP@20
RETAIL							
STAN_ER	*0.0350	0.0759	0.5214	0.7043	0.4411	0.8374	0.0576
VSTAN_EBR	*0.0350	0.0758	*0.5215	*0.7062	*0.4432	0.8525	0.0553
VSKNN_EBR	0.0343	0.0750	0.5097	0.6938	0.4155	*0.8632	0.0534
NARM_R	0.0320	0.0691	0.4841	0.6419	0.3850	0.8008	0.0614
STAN	0.0311	0.0680	0.4837	0.6747	0.4411	0.7818	0.0582
VSTAN	0.0310	0.0675	0.4825	0.6745	0.4397	0.7947	0.0580
VSKNN	0.0303	0.0669	0.4646	0.6476	0.4164	0.8055	<u>0.0469</u>
SR_BR	0.0301	0.0662	0.4547	0.6018	0.3666	0.8063	0.0552
GRU4REC_R	0.0292	0.0621	0.4565	0.6417	0.4305	0.9086	0.0405
GRU4REC	0.0272	0.0576	0.4367	0.6172	0.4196	0.9059	0.0394
NARM	0.0252	0.0542	0.4086	0.5650	0.3566	0.7620	0.0622
IIRNN	<u>0.0239</u>	<u>0.0524</u>	<u>0.3775</u>	0.5108	0.3190	<u>0.7709</u>	0.0689
HGRU4REC	0.0226	0.0485	0.3681	<u>0.5165</u>	<u>0.3296</u>	0.7502	0.0425
NCSF	0.0217	0.0468	0.3625	0.5042	0.3120	0.6871	0.0967
SR	0.0213	0.0460	0.3477	0.4847	0.3265	0.7186	0.0528
SHAN	0.0205	0.0451	0.3448	0.4498	0.2673	0.3406	0.1276
NSAR	0.0169	0.0370	0.2830	0.3702	0.2160	0.5813	0.0671

Table 4: Results of the performance comparison on the XING dataset with the focus on the comparison of **simple (non-neural)** methods and **neural session-aware** ones. The best results for each metric are highlighted in bold font. The next best results for algorithms from the other category (either simple methods or session-aware ones) are underlined. Non-neural methods are highlighted in light gray, session-based ones in gray and neural session-aware ones in dark gray.

Metrics	MAP@20	P@20	R@20	HR@20	MRR@20	COV@20	POP@20
XING							
VSTAN_R	*0.0194	*0.0497	*0.3031	*0.4445	*0.2837	0.9581	0.0373
STAN_R	*0.0194	0.0495	0.3027	0.4436	0.2828	0.9563	0.0395
VSKNN_R	0.0182	0.0466	0.2880	0.4304	0.2691	*0.9660	0.0344
NARM_R	0.0174	0.0448	0.2747	0.3961	0.2095	0.9400	0.0452
SR_BR	0.0158	0.0413	0.2452	0.3463	0.1852	0.9459	0.0371
GRU4REC_R	0.0151	0.0387	0.2512	0.3959	0.2721	0.9363	0.0311
VSKNN	0.0139	0.0357	0.2312	0.3783	0.2605	0.9193	<u>0.0305</u>
VSTAN	0.0138	0.0353	0.2368	0.3890	0.2747	0.8996	0.0353
STAN	0.0137	0.0352	0.2367	0.3887	0.2734	0.8950	0.0386
NARM	0.0117	0.0304	0.2031	0.3320	0.2035	0.8252	0.0480
GRU4REC	0.0113	0.0284	0.2007	0.3454	0.2653	0.9174	0.0270
NCSF	<u>0.0101</u>	<u>0.0262</u>	<u>0.1800</u>	<u>0.2982</u>	<u>0.1706</u>	0.7885	0.0683
SR	0.0092	0.0238	0.1567	0.2532	0.1633	0.8279	0.0321
NSAR	0.0086	0.0229	0.1449	0.2013	0.0968	0.8268	0.0361
HGRU4REC	0.0081	0.0203	0.1464	0.2524	0.1681	<u>0.8474</u>	0.0296
HIRNN	0.0072	0.0185	0.1274	0.2046	0.1254	0.8387	0.0484
SHAN	0.0051	0.0151	0.0932	0.1231	0.0503	0.2673	0.1329

Table 5: Results of the performance comparison on the COSMETICS dataset with the focus on the comparison of **simple (non-neural)** methods and **neural session-aware** ones. The best results for each metric are highlighted in bold font. The next best results for algorithms from the other category (either simple methods or session-aware ones) are underlined. Non-neural methods are highlighted in light gray, session-based ones in gray and neural session-aware ones in dark gray.

