

ASSIGNMENT 03 [Final-TERM]



American International University- Bangladesh (AIUB)

Submitted by:

Name: Nokibul Arfin Siam.

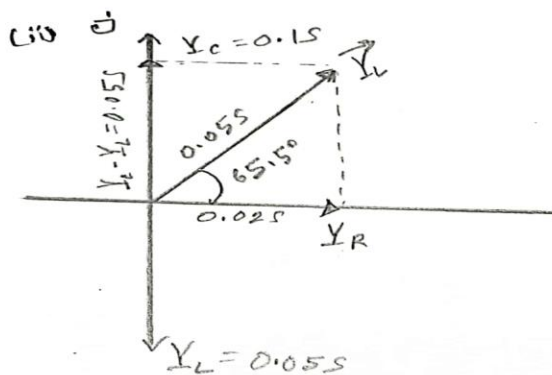
Student ID: 21-44793-1.

Section: K.

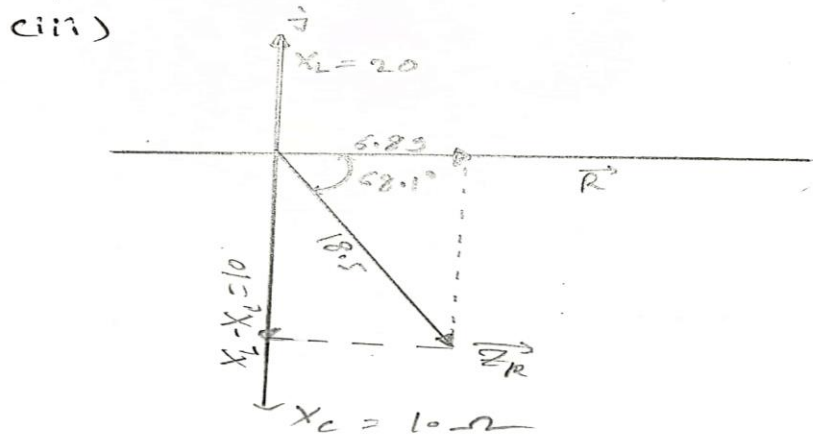
Problem-01

$$\begin{aligned}
 1. \text{ Admittance, } \vec{Y} &= \frac{1}{X_C} + \frac{1}{R} + \frac{1}{X_L} \\
 &= \frac{1}{-j10} + \frac{1}{44} + \frac{1}{j20} \\
 &= 0.025 + j0.055 \\
 &= 0.05 \angle 65.5^\circ
 \end{aligned}$$

$$\begin{aligned}
 \text{Impedance, } \vec{Z}_T &= \frac{1}{\vec{Y}_T} \\
 &= \frac{1}{0.025 + j0.055} \\
 &= 6.89 - j17.24 \\
 &= 18.5 \angle -68.1^\circ
 \end{aligned}$$



$$\begin{aligned}
 Y_C &= \frac{1}{X_C} = \frac{-1}{j10} = j0.055 \\
 Y_L &= \frac{1}{X_L} = \frac{1}{j20} = j0.055 \\
 Y_R &= \frac{1}{R} = \frac{1}{44} = 0.02
 \end{aligned}$$



$$\begin{aligned}
 \text{vi) } C &= \frac{1}{\omega X_C} = \frac{1}{314 \times 10} \\
 &= 3.18 \times 10^{-4} \times 10^{-6} \\
 &= 3.18 \times 10^{-10} \text{ mF}
 \end{aligned}$$

$$\begin{aligned}
 L &= \frac{X_L}{\omega} \\
 &= \frac{20}{314} = 0.063 \text{ H}
 \end{aligned}$$

