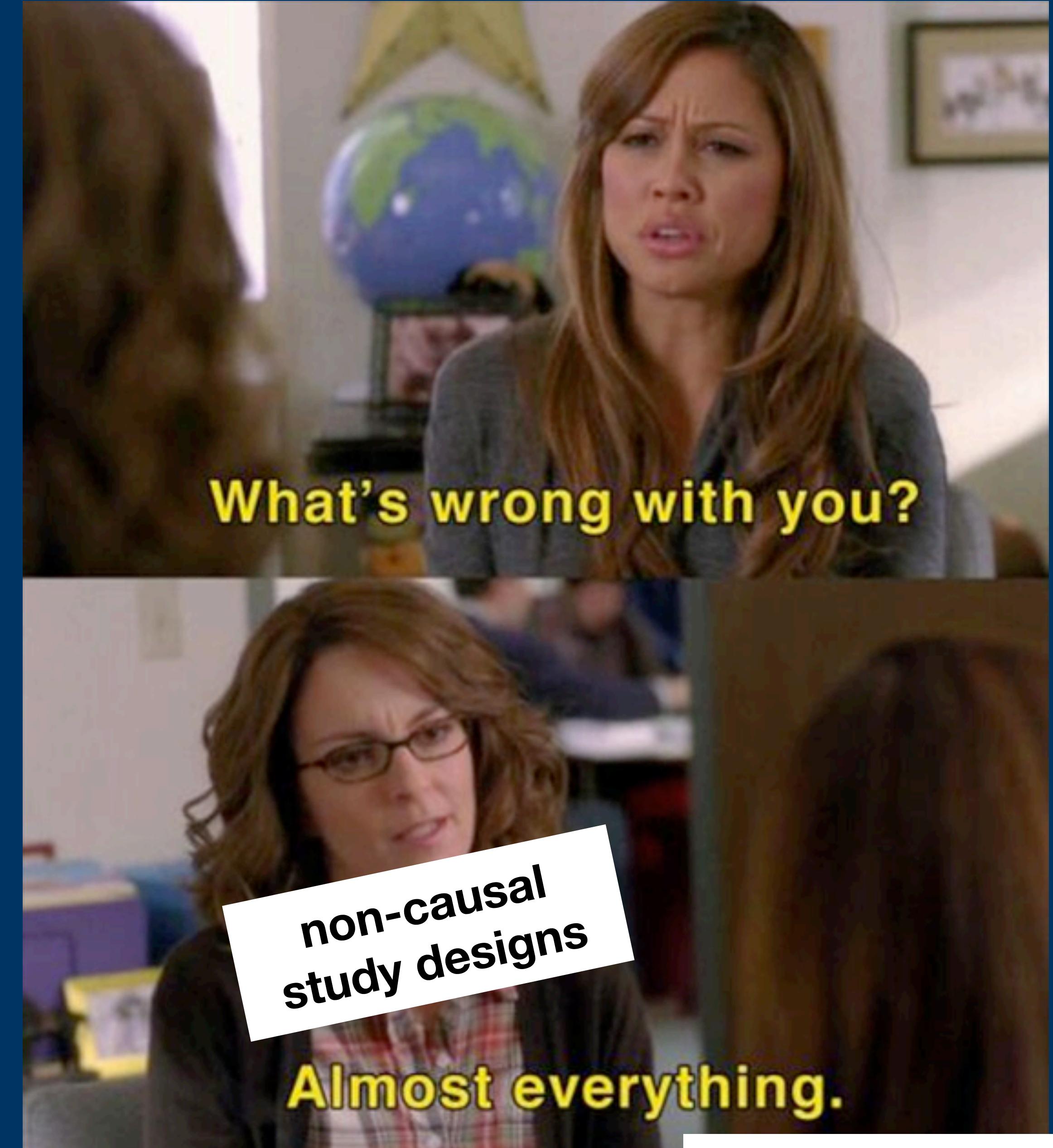


# Experiments. Blergh!

API 202: TF Session 4

# ALL

Nolan M. Kavanagh  
February 20, 2026



# Goals for today

- 1. Review the benefits of randomization.**
- 2. Discuss bias in randomized experiments.**
- 3. Experience the magic of difference-in-differences.**
- 4. Practice interpreting difference-in-differences.**