Metrics	MAP@20	P@20	R@20	HR@20	MRR@20	COV@20	POP@20
COSMETICS							
STAN_EBR	*0.0212	0.0741	*0.2819	*0.4270	0.1741	0.9585	0.0708
VSTAN_EBR	0.0210	*0.0751	0.2766	0.3959	0.1682	0.9512	0.0606
VSKNN_EBR	0.0209	0.0749	0.2744	0.4128	0.1683	*0.9714	0.0601
GRU4REC_R	0.0176	0.0617	0.2410	0.3808	0.1575	0.9114	0.0473
NARM_R	0.0175	0.0644	0.2337	0.3273	0.1223	0.9130	0.0674
VSKNN	0.0175	0.0628	0.2405	0.3870	0.1665	0.9626	<u>0.0562</u>
STAN	0.0173	0.0619	0.2494	0.4035	0.1760	0.9419	0.0655
VSTAN	0.0172	0.0615	0.2490	0.4041	*0.1765	0.9449	0.0648
SR_BR	0.0170	0.0623	0.2286	0.3386	0.1354	0.9528	0.0613
GRU4REC	0.0143	0.0504	0.2083	0.3383	0.1417	0.8811	0.0449
NCSF	<u>0.0133</u>	<u>0.0489</u>	<u>0.1903</u>	<u>0.2969</u>	0.1099	0.6973	0.1043
NARM	0.0129	0.0473	0.1891	0.2970	0.1175	0.8566	0.0694
HGRU4REC	0.0123	0.0442	0.1797	<u>0.2969</u>	<u>0.1198</u>	<u>0.9332</u>	0.0468
IIRNN	0.0123	0.0458	0.1761	0.2825	0.1119	0.8909	0.0778
SR	0.0111	0.0411	0.1654	0.2755	0.1161	0.9179	0.0574
NSAR	0.0081	0.0324	0.1217	0.1845	0.0617	0.7748	0.0680
SHAN	0.0054	0.0226	0.0898	0.1225	0.0434	0.2166	0.1985

Table 6: Results of the performance comparison on the LASTFM dataset with the focus on the comparison of **simple (non-neural)** methods and **neural session-aware** ones. The best results for each metric are highlighted in bold font. The next best results for algorithms from the other category (either simple methods or session-aware ones) are underlined. Non-neural methods are highlighted in light gray, session-based ones in gray and neural session-aware ones in dark gray.

Metrics	MAP@20	P@20	R@20	HR@20	MRR@20	COV@20	POP@20
LASTFM							
VSKNN_EB	*0.0493	*0.1003	*0.4248	*0.5383	0.1771	0.5053	0.0499
VSKNN	0.0474	0.0964	0.4104	0.5227	0.1725	0.5091	<u>0.0479</u>
VSTAN_EB	0.0449	0.0943	0.4088	0.5291	0.1938	0.5080	0.0528
STAN_EBR	0.0442	0.0924	0.3972	0.5159	0.1902	0.4965	0.0564
STAN	0.0400	0.0856	0.3760	0.5012	0.1886	0.5067	0.0557
VSTAN	0.0394	0.0852	0.3791	0.5100	0.1935	<u>0.5115</u>	0.0555
SR_B	0.0359	0.0778	0.3408	0.4622	<u>0.3487</u>	0.5010	0.0549
SR	0.0348	0.0765	0.3383	0.4615	0.3350	0.4982	0.0544
IIRNN	<u>0.0311</u>	<u>0.0724</u>	<u>0.3270</u>	<u>0.4729</u>	0.3491	0.4443	0.0732
GRU4REC	0.0307	0.0701	0.3175	0.4681	0.3342	0.5124	0.0468
NSAR	0.0280	0.0675	0.3044	0.4350	0.2906	0.4937	0.0483
NARM	0.0272	0.0658	0.3002	0.4510	0.3192	0.4748	0.0633
NCSF	0.0219	0.0556	0.2639	0.4393	0.2434	0.4875	0.0712
HGRU4REC	0.0208	0.0517	0.2464	0.4206	0.3167	0.5647	0.0404
SHAN	0.0072	0.0223	0.0920	0.1149	0.0345	0.0824	0.1640

596 *RETAIL*. Quite surprisingly, simple nearest-neighbor recommenders win on
 597 all the accuracy measures on this dataset, with STAN_ER and VSTAN_EBR
 598 being the best-performing methods. Moreover, the heuristic extensions of
 599 the session-based algorithms further improve their accuracy performance in
 600 all but one cases (MRR for VSKNN_EBR).

601 Probably even more surprising is that we find the session-*aware* meth-
 602 ods at the very end of the performance ranking. This means that they are
 603 actually outperformed by methods which do not consider any long-term pref-
 604 erence information at all. Specifically, all neural and non-neural session-based
 605 methods, except the basic SR method, outperform all session-*aware* methods
 606 for all accuracy metrics.

607 The best results in the class of neural session-*aware* recommendation
 608 algorithms are achieved by IIRNN and HGRU4REC. These two methods are,
 609 however, the earliest proposed session-aware recommendation methods in
 610 this comparison. Differently from the original paper, HGRU4REC is not able
 611 to outperform the last version of GRU4REC on this dataset.¹³

612 *XING*. Similar patterns are also found for the XING dataset, where (i) the
 613 neighborhood-based methods led to the best results, (ii) the extensions re-
 614 sulted in performance improvements in all cases, (iii) and session-*aware*
 615 techniques were outperformed by all other methods, except the SR method.
 616 Among the session-*aware* recommendation methods, this time NCSF achieves
 617 the best accuracy results for all metrics, even though it was not originally

¹³Using alternative loss functions for HGRU4REC might help improving its performance. Such modifications of the original algorithms are however not in the scope of our work.

618 evaluated on this dataset.

