

ASSIGNMENT 01 [Final-TERM]



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Problem-1:-

$$V(t) = 100 \sin(314t + 70^\circ) \text{ V}$$

$$i(t) = 20 \sin(314t + 100^\circ) \text{ A}$$

a.

(i) From equation $V(t)$ & $i(t)$,

$$V_m = 100 \text{ V}$$

$$I_m = 20 \text{ A.}$$

$$\therefore \text{impedence, } Z = \frac{V_m}{I_m} = \frac{100 \text{ V}}{20 \text{ A}} = 5 \Omega$$

(ii) Admittance,

$$Y = \frac{1}{Z} = \frac{1}{5}$$

$$= 0.2 \text{ S}$$

$$= 200 \text{ mS}$$

b.

(i) From equation,

$$\theta_v = 70^\circ$$

$$\theta_i = 100^\circ$$

$$\therefore \theta_z = \theta_v - \theta_i = (70^\circ - 100^\circ) = -30^\circ$$

 \therefore The resistance,

$$R = Z \cos \theta_z = 5 \cos(-30^\circ) \\ = 4.33 \, \Omega$$

(ii) The reactance,

$$X = Z \sin \theta_z = 5 \sin(-30^\circ) \\ = -2.5 \, \Omega$$

(iii) We know,

$$Y = 200 \, \text{mS}$$

From equation,

$$\theta_v = 70^\circ$$

$$\theta_i = 100^\circ$$

$$\therefore \theta_y = \theta_i - \theta_v = (100^\circ - 70^\circ) = 30^\circ$$

 \therefore The conductance,

$$G = Y \cos \theta_y = 200 \cos(30^\circ) \\ = 173.20 \, \text{mS}$$

(iv) The susceptance,

$$B = Y \sin \theta_y = 200 \sin(30^\circ) \\ = 100 \text{ mS}$$

c.

(i) Here,

$$\theta_v = 70^\circ$$

$$\theta_i = 100^\circ$$

$$\therefore \theta = \theta_v - \theta_i = (70^\circ - 100^\circ) = -30^\circ$$

$$\therefore \text{Power factor, pf} = \cos \theta = \cos(-30^\circ) \\ = 0.87$$

(ii) The reactive factor,

$$\text{rf} = \sin \theta = \sin(-30^\circ) \\ = -0.5$$

(iii) Here,

$$V_m = 100 \text{ V}$$

$$I_m = 20 \text{ A}$$

$$\theta = -30^\circ$$

$$\text{The power, } P = \frac{V_m I_m}{2} \cos \theta \\ = \frac{100 \times 20}{2} \cos(-30^\circ) \\ = 866.03 \text{ W}$$

(iv) The reactive power,

$$Q = \frac{V_m I_m}{2} \sin \theta \\ = \frac{100 \times 20}{2} \sin(-30^\circ) \\ = -500 \text{ var}$$

(v) The apparent power,

$$\begin{aligned}
 S &= \frac{V_m I_m}{2} \\
 &= \frac{100 \times 20}{2} \\
 &= 1000 \text{ VA}
 \end{aligned}$$

d. Voltage and current in polar form

$$\therefore V = (0.707 \times 100) \angle 70^\circ = 70.7 \angle 70^\circ \text{ V}$$

$$\therefore I = (0.707 \times 20) \angle 100^\circ = 14.14 \angle 100^\circ \text{ A}$$

e. $S = VI$

$$= (70.7 \angle 70^\circ) (14.14 \angle 100^\circ)$$

$$= (70.7 \angle 70^\circ) (14.14 \angle -100^\circ)$$

$$= 999.83 \angle -30$$

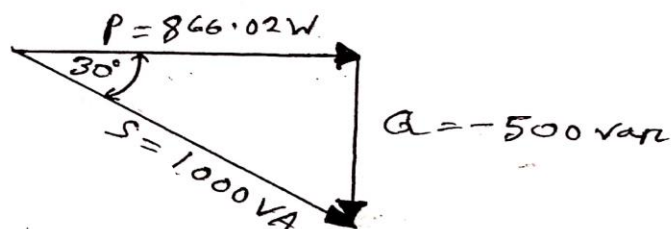
$$= 865.88 + 499.915j$$

f. we find,

$$P = 866.02 \text{ W}$$

$$Q = -500 \text{ var}$$

$$S = 1000 \text{ VA}$$



Problem - 2

$$a. \quad v(t) = 50 \sin(377t + 30^\circ) \text{ V}$$

(i)

$$R = 20.0 \text{ } \Omega$$

$$\therefore Z = 20$$

$$\theta_Z = 0^\circ$$

$$\therefore I_m = \frac{V_m}{Z} = \frac{50}{20} = 2.5 \text{ A}$$

$$\therefore \theta_i = \theta_v - \theta_Z$$

$$\Rightarrow \theta_i = 30 - 0^\circ$$

$$\therefore \theta_i = 30^\circ$$

$$\therefore i(t) = 2.5 \sin(377t + 30^\circ) \text{ A}$$

$$(ii) \quad L = 50 \text{ mH} = 0.05 \text{ H}$$

$$Z = X_L = \omega L = 377 \times 0.05 = 18.85$$

$$\theta_Z = 90^\circ$$

$$\therefore I_m = \frac{V_m}{Z} = \frac{50}{18.85} = 2.65 \text{ A}$$

$$\theta_i = \theta_v - \theta_Z$$

$$= 30^\circ - 90^\circ$$

$$= -60^\circ$$

$$\therefore i(t) = 2.65 \sin(377t - 60^\circ) \text{ A}$$

(iii)

$$C = 200 \mu F = 0.0002 F$$

$$Z = X_C = \frac{1}{\omega C}$$

$$= \frac{1}{377 \times 0.0002}$$

$$= 13.26$$

$$\theta_Z = -90^\circ$$

$$\therefore I_m = \frac{V_m}{Z} = \frac{50}{13.26} = 3.77 A$$

$$\theta_i = \theta_v - \theta_Z$$

$$= 30^\circ - (-90^\circ)$$

$$= 120^\circ$$

$$\therefore i(t) = 3.77 \sin(377t + 120^\circ) A$$

b.

$$i(t) = 5 \sin(200t + 50^\circ) A$$

(i)

$$R = 10 \text{ ohm.}$$

$$\therefore Z = 10 \Omega.$$

$$\theta_Z = 0^\circ$$

$$\therefore V_m = Z I_m = 10 \times 5 = 50 V$$

$$\theta_v = \theta_i + \theta_Z$$

$$= 50^\circ + 0^\circ$$

$$= 50^\circ$$

$$\therefore v(t) = 50 \sin(200t + 50^\circ) V$$

$$(ii) X_L = Z = 20 \Omega,$$

$$\theta_Z = 90^\circ,$$

$$\therefore V_m = I_m Z = 5 \times 20 = 100 \text{ V}$$

$$\begin{aligned} \therefore \theta_V &= \theta_i + \theta_Z \\ &= 50^\circ + 90^\circ \\ &= 140^\circ \end{aligned}$$

$$\therefore V(t) = 100 \sin(200t + 140^\circ) \text{ V}$$

$$(iii) X_C = Z = 15 \Omega,$$

$$\theta_Z = -90^\circ$$

$$\therefore V_m = Z I_m = 15 \times 5 = 75 \text{ V}$$

$$\therefore \theta_V = \theta_i + \theta_Z = 50^\circ + (-90^\circ) = -40^\circ$$

$$\therefore V(t) = 75 \sin(200t - 40^\circ) \text{ V}$$

THE END