

# CS 485/585 - Cryptography

Winter 2020

## Program 1

**Due February 19<sup>th</sup> (before class)**

200 points

**Submit to:** see instructions below.

Write a program for the block-encryption algorithm called **PSU-CRYPT** (based on *Twofish* by Bruce Schneier, John Kelsey, Doug Whiting, David Wagner, Chris Hall and *SKIPJACK* by the NSA combined). PSU-CRYPT is described below. Implement **PSU-CRYPT** using a 64 bit block size and a 64 bit key. Graduate students are required to implement a 64 bit block size with an 80 bit key.

The majority of the code **MUST** be your own work. Code that is not yours (for example from a book) must be clearly documented. You may use any standard programming language that will not have difficulty compiling and testing on the PSU lab machines. Give this some thought since you are manipulating blocks of bits. Make sure your language supports the operations easily. Please test your program on the lab.

## Input and Output

As input your program should take a standard ASCII text file (to standardize grading, call the file **plaintext.txt**) and a randomly chosen secret key represented in HEX (put this in a file called **key.txt**). As output your program should return a HEX text file (call the file **cyphertext.txt**) which is the encryption of the input file under **PSU-CRYPT**. This is of course reversed for decryption.

## Overall Structure of PSU-CRYPT

**PSU-CRYPT** is a block encryption algorithm where the block size is 64 bits. The input file is encrypted 64 bits at a time. Each 64-bit input block is divided into 4 words, **w<sub>0</sub>, w<sub>1</sub>, w<sub>2</sub>, w<sub>3</sub>** (16 bits each).

### To Encrypt:

- Input *whitening* step:
  - The input is the 64-bit block divided into 4 words **w<sub>0</sub>, w<sub>1</sub>, w<sub>2</sub>, w<sub>3</sub>**.
  - XOR each word with 16 bits of the key **K = K<sub>0</sub>K<sub>1</sub>K<sub>2</sub>K<sub>3</sub>**.
  - The output is
    - **R<sub>0</sub> = w<sub>0</sub> ⊕ K<sub>0</sub>, R<sub>1</sub> = w<sub>1</sub> ⊕ K<sub>1</sub>,**
    - **R<sub>2</sub> = w<sub>2</sub> ⊕ K<sub>2</sub>, R<sub>3</sub> = w<sub>3</sub> ⊕ K<sub>3</sub>.**
- Set the round number to **round=0**. After each of the 16 rounds increment **round** by one.
- Compute **F(R<sub>0</sub>, R<sub>1</sub>, round)**. This function returns two values **F<sub>0</sub>** and **F<sub>1</sub>**.
  - Compute **R<sub>2</sub> ⊕ F<sub>0</sub>**. This value is **R<sub>0</sub>** for the next round.
  - Compute **R<sub>3</sub> ⊕ F<sub>1</sub>**. This value is **R<sub>1</sub>** for the next round.
  - The value **R<sub>0</sub>** becomes **R<sub>2</sub>** for the next round.
  - The value **R<sub>1</sub>** becomes **R<sub>3</sub>** for the next round.
  - Repeat for 16 rounds (but not the whitening step this only happens at the start of the first round).

- After the last of the 16 rounds:
  - Undo the last swap by setting
    - $y_0$  to  $R_2$  from the end of the 16<sup>th</sup> round;
    - $y_1$  to  $R_3$  from the end of the 16<sup>th</sup> round;
    - $y_2$  to  $R_0$  from the end of the 16<sup>th</sup> round and
    - $y_3$  to  $R_1$  from the end of the 16<sup>th</sup> round.
- Output whitening step:
  - XOR each word with 16 bits of the key  $\mathbf{K} = \mathbf{K}_0\mathbf{K}_1\mathbf{K}_2\mathbf{K}_3$ .  
The input is  $y_0, y_1, y_2, y_3$ . The output is
    - $C_0 = y_0 \oplus K_0, C_1 = y_1 \oplus K_1,$
    - $C_2 = y_2 \oplus K_2, C_3 = y_3 \oplus K_3.$
 The value  $C_0C_1C_2C_3$  is the ciphertext.

### To Decrypt:

This is a Feistel cipher. The algorithm to decrypt is the same as the algorithm to encrypt except that the keys are generated and used in reverse order (see the sections below on keys).

### Subroutines

The program can be broken into several logical subroutines. Function **F()**, the **G-permutation** and the **Key Schedule** are explained in terms of their inputs and outputs.