619 Note that the reminders worked generally very well on this dataset. Re-
620 minders for example help to improve the performance of the neural session-
621 based techniques (GRU4REC, NARM) to an extent that they sometimes out-
622 perform the basic nearest-neighbor techniques. However, when the extensions
623 are also considered for the neighborhood-based techniques, their accuracy re-
624 sults are again much higher than those of the neural techniques.

625 *COSMETICS*. We observe similar results also on the COSMETICS dataset.
626 Neighborhood-based methods lead to the best results for all accuracy metrics,
627 and the extensions resulted in performance improvements in almost all cases.
628 Moreover, all methods except SR and NARM outperform the session-*aware*
629 techniques. Looking at the session-*aware* methods, we notice that NCSF has
630 the best performance in all the accuracy metrics, except for the MRR, and
631 HGRU4REC achieves the best results for the Hit Rate (along with NCSF) and
632 the MRR.

633 *LASTFM*. The picture for this dataset is slightly different from the others
634 in certain respects. First, while nearest-neighbor approaches again lead to
635 the best results for Precision, Recall, MAP, and HR, these methods are
636 outperformed by all neural session-based and session-aware methods except
637 SHAN on the MRR. However, none of them, except IIRNN, outperforms the
638 simple SR method and its extended version. The best results are obtained
639 by IIRNN, which is however one of the earliest session-aware methods. Note,
640 however, that the results by IIRNN are only minimally better than SR_B.
641 Nonetheless, further investigations are needed to understand the reasons why
642 some methods perform very well on the MRR on this particular dataset.

643 A second difference to the other datasets is that while applying the simple
 644 extensions EXTEND and BOOST again proves to be beneficial, the reminder
 645 extension does not improve the performance of the original methods in some
 646 cases for this dataset.¹⁴ Therefore, we only report the results of the original
 647 neural session-based methods (GRU4REC and NARM).

648 *Summary and Additional Observations.* Table 7 summarizes the findings pre-
 649 sented in Table 3–6 by reporting the best performing approaches on the in-
 650 dividual datasets. In Table 7, we can see that VSKNN, STAN and VSTAN
 651 with their extensions largely dominate the field across the datasets and mea-
 652 sures, and we recommend that these methods are considered as additional
 653 baselines in future performance comparisons. Only in one case a method
 654 from another category (i.e., IIRNN, an early proposed neural session-aware
 655 method) appeared among the best performing approaches.

656 Looking at the best models among the neural approaches, including both
 657 session-based and session-aware, in Table 8, we notice that NARM_R and
 658 GRU4REC_R outperform the session-aware models on the RETAIL, XING,
 659 and COSMETICS datasets. On the LASTFM dataset, where the reminder
 660 extension did not lead to any performance improvements for the neural
 661 session-based models, IIRNN is the best one. As a side observation, we see
 662 that the ranking of the neural algorithms is often not correlated with the
 663 publication year of the methods, i.e., newer methods are not consistently
 664 better than older ones.

¹⁴In some cases, the optimal weights for the reminders were 0 after tuning the hyperpa-
 rameters.

Table 7: Best performing approaches for each dataset and each accuracy metric. Algorithms that were significantly better than the best performing algorithms from the other category (either **non-neural** or **neural session-aware**) are marked with *.

Datasets	RETAIL	XING	COSMETICS	LASTFM
MAP@20	*STAN_ER/VSTAN_EBR	*VSTAN_R/STAN_R	*STAN_EBR	*VSKNN_EB
P@20	STAN_ER	*VSTAN_R	*VSTAN_EBR	*VSKNN_EB
R@20	*VSTAN_EBR	*VSTAN_R	*STAN_EBR	*VSKNN_EB
HR@20	*VSTAN_EBR	*VSTAN_R	*STAN_EBR	*VSKNN_EB
MRR@20	*VSTAN_EBR	*VSTAN_R	*VSTAN	IIRNN

Table 8: Best performing approaches for each dataset and each accuracy metric for neural methods (session-based and session-aware).

Datasets	RETAIL	XING	COSMETICS	LASTFM
MAP@20	NARM_R	NARM_R	GRU4REC_R	IIRNN
P@20	NARM_R	NARM_R	NARM_R	IIRNN
R@20	NARM_R	NARM_R	GRU4REC_R	IIRNN
HR@20	NARM_R	NARM_R	GRU4REC_R	IIRNN
MRR@20	GRU4REC_R	GRU4REC_R	GRU4REC_R	IIRNN

665 4.2. Coverage and Popularity

666 Tables 3–6 also report the values of *coverage* and *popularity bias* of the
667 algorithms. We can make the following observations.

668 *Coverage.* SHAN consistently has the lowest *coverage* value across all datasets.
669 In other words, it has the highest tendency to recommend the same set of
670 items to different users. This sets the algorithm apart from all other tech-
671 niques. The coverage values of most other techniques are often not too far
672 apart, and the difference between nearest-neighbor algorithms and neural
673 algorithms is often small. However, all nearest-neighbors methods (both

original and extended versions) outperform all session-*aware* models for all datasets except for the LASTFM dataset, where HGRU4REC achieves the best result. No other consistent pattern can be found here. What can be observed is that the achieved level of coverage and the ranking of the algorithms in this respect seems to depend on the datasets.

