Full name ____

ID NUMBER _

Read and follow the directions.

1. (4 points) Solve the following system and give your answer as an ordered pair (x, y).

$$x + y = 6$$

$$4x - 2y = 2$$

Solution. Using elimination, we add 2 times the first equation to second equation as follows:

$$2x + 2y = 12$$

$$\frac{+4x - 2y = 2}{6x + 0y = 14}$$

Since 6x = 14, we have that $x = \frac{7}{3}$. Using the first equation with this information we find that $\frac{7}{3} + y = 6 \implies y = \frac{11}{3}$.

2. (3 points) Solve the following exponential equation.

$$3^x = 21$$

$$\ln(3^x) = \ln(21) \implies x \ln(3) = \ln(21) \implies x = \frac{\ln(21)}{\ln(3)}$$

3. (3 points) Solve the following logarithmic equation.

$$\log_5(8-7x) = \log_5(x)$$

$$8 - 7x = x \implies 8 = 8x \implies x = 1$$

Checking this answer, we see that $\log_5(8-7) = \log_5(1)$, so it is correct and there are no domain issues.

4. (0 points) Draw your favorite part of summer, to celebrate finishing your last quiz.

USEFUL FORMULAS

$$\bullet \quad m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$\bullet \quad x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\bullet \quad y = mx + b$$

•
$$I = Prt$$

$$\bullet \quad \frac{1}{a^n} = a^{-n}$$

$$\bullet \quad Ax + By = C$$

$$\bullet \quad A = P + Prt$$

$$\bullet \qquad \left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}, (b \neq 0)$$

$$\bullet \quad y - y_1 = m(x - x_1)$$

$$\bullet \quad a^2 + b^2 = c^2$$

$$\bullet \quad a^2 + b^2 = c^2$$

•
$$a^2 - b^2 = (a+b)(a-b)$$

•
$$i = \sqrt{-1}$$

•
$$a^3 + b^3 = (a+b)(a^2 - ab + b^2)$$
• $\frac{f(x+h) - f(x)}{h}$

$$\bullet \qquad i^2 = -1$$

•
$$a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

$$f(x) = a(x-h)^2 + k$$

•
$$(a+b)^2 = a^2 + 2ab + b^2$$

 $\log_a MN = \log_a M + \log_a N$

•
$$(a-b)^2 = a^2 - 2ab + b^2$$

$$\bullet \quad a^m a^n = a^{m+n}$$

•
$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$a^m a^n = a^{m+n}$$

• $\left(-\frac{b}{2a}, f\left(-\frac{b}{2a}\right)\right)$

•
$$\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right)$$

•
$$a^0 = 1$$

$$\bullet \quad \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

$$\bullet \quad \frac{a^m}{a^n} = a^{m-n}$$

•
$$(x-h)^2 + (y-k)^2 = r^2$$

$$\bullet \quad \frac{a^m}{a^n} = a^{m-n}$$

$$(a^m)^n = a^{m \cdot n}$$

$$\bullet \quad \log_b M = \frac{\log_a M}{\log_a b}$$

 $\log_a M^p = p \log_a M$

$$\bullet \quad \log_a a = 1, \ \log_a 1 = 0$$

$$\bullet \quad \log_a a^x = x, \quad a^{\log_a x} = x$$