# Overview of our sample data

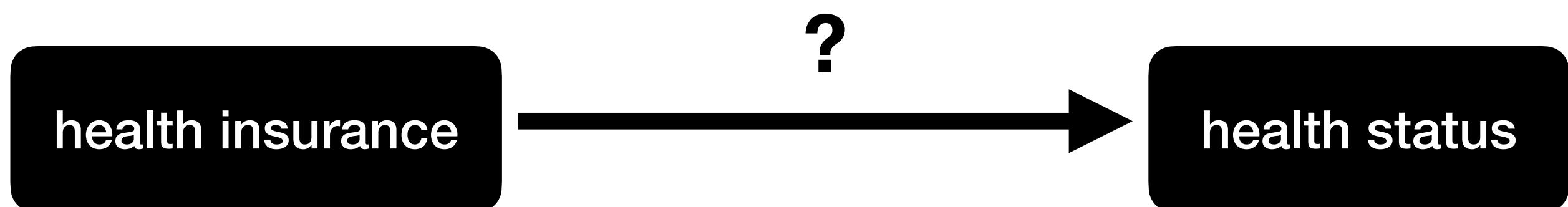
Dataset of over 2 million U.S. adults from 2011–2019

state	<b>State of respondent</b>	<i>Behavioral Risk Factor Surveillance System</i>
year	<b>Year when surveyed</b>	<i>Behavioral Risk Factor Surveillance System</i>
age	<b>Dummy for under 50 (1) or not (0)</b>	<i>Behavioral Risk Factor Surveillance System</i>
gender	<b>Dummy for man (1) or woman (0)</b>	<i>Behavioral Risk Factor Surveillance System</i>
race_eth	<b>Dummy for white/non-Latin (1) or not (0)</b>	<i>Behavioral Risk Factor Surveillance System</i>
married	<b>Dummy for married (1) or not (0)</b>	<i>Behavioral Risk Factor Surveillance System</i>
education	<b>Dummy for college-educated (1) or not (0)</b>	<i>Behavioral Risk Factor Surveillance System</i>
income	<b>Dummy for income &lt;\$35,000 (1) or not (0)</b>	<i>Behavioral Risk Factor Surveillance System</i>
insurance	<b>Dummy for health insurance (1) or not (0)</b>	<i>Behavioral Risk Factor Surveillance System</i>
expansion	<b>Dummy for Medicaid expansion state (1) or not (0)</b>	<i>Administrative</i>
post_2014	<b>Dummy for 6/1/2014 onward (1) or pre-2014 (0)</b>	<i>Administrative</i>

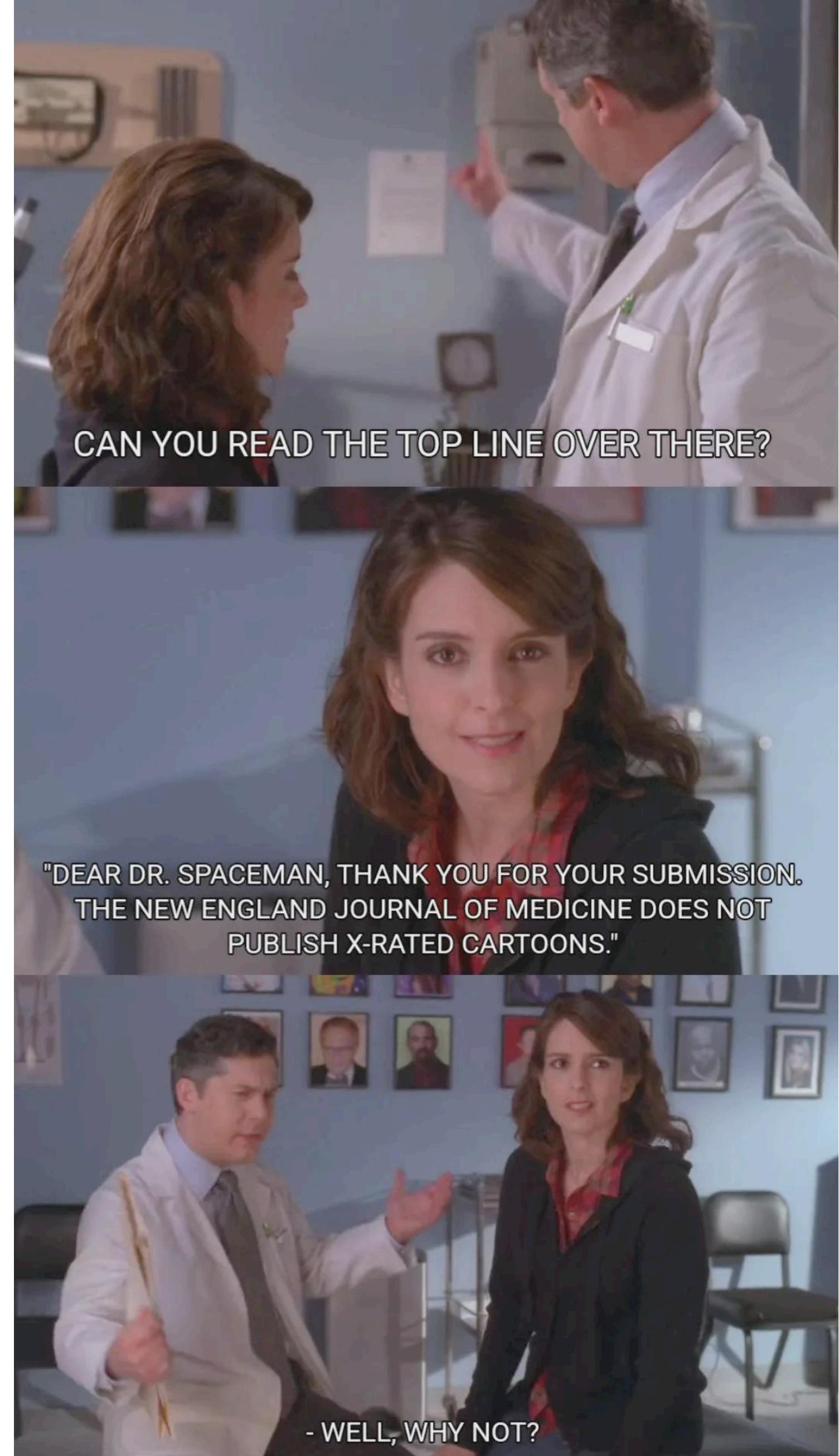
# I have an idea!

