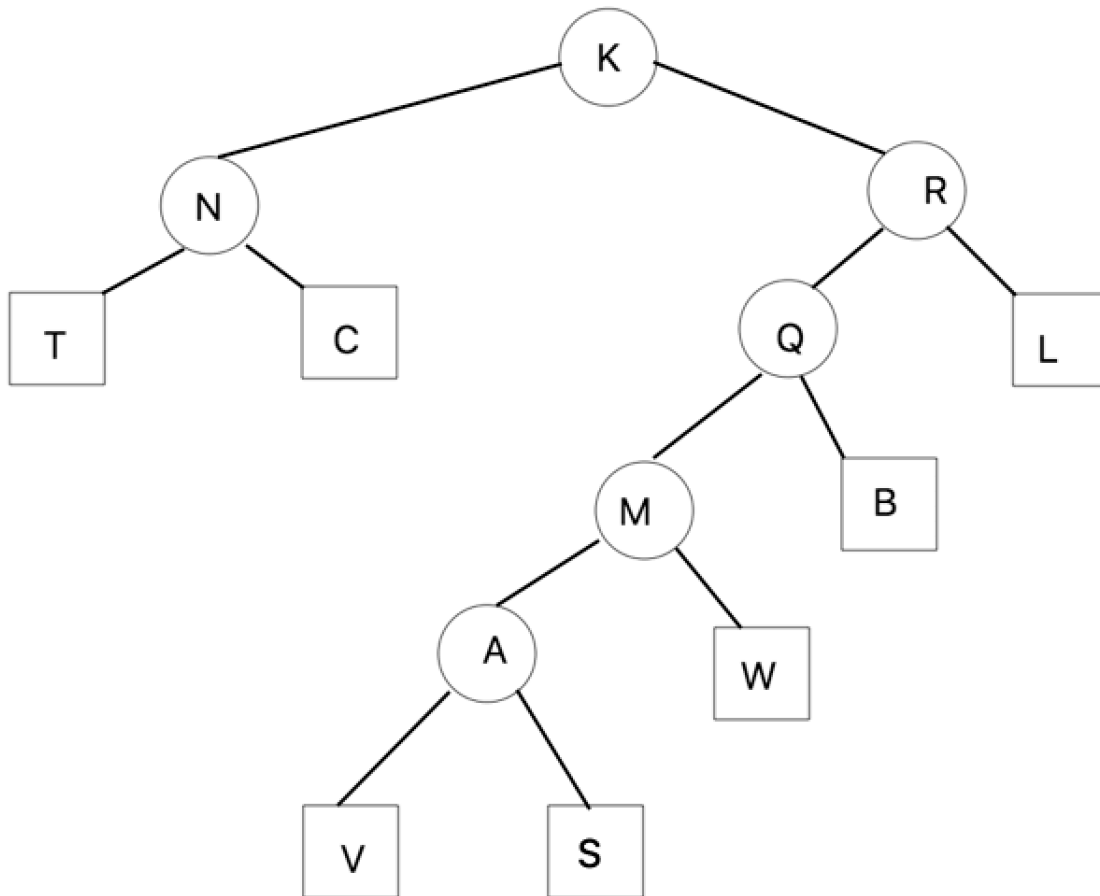


Question 1

A)



B)

To place all elements, I followed the rule: Left $2n + 1$ and Right $2n + 2$.

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48
K	N	R	T	C	Q	L					M	B											A	W																						V	S	

The root, K, is at index 0. $N=2 \times 0 + 1=1$. $R=2 \times 0 + 2=2$. T is left child of $N=2 \times 1 + 1=3$ and C is right child of $N=2 \times 1 + 2=4$. Q is left child of $R=2 \times 2 + 1=5$ and L is right child of $R=2 \times 2 + 2=6$. M is left child of $Q=2 \times 5 + 1=11$ and B is right child of $Q=2 \times 5 + 2=12$. A is left child of $M=2 \times 11 + 1=23$ and W is right child of $M=2 \times 11 + 2=24$. V is left child of $A=2 \times 23 + 1=47$ and S is right child of $A=2 \times 23 + 2=48$.

