

- a.** Consider that “ST Computer” is a printing shop. In this shop there are five price range for printing pages. Assume that the shop max printing capacity per day  $P = 1000$  pages. Our target is to make maximum profit every day.

Item(i)	1	2	3	4	5
Pages(pg)	200	300	400	500	700
Price	200	250	350	400	550

**b.**

```
#include<stdio.h>
```

```
void knapSack(int P, int n, int price[], int pg[]);  
int getMax(int x, int y);
```

```
int main(void)  
{
```

```
    int price[] = {200,250,350,400,550};  
    int pg[] = {200,300,400,500,700};
```

```
    int n = 5;  
    int P = 1000;
```

```
    knapSack(P, n, price, pg);
```

```
    return 0;  
}
```

```
int getMax(int x, int y)  
{  
    if(x > y)  
    {  
        return x;  
    }  
    else
```

```

    {
        return y;
    }
}

void knapSack(int P, int n, int price[], int pg[]) {
    int i, p;
    int N[n+1][P+1];

    for(p = 0; p <= P; p++)
    {
        N[0][p] = 0;
    }

    for(i = 0; i <= n; i++)
    {
        N[i][0] = 0;
    }

    for(i = 1; i <= n; i++)
    {
        for(p = 1; p <= P; p++)
        {
            if(pg[i] <= p)
            {
                N[i][p] = getMax(N[i-1][p], price[i] + N[i-1][p - pg[i]]);
            }
            else
            {
                N[i][p] = N[i-1][p];
            }
        }
    }

    printf("Maximum earn: %d\n", N[n][P]);
}

```

**c.**

The worst-case time complexity of 0/1 knapsack algorithm is  $O(N*W)$ .  $N$  represent capacity and  $W$  represent the value of object.

**d.**

Dynamic programming is an effective method for fixing problems. Dynamic programming works through solving subproblems and using the results of those subproblems to extra quickly calculate the solution to a bigger problem. The divide-and-conquer paradigm (which additionally makes use of the concept of solving subproblems), dynamic programming usually involves solving all possible subproblems instead of a small component. One use of dynamic programming is the problem of 0/1 knapsack. In this dynamic programming problem, we've  $n$  objects each with a related pages and charges. The goal is to fill the knapsack with objects such that we've a maximum price without crossing the page limit of the knapsack. Dynamic programming produces a simpler algorithm. The key point to eliminate is that the using dynamic programming, we will reduce the problems of finding all of the shortest paths to fixing a series of subproblems that can be reused again and again to resolve large problems. Every time we attempt to solve a problem using dynamic programming.

## e. Dry run

### 1<sup>st</sup> phase

```
for( i=1; i<=5; i++)  
  for(p=200; p<=1000; p++)  
    if(pg[1]<=200)  
      N[1][200] = getMax(N[0][200], price[1] + N[0][200 - pg[1]]);  
                = N[0][200] = 0, 200 + N[0][0]  
                = getMax(200)  
N[1][200] = 200
```

```
for( i=1; i<=5; i++)  
  for(p=300; p<=1000; p++)  
    if(pg[1]<=300)  
      N[1][300] = getMax(N[1-1][300], price[1] + N[1-1][300 - pg[1]]);  
                = N[0][300] = 0, 200 + N[0][300-200]  
                = N[0][300] = 0, 200 + N[0][100]  
                = getMax(200)  
N[1][300] = 200
```

```
for( i=1; i<=5; i++)  
  for(p=400; p<=1000; p++)  
    if(pg[1]<=400)  
      N[1][400] = getMax(N[1-1][400], price[1] + N[1-1][400 - pg[1]]);  
                = N[0][400] = 0, 200 + N[0][400-200]  
                = N[0][400] = 0, 200 + N[0][200]  
                = getMax(200)  
N[1][400] = 200
```

```
for( i=1; i<=5; i++)  
  for(p=500; p<=1000; p++)  
    if(pg[1]<=500)  
      N[1][500] = getMax(N[1-1][500], price[1] + N[1-1][500 - pg[1]]);  
                = N[0][500] = 0, 200 + N[0][500-200]  
                = N[0][500] = 0, 200 + N[0][300]  
                = getMax(200)  
N[1][500] = 200
```



= getMax(250)

**N[2][300] = 250**

for( i=2; i<=5; i++)

for(p=400; p<=1000; p++)

if(pg[2]<=400)

N[2][400] = getMax(N[2-1][400], price[2] + N[2-1][400 - pg[2]]);

= N[1][400] = 200, 250 + N[1][400-300]

= N[1][400] = 200, 250 + N[1][100]

= getMax(250)

**N[2][400] = 250**

for( i=2; i<=5; i++)

for(p=500; p<=1000; p++)

if(pg[2]<=500)

N[2][500] = getMax(N[2-1][500], price[2] + N[2-1][500 - pg[2]]);

= N[1][500] = 200, 250 + N[1][500-300]

= N[1][500] = 200, 250 + N[1][200] **[N[1][200] = 200]**

= getMax(450)

**N[2][500] = 450**

for( i=2; i<=5; i++)

for(p=700; p<=1000; p++)

if(pg[2]<=700)

N[2][700] = getMax(N[2-1][700], price[2] + N[2-1][700 - pg[2]]);

$$= N[1][700] = 200, 250 + N[0][700-300]$$

$$= N[1][500] = 200, 250 + N[1][400] \text{ } [N[1][400] = 200]$$

$$= \text{getMax}(450)$$

$$N[2][700] = 450$$

N[i,p]	p=0	200	300	400	500	600	700	800	900	1000
i= 0	0	0	0	0	0	0	0	0	0	0
1	0	200	200	200	200	200	200	200	200	200
2	0	200	250	250	450	450	450	450	450	450
3	0	200	250	350	350	550	600	600	800	800
4	0	200	250	350	400	400	600	650	750	850
5	0	200	250	350	400	400	500	500	750	800