

Mat 486  
Homework5  
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#####

Four documents:

d1: Shipment of gold damaged in a fire.  
d2: Delivery of silver arrived in a silver truck.  
d3: Shipment of gold arrived in a truck.  
d4: Shipment of gold arrived in a silver truck

#####

1.

Repeat the rank-2 analysis for the query  $q = \text{"gold silver truck"}$  and report your findings. A cosine similarity test threshold of 0.5 is considered relevant (this means that the angle between the vectors is  $< 60$  degrees), while a 0.8 threshold is very good.

```
> restart( ) :
> with(LinearAlgebra) : with(plots) : interface(rtablesize = 15) :
> A := Matrix(11, 4, [ <1, 0, 1, 0, 1, 1, 1, 1, 1, 0, 0>, <1, 1, 0, 1, 0, 0, 1, 1, 0, 2, 1>, <1, 1, 0, 0, 0, 1,
1, 1, 1, 0, 1>, <1, 1, 0, 0, 0, 1, 1, 1, 1, 1, 1> ] );
```

$$A := \begin{bmatrix} 1 & 1 & 1 & 1 \\ 0 & 1 & 1 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 1 & 0 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 0 & 1 & 1 \\ 0 & 2 & 0 & 1 \\ 0 & 1 & 1 & 1 \end{bmatrix}$$

(1)

```
# New query vector
```

```
> q_1 := <0, 0, 0, 0, 0, 1, 0, 0, 0, 1, 1>
```

(2)

$$q_1 := \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 1 \\ 0 \\ 0 \\ 0 \\ 1 \\ 1 \end{bmatrix} \quad (2)$$

```
> U, S, Vt := SingularValues(A, output = ['U','S','Vt']) :
```

```
#Create the rank 2 approximation
```

```
> Sm2 := DiagonalMatrix(S1..2, 2, 2)
```

$$Sm2 := \begin{bmatrix} 4.93115367652474 & 0. \\ 0. & 2.36166782730918 \end{bmatrix} \quad (3)$$

```
# The rows of Um2 provide the coordinates of the 11 words
```

```
> Um2 := SubMatrix(U, 1..11, 1..2)
```

$$Um2 := \begin{bmatrix} -0.402466375103054 & -0.0770159571941109 \\ -0.321939474302626 & 0.199720711331478 \\ -0.0805269008004283 & -0.276736668525589 \\ -0.107635642500810 & 0.302469353467979 \\ -0.0805269008004284 & -0.276736668525589 \\ -0.294830732602244 & -0.379485310662090 \\ -0.402466375103054 & -0.0770159571941109 \\ -0.402466375103054 & -0.0770159571941109 \\ -0.294830732602244 & -0.379485310662090 \\ -0.329192168331150 & 0.608076165234006 \\ -0.321939474302626 & 0.199720711331478 \end{bmatrix} \quad (4)$$

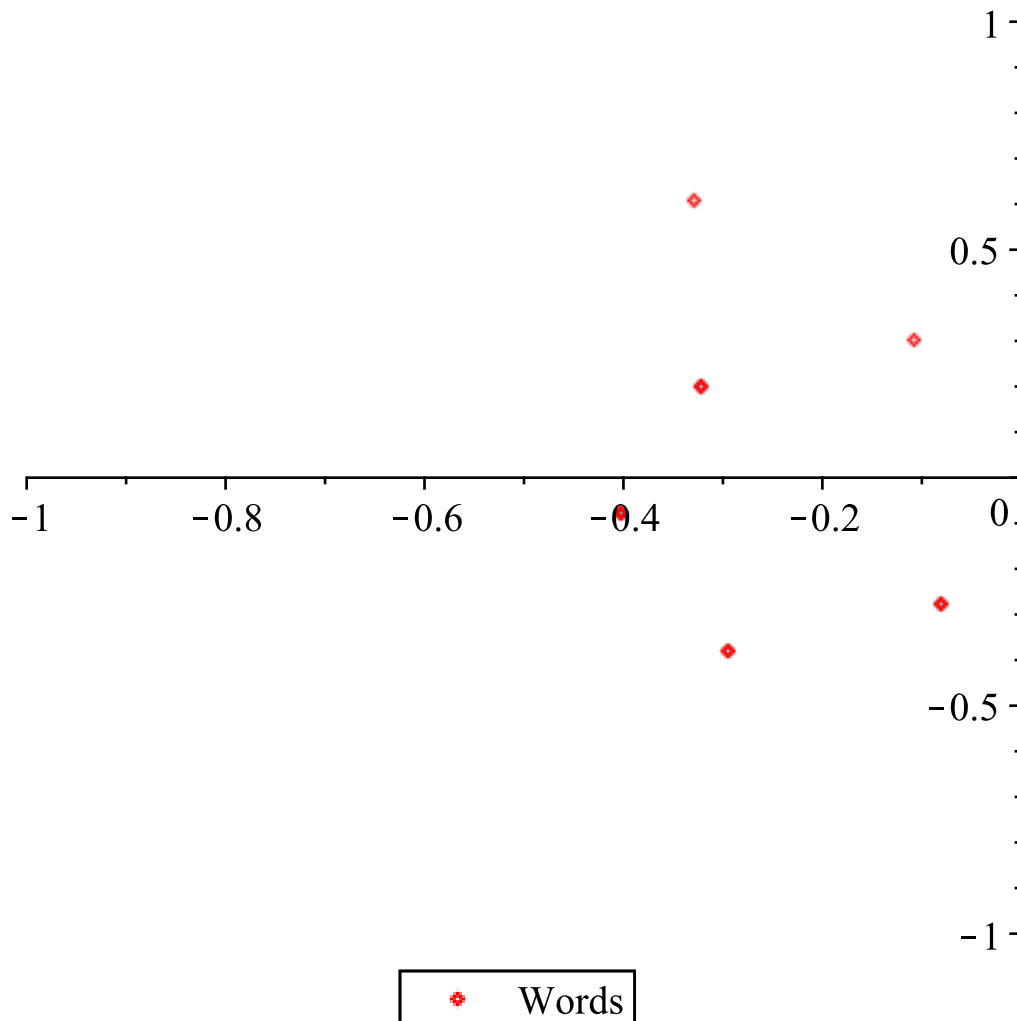
```
# The columns of Vtm2 provide the coordinates of the 4 documents
```

```
> Vtm2 := SubMatrix(Vt, 1..2, 1..4)
```

$$Vtm2 := \begin{bmatrix} -0.397090522941175, & -0.530767894242970, & -0.495003745419503, \\ -0.561761382663360, \\ -0.653560086693608, & 0.714332140832334, & -0.250067796755502, \\ 0.00740963432202280 \end{bmatrix} \quad (5)$$