About 9% of Americans don't have health insurance.

If they had insurance, they might get healthier.



I, too, have been rejected by the  
New England Journal of Medicine.



**Why can't we just compare  
insured and uninsured folks?**

**What are we worried about?**

**Say it with me!**

# Why can't we just compare insured and uninsured folks?

There are, uh, a few omitted variables.

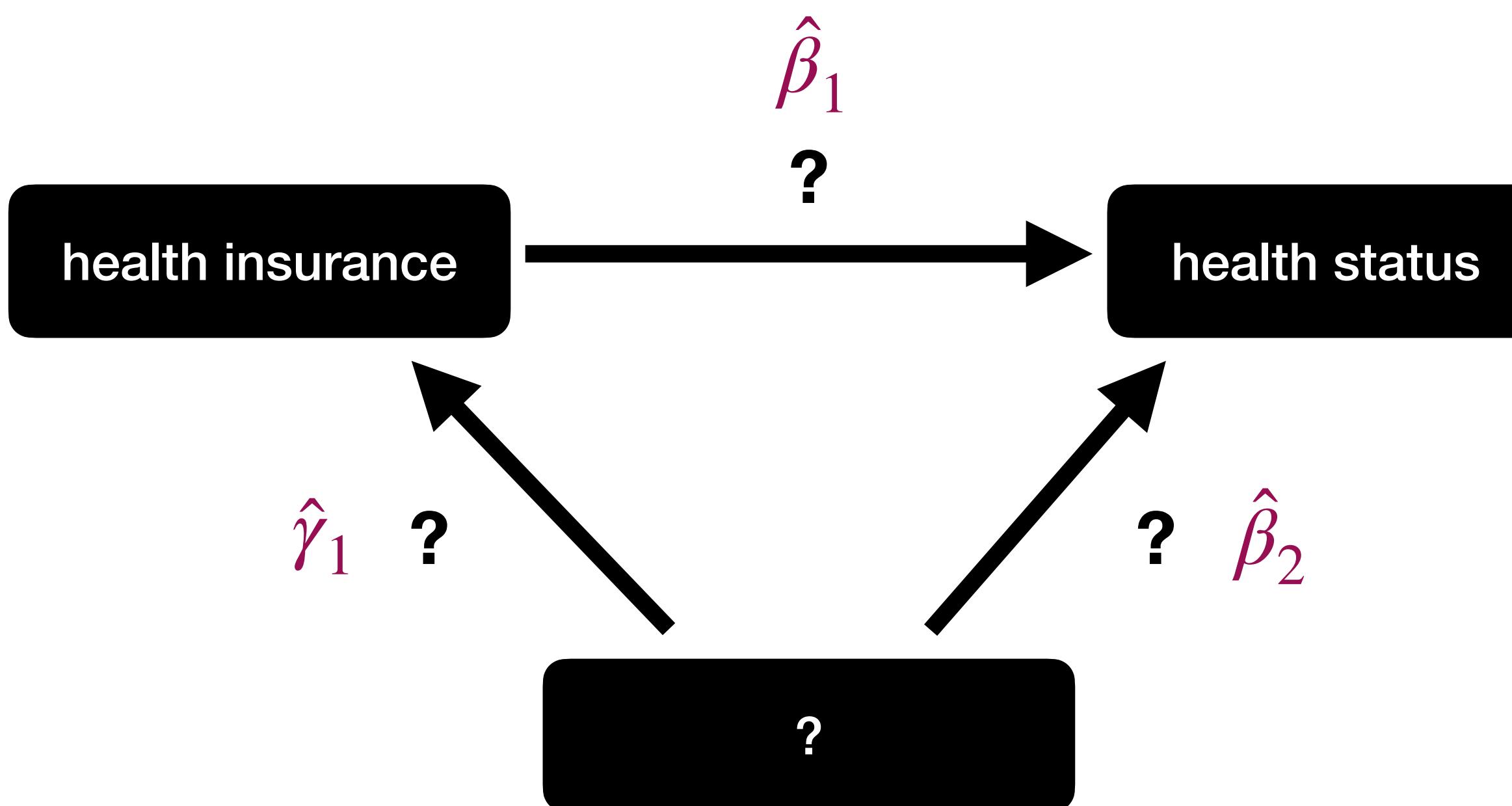
	<b>Uninsured</b> (n=213,714)	<b>Insured</b> (n=2,039,416)	<b>Difference</b>	<b>t-test</b> (P-value)
<b>Percent under 50 years</b>	60.9%	33.2%	+27.7 pp	P<0.001
<b>Percent men</b>	48.5%	43.0%	+5.5 pp	P<0.001
<b>Percent non-Latin white</b>	58.8%	80.3%	-21.5 pp	P<0.001
<b>Percent married</b>	38.5%	56.0%	-17.5 pp	P<0.001
<b>Percent college-educated</b>	16.4%	39.0%	-22.6 pp	P<0.001
<b>Percent with income &lt;\$35,000</b>	71.3%	35.7%	+35.6 pp	P<0.001

