

ASSIGNMENT 01 [MID-TERM]



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Submitted by:

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The variables value according to ID:

m_1	m_2	m_3	m_4	m_5
4	4	7	9	3

1

Problem-1:

a. Hence,

$$m_5 = 3.$$

$$R_1 = 5.2 + (2 \times 3)$$

$$= 11.2 \text{ K}\Omega.$$

We know,

$$R_A = \left(\frac{1}{R_6} + \frac{1}{R_7} \right)^{-1} + R_8 + R_9$$

$$= \left(\frac{1}{9} + \frac{1}{6} \right)^{-1} + 3.3 + 5.1$$

$$= 12 \text{ K}\Omega,$$

$$R_B = \left(\frac{1}{R_2} + \frac{1}{R_3} + \frac{1}{R_4 + R_5} \right)^{-1}$$

$$= \left(\frac{1}{16} + \frac{1}{32} + \frac{1}{20+12} \right)^{-1} \text{ K}\Omega$$

$$= 8 \text{ K}\Omega.$$

$$\begin{aligned} R_C &= \left(\frac{1}{R_A} + \frac{1}{R_B} \right)^{-1} \\ &= \left(\frac{1}{12} + \frac{1}{8} \right)^{-1} \text{ k}\Omega \\ &= 4.8 \text{ k}\Omega \end{aligned}$$

$$\begin{aligned} R_T &= R_1 + R_C \\ &= (11.2 + 4.8) \text{ k}\Omega \\ &= 16 \text{ k}\Omega \end{aligned}$$

$$I_S = \frac{V}{R_T} = \frac{280}{16} = 17.5 \text{ mA.}$$

$$\begin{array}{l|l} I_1 = \frac{R_C}{R_B} \times I_S & I_2 = \frac{R_B}{R_2} \times I_1 \\ = \frac{4.8}{8} \times 17.5 & = \frac{8}{16} \times 10.5 \\ = 10.5 \text{ mA} & = 5.25 \text{ mA.} \end{array}$$

$$I_5 = I_S - I_1 = (27.5 - 12) = 5.5 \text{ mA.}$$

3

$$\begin{aligned} I_6 &= \frac{R_p}{R_6} \times I_5 \\ &= \frac{3.6}{9} \times 5.5 \\ &= 2.2 \text{ mA.} \end{aligned}$$

$$\begin{aligned} \frac{1}{R_p} &= \left(\frac{1}{R_6} + \frac{1}{R_7} \right)^{-1} \\ &= \left(\frac{1}{9} + \frac{1}{6} \right)^{-1} \\ &= 3.6 \text{ mA.} \end{aligned}$$

$$I_8 = I_5 = 5.5 \text{ mA.}$$

b. Here,

$$\begin{aligned} V_2 &= I_2 R_2 \\ &= (5.25 \times 16) \text{ V} \\ &= 84 \text{ V} \end{aligned}$$

$$\begin{aligned} V_7 &= (I_5 - I_6) \times R_7 \\ &= (5.5 - 2.2) \times 6 \\ &= 19.8 \text{ V} \end{aligned}$$

4

$$\begin{aligned}
 V_8 &= I_8 R_8 \\
 &= (5.5 \times 3.3) \text{ V} \\
 &= 18.15 \text{ V}
 \end{aligned}$$

$$\begin{aligned}
 V_9 &= I_9 R_9 \quad [I_8 = I_9] \\
 &= (5.5 \times 5.1) \text{ V} \\
 &= 28.05 \text{ V.}
 \end{aligned}$$

C.

$$\begin{aligned}
 P_{R_2} &= I_2^2 R_2 \\
 &= (5.25)^2 \times 16 \\
 &= 441 \text{ kW.}
 \end{aligned}$$

$$R_2 = 16 \text{ k}\Omega$$

$$R_6 = 9 \text{ k}\Omega$$

$$R_9 = 5.1 \text{ k}\Omega$$

$$\begin{aligned}
 P_{R_6} &= I_6^2 R_6 \\
 &= (2.2)^2 \times 9 \\
 &= 43.56 \text{ kW.}
 \end{aligned}$$

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$$P_{R_9} = I_9^2 R_9 \quad [I_8 = I_9]$$

$$= (5.5)^2 \times 5.1.$$

$$= 154.28 \text{ kW.}$$

Problem-2

$$m_4 = 9$$

$$R_1 = 2(1+9) = 20 \Omega$$

$$R_2 = R_4 = 3(1+9) = 30 \Omega$$

$$R_3 = 5(1+9) = 50 \Omega$$

a.