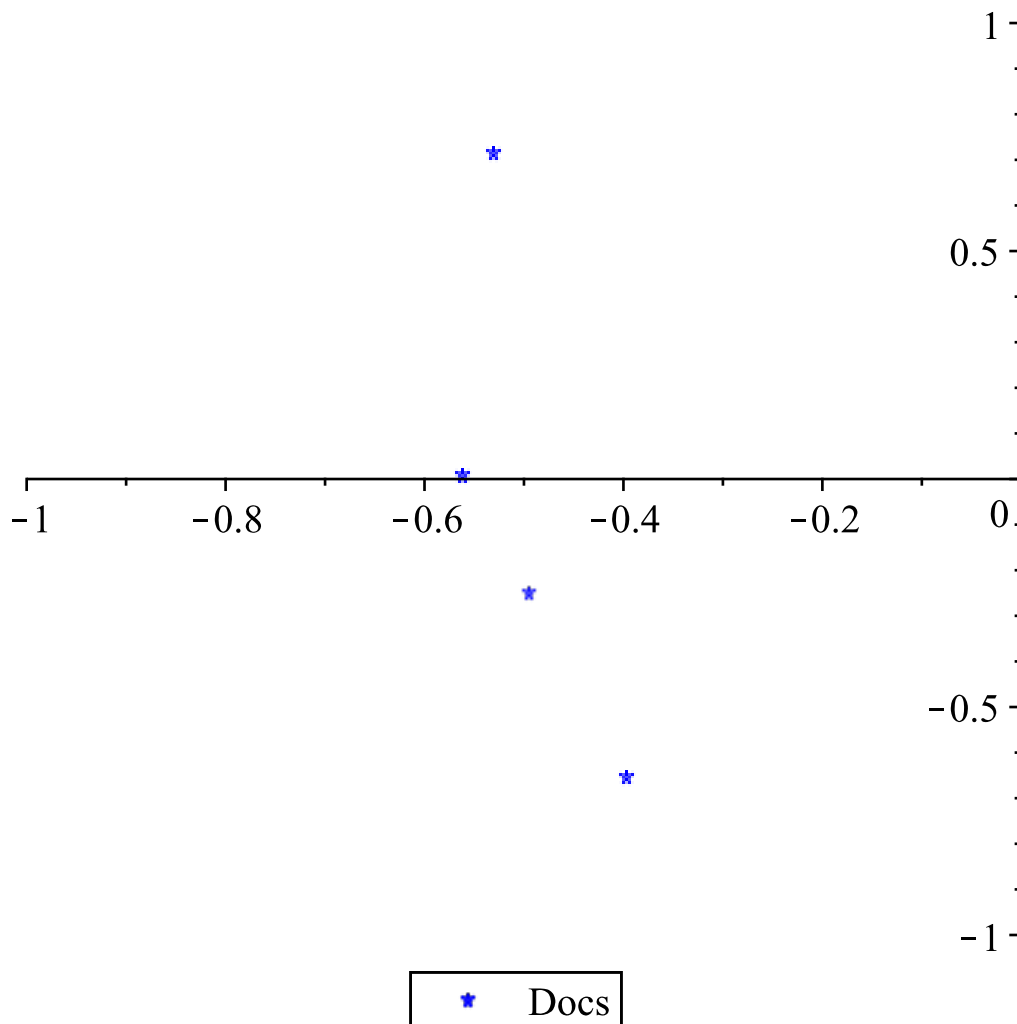
# Plot the 11 words, some do overlap

```
> plot1_2d := pointplot(Um2, legend="Words", color=red, axes=normal, view=[-1..0,-1..1]) : display(plot1_2d)
```



# Plot the 4 documents

```
> plot2_2d := pointplot(Vtm2, legend="Docs", color=blue, symbol=asterisk, axes=normal, view=[-1..0,-1..1]) : display(plot2_2d)
```



#We compute the coordinates of the new query

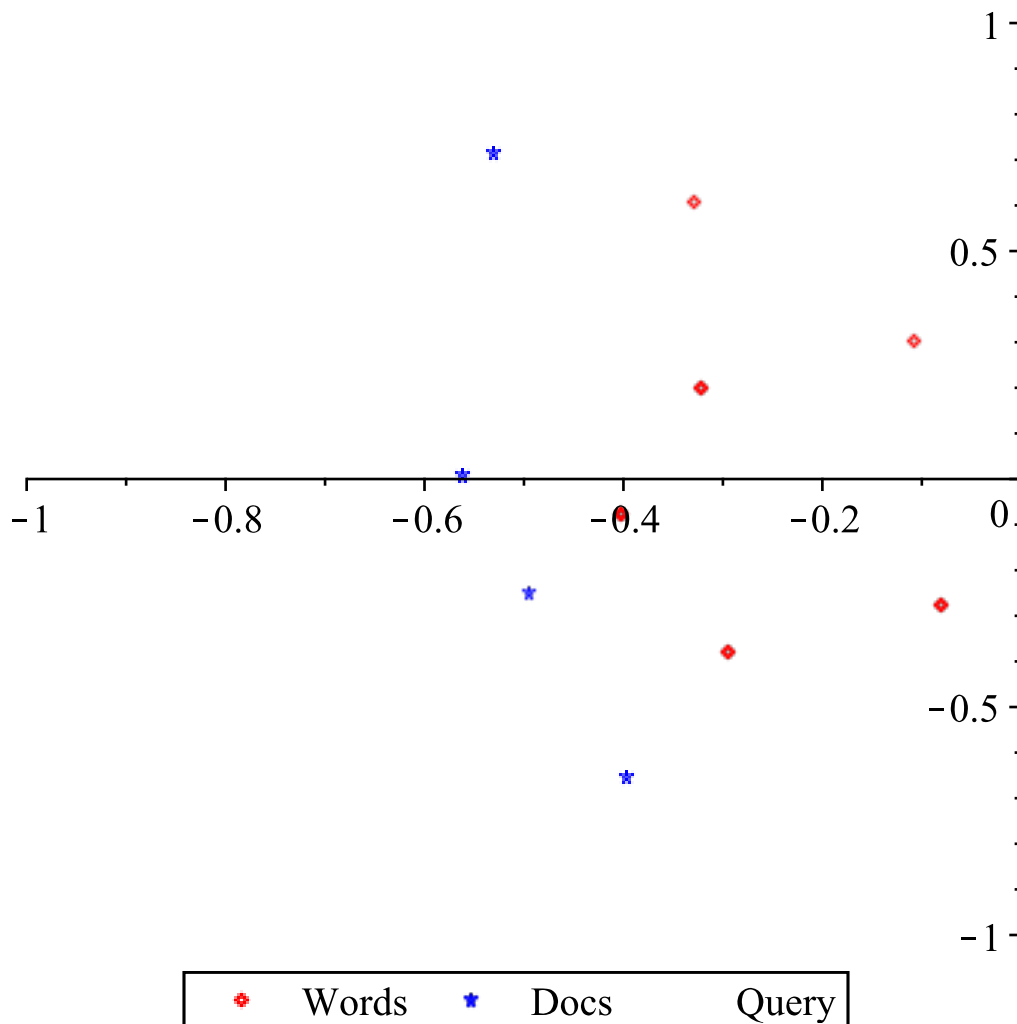
```
> qcoord_2 := Transpose(q_1).(Um2.MatrixInverse(Sm2))
```

```
qcoord_2 := [ -0.191833886609409  0.181359783518498 ]
```

(6)

# Combine the plots

```
> plot3_2d := pointplot(qcoord_2, symbol=box, legend="Query", axes=normal) :
display(plot1_2d, plot2_2d, plot3_2d)
```



# We run some similarity tests between the four documents and the new query.

$$\begin{aligned} > \text{doc1} := \text{Column}(\text{Vtm2}, 1) : \text{test1} := \frac{qcoord\_2 \cdot \text{doc1}}{\text{Norm}(qcoord\_2, 2) \cdot \text{Norm}(\text{doc1}, 2)} \\ & \text{test1} := -0.2097941873 \end{aligned} \quad (7)$$

$$\begin{aligned} > \text{doc2} := \text{Column}(\text{Vtm2}, 2) : \text{test2} := \frac{qcoord\_2 \cdot \text{doc2}}{\text{Norm}(qcoord\_2, 2) \cdot \text{Norm}(\text{doc2}, 2)} \\ & \text{test2} := 0.9848249865 \end{aligned} \quad (8)$$

$$\begin{aligned} > \text{doc3} := \text{Column}(\text{Vtm2}, 3) : \text{test3} := \frac{qcoord\_2 \cdot \text{doc3}}{\text{Norm}(qcoord\_2, 2) \cdot \text{Norm}(\text{doc3}, 2)} \\ & \text{test3} := 0.3388280712 \end{aligned} \quad (9)$$

$$\begin{aligned} > \text{doc4} := \text{Column}(\text{Vtm2}, 4) : \text{test4} := \frac{qcoord\_2 \cdot \text{doc4}}{\text{Norm}(qcoord\_2, 2) \cdot \text{Norm}(\text{doc4}, 2)} \\ & \text{test4} := 0.7356638059 \end{aligned} \quad (10)$$