# Omitted variable bias will haunt your dreams.

Let's say that in our short regression, having insurance = better health.

$$\hat{\alpha}_1 > 0$$

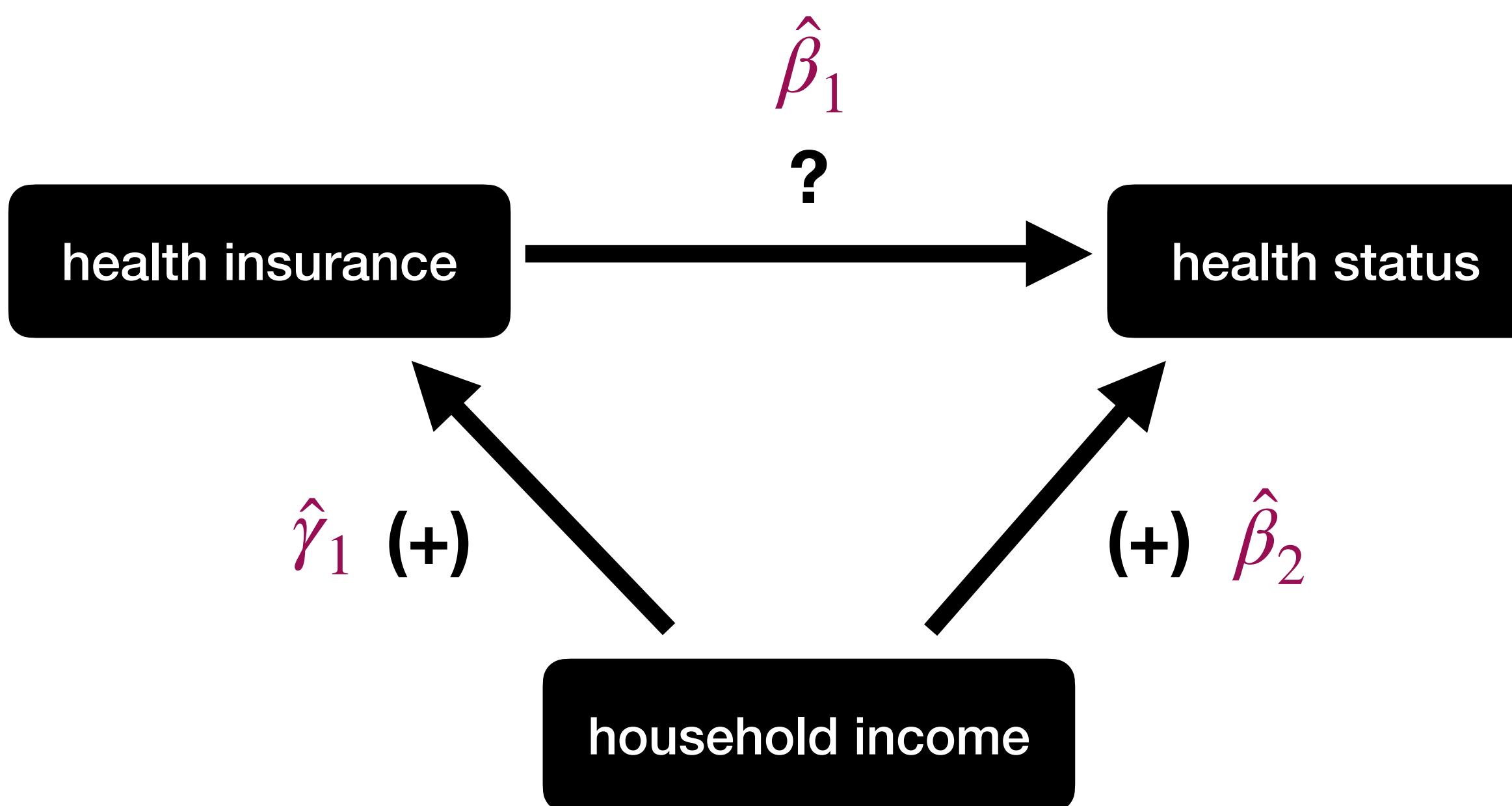
What might be an omitted variable?