Question 2

A)

Step 1: find the amount of value to put at the bottom of the tree. formula: $(n+1)/2$

Step 2: place the first 8 elements at the bottom

Step 3: place the next 4 elements on top

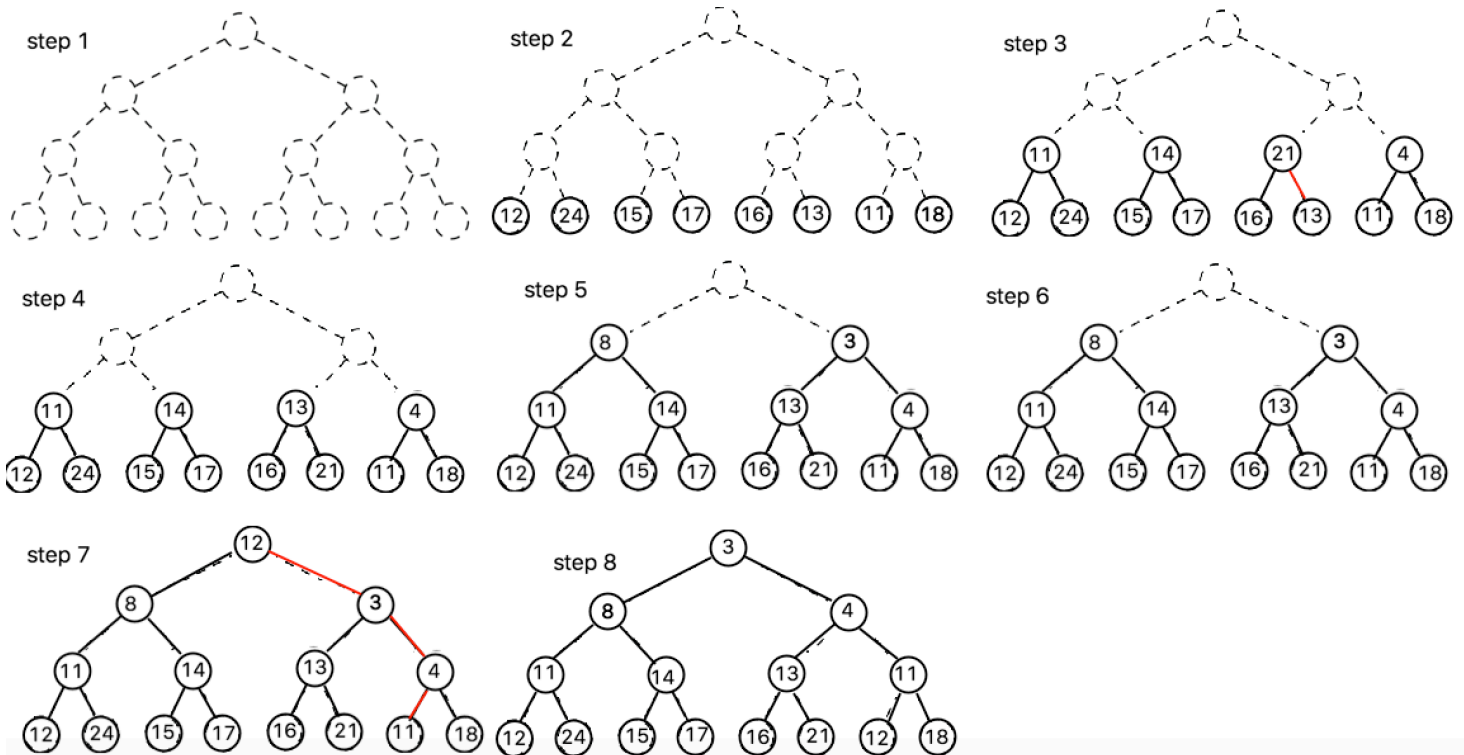
Step 4: make sure the heap order is respected and do the modifications