**Answer: for Rank 2 analysis cosine similarity test  
for query q="gold silver truck" shows :  
Very good for  
doc2 =0.9848**

relevant for doc4=0.7357

#####

2

Perform a rank-3 SVD analysis for the same query q="gold silver truck" and report your findings

\*\*\*\*\*

> Sm3 := DiagonalMatrix(S<sub>1..3</sub>, 3, 3);

$$Sm3 := \begin{bmatrix} 4.93115367652474 & 0. & 0. \\ 0. & 2.36166782730918 & 0. \\ 0. & 0. & 1.37385875035970 \end{bmatrix} \quad (11)$$

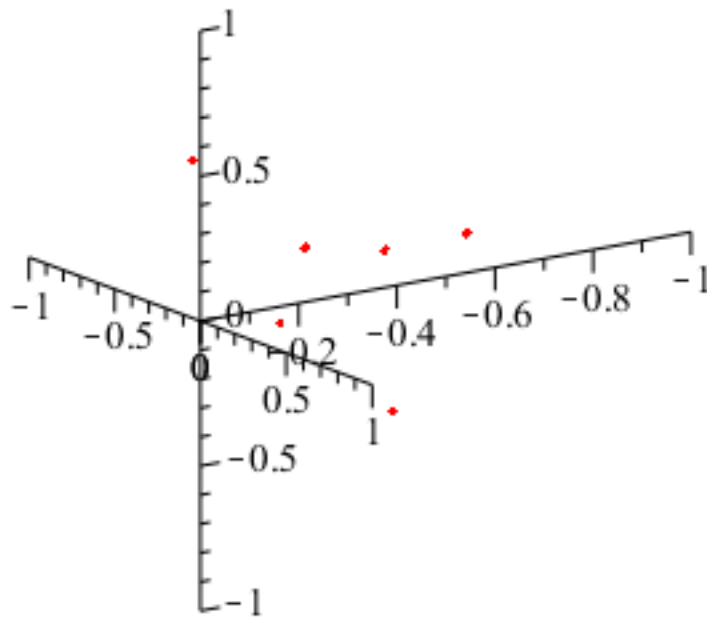
> Um3 := SubMatrix(U, 1..11, 1..3);

$$Um3 := \begin{bmatrix} -0.402466375103054 & -0.0770159571941109 & 0.103979350121338 \\ -0.321939474302626 & 0.199720711331478 & -0.364947747899966 \\ -0.0805269008004283 & -0.276736668525589 & 0.468927098021304 \\ -0.107635642500810 & 0.302469353467979 & 0.286328369561831 \\ -0.0805269008004284 & -0.276736668525589 & 0.468927098021304 \\ -0.294830732602244 & -0.379485310662090 & -0.182349019440493 \\ -0.402466375103054 & -0.0770159571941109 & 0.103979350121338 \\ -0.402466375103054 & -0.0770159571941109 & 0.103979350121338 \\ -0.294830732602244 & -0.379485310662090 & -0.182349019440493 \\ -0.329192168331150 & 0.608076165234006 & 0.336035199548203 \\ -0.321939474302626 & 0.199720711331478 & -0.364947747899966 \end{bmatrix} \quad (12)$$

> Vtm3 := SubMatrix(Vt, 1..3, 1..4)

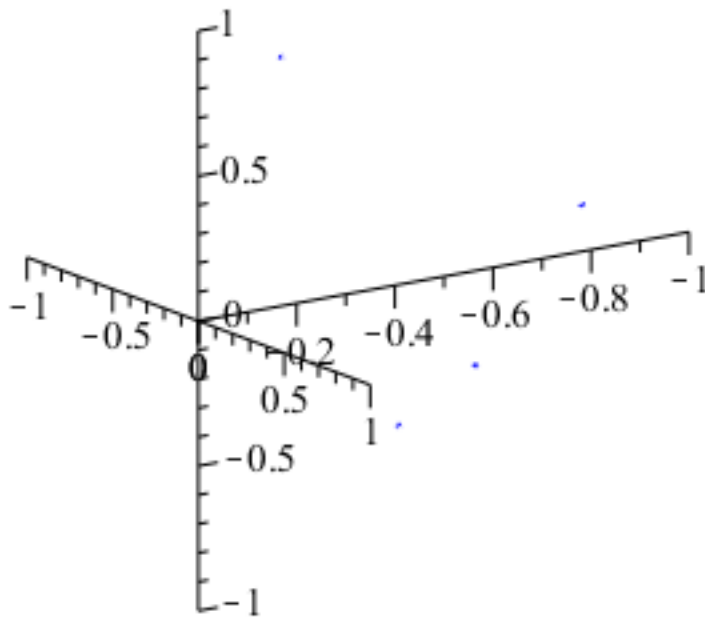
$$Vtm3 := \begin{bmatrix} -0.397090522941175, & -0.530767894242970, & -0.495003745419503, \\ -0.561761382663360, \\ -0.653560086693608, & 0.714332140832334, & -0.250067796755502, \\ 0.00740963432202280, \\ 0.644239596897351, & 0.393374735998748, & -0.569676820205855, \\ -0.325084572669329 \end{bmatrix} \quad (13)$$

> plot1\_3d := pointplot3d(Um3, color = red, axes = normal, view = [-1..0, -1..1, -1..1]) :  
display(plot1\_3d);




---

> `plot2_3d := pointplot3d(Vtm3, color = blue, symbol = asterisk, axes = normal, view = [-1 .. 0, -1 .. 1, -1 .. 1]) : display(plot2_3d);`

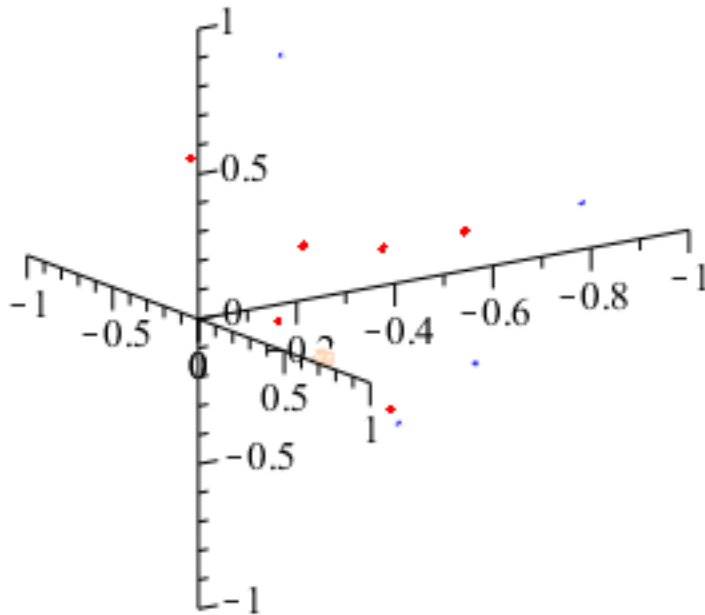


```

> qcoord_3 := Transpose(q_1).(Um3 • MatrixInverse(Sm3));
qcoord_3 := [ -0.191833886609409  0.181359783518498  -0.153772407634296 ]
(14)
> plot3_3d := pointplot3d(qcoord_3, symbol=box, axes=normal) : display(plot1_3d, plot2_3d,
plot3_3d);