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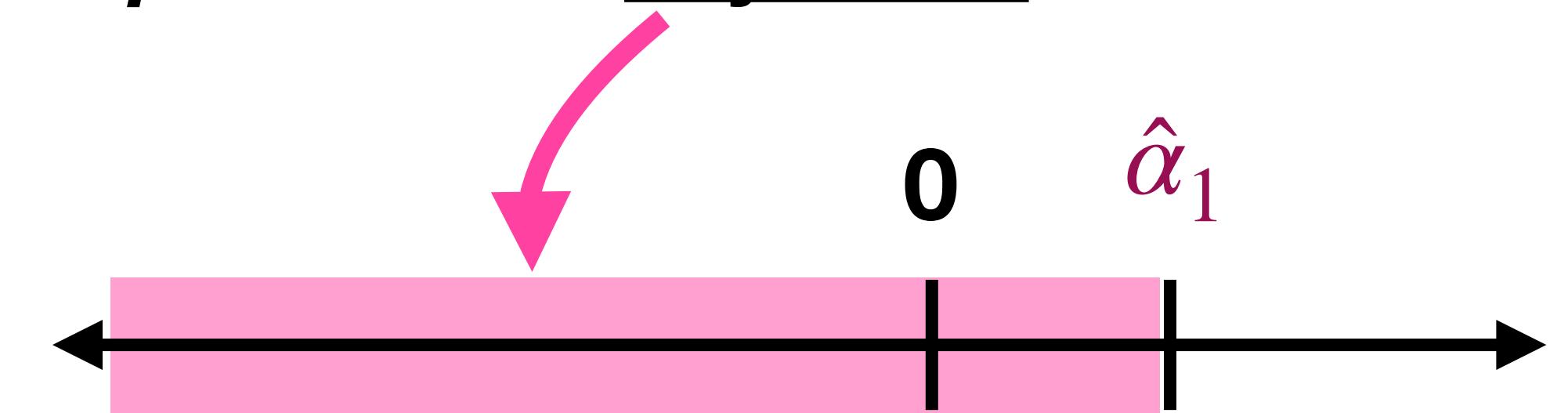
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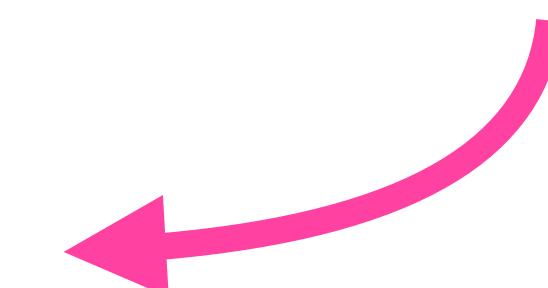
$$\hat{\alpha}_1 > 0$$

$\hat{\beta}_1$  could be anywhere in here.