Popularity Bias. GRU4REC and HGRU4REC consistently have the lowest tendency to recommend popular items. In contrast, SHAN exhibits the highest *popularity bias* with a considerable difference. Moreover, IIRNN and NCSF achieve higher values than all other methods across all datasets. The neighborhood-based approaches are often in the middle. They are therefore not generally focusing more on popular items than neural approaches. Finally, we observe that using the proposed session-aware extensions in most cases leads to a higher *popularity bias*.

4.3. Scalability

For the sake of brevity, we only report the results for two datasets here and provide the results for the other datasets in the appendix. We made all the measurements on the validation slice (i.e., the largest slice in terms of the number of events) for each dataset. Table 9 and Table 10 show the results for the LASTFM and XING, respectively. We selected these two datasets for the discussion because they are larger than the other two datasets and differ in some key characteristics. The LASTFM dataset for example contains the largest number of events, but only a smaller number of users. The XING dataset, on the other hand, contains events from a larger number of users. The algorithms in these tables are grouped by the type of approach (non-

Table 9: Running times on the LASTFM dataset.

	Training Time (s)	Prediction Time (ms)
SR	4.05	25.88
VSKNN	1.23	169.29
STAN	1.02	251.66
VSTAN	1.17	405.32
SR_B	12.58	37.12
VSKNN_EB	2.08	188.65
STAN_EBR	2.81	466.23
VSTAN_EB	1.97	627.66
GRU4REC	101.20	30.18
NARM	3726.80	8.92
HGRU4REC	218.71	27.18
IIRNN	7702.04	245.06
NCSF	532.62	30.75
NSAR	1621.05	15.79
SHAN	35298.70	30.98

neural, session-based neural, session-aware neural). We report running times of the session-based algorithms (neural and non-neural) both for the best-performing extension and the corresponding method.

The overall results are similar across all datasets. In terms of the *training* times, the non-neural models are consistently the fastest because “training” for such models mainly involves the initialization of data structures (nearest-neighbor techniques) or the collection of simple count statistics (SR). Interestingly, strong differences can be observed between the neural session-*based* methods GRU4REC and NARM, with GRU4REC being orders of magnitude faster than NARM in the training phase. The performance of the session-

Table 10: Running times on the XING dataset.

	Training Time (s)	Prediction Time (ms)
SR	2.66	6.69
VSKNN	0.58	10.88
STAN	0.54	9.37
VSTAN	0.58	9.85
SR_BR	7.23	22.76
VSKNN_R	1.09	25.45
STAN_R	1.00	44.26
VSTAN_R	1.97	44.83
GRU4REC	53.89	10.54
NARM	1769.09	10.12
GRU4REC_R	47.64	23.26
NARM_R	1762.86	20.37
HGRU4REC	60.54	10.27
IIRNN	7229.03	250.39
NCSF	192.25	35.60
NSAR	12562.06	34.81
SHAN	13393.82	35.50

708 *aware* methods, finally, exhibit a large spread. HGRU4REC, which is based
709 on GRU4REC, is the fastest method here. However, some session-aware meth-
710 ods can take very long¹⁵, in particular the SHAN method.

711 Looking at the time that is needed to generate one recommendation list
712 (*prediction time*, in milliseconds), we observe that most neural methods are
713 among the fastest techniques on the LASTFM dataset, with prediction times
714 being in the range of a few dozen milliseconds. However, the running time for

¹⁵Note that for the IIRNN method on the XING dataset we had to set max_epoch=20 (instead of 100) because of its very high computational complexity on this dataset.

715 the neural IIRNN method, which is the best performing neural method on this
 716 dataset¹⁶, is much higher than for the other neural methods. For the XING
 717 dataset, it even is the slowest among all compared methods. The running
 718 times for the simple SR method are in the range of the neural methods. For
 719 the nearest-neighbor techniques, the prediction times depend on the dataset
 720 characteristics. For the XING dataset, for example, the prediction times are
 721 in the range of the neural methods. On the other hand, for the LASTFM
 722 dataset, where, on average, there is a large number of sessions in the history
 723 of the users, the time needed for creating one recommendation list can go up
 724 to a few hundred milliseconds.

725 Generally, the use of the proposed extensions (BOOST, EXTEND, RE-
 726 MIND) leads to increased computation times for training and predicting.
 727 Note, however, that the more efficient basic versions of the nearest-neighbor
 728 techniques already outperform all neural *session-aware* methods in all cases,
 729 except one.

730 Overall, as mentioned above, we observe quite a spread regarding the
 731 running times among the neural methods. A detailed theoretical analysis of
 732 the computational complexity of the underlying network architectures and
 733 individual architecture elements is however beyond the scope of our present
 734 work, which focuses on the empirical evaluation of various algorithms in
 735 terms of their prediction accuracy.

¹⁶Remember, however, that all nearest-neighbors methods—both the basic and extended versions—outperformed the IIRNN method on all accuracy metrics, except MRR.

736 5. Implications, Limitations, and Future Work

737 5.1. Implications and Guidelines

738 Different factors may have contributed to the surprising observations
739 made in this paper. First, we can assume that session-*based* algorithms,
740 which are often used as baselines to benchmark session-*aware* ones, have im-
741 proved over time. This might for example be the case for the HGRU4REC
742 method, which most probably used an earlier version of GRU4REC both as a
743 session-based baseline and as a building block for the newly proposed method.