$$\text{v) } e(t) = 70.8 \sin(3.14t + 60^\circ) \text{ V}$$

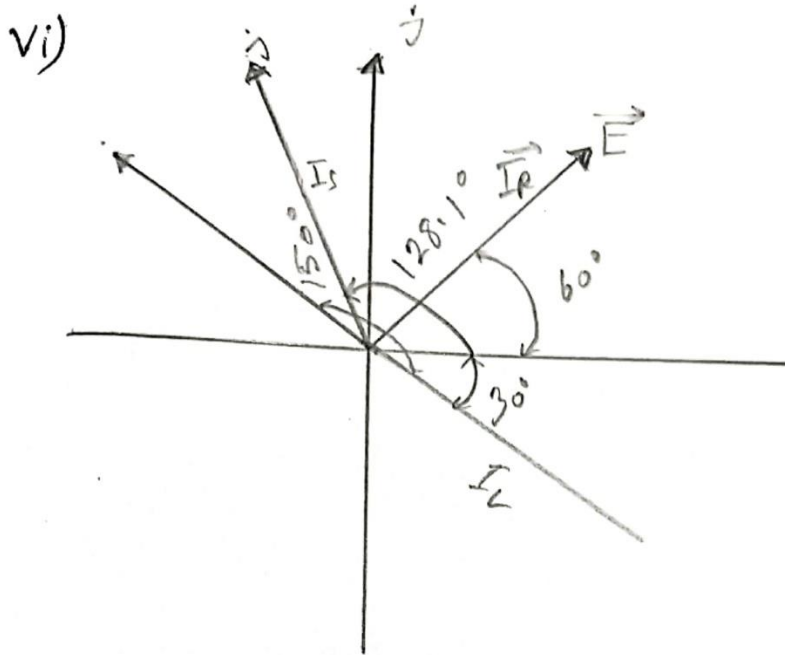
$$\vec{E} = 50.1 \angle 60^\circ$$

$$I_S \Rightarrow \frac{\vec{E}}{\vec{Z}_T} = \frac{50.1 \angle 60^\circ}{18.5 \angle -68.1^\circ} = 2.7 \angle 128.1^\circ$$

$$I_R \Rightarrow \frac{\vec{E}}{\vec{R}} = \frac{50.1 \angle 60^\circ}{44 \angle 0^\circ} = 1.13 \angle 60^\circ$$

$$I_L \Rightarrow \frac{\vec{E}}{\vec{X}_L} = \frac{50.1 \angle 60^\circ}{20 \angle 90^\circ} = 2.5 \angle -30^\circ$$

$$I_C \Rightarrow \frac{\vec{E}}{\vec{X}_C} = \frac{50.1 \angle 60^\circ}{10 \angle -90^\circ} = 5.01 \angle 150^\circ$$



vii) KCL,

$$\begin{aligned}\therefore I_s &= I_p + I_L + I_C \\ &= (1.13 \angle 60^\circ) + (2.5 \angle -30^\circ) + (5.01 \angle 150^\circ) \\ &= 2.7 \angle 125.7^\circ\end{aligned}$$

viii) $S = E I_s^*$

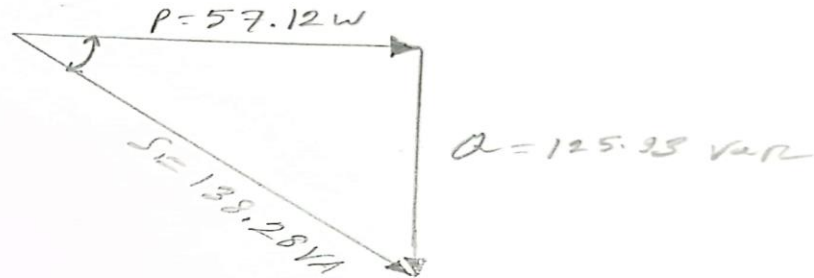
$$\begin{aligned}&= (50.1 \angle 60^\circ) \times (2.7 \angle 125.7^\circ)^* \\ &= (50.1 \angle 60^\circ) \times (2.7 \angle -125.7^\circ) \\ &= 135.27 \angle -65.7^\circ \\ &= 55.67 - j123.28\end{aligned}$$

∴ Apparent power, $S = 135.27$

Avg Power, $P = 55.67 \text{ W}$

Reactive, $Q_L = -123.28 \text{ Var}$

ix)



x) Power factor, $pf = \cos \theta_s$
 $= \cos(-65.3^\circ)$
 $= 0.418$ (leading)

$$xi) I_s \Rightarrow \frac{2.76}{0.707} = 18.05 \sin(314t + 125.6^\circ)$$

$$I_R \Rightarrow \frac{1.14}{0.707} = 1.612 \sin(314t + 60^\circ)$$

$$I_L \Rightarrow \frac{2.51}{0.707} = 3.55 \sin(314t - 30^\circ)$$

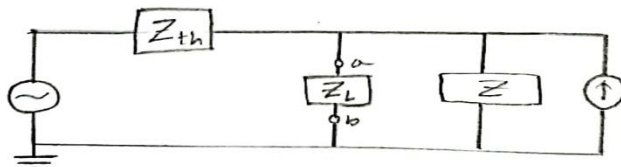
$$I_C \Rightarrow \frac{5.01}{0.707} = 7.09 \sin(314t + 150^\circ)$$