Step 5: place the next 2 elements

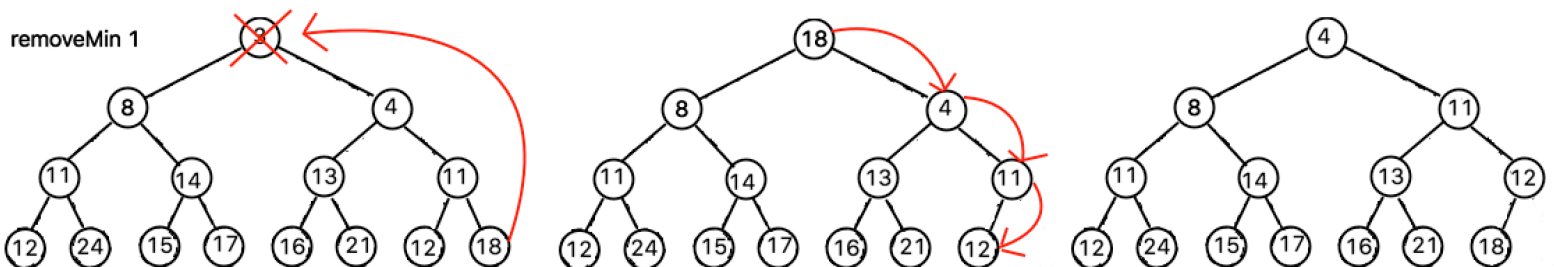
Step 6: make sure the heap order is respected and do the modifications