Our bias is positive, so  $\hat{\alpha}_1$  must be to the right of  $\hat{\beta}_1$ .

**Bias formula**  $\hat{\alpha}_1 - \hat{\beta}_1 = \hat{\beta}_2 * \hat{\gamma}_1 = (+)(+) = (+)$





# Let's just randomize people!

Pick 10,000 uninsured folks & randomly split them into two groups.

	<b>Uninsured</b> (n=213,714)	<b>Group A</b> (n=5,000)	<b>Group B</b> (n=5,000)	<b>Difference</b> (A – B)	<b>t-test</b> (P-value)
<b>Percent under 50 years</b>	60.9%				
<b>Percent men</b>	48.5%				
<b>Percent non-Latin white</b>	58.8%				<b>What do we expect the two groups to look like?</b>
<b>Percent married</b>	38.5%				
<b>Percent college-educated</b>	16.4%				
<b>Percent with income &lt;\$35,000</b>	71.3%				

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<b>Percent under 50 years</b>	60.9%	62.0%	60.1%	+1.9 pp	P=0.05
<b>Percent men</b>	48.5%	48.6%	49.0%	-0.4 pp	P=0.70
<b>Percent non-Latin white</b>	58.8%	57.9%	58.0%	-0.1 pp	P=0.98
<b>Percent married</b>	38.5%	37.1%	39.4%	-2.3 pp	P=0.02
<b>Percent college-educated</b>	16.4%	15.9%	16.3%	-0.4 pp	P=0.57
<b>Percent with income &lt;\$35,000</b>	71.3%	71.3%	70.6%	+0.7 pp	P=0.44

Notice that the groups are much more “balanced” on all variables than before.

# Let's just randomize people!

Pick 10,000 uninsured folks & randomly split them into two groups.

	<b>Uninsured</b> (n=213,714)	<b>Group A</b> (n=5,000)	<b>Group B</b> (n=5,000)	<b>Difference</b> (A – B)	<b>t-test</b> (P-value)
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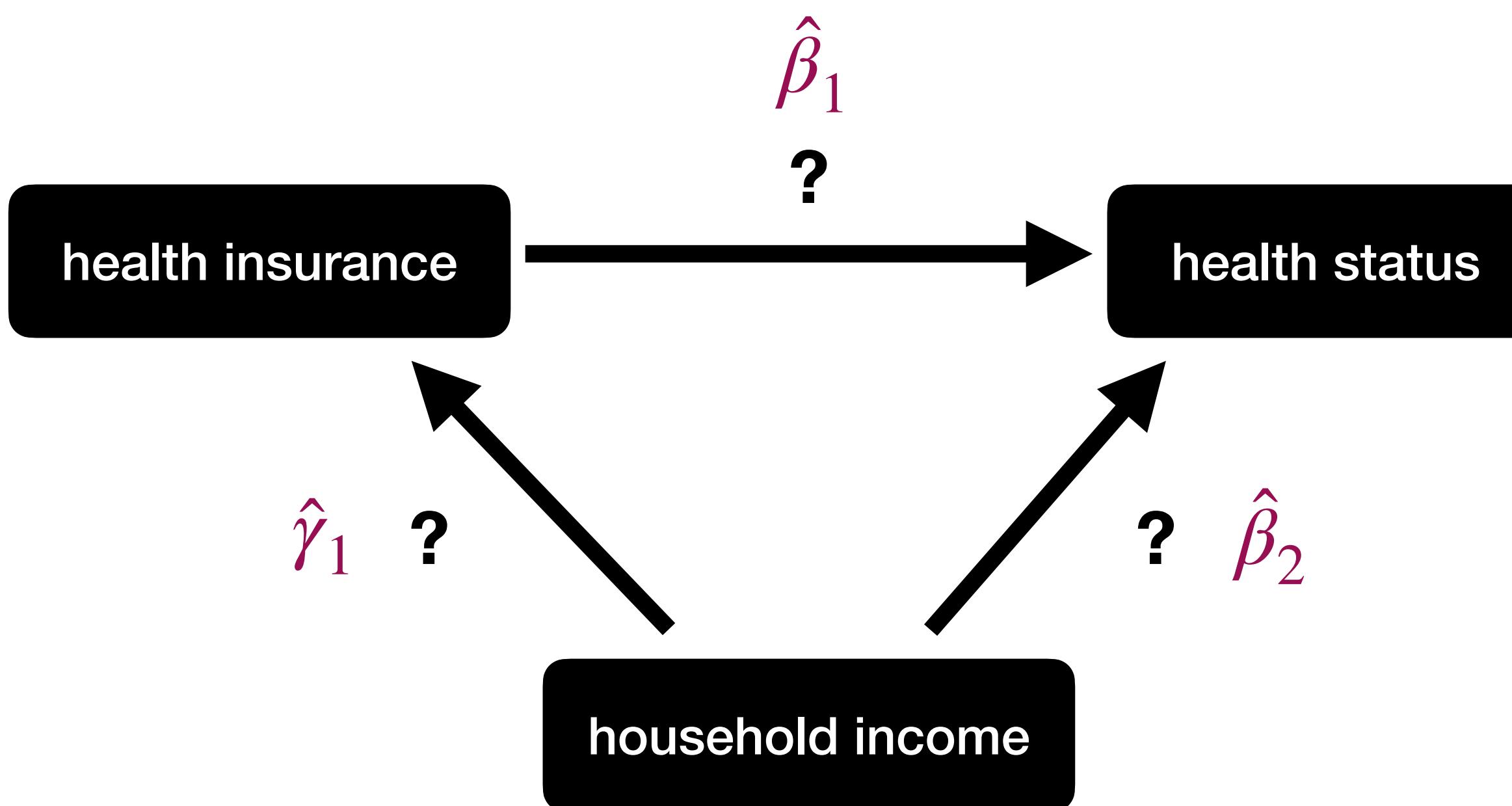
Sometimes we'll get "significant" values just due to chance. We should expect that about 5% of the time!