Loop equation-1: -

$$(R_1 + R_2 + R_3)I_1 - R_3 I_2 = 35$$

$$\Rightarrow (20 + 30 + 50)I_1 - 30 I_2 = 35$$

$$\therefore 100 I_1 - 30 I_2 = 35 \quad (1)$$

$$(R_3 + R_4)I_2 - R_3 I_3 = -74$$

$$\Rightarrow (50 + 30)I_2 - 50 I_3 = -74$$

$$\therefore 80I_2 - 50I_3 = -74 \quad (2)$$

b.

$$100I_1 - 30I_2 = 35 \quad (1)$$

$$80I_2 - 50I_3 = -74 \quad (2)$$

$$\therefore (2) \times 2$$

$$-100I_1 + 160I_2 = -148$$

$$100I_1 - 30I_2 = 35$$

$$130I_2 = -113$$

$$\therefore I_2 = \frac{-113}{130} = -0.87A$$

$$\therefore 100I_1 - 30I_2 = 35$$

$$\Rightarrow 100I_1 = (30 \times -0.87) + 35$$

$$\Rightarrow 100I_1 = 35 + 26.1$$

$$\Rightarrow I_1 = \frac{61.1}{100}$$

$$\therefore I_1 = 0.611A.$$

$$I_3 = I_1 - I_2 = (-0.87 - 0.611)A \\ = -1.481A$$

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Problem-3

$$m_5 = 3$$

$$R_1 = 4(1+3) = 16 \Omega$$

$$R_2 = R_4 = 8(1+3) = 32 \Omega$$

$$R_3 = 16(1+3) = 64 \Omega$$

a. For node V_1 ,

$$\left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \right) V_1 - \left(\frac{1}{R_3} \right) V_2 = -5A$$

$$\Rightarrow \left(\frac{1}{16} + \frac{1}{32} + \frac{1}{64} \right) V_1 - \left(\frac{1}{64} \right) V_2 = -5A$$

$$\Rightarrow \left(\frac{7}{64} \right) V_1 - \left(\frac{1}{64} \right) V_2 = -5A$$

$$\Rightarrow 7V_1 - V_2 = -320A$$

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For node V_2

$$\left(\frac{1}{R_3} + \frac{1}{R_2}\right)V_2 - \left(\frac{1}{R_3}\right)V_1 = -4A$$

$$\Rightarrow \left(-\frac{1}{64} + \frac{1}{32}\right)V_2 - \left(\frac{1}{64}\right)V_1 = -4A$$

$$\Rightarrow \frac{3V_2}{64} - \frac{V_1}{64} = -4A$$

$$\Rightarrow 3V_2 - V_1 = -256A.$$

b.

$$7V_1 - V_2 = -320A.$$

$$3V_2 - V_1 = -256A.$$

$$D = \begin{vmatrix} 7 & -1 \\ -1 & 3 \end{vmatrix} = 21 - 1 = 20$$

9'

$$D_2 = \begin{vmatrix} -320 & -1 \\ -256 & 3 \end{vmatrix} = -960 - 256 = -1216$$

$$D_2 = \begin{vmatrix} 7 & -320 \\ -1 & -256 \end{vmatrix} = -1792 - 320 = -2112$$

$$V_1 = \frac{D_1}{D} = \frac{-1216}{20} = -60.8$$

$$V_2 = \frac{D_2}{D} = \frac{-2112}{20} = -105.6$$

$$I_3 = \frac{V}{R_3}$$

$$= \frac{V_1 - V_2}{R_3}$$

$$= \frac{(-60.8) - (-105.6)}{64}$$

$$= 0.7 A$$

THE END