### Functions F( $R_0, R_1, \text{round}$ )

- To Encrypt:
  - Input:  $R_0, R_1$  and the **round** number (or the round number may be global).
  - Note: In every call to **F()** a total of 12 subkeys are used, 4 in each call to **G()** and 4 directly in **F()**. You may want to compute all 12 subkeys at the start of **F()** since you will need them generated in reverse order for decryption. Then pass keys to **G()**. You can also pre-compute all subkeys for all rounds at the start.

Compute  $T_0 = \mathbf{G}(R_0, \text{round})$

Compute  $T_1 = \mathbf{G}(R_1, \text{round})$

Compute  $F_0 = (T_0 + 2 \cdot T_1 + \text{concatenate}(\mathbf{K}(4 \cdot \text{round}) \mathbf{K}(4 \cdot \text{round} + 1))) \bmod 2^{16}$

Compute  $F_1 = (2 \cdot T_0 + T_1 + \text{concatenate}(\mathbf{K}(4 \cdot \text{round} + 2) \mathbf{K}(4 \cdot \text{round} + 3))) \bmod 2^{16}$

Note: **concatenation**( $x, y$ ) is just the concatenation of two bytes.  $\mathbf{K}(x)$  is a call to the key scheduler to get a key based on value  $x$ . Again, keys may already be precomputed.

Output:  $F_0, F_1$ .

- To Decrypt: The **F()** function is not run in reverse for decryption. Only the subkeys are used in reverse order. It may be easier to understand if, at the entry to the **F()** function, you generate all the subkeys for that call and then use them. This implies passing keys to the **G()** function as arguments.
- For encryption the order of construction and use of subkeys is:
  - $\mathbf{GK}_1 = \mathbf{K}(4 \cdot \text{round})$  first call to **G()**
  - $\mathbf{GK}_2 = \mathbf{K}(4 \cdot \text{round} + 1)$
  - $\mathbf{GK}_3 = \mathbf{K}(4 \cdot \text{round} + 2)$
  - $\mathbf{GK}_4 = \mathbf{K}(4 \cdot \text{round} + 3)$
  - $\mathbf{GK}_5 = \mathbf{K}(4 \cdot \text{round})$  second call to **G()**
  - $\mathbf{GK}_6 = \mathbf{K}(4 \cdot \text{round} + 1)$
  - $\mathbf{GK}_7 = \mathbf{K}(4 \cdot \text{round} + 2)$

$$\mathbf{GK}_8 = \mathbf{K}(4 \cdot \mathbf{round} + 3)$$

$$\mathbf{K}_9 = \mathbf{K}(4 \cdot \mathbf{round}) \quad \text{for } \mathbf{F}_0 \text{ and } \mathbf{F}_1$$

$$\mathbf{K}_{10} = \mathbf{K}(4 \cdot \mathbf{round} + 1)$$

$$\mathbf{K}_{11} = \mathbf{K}(4 \cdot \mathbf{round} + 2)$$

$$\mathbf{K}_{12} = \mathbf{K}(4 \cdot \mathbf{round} + 3)$$

- For decryption the subkeys are used as the reverse list:

$$\mathbf{K}_{12} = \mathbf{K}(4 \cdot \mathbf{round} + 3) \quad \text{used first}$$

$$\mathbf{K}_{11} = \mathbf{K}(4 \cdot \mathbf{round} + 2) \quad \text{used second}$$

$$\mathbf{K}_{10} = \mathbf{K}(4 \cdot \mathbf{round} + 1) \quad \text{used third, etc.}$$

$$\mathbf{K}_9 = \mathbf{K}(4 \cdot \mathbf{round})$$

$$\mathbf{GK}_8 = \mathbf{K}(4 \cdot \mathbf{round} + 3)$$

$$\mathbf{GK}_7 = \mathbf{K}(4 \cdot \mathbf{round} + 2) \text{ etc., until } \mathbf{GK}_1 = \mathbf{K}(4 \cdot \mathbf{round})$$

For decryption, the algorithms for  $\mathbf{F}()$  and  $\mathbf{G}()$  are not changed only the order of the subkeys.

### G-permutation $\mathbf{G}(\mathbf{w}, \mathbf{round})$

The input is 16 bits,  $\mathbf{w}$  and the **round** number (and maybe the subkeys). A fixed table, called the **F-table**, is used to perform a substitution (see last page).