744 Another potential reason may however also lie in methodological issues
745 and problematic research practices that were observed previously not only for
746 more traditional top-n recommendation tasks, but also for other areas of ap-
747 plied machine learning such as information retrieval or time-series forecasting
748 [3, 7, 30, 49]. According to several of these works, one main problem seems
749 to be that researchers often invest substantial efforts to refine and fine-tune
750 their newly proposed methods, but do not invest similar efforts to optimize
751 the baselines to which they compare their new methods. This phenomenon
752 can be seen as a form of a *confirmation bias*, where researchers mainly seek
753 for evidence supporting their theories and claims, but do not appropriately
754 consider other evidences or indications. In that context, also reproducibility
755 issues can play a role; see also the discussion of reproducibility problems in
756 AI and empirical computer science in general [9, 6]. While researchers in
757 recent years more frequently publicly share the code of their newly proposed
758 models, they only very rarely share the code of the baselines or the code that
759 was used to fine-tune all algorithms in the experimental evaluations.

760 Another related problem can also lie in the *choice* of the baselines. In

761 particular in recent years we observe that researchers only consider very
762 recent baselines in their evaluations or limit themselves to neural methods
763 [7]. This leads to the effect that long-known or more simple methods are
764 overlooked and not considered as competitive baselines. This, in turn, can
765 lead to a *cascade* effect, where only the most recent models are considered
766 to represent the state-of-the-art, even though they are probably not better
767 than what existed earlier.

768 A number of measures can be taken to avoid that we only observe illusions
769 of progress in this area in the future. In terms of *reproducibility*, Gundersen
770 et al. [10] recently proposed a number of guidelines for reproducible research
771 in AI in general, which in principle also apply for research in recommender
772 systems research. Transferred to our specific problem setting, it is important
773 that scholars make it as easy as possible for others to replicate their research.
774 This in particular includes the publication of a number of artifacts such as
775 (i) the code of the proposed model *and* the baselines, (ii) the used datasets,
776 before and after any preprocessing, and the code used for pre-processing,
777 (iii) the code for running the experiments, including the code for tuning the
778 hyper-parameters, (iv) documentation and appropriate installation instruc-
779 tions.

780 Furthermore, in order to ensure progress, Ferrari Dacrema et al. [7] sug-
781 gest a number of guidelines for top-n recommendation settings that are
782 also relevant for session-aware recommendation problems. Specifically, re-
783 searchers are encouraged to (i) include algorithms from different *families*
784 in the experimental evaluations, i.e., not only consider neural techniques,
785 (ii) optimize all baselines models in a systematic and automated way, and

786 to (iii) carefully select and document the hyperparameter ranges and the
787 optimization strategy.

788 5.2. Research Limitations and Future Work

789 In our work so far, we performed experiments for a variety of domains—
790 including e-commerce, music, or job recommendation (social media)—using
791 publicly available and commonly used datasets. Nonetheless, further exper-
792 iments with additional datasets are needed and are part of our future work.
793 Such experiments will help us ensure that our findings generalize to other
794 domains and that they are not tied to specific dataset characteristics. Our
795 experiments so far however indicate that the ranking of the *family* of algo-
796 rithms is quite consistent across experiments, with today’s neural approaches
797 to session-aware recommendation not being among the top-performing tech-
798 niques, and non-neural techniques working well across datasets.

799 Nonetheless, an interesting area for future work lies in an improved un-
800 derstanding in which ways dataset characteristics impact the performance
801 and ranking of different algorithms, as was done for more traditional recom-
802 mendation scenarios in [2]. Moreover, it would be interesting to analyze how
803 sensitive the different algorithms are with respect to slight changes, including
804 both the characteristics of the input data and hyperparameters. In practical
805 environments, in which datasets continuously evolve due to new items and
806 users, algorithms that are more robust with respect to these aspects, might
807 be preferable. Finally, regarding running times—in particular for datasets
808 where there is a larger set of past sessions per user—further performance
809 enhancements of the nearest-neighbor methods might be achieved through
810 additional engineering efforts.

811 Regarding the set of session-aware algorithms that were benchmarked in
812 our work, we expect that a constant stream of new proposals will be pub-
813 lished in the future. As such, our experimental evaluation can only represent
814 a snapshot of the state-of-the-art in the area. Our current snapshot is fur-
815 thermore limited to works where the source code was publicly available, as
816 was done in [7]. An additional constraint that we applied when selecting
817 baselines was that the code had to be written in Python. In our literature
818 search, we only identified two related works that were not written in Python,
819 [4] and [16]. The method proposed in [4] was written in Java, but no source
820 code was provided. The work presented in [16] was written in MATLAB but
821 is only marginally relevant for our work, as it *(i)* focuses on diversity as-
822 pects and *(ii)* provides a performance comparison only with session-based or
823 sequential approaches, whereas our work focuses on session-aware techniques.

824 Finally, we observed that the size of the datasets used in the experiments,
825 both in the original papers and in our work, are small compared to the
826 amounts of data that are available in real-world deployments. The current
827 limitations of the investigated deep learning models might therefore be a
828 result of these dataset limitations, see also [21]. With more data and in
829 particular with data spanning longer periods of time, neural techniques might
830 be favorable and better suited to combine long-term preference signals with
831 short-term user intents than today’s methods.