# What happens to the omitted variable bias?

Let's say that in our short regression, having insurance = better health.

$$\hat{\alpha}_1 > 0$$

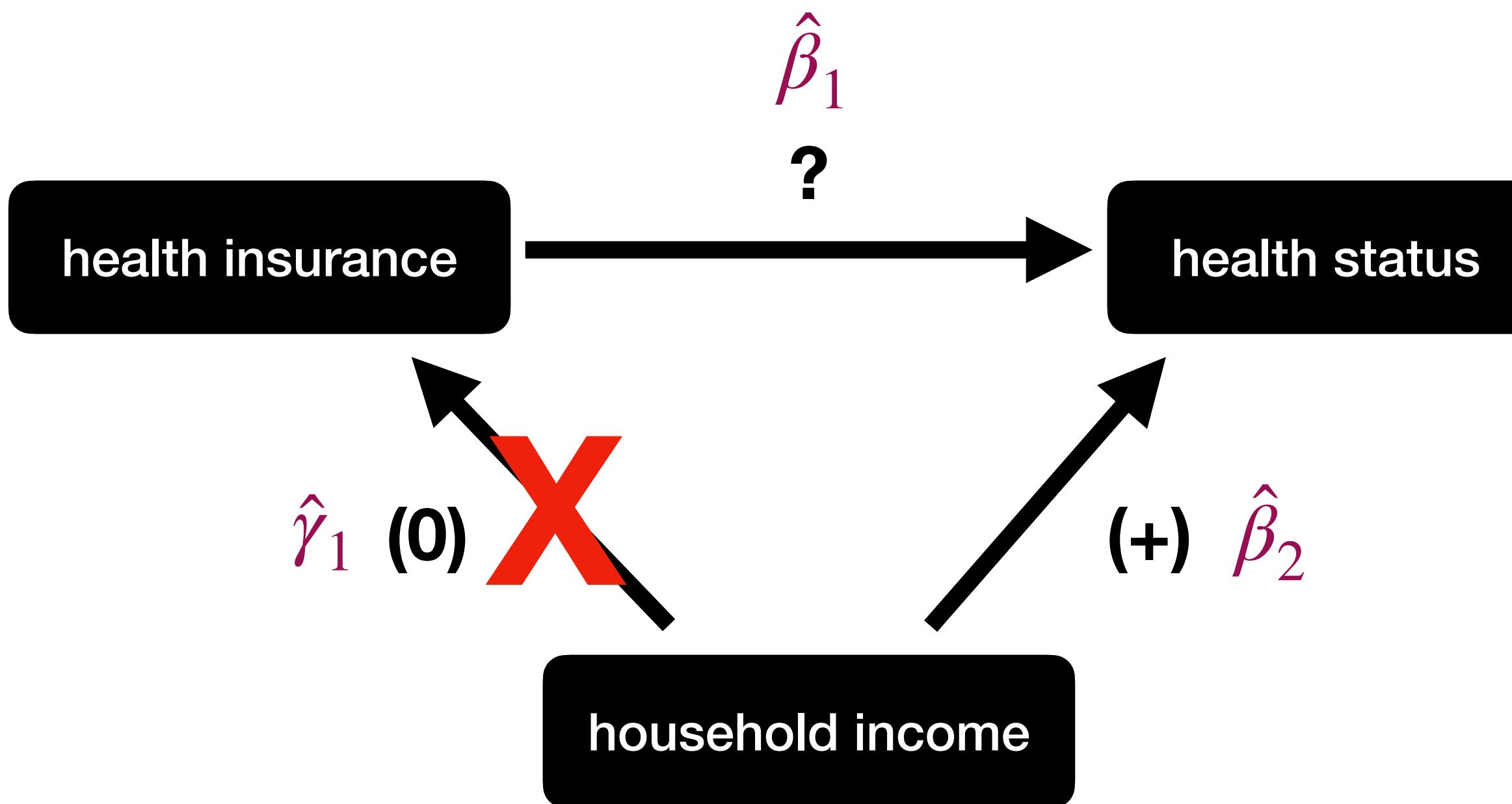
Now, sign the bias again.