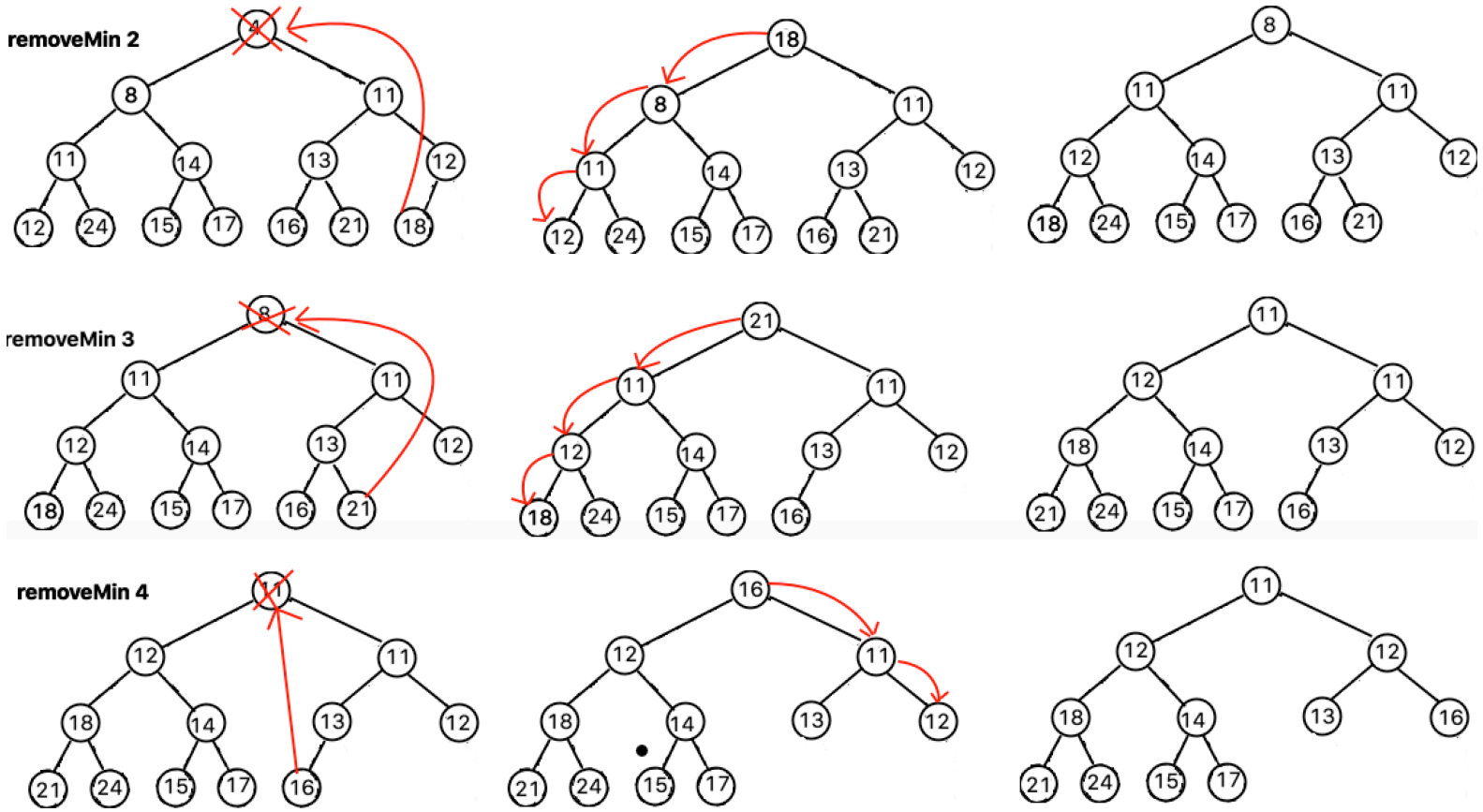
Step 7: place the last element

Step 8: make sure the heap order is respected and do the modifications

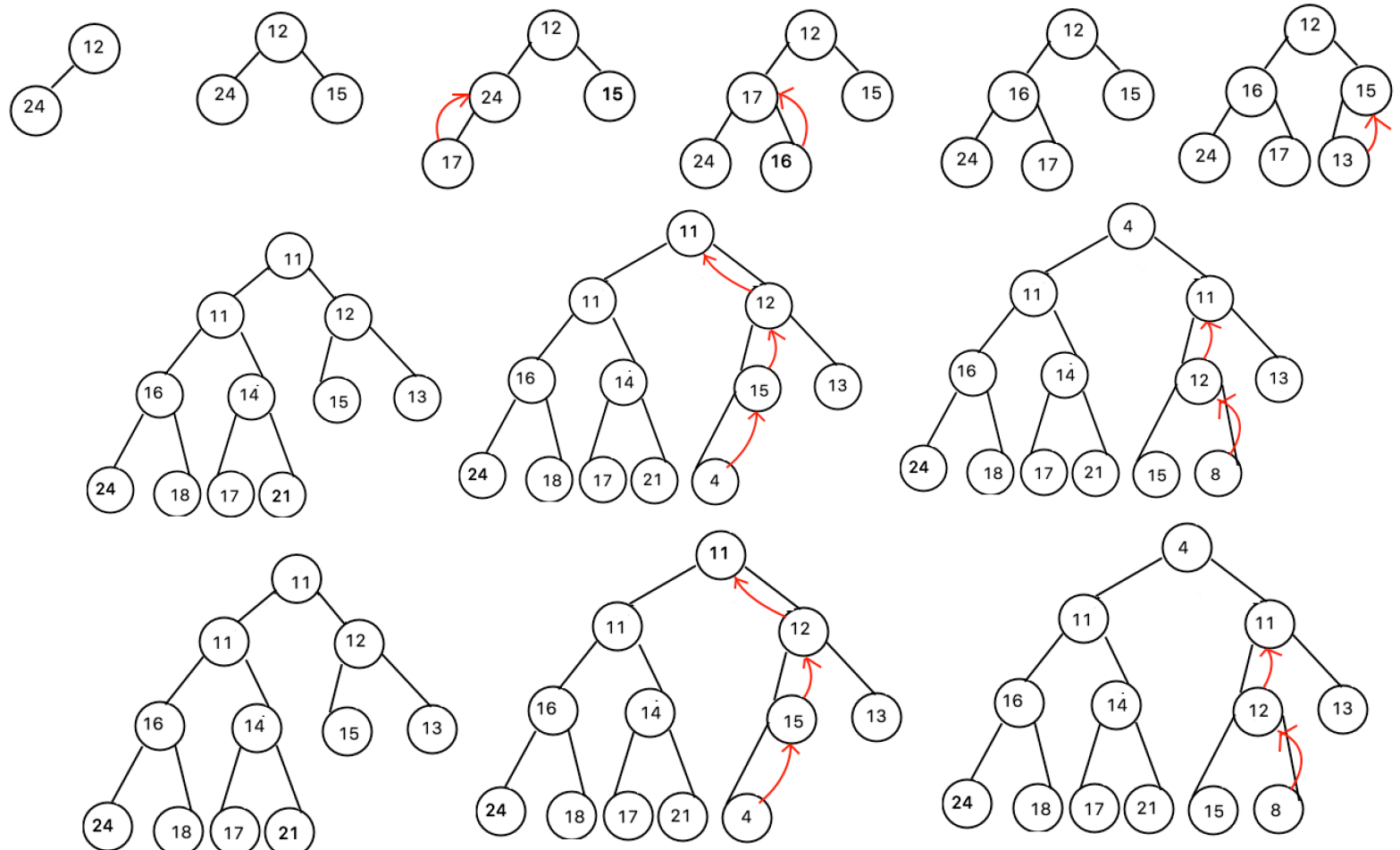


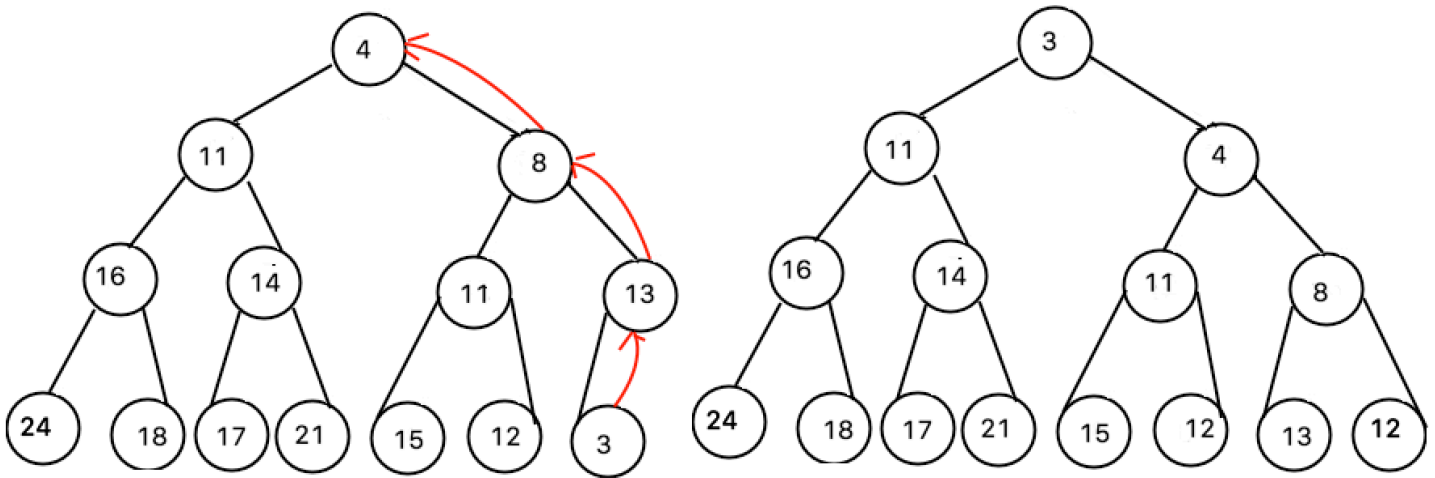
Now performing the **removeMin**:





B)





Question 3

depthCalculator(Tree T)

Input: Tree T which has n number of nodes

Output: The depth of all nodes of tree T

Node temp <- T.root()

temp.depth() == 0

helperDepth(T, temp)

helperDepth(Tree T, Node temp)

Input: Tree T and Node temp from method depth Calculator

for (i <- all children of temp)

i.setDepth <- i.getParent.getDepth() + 1

helperDepth(T, i)

A) The time complexity of the algorithm is $O(n)$ because we need to visit each node once.

B) I believe the best time complexity for this algorithm is $O(n)$ because in the best case, the algorithm will need to access once every node to get their depth and do the sum of all nodes' depths.