832 6. Summary

833 Our in-depth empirical investigation of five recent neural approaches to
834 session-aware recommendation has revealed that these methods, contrary

835 to the claims in the respective papers, are not effective at leveraging long-
836 term preference information for improved recommendations. According to
837 our experiments, these methods are almost consistently outperformed by
838 methods that only consider the very last interactions of a user. Furthermore,
839 our analyses showed that non-neural methods based on nearest neighbors
840 can lead to better performance results than ones based on deep learning, as
841 was also previously observed for session-based recommendation in [29].

842 We see the reasons for these unexpected phenomena in methodological
843 issues that are not limited to session-aware recommendation scenarios, in
844 particular in the choice of the baselines in experimental evaluations or the
845 lack of proper tuning of the baselines. On a more positive note, our findings
846 suggest that there are many opportunities for the development of better
847 neural and non-neural methods for session-aware recommendation problems.
848 We in particular believe that it is promising to look at repeating patterns,
849 seasonal effects, or trends in the data. Moreover, the incorporation of side
850 information (e.g., category information about items) as well as contextual
851 information should help to further improve the prediction performance of
852 new algorithms.

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1035 *ternational Joint Conference on Artificial Intelligence*, IJCAI'18, page
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1037 **Appendix A. Hyperparameter ranges and optimal values**

Table A.11: Hyperparameter space for simple methods.

Algorithm/Extension	Hyperparameter	Type	Range	Steps
SR	steps	Integer	2 - 15	14
		Integer	20, 25, 30	
	weighting	Categorical	linear, div, quadratic, log	
VSKNN	k	Integer	50, 100, 500, 1000, 1500	
	sample_size	Integer	500, 1000, 2500, 5000, 10000	
	weighting	Categorical	same, div, linear, quadratic, log	
	weighting_score	Categorical	same, div, linear, quadratic, log	
	idf_weighting	Boolean/Integer	False, 1, 2, 5, 10	
STAN	k	Integer	100, 200, 500, 1000, 1500, 2000	
	sample_size	Integer	1000, 2500, 5000, 10000	
	lambda_spw	Real	0.00001, 0.4525, 0.905, 1.81, 3.62, 7.24	
	lambda_snh	Real	2.5, 5, 10, 20, 40, 80, 100	
	lambda_inh	Real	0.00001, 0.4525, 0.905, 1.81, 3.62, 7.24	
VSTAN	k	Integer	100, 200, 500, 1000, 1500, 2000	
	sample_size	Integer	1000, 2500, 5000, 10000	
	similarity	Categorical	cosine, vec	
	lambda_spw	Real	0.00001, 0.4525, 0.905, 1.81, 3.62, 7.24	
	lambda_snh	Real	2.5, 5, 10, 20, 40, 80, 100	
	lambda_inh	Real	0.00001, 0.4525, 0.905, 1.81, 3.62, 7.24	
	lambda_ipw	Real	0.00001, 0.4525, 0.905, 1.81, 3.62, 7.24	
BOOST (For SR, VSKNN, STAN and VSTAN) Tune together with other hyperparameters of the algorithm	boost_own_sessions	Real	0.1-3.9	20
EXTEND (For VSKNN, STAN and VSTAN) Tune together with other hyperparameters of the algorithm	extend_session_length	Integer	1 - 25	25
REMIND (For VSKNN, STAN and VSTAN) Tune with the optimal set of hyperparameters of the algorithm	reminders	Boolean	True	
	remind_strategy	Categorical	hybrid	
	remind_sessions_num	Integer	1 - 10	
	weight_Rel	Integer	1 - 10	
	weight_IRec	Integer	0 - 9	
REMIND (For SR) Tune with the optimal set of hyperparameters of the algorithm	weight_SSim	Integer	0 - 9	10
	reminders	Boolean	True	
	remind_strategy	Categorical	hybrid	
	remind_sessions_num	Integer	1 - 10	
	weight_Rel	Integer	1 - 10	
	weight_IRec	Integer	0 - 9	

For STAN and VSTAN, we used the same hyperparameters space for lambda_spw, lambda_inh, and lambda_ipw on all datasets. However, ranges for these hyperparameters can be set for each dataset separately based on its mean average length of the sessions. Ranges can be set as {0.785, 1.57, 3.14, 6.28, 12.56} for the RETAIL dataset, {0.7025, 1.405, 2.81, 5.62, 11.24} for the XING dataset, {1.03, 2.06, 4.12, 8.24, 16.48} for the COSMETICS dataset, and {0.99, 1.98, 3.96, 7.92, 15.84} for the LASTFM dataset. This will lead to slightly different results.

Table A.12: Hyperparameter search space for neural methods.