```





$$\begin{aligned} &> \text{doc1} := \text{Column}(\text{Vtm3}, 1) : \text{test1} := \frac{qcoord\_3 \cdot \text{doc1}}{\text{Norm}(qcoord\_3, 2) \cdot \text{Norm}(\text{doc1}, 2)} \\ &\text{test1} := -0.4629272750 \end{aligned} \quad (15)$$

$$\begin{aligned} &> \text{doc2} := \text{Column}(\text{Vtm3}, 2) : \text{test2} := \frac{qcoord\_3 \cdot \text{doc2}}{\text{Norm}(qcoord\_3, 2) \cdot \text{Norm}(\text{doc2}, 2)} \\ &\text{test2} := 0.5748450260 \end{aligned} \quad (16)$$

$$\begin{aligned} &> \text{doc3} := \text{Column}(\text{Vtm3}, 3) : \text{test3} := \frac{qcoord\_3 \cdot \text{doc3}}{\text{Norm}(qcoord\_3, 2) \cdot \text{Norm}(\text{doc3}, 2)} \\ &\text{test3} := 0.5648804643 \end{aligned} \quad (17)$$

$$\begin{aligned} &> \text{doc4} := \text{Column}(\text{Vtm3}, 4) : \text{test4} := \frac{qcoord\_3 \cdot \text{doc4}}{\text{Norm}(qcoord\_3, 2) \cdot \text{Norm}(\text{doc4}, 2)} \\ &\text{test4} := 0.8022956779 \end{aligned} \quad (18)$$

**Answer: for Rank 3 analysis cosine similarity test**

**for query q="gold silver truck" shows :**

**Very good for**

**doc4=0.8022**

**relevant:**

**doc2=0.5748**

**doc3=0.5649**

We can see that rank 3 has better approximation

#####

3

Repeat steps 1 and 2 for a new query q="shipment truck" and report your findings.

\*\*\*\*\*

\*\*\*\*\*

Analysis for rank 2

\*\*\*\*\*

# New query vector

>  $q\_2 := \langle 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 1 \rangle$

$$q\_2 := \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 1 \\ 0 \\ 1 \end{bmatrix}$$

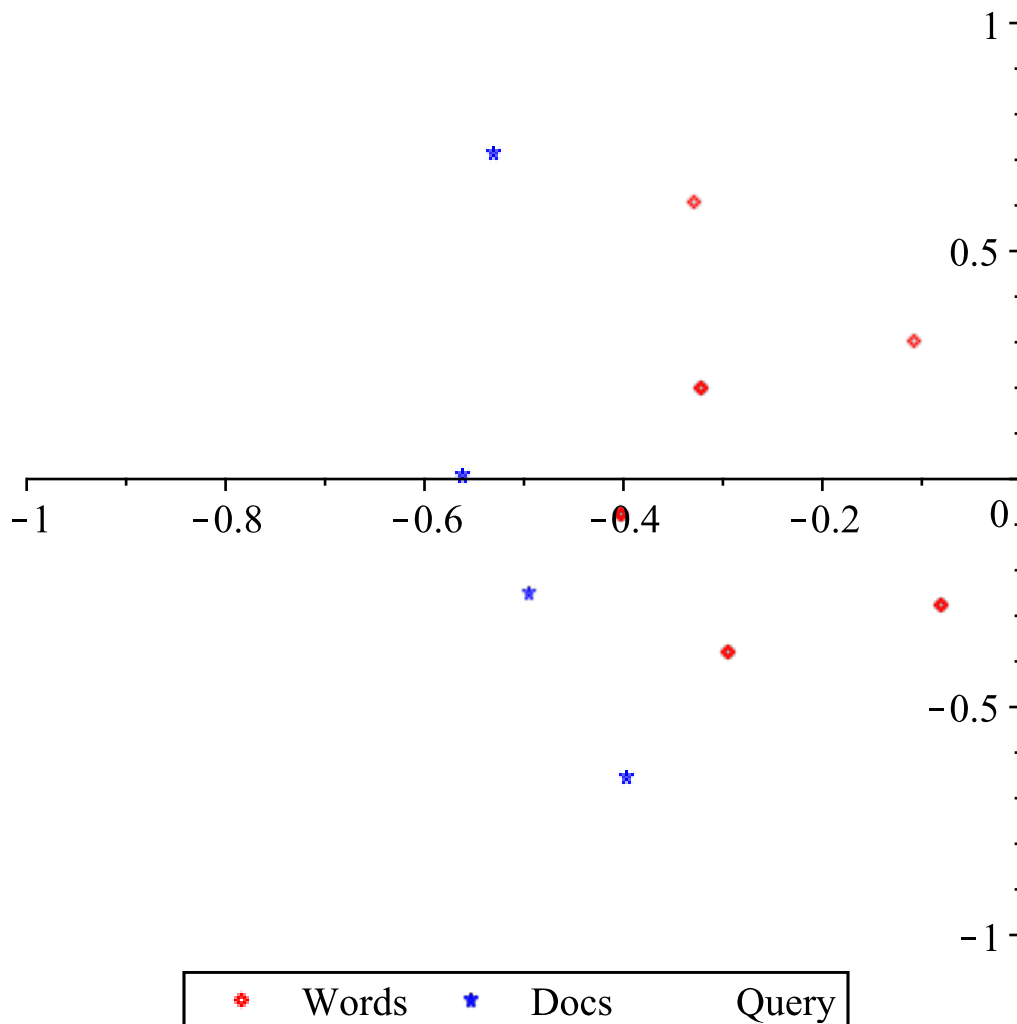
(19)

>  $qcoord\_2 := \text{Transpose}(q\_2) \cdot (Um2.MatrixInverse(Sm2))$

$$qcoord\_2 := \begin{bmatrix} -0.125076249365553 & -0.0761176475590267 \end{bmatrix}$$

(20)

>  $plot3\_2d := \text{pointplot}(qcoord\_2, \text{symbol} = \text{box}, \text{legend} = \text{"Query"}, \text{axes} = \text{normal}) :$   
 $\text{display}(plot1\_2d, plot2\_2d, plot3\_2d)$



>

$$\begin{aligned} > \text{doc1} := \text{Column}(\text{Vtm2}, 1) : \text{test1} := \frac{qcoord\_2 \cdot \text{doc1}}{\text{Norm}(qcoord\_2, 2) \cdot \text{Norm}(\text{doc1}, 2)} \\ & \text{test1} := 0.8878595363 \end{aligned} \quad (21)$$

$$\begin{aligned} > \text{doc2} := \text{Column}(\text{Vtm2}, 2) : \text{test2} := \frac{qcoord\_2 \cdot \text{doc2}}{\text{Norm}(qcoord\_2, 2) \cdot \text{Norm}(\text{doc2}, 2)} \\ & \text{test2} := 0.09219504386 \end{aligned} \quad (22)$$

$$\begin{aligned} > \text{doc3} := \text{Column}(\text{Vtm2}, 3) : \text{test3} := \frac{qcoord\_2 \cdot \text{doc3}}{\text{Norm}(qcoord\_2, 2) \cdot \text{Norm}(\text{doc3}, 2)} \\ & \text{test3} := 0.9968881269 \end{aligned} \quad (23)$$

$$\begin{aligned} > \text{doc4} := \text{Column}(\text{Vtm2}, 4) : \text{test4} := \frac{qcoord\_2 \cdot \text{doc4}}{\text{Norm}(qcoord\_2, 2) \cdot \text{Norm}(\text{doc4}, 2)} \\ & \text{test4} := 0.8473154702 \end{aligned} \quad (24)$$

