Statistical Analysis of Networks

Statistics 218
Professor: Mark S. Handcock

Homework 1

Due date on the Bruinlearn Assignments page

You will need the networkdata and sna packages. To install the packages from inside R:

```
install.packages("network")
install.packages("sna")
install.packages("networkdata",repos="http://faculty.stat.ucla.edu/handcock")
```

1) Visualization and Sociality: Here we consider the three network data sets in the networkdata package

```
library(networkdata)
data(butland_ppi)
data(addhealth9)
data(tribes)
```

Useful other packages are:

```
library(sna)
library(network)
```

You can check the nature of the networks, via, help(tribes), etc. These networks need to be processed a bit for the analysis to match those reported in class. For the Add Health 9 network, consider only the (known) boys (via addhealth9\$X[,"female"]==0). Next consider the undirected versions of the networks (For the Add Health 9 network we choose to say there is a tie if either boy nominates the other as a friend. For the tribes take the positive relations. Next consider only the largest component (see, e.g., component.dist in sna).

- a) Create network objects from the networks, using either network or igraph.
- **b)** Plot the networks so as to visualize their structure.
- c) For each network, use the degree() function in the sna package to find the degree sequence. Note that for undirected networks, this function returns twice the degrees. You may also find the table command helpful. *Hint:* The gmode option in degree is important.
- d) For each network, summarize the degree sequence using node-level graphical and numerical summaries (e.g., barplot).
- 2) Visualizing Connectivity: Here we consider the Florentine marriage data from the network package.

library(networkdata) data(florentine)

- a) Plot the network, with the names labeled.
- b) Which families have the highest and lowest degrees? What are their degrees?
- c) Use the degree() function in the sna package to find the degree distribution. Note that for undirected networks, this function returns twice the degrees. You may also find the table command helpful.
 - d) Which family is excluded from the large component?
- 3) Degree distributions: Degree distributions summarize the densities of ties of the population of nodes. In this question we explore the interactions between proteins of the yeast S. cerevisiae. The nodes are types of proteins in the yeast and a directed tie is said to exist if a protein binds to the target protein in a "wet lab" experiment set up to test just this. Not all protein combinations are tested. Here we will consider a series of "mapping" experiments conducted in 2008 that covered approximately 20% of all yeast binary interactions (Yu et. al Science (2008))
- a) Go to the home page of the "Yeast Interactome Project": http://interactome.dfci.harvard.edu/S_cerevisiae/
 From there download the interactions from CCSB-YI11. These comprise 1809 interactions among 1278 proteins. Construct a network object from this edge-list.
- b) Construct the out-degree sequence for the network. Construct the in-degree sequence. Are the in- and out-degrees correlated? Use the sum of the in-degree and out-degree as an overall measure of the proteins activity (which we will refer to as its degree).