Algorithm	Fixed Hyperparameter Values	Hyperparameter	Type	Range	Steps
GRU4REC	layer_size = 100	learning_rate	Real	0.01 - 0.1	10
			Real	0.1 - 0.5	5
		momentum	Real	0 - 0.9	10
		loss	Categorical	bpr-max, top1-max	
		final_act	Categorical	elu-0.5, linear	
		dropout_p_hidden	Real	0 - 0.9	10
		constrained_embedding	Boolean	True, False	
GRU4REC_R	The optimal set of hyperparameters of GRU4REC reminders = True remind_strategy = hybrid	remind_sessions_num	Integer	1 - 10	10
		weight_Rel	Integer	1 - 10	10
		weight_IRec	Integer	0 - 9	10
NARM	epochs = 20 layer_size = 100	factors	Integer	50, 100	
		learning_rate	Real	0.01-0.001	10
			Real	0.001-0.0001	10
NARM_R	The optimal set of hyperparameters of NARM reminders = True remind_strategy = hybrid	remind_sessions_num	Integer	1 - 10	10
		weight_Rel	Integer	1 - 10	10
		weight_IRec	Integer	0 - 9	10
HGRU4REC	session_layers = 100 user_layers = 100 loss = top1 (as in the original paper)	user_propagation_mode	Categorical	init, all	
			Real	0.01-0.1	10
		learning_rate	Real	0.1-0.5	5
		momentum	Real	0 - 0.9	10
		final_activation	Categorical	linear, relu, tanh	
		dropout_p_hidden_usr	Real	0 - 0.9	10
		dropout_p_hidden_ses	Real	0 - 0.9	10
		dropout_p_init	Real	0 - 0.9	10
	batch_size	Integer	50, 100		
HIRNN	max_epoch = 100 for RETAIL, LASTFM and COSMETICS max_epoch = 20 for XING because of the computational complexity	dropout_pkeep	Real	0.1 - 1	10
			Real	0.01 - 0.001	10
		learning_rate	Real	0.001 - 0.0001	10
		embedding_size	Integer	50, 100	
		max_session_representations	Integer	1, 5, 10, 15, 20	
	use_last_hidden_state	Boolean	True, False		
SHAN	global_dimension = 100 epochs = 100 (as in the original paper)	lambda_uv	Real	0.01, 0.001, 0.0001	
		lambda_a	Integer	1, 10, 50	
NCSF		max_nb_his_sess	Integer	0, 1, 2, 5, 10	
		att_alpha	Real	0.01, 0.1, 1, 10	
		window_sz	Integer	1 - 10	10
NSAR	epochs = 20 keep_pr = 0.25 (as in the original paper) batch_size = 64 for RETAIL, LASTFM and COSMETICS (as in the original paper) batch_size = 32 for XING because of memory limitations				
		learning_rate	Real	0.001 - 0.01	10
			Real	0.01 - 0.05	5
		hidden_units	Integer	50, 100	

Table A.13: Optimal hyperparameters for simple methods.

Algorithm	Hyperparameter	RETAIL	XING	COSMETICS	LASTFM
SR	steps	15	25	15	8
	weighting	quadratic	quadratic	div	quadratic
SR with extensions	best extension	SR_BR	SR_BR	SR_BR	SR_B
	steps	12	30	15	20
	weighting	quadratic	quadratic	div	quadratic
	boost_own_sessions	3.1	1.9	3.7	3.1
	reminders	True	True	True	-
	remind_strategy	hybrid	hybrid	hybrid	-
	remind_sessions_num	2	6	9	-
	weight_base	5	8	8	-
VSKNN	weight_IRec	3	4	3	-
	k	50	100	100	50
	sample_size	500	500	10000	500
	weighting	log	log	quadratic	quadratic
	weighting_score	linear	quadratic	div	quadratic
VSKNN with extensions	idf_weighting	10	10	10	5
	best extension	VSKNN_EBR	VSKNN_R	VSKNN_EBR	VSKNN_EB
	k	1500	100	1500	50
	sample_size	1000	500	10000	500
	weighting	log	log	quadratic	quadratic
	weighting_score	linear	quadratic	div	quadratic
	idf_weighting	1	10	10	1
	extend_session_length	8	-	2	3
	boost_own_sessions	0.1	-	0.9	2.5
	reminders	True	True	True	-
	remind_strategy	hybrid	hybrid	hybrid	-
	remind_sessions_num	4	8	10	-
	weight_base	8	2	9	-
STAN	weight_IRec	1	1	2	-
	weight_SSim	1	0	3	-
	k	1500	100	500	100
	sample_size	2500	10000	2500	10000
	lambda_spw	0.905	0.4525	0.905	0.00001
STAN with extensions	lambda_snh	100	80	40	80
	lambda_inh	0.4525	0.4525	0.4525	3.62
	best extension	STAN_ER	STAN_R	STAN_EBR	STAN_EBR
	k	200	100	1500	100
	sample_size	1000	10000	5000	2500
	lambda_spw	0.905	0.4525	0.905	0.00001
	lambda_snh	100	80	100	100
	lambda_inh	0.905	0.4525	7.24	7.24
	extend_session_length	2	-	2	17
	boost_own_sessions	-	-	1.9	2.7
	reminders	True	True	True	True
	remind_strategy	hybrid	hybrid	hybrid	hybrid
	remind_sessions_num	9	3	4	3
VSTAN	weight_base	10	10	10	5
	weight_IRec	3	2	1	0
	weight_SSim	2	1	1	6
	k	200	1500	500	1000
	sample_size	5000	10000	1000	5000
	similarity	vec	cosine	cosine	cosine
	lambda_spw	1.81	3.62	3.62	1.81
VSTAN with extensions	lambda_snh	40	20	80	100
	lambda_inh	0.905	0.4525	0.4525	1.81
	lambda_ipw	0.905	0.4525	0.905	0.0001
	lambda_idf	False	10	False	False
	best extension	VSTAN_EBR	VSTAN_R	VSTAN_EBR	VSTAN_EB
	k	2000	1500	500	1000
	sample_size	10000	10000	1000	10000
	similarity	cosine	cosine	cosine	cosine
	lambda_spw	0.905	3.62	0.905	0.4525
	lambda_snh	80	20	80	100
	lambda_inh	1.81	0.4525	0.4525	3.62
	lambda_ipw	3.62	0.4525	3.62	0.4525
	lambda_idf	5	10	1	5
VSTAN with extensions	extend_session_length	5	-	1	7
	boost_own_sessions	0.1	-	3.1	3.7
	reminders	True	True	True	-
	remind_strategy	hybrid	hybrid	hybrid	-
	remind_sessions_num	2	3	5	-
	weight_base	6	9	7	-
	weight_IRec	2	1	1	-
	weight_SSim	0	5	0	-