\*\*\*\*\*

**Answer: for Rank 2 analysis cosine similarity test**  
**for query q="shipment truck" shows :**  
**Very good for**  
**doc3=0.9969**

doc1=0.8879  
doc4= 0.8473

\*\*\*\*\*

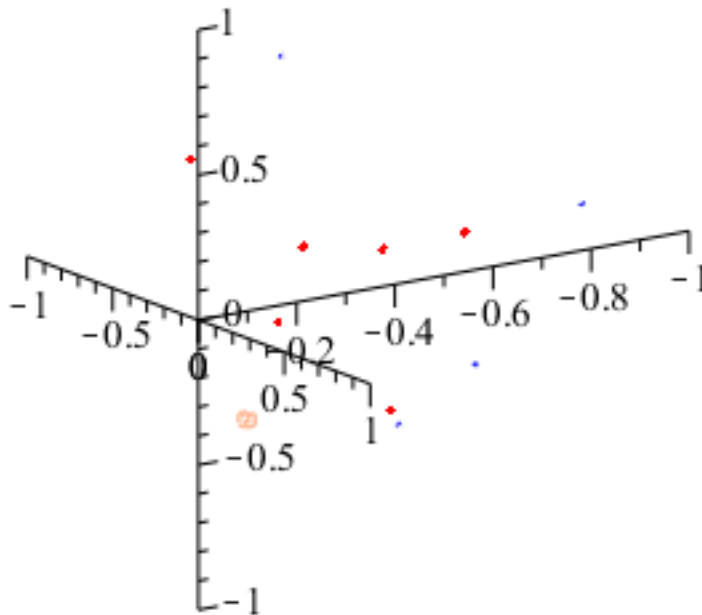
### Analysis for rank 3

\*\*\*\*\*

```
> qcoord_3 := Transpose(q_2).(Um3 • MatrixInverse(Sm3))
qcoord_3 := [ -0.125076249365553  -0.0761176475590267  -0.398364655170822 ] (25)
```

# Combine the plots

```
> plot3_3d := pointplot3d(qcoord_3, symbol=box, axes=normal) : display(plot1_3d, plot2_3d,
plot3_3d)
```



```
> doc1 := Column(Vtm3, 1) : test1 :=  $\frac{qcoord\_3 \cdot doc1}{Norm(qcoord\_3, 2) \cdot Norm(doc1, 2)}$ 
test1 := -0.3704790850 (26)
```

```
> doc2 := Column(Vtm3, 2) : test2 :=  $\frac{qcoord\_3 \cdot doc2}{Norm(qcoord\_3, 2) \cdot Norm(doc2, 2)}$ 
test2 := -0.3503806681 (27)
```

$$\begin{aligned} > \text{doc3} := \text{Column}(\text{Vtm3}, 3) : \text{test3} := \frac{qcoord\_3 \cdot \text{doc3}}{\text{Norm}(qcoord\_3, 2) \cdot \text{Norm}(\text{doc3}, 2)} \\ & \text{test3} := 0.9124401690 \end{aligned} \quad (28)$$

$$\begin{aligned} > \text{doc4} := \text{Column}(\text{Vtm3}, 4) : \text{test4} := \frac{qcoord\_3 \cdot \text{doc4}}{\text{Norm}(qcoord\_3, 2) \cdot \text{Norm}(\text{doc4}, 2)} \\ & \text{test4} := 0.7230941199 \end{aligned} \quad (29)$$

Answer: for Rank 2 analysis cosine similarity test  
 for query q="shipment truck"  
 Very good for documents are  
 doc3=0.9124  
 doc4=0.7231

Rank 3 has better approximation

#####

## II. Consider the following term-document example :

The  $t = 6$  terms:

T1: bak(e,ing)  
 T2: recipes  
 T3: bread  
 T4: cake  
 T5: pastr(y,ies)  
 T6: pie

The  $d = 5$  document titles:

D1: How to Bake Bread Without Recipes  
 D2: The Classic Art of Viennese Pastry  
 D3: Numerical Recipes: The Art of Scientific Computing  
 D4: Breads, Pastries, Pies and Cakes: Quantity Baking Recipes  
 D5: Pastry: A Book of Best French Recipes

and the query: q=**baking bread**

\*\*\*\*\*

>  $A := \text{Matrix}(6, 5, [ \langle 1, 1, 1, 0, 0, 0 \rangle, \langle 0, 0, 0, 0, 1, 0 \rangle, \langle 0, 1, 0, 0, 0, 0 \rangle, \langle 1, 1, 1, 1, 1, 1 \rangle, \langle 0, 1, 0, 0, 1, 0 \rangle ] )$ ;

$$A := \begin{bmatrix} 1 & 0 & 0 & 1 & 0 \\ 1 & 0 & 1 & 1 & 1 \\ 1 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 & 0 \end{bmatrix} \quad (30)$$

>  $q := \langle 1, 0, 1, 0, 0, 0 \rangle$

$$q := \begin{bmatrix} 1 \\ 0 \\ 1 \\ 0 \\ 0 \\ 0 \end{bmatrix} \quad (31)$$

>  $U, S, Vt := \text{SingularValues}(A, \text{output} = ['U', 'S', 'Vt'])$

$U, S, Vt := [[ -0.415139716033301, 0.408248290463863, 0.162729146205422,$  (32)

$-0.366758196200682, -0.707106781186548, -3.88923546639465 \cdot 10^{-15},$

$[ -0.590723295429479, 4.44089209850063 \cdot 10^{-16}, -0.729386490672964,$

$0.345023673768503, -2.22044604925031 \cdot 10^{-16}, 3.42334571175266 \cdot 10^{-18},$

$[ -0.415139716033301, 0.408248290463863, 0.162729146205422,$

$-0.366758196200682, 0.707106781186548, 3.88581212068290 \cdot 10^{-15},$

$[ -0.258865830839363, 0., 0.440768092169533, 0.488581590472949,$

$3.63598040564739 \cdot 10^{-15}, -0.707106781186548 ],$

$[ -0.415139716033301, -0.816496580927726, 0.162729146205422,$

$-0.366758196200682, 3.60822483003176 \cdot 10^{-16}, 4.37348322807471 \cdot 10^{-18},$

$[ -0.258865830839363, 5.55111512312578 \cdot 10^{-17}, 0.440768092169533,$

$0.488581590472949, -4.13558076672871 \cdot 10^{-15}, 0.707106781186548 ]],$

$\begin{bmatrix} 3.01546471512117 \\ 1.41421356237309 \\ 1.20531141460241 \\ 0.673941351816550 \\ 1.76346875900021 \cdot 10^{-17} \\ 0. \end{bmatrix}, [[ -0.471238386697216, -0.137670228390193,$