- To Encrypt and Decrypt: Algorithm **G**

Input:  $\mathbf{w}, \mathbf{round}$ :

Let  $\mathbf{g}_1$  be the left (high) 8 bits of  $\mathbf{w}$ .

Let  $\mathbf{g}_2$  be the right (low) 8 bits of  $\mathbf{w}$ .

$$\mathbf{g}_3 = \mathbf{Ftable}(\mathbf{g}_2 \oplus \mathbf{K}(4 \cdot \mathbf{round})) \oplus \mathbf{g}_1$$

$$\mathbf{g}_4 = \mathbf{Ftable}(\mathbf{g}_3 \oplus \mathbf{K}(4 \cdot \mathbf{round} + 1)) \oplus \mathbf{g}_2$$

$$\mathbf{g}_5 = \mathbf{Ftable}(\mathbf{g}_4 \oplus \mathbf{K}(4 \cdot \mathbf{round} + 2)) \oplus \mathbf{g}_3$$

$$\mathbf{g}_6 = \mathbf{Ftable}(\mathbf{g}_5 \oplus \mathbf{K}(4 \cdot \mathbf{round} + 3)) \oplus \mathbf{g}_4$$

Output:  $\mathbf{g}_5 \mathbf{g}_6$  (the concatenation).

### The Key Schedule $\mathbf{K}(\mathbf{x})$

- Encryption:

**Input:** A number  $\mathbf{x}$  and it is assumed that  $\mathbf{K}()$  has access to the current, stored, 64 bit key  $\mathbf{K}$ . The key is 64 bits and so 8 bytes long. Label the bytes 0 through 7 so  $\mathbf{K} = \mathbf{k}_7, \mathbf{k}_6, \mathbf{k}_5, \mathbf{k}_4, \mathbf{k}_3, \mathbf{k}_2, \mathbf{k}_1, \mathbf{k}_0$ . Left circular rotate  $\mathbf{K}$  by 1 bit and store this rotated value as the new key  $\mathbf{K}'$ .

**Output:** The  $\mathbf{x} \bmod 8$  byte of the key  $\mathbf{K}'$ . So if  $\mathbf{x} = 18$  then since  $18 \bmod 8 = 2$  output the third byte ( $\mathbf{k}_2$ ) of  $\mathbf{K}$ . This allows us to output the first byte when, for example  $\mathbf{x} = 16$  and  $16 \bmod 8 = 0$ , so the output byte is  $\mathbf{k}_0$ .

- Decryption:

**Input:** A number  $\mathbf{x}$  and it is assumed that  $\mathbf{K}()$  has access to the current, stored, 64 bit key  $\mathbf{K}$ . The key is 64 bits and so 8 bytes long. Label the bytes 0 through 7 as for encryption. Now  $\mathbf{z}$  is the  $\mathbf{x} \bmod 8$  byte of the key  $\mathbf{K}$ . Right rotate  $\mathbf{K}$  by 1 bit and store this value as the new key  $\mathbf{K}'$ . Unlike encryption, the subkey is gotten before the rotation of the key.

**Output:**  $\mathbf{z}$ .

Instead you can generate ALL subkeys when the program starts, in this case decryption keys are just the keys used in reverse order.

## More on Keys

For the keys: The  $\mathbf{F}()$  function is called with  $\mathbf{R}_0, \mathbf{R}_1$

- The **F()** function calls the **G()** function twice
  - Each call to **G()** call **K()** 4 times 8 keys
  - The **F()** function then directly call **K()** 4 times 4 keys
  - So 1 call to the **F()** functions uses 12 subkeys keys

There are 16 calls to the **F()** function so  $16 \cdot 12 = 192$  subkeys are generated from the initial secret key **K**. Each time **K()** is called (and a subkey is generated) the key **K** is left rotated by 1 bit. Since the initial secret key **K** is 64 bits long and  $64 \cdot 3 = 192$  then after 16 rounds the final key (after all of the rotations) should be same as the initial secret key. This is important for decryption. Also note that the input and output whitening steps do not shift the key bits. It is probably easiest to generate ALL keys at the beginning of the encryption or decryption.

When you are testing your program, if you use a smaller number of rounds (say 2), then you must save the final value of the key (since it will not be rotated enough to be the same as the original secret key) and then use that to decrypt.

The generation of subkeys for decryption is different then that for encryption.