Table A.14: Optimal hyperparameters for neural methods.

Algorithm	Hyperparameter	RETAIL	XING	COSMETICS	LASTFM
GRU4REC	learning_rate	0.08	0.05	0.03	0.04
	momentum	0.1	0.6	0.3	0.1
	loss	top1-max	top1-max	bpr-max	bpr-max
	final_act	linear	elu-0.5	linear	linear
	dropout_p_hidden	0.7	0.8	0.7	0
	constrained_embedding	True	True	True	False
GRU4REC_R	learning_rate	0.08	0.05	0.03	0.04
	momentum	0.1	0.6	0.3	0.1
	loss	top1-max	top1-max	bpr-max	bpr-max
	final_act	linear	elu-0.5	linear	linear
	dropout_p_hidden	0.7	0.8	0.7	0
	constrained_embedding	True	True	True	False
	reminders	True	True	True	True
	remind_strategy	hybrid	hybrid	hybrid	hybrid
	remind_sessions_num	3	3	2	4
	weight_base	9	9	7	4
	weight_IRec	2	4	3	0
NARM	factors	50	100	100	100
	learning_rate	0.01	0.007	0.007	0.007
NARM_R	factors	50	100	100	100
	learning_rate	0.01	0.007	0.007	0.007
	reminders	True	True	True	True
	remind_strategy	hybrid	hybrid	hybrid	hybrid
	remind_sessions_num	4	7	3	6
	weight_base	10	7	7	3
	weight_IRec	7	3	6	0
HGRU4REC	user_propagation_mode	all	all	init	all
	learning_rate	0.06	0.08	0.04	0.09
	momentum	0.3	0.6	0.5	0.5
	final_act	linear	tanh	linear	linear
	dropout_p_hidden_usr	0.4	0.8	0.5	0.7
	dropout_p_hidden_ses	0.3	0	0.3	0.1
	dropout_p_init	0.4	0.6	0.1	0.3
IIRNN	batch_size	50	100	50	50
	dropout_pkeep	0.4	0.6	0.5	0.6
	learning_rate	0.002	0.002	0.001	0.001
	embedding_size	100	100	100	100
	max_session_representations	15	1	1	20
SHAN	use_last_hidden_state	False	False	True	True
	lambda_uv	0.01	0.01	0.01	0.01
NCSF	lambda_a	1	1	1	10
	max_nb_his_sess	5	0	0	0
	att_alpha	10	10	1	1
NSAR	window_sz	2	2	3	1
	learning_rate	0.01	0.004	0.007	0.003
	hidden_units	100	100	100	100

Table A.15: Running times on the RETAIL dataset.

	Training Time (s)	Prediction Time (ms)
SR	0.42	3.24
VSKNN	0.09	4.42
STAN	0.08	4.29
VSTAN	0.09	4.55
SR_BR	0.78	12.99
VSKNN_EBR	0.24	20.85
STAN_ER	0.19	24.42
VSTAN_EBR	0.24	14.99
GRU4REC	12.95	4.00
NARM	102.73	5.50
GRU4REC_R	10.46	13.61
NARM_R	93.90	15.07
HGRU4REC	23.92	4.07
IIRNN	1307.41	87.34
NCSF	82.54	25.81
NSAR	475.46	21.51
SHAN	1661.60	12.32

Table A.16: Running times on the COSMETICS dataset.

	Training Time (s)	Prediction Time (ms)
SR	0.62	2.64
VSKNN	0.14	4.45
STAN	0.13	6.06
VSTAN	0.14	6.81
SR_BR	1.55	8.14
VSKNN_EBR	0.33	14.92
STAN_EBR	0.32	18.37
VSTAN_EBR	0.33	12.42
GRU4REC	13.56	3.86
NARM	159.79	5.62
GRU4REC_R	11.74	9.32
NARM_R	135.13	21.91
HGRU4REC	36.74	3.85
IIRNN	1034.02	59.08
NCSF	40.59	10.66
NSAR	387.43	11.26
SHAN	2344.50	11.58