$-0.195897929916829, -0.780600778846626, -0.333568158307022 ],$

$[ 0.577350269189626, -0.577350269189626, 9.71445146547012 \cdot 10^{-17},$

$-1.11022302462516 \cdot 10^{-16}, -0.577350269189626 ],$

```
[ -0.335123515274566, 0.135010043241896, -0.605143601758358,
0.531262812684466, -0.470133558516463 ],
[ -0.576448852093306, -0.544198979944052, 0.511949107794798,
0.329275337556019, -0.0322498721492537 ],
[ 0., 0.577350269189626, 0.577350269189626, -1.11022302462516 10-16,
-0.577350269189625 ]]
```

```
> Sm2 := DiagonalMatrix(S1..2, 2, 2)
```

$$Sm2 := \begin{bmatrix} 3.01546471512117 & 0. \\ 0. & 1.41421356237309 \end{bmatrix}$$

(33)

```
# The rows of Um2 provide the coordinates of the 6 words
```

```
> Um2 := SubMatrix(U, 1..6, 1..2)
```

$$Um2 := \begin{bmatrix} -0.415139716033301 & 0.408248290463863 \\ -0.590723295429479 & 4.44089209850063 \cdot 10^{-16} \\ -0.415139716033301 & 0.408248290463863 \\ -0.258865830839363 & 0. \\ -0.415139716033301 & -0.816496580927726 \\ -0.258865830839363 & 5.55111512312578 \cdot 10^{-17} \end{bmatrix}$$

(34)

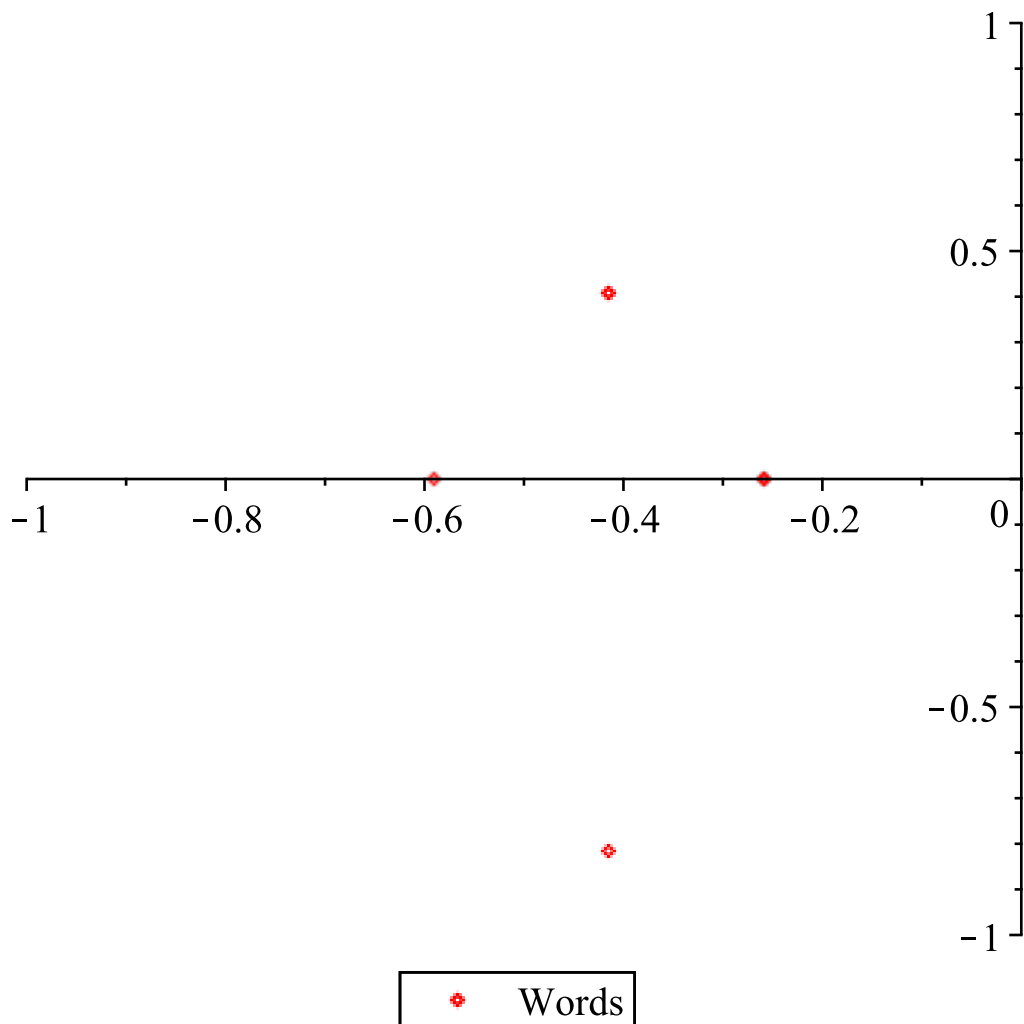
```
# The columns of Vtm2 provide the coordinates of the 5 documents
```

```
> Vtm2 := SubMatrix(Vt, 1..2, 1..5)
```

```
Vtm2 := [[ -0.471238386697216, -0.137670228390193, -0.195897929916829,
-0.780600778846626, -0.333568158307022 ],
[ 0.577350269189626, -0.577350269189626, 9.71445146547012 10-17,
-1.11022302462516 10-16, -0.577350269189626 ]]
```

(35)

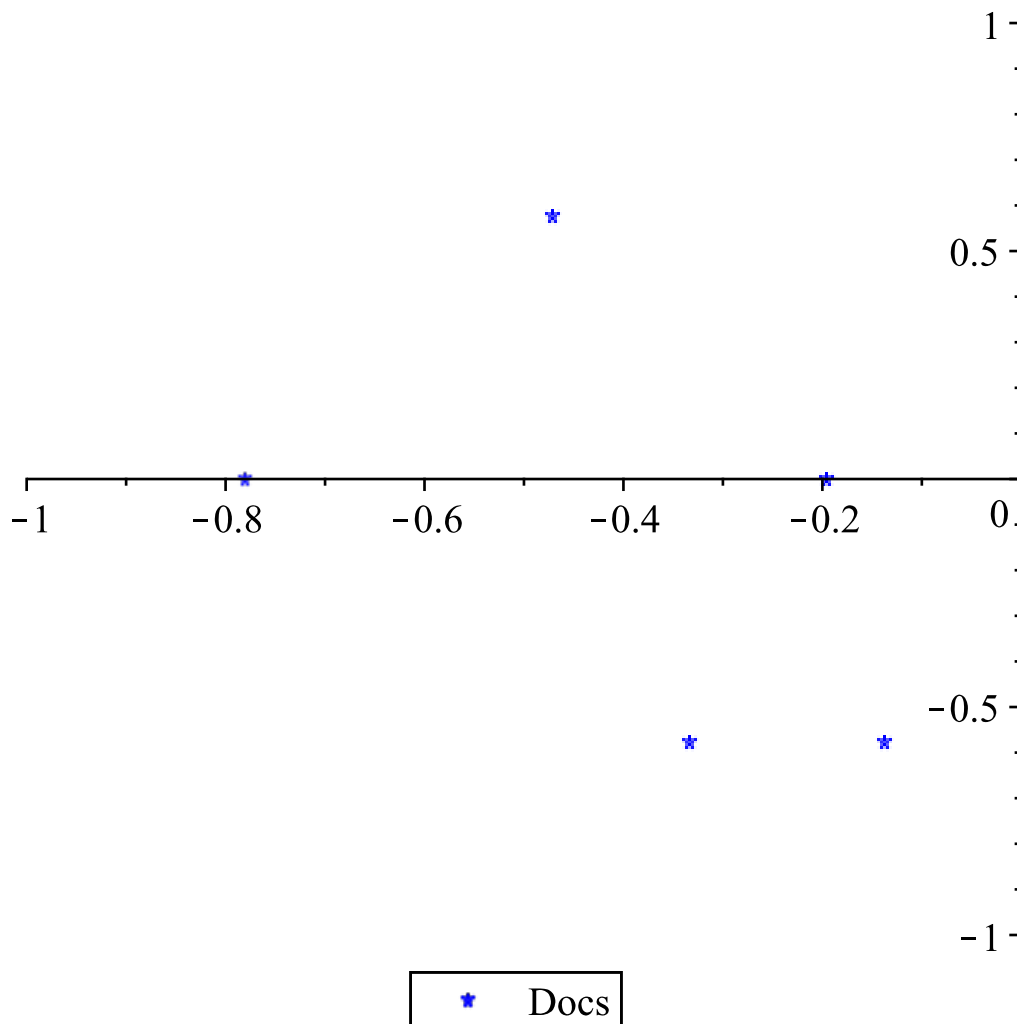
```
> plot1_2d := pointplot(Um2, legend="Words", color=red, axes=normal, view=[-1..0, -1
..1]) : display(plot1_2d)
```