- Key Generation for Encryption is:
  - Left rotate
  - Pick out the key bits
- Key Generation for Decryption is:
  - Pick out the key bits
  - Right rotate

## F-table

The SKIPJACK F-table is in hexadecimal. The high order 4 bits of input index the row and the low order 4 bits index the column. Rows and columns are indexed starting at 0. For example **Ftable(7a) = d6** since the 7<sup>th</sup> row and the 10<sup>th</sup> column (HEX for 10 is a) contains **d6**. The F-table values:

**f**table[ ] =

```
{0xa3,0xd7,0x09,0x83,0xf8,0x48,0xf6,0xf4,0xb3, 0x21,0x15,0x78,0x99,0xb1,0xaf,0xf9,
0xe7,0x2d,0x4d,0x8a,0xce,0x4c,0xca,0x2e,0x52,0x95,0xd9,0x1e,0x4e,0x38,0x44,0x28,
0x0a,0xdf,0x02,0xa0,0x17,0xf1,0x60,0x68,0x12,0xb7,0x7a,0xc3,0xe9,0xfa,0x3d,0x53,
0x96,0x84,0x6b,0xba,0xf2,0x63,0x9a,0x19,0x7c,0xae,0xe5,0xf5,0xf7,0x16,0x6a,0xa2,
0x39,0xb6,0x7b,0x0f,0xc1,0x93,0x81,0x1b,0xee,0xb4,0x1a,0xea,0xd0,0x91,0x2f,0xb8,
0x55,0xb9,0xda,0x85,0x3f,0x41,0xbf,0xe0,0x5a,0x58,0x80,0x5f,0x66,0x0b,0xd8,0x90,
0x35,0xd5,0xc0,0xa7,0x33,0x06,0x65,0x69,0x45,0x00,0x94,0x56,0x6d,0x98,0x9b,0x76,
0x97,0xfc,0xb2,0xc2,0xb0,0xfe,0xdb,0x20,0xe1,0xeb,0xd6,0xe4,0xdd,0x47,0x4a,0x1d,
0x42,0xed,0x9e,0x6e,0x49,0x3c,0xcd,0x43,0x27,0xd2,0x07,0xd4,0xde,0xc7,0x67,0x18,
0x89,0xcb,0x30,0x1f,0x8d,0xc6,0x8f,0xaa,0xc8,0x74,0xdc,0xc9,0x5d,0x5c,0x31,0xa4,
0x70,0x88,0x61,0x2c,0x9f,0x0d,0x2b,0x87,0x50,0x82,0x54,0x64,0x26,0x7d,0x03,0x40,
0x34,0x4b,0x1c,0x73,0xd1,0xc4,0xfd,0x3b,0xcc,0xfb,0x7f,0xab,0xe6,0x3e,0x5b,0xa5,
0xad,0x04,0x23,0x9c,0x14,0x51,0x22,0xf0,0x29,0x79,0x71,0x7e,0xff,0x8c,0x0e,0xe2,
0x0c,0xef,0xbc,0x72,0x75,0x6f,0x37,0xa1,0xec,0xd3,0x8e,0x62,0x8b,0x86,0x10,0xe8,
0x08,0x77,0x11,0xbe,0x92,0x4f,0x24,0xc5,0x32,0x36,0x9d,0xcf,0xf3,0xa6,0xbb,0xac,
0x5e,0x6c,0xa9,0x13,0x57,0x25,0xb5,0xe3,0xbd,0xa8,0x3a,0x01,0x05,0x59,0x2a,0x46}
```

## Graduate Students

Graduate students are required implement 64-bit block and 80-bit key sizes. This will then mean that you cipher will need to do 20 rounds so that the key is completely rotated 3 times.

Graduate students are also required to make their programs interoperate. Test your programs to see if they will interoperate by sending each other encrypted messages. It is also advisable for you, as a group, to use/build test vectors for the different subroutines so that you can jointly check your progress.

## Submitting your solution

**Turn in electronically:** All of your source code, documentation, etc. archived in a single compressed file. The compressed file name much include your last name. When you send in your code include the course number / project name in the subject line. Also include a text file named **README** that includes

1. Your name and an email address you can be contacted at.
2. A brief description of what you are submitting.
3. A precise description of how to build and use your program on the PSU system
4. A list of files that should be in the archive, and a one line description of each file.

Make sure you thoroughly test your code. This project is due before class on the due date.

Submit this Project to me at [bcsbm@pdx.edu](mailto:bcsbm@pdx.edu)

**Demoing your solution, I will schedule short lab secessions for each of you to demo your code.**