Problem-2:

a) i) $\vec{Z}_{th} = 6 + j8$
 $= 10 \angle 53.1^\circ$

$$\vec{E}_{th} = 20 \angle 0^\circ$$

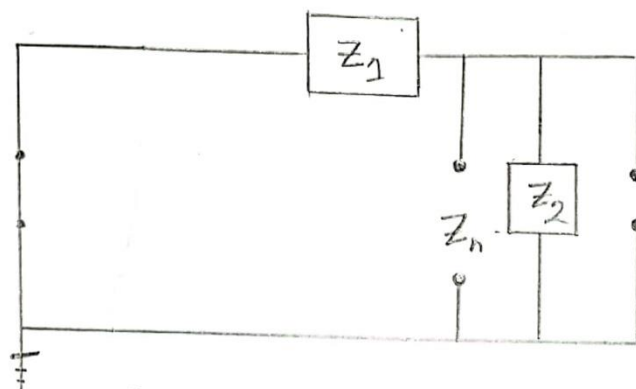
(ii)



Thevenin equivalent circuit

b)

$$\textcircled{i} \vec{E} = 20\text{V} \angle 0^\circ$$

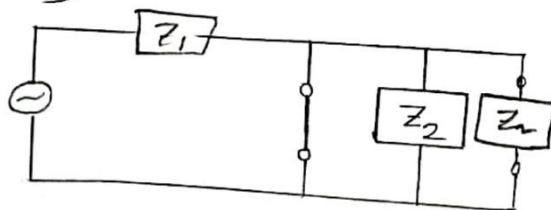


$$\begin{aligned} \vec{Z}_1 &= 6 + j8 \\ &= 10 \angle 53.1^\circ \end{aligned}$$

$$\begin{aligned} \vec{Z}_2 &= 9 - j12 \\ &= 15 \angle -53.1^\circ \end{aligned}$$

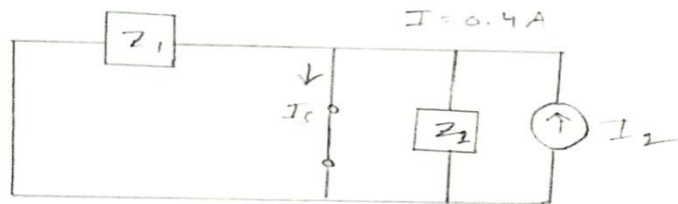
$$\vec{Z}_n = Z_1 \parallel Z_2 = 9.65 \angle 12.92^\circ$$

Forc-(E)



$$\therefore \vec{I}_S = \frac{\vec{E}}{\vec{Z}_1} = \frac{20 \angle 0^\circ}{10 \angle 53.1^\circ} = 2 \angle -53.1^\circ$$

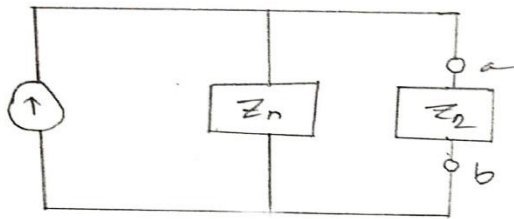
For (I_e)



$$\therefore \vec{I}_2 = 0.4 \angle 20^\circ$$

$$\begin{aligned} \therefore \vec{I}_N &= \vec{I}_S + \vec{I}_2 \\ &= (2 \angle -53.1^\circ) + (0.4 \angle 20^\circ) \\ &= 2.15 \angle -42.89^\circ \end{aligned}$$

(ii)



Norton's equivalent circuit

©

$$\begin{aligned} Z_L &= (Z_{th})^* \\ &= 6 - j8 \end{aligned}$$

$$\begin{aligned} \text{Maximum power, } P &= \frac{E_{th}^2}{4Z_L} \\ &= \frac{20^2}{4 \times 6} \\ &= 16.7 \text{ W} \end{aligned}$$