# Plot the 5 documents

```
> plot2_2d := pointplot(Vtm2, legend="Docs", color=blue, symbol=asterisk, axes=normal,
view=[-1..0,-1..1]) : display(plot2_2d)
```





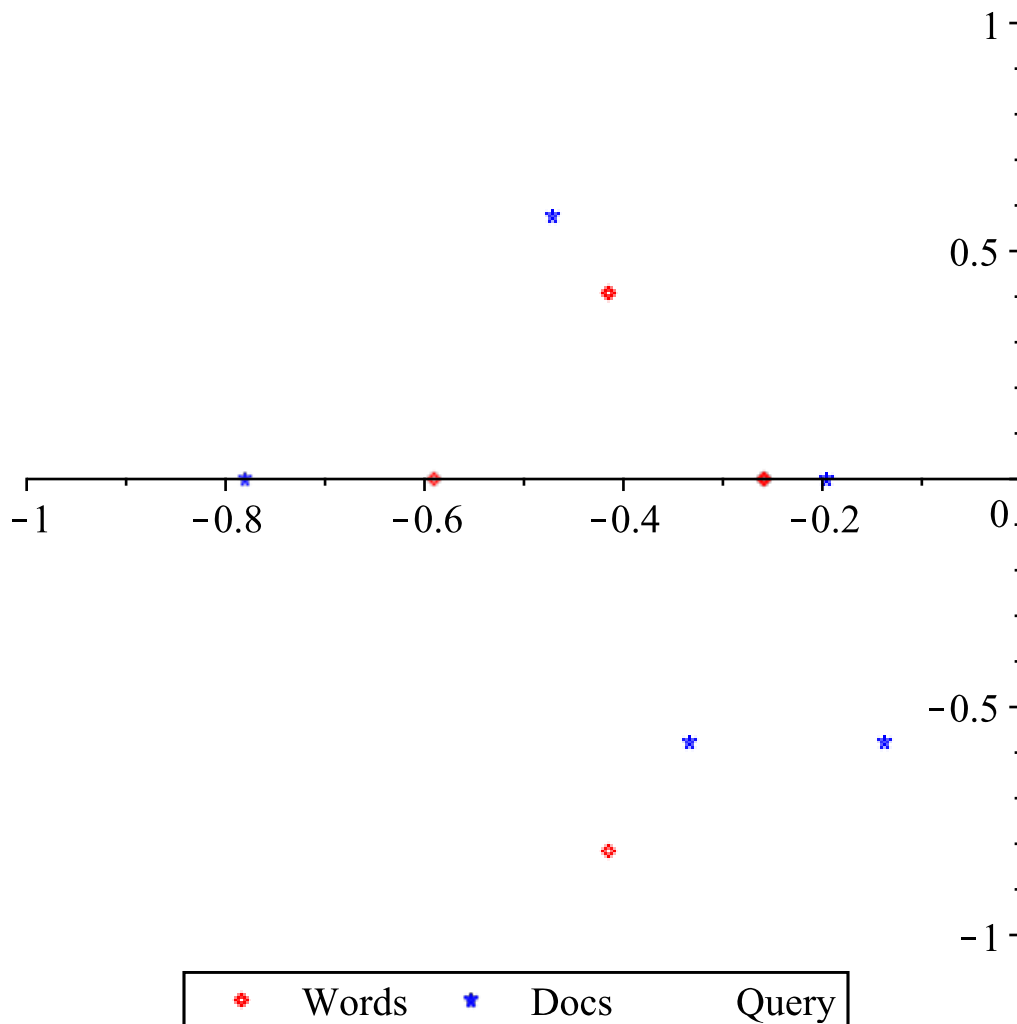
```
> qcoord_2 := Transpose(q).(Um2.MatrixInverse(Sm2))
```

```
qcoord_2 := [ -0.275340456780387  0.577350269189626 ]
```

**(36)**

```
# Combine the plots
```

```
> plot3_2d := pointplot(qcoord_2, symbol=box, legend="Query", axes=normal) :  
display(plot1_2d, plot2_2d, plot3_2d)
```



$$\begin{aligned} > \text{doc1} := \text{Column}(\text{Vtm2}, 1) : \text{test1} := \frac{qcoord\_2 \cdot \text{doc1}}{\text{Norm}(qcoord\_2, 2) \cdot \text{Norm}(\text{doc1}, 2)} \\ & \text{test1} := 0.9714457632 \end{aligned} \quad (37)$$

$$\begin{aligned} > \text{doc2} := \text{Column}(\text{Vtm2}, 2) : \text{test2} := \frac{qcoord\_2 \cdot \text{doc2}}{\text{Norm}(qcoord\_2, 2) \cdot \text{Norm}(\text{doc2}, 2)} \\ & \text{test2} := -0.7781502377 \end{aligned} \quad (38)$$

$$\begin{aligned} > \text{doc3} := \text{Column}(\text{Vtm2}, 3) : \text{test3} := \frac{qcoord\_2 \cdot \text{doc3}}{\text{Norm}(qcoord\_2, 2) \cdot \text{Norm}(\text{doc3}, 2)} \\ & \text{test3} := 0.4304582471 \end{aligned} \quad (39)$$

$$\begin{aligned} > \text{doc4} := \text{Column}(\text{Vtm2}, 4) : \text{test4} := \frac{qcoord\_2 \cdot \text{doc4}}{\text{Norm}(qcoord\_2, 2) \cdot \text{Norm}(\text{doc4}, 2)} \\ & \text{test4} := 0.4304582469 \end{aligned} \quad (40)$$

$$\begin{aligned} > \text{doc5} := \text{Column}(\text{Vtm2}, 5) : \text{test5} := (qcoord\_2 \cdot \text{doc5}) / (\text{Norm}(qcoord\_2, 2) \cdot \text{Norm}(\text{doc5}, 2)) \\ & \text{test5} := -0.5662031223 \end{aligned} \quad (41)$$

\*\*\*\*\*

**Answer: for Rank 2 analysis cosine similarity test**  
**for query q="baking bread "shows :**  
**Very good for**

**doc1 =0.9714**

**the other document shows less then 0.5 (less then relevant)**

\*\*\*\*\*

**>** *Sm3 := DiagonalMatrix(S<sub>1..3</sub>, 3, 3);*

$$Sm3 := \begin{bmatrix} 3.01546471512117 & 0. & 0. \\ 0. & 1.41421356237309 & 0. \\ 0. & 0. & 1.20531141460241 \end{bmatrix} \quad (42)$$

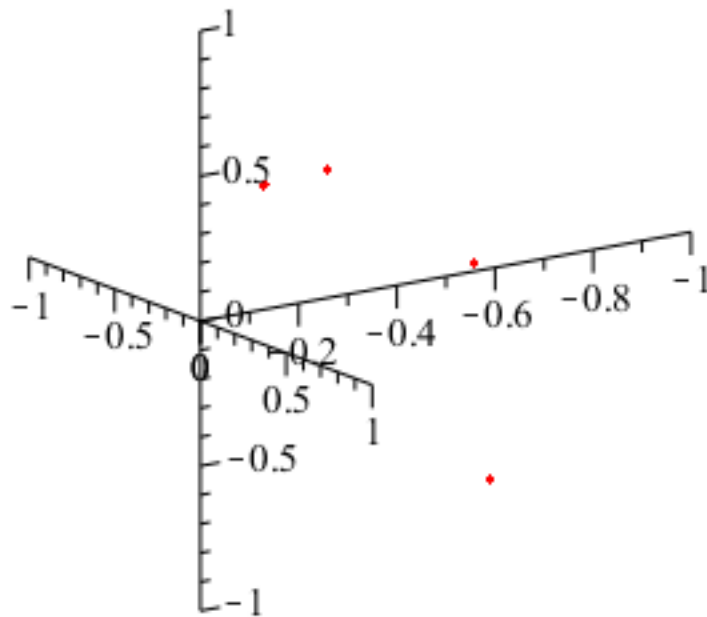
**>** *Um3 := SubMatrix(U, 1..6, 1..3);*

$$Um3 := \begin{bmatrix} -0.415139716033301 & 0.408248290463863 & 0.162729146205422 \\ -0.590723295429479 & 4.44089209850063 \cdot 10^{-16} & -0.729386490672964 \\ -0.415139716033301 & 0.408248290463863 & 0.162729146205422 \\ -0.258865830839363 & 0. & 0.440768092169533 \\ -0.415139716033301 & -0.816496580927726 & 0.162729146205422 \\ -0.258865830839363 & 5.55111512312578 \cdot 10^{-17} & 0.440768092169533 \end{bmatrix} \quad (43)$$

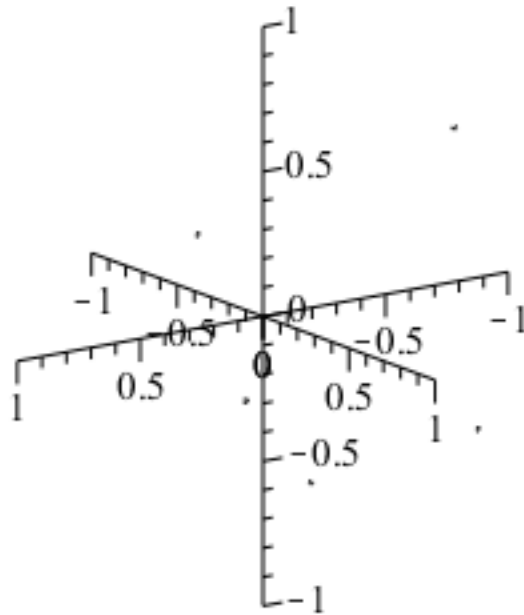
**>** *Vtm3 := SubMatrix(Vt, 1..3, 1..5)*

$$Vtm3 := \begin{bmatrix} -0.471238386697216, & -0.137670228390193, & -0.195897929916829, \\ -0.780600778846626, & -0.333568158307022, \\ 0.577350269189626, & -0.577350269189626, & 9.71445146547012 \cdot 10^{-17}, \\ -1.11022302462516 \cdot 10^{-16}, & -0.577350269189626, \\ -0.335123515274566, & 0.135010043241896, & -0.605143601758358, \\ 0.531262812684466, & -0.470133558516463 \end{bmatrix} \quad (44)$$

**>** *plot1\_3d := pointplot3d(Um3, color = red, axes = normal, view = [-1..0, -1..1, -1..1]) :*  
*display(plot1\_3d);*



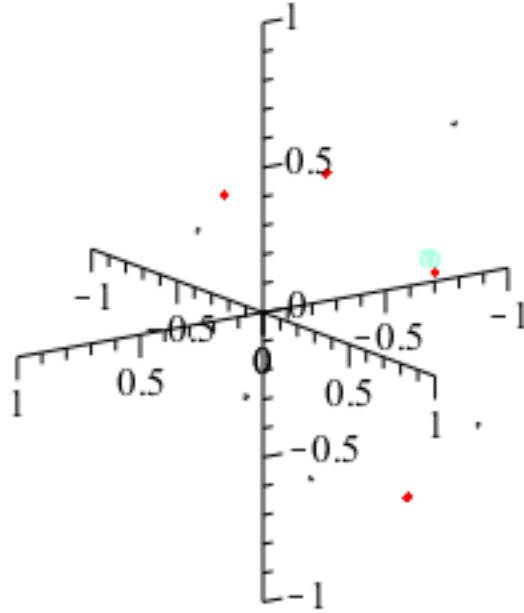
```
> plot2_3d := pointplot3d(Vtm3, color = black, symbol = asterisk, axes = normal, view = [-1 .. 1, -1 .. 1, -1 .. 1]) : display(plot2_3d);
```



```

> qcoord_3 := Transpose(q).(Um3 • MatrixInverse(Sm3));
qcoord_3 := [ -0.275340456780387  0.577350269189626  0.270020086483792 ] (45)
> plot3_3d := pointplot3d(qcoord_3, symbol = box, axes = normal) : display(plot1_3d, plot2_3d,
plot3_3d);

```



$$\begin{aligned} &> \text{doc1} := \text{Column}(\text{Vtm3}, 1) : \text{test1} := \frac{qcoord\_3 \cdot \text{doc1}}{\text{Norm}(qcoord\_3, 2) \cdot \text{Norm}(\text{doc1}, 2)} \\ &\text{test1} := 0.6567412211 \end{aligned} \quad (46)$$

$$\begin{aligned} &> \text{doc2} := \text{Column}(\text{Vtm3}, 2) : \text{test2} := \frac{qcoord\_3 \cdot \text{doc2}}{\text{Norm}(qcoord\_3, 2) \cdot \text{Norm}(\text{doc2}, 2)} \\ &\text{test2} := -0.6127748991 \end{aligned} \quad (47)$$

$$\begin{aligned} &> \text{doc3} := \text{Column}(\text{Vtm3}, 3) : \text{test3} := \frac{qcoord\_3 \cdot \text{doc3}}{\text{Norm}(qcoord\_3, 2) \cdot \text{Norm}(\text{doc3}, 2)} \\ &\text{test3} := -0.2478655574 \end{aligned} \quad (48)$$

$$\begin{aligned} &> \text{doc4} := \text{Column}(\text{Vtm3}, 4) : \text{test4} := \frac{qcoord\_3 \cdot \text{doc4}}{\text{Norm}(qcoord\_3, 2) \cdot \text{Norm}(\text{doc4}, 2)} \\ &\text{test4} := 0.5466612853 \end{aligned} \quad (49)$$

$$\begin{aligned} &> \text{doc5} := \text{Column}(\text{Vtm3}, 4) : \text{test5} := \frac{qcoord\_3 \cdot \text{doc5}}{\text{Norm}(qcoord\_3, 2) \cdot \text{Norm}(\text{doc5}, 2)} \\ &\text{test5} := 0.5466612853 \end{aligned} \quad (50)$$

\*\*\*\*\*

**Answer: for Rank 3 analysis cosine similarity test  
for query q="baking bread "shows :  
relevant for**

**best**

**doc1 =0.6567**

**less relavent**

**doc4=doc5=0.5467**

\*\*\*\*\*