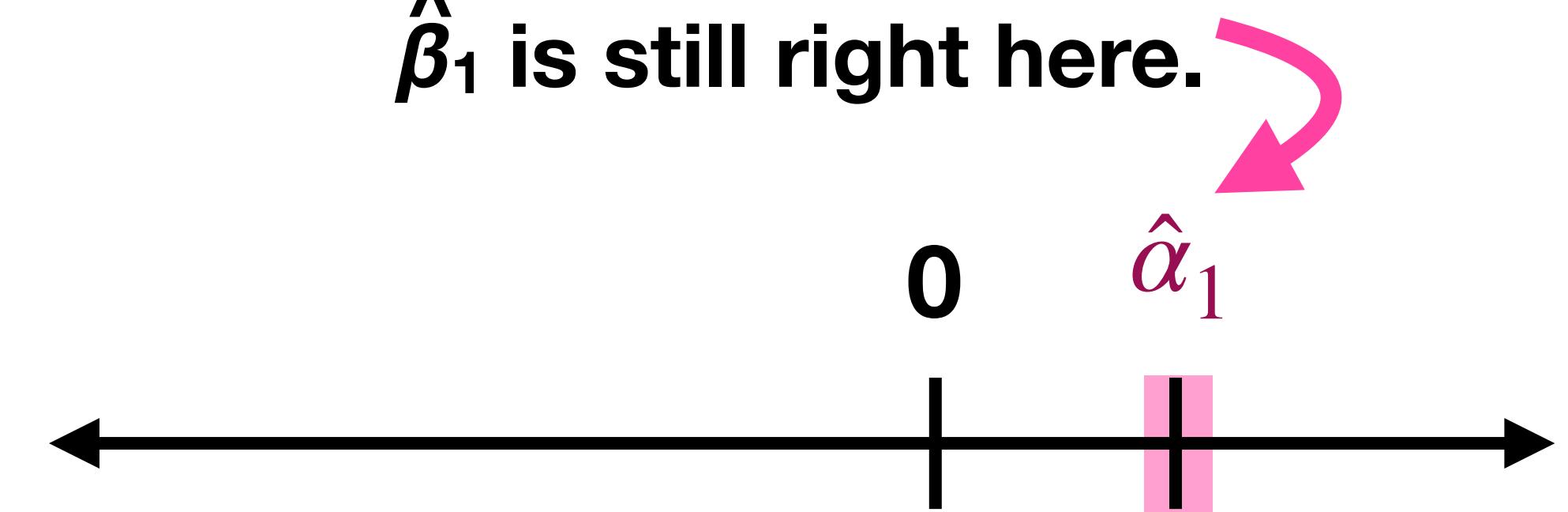
# What happens to the omitted variable bias?

Let's say that in our short regression, having insurance = better health.

Now, sign the bias again.



In a well-executed experiment,  
 $\hat{\beta}_1$  is still right here.



We have no bias, so  $\hat{\alpha}_1 = \hat{\beta}_1$ .

**Bias formula**  $\hat{\alpha}_1 - \hat{\beta}_1 = \hat{\beta}_2 * \hat{\gamma}_1 = (+) * 0 = 0$





Ha ha!  
Eliminating a million omitted variables

# **Someone actually did that!**

**The Oregon Health Insurance Experiment made an insurance lottery.**

**Lottery winners were *eligible to enroll* in Medicaid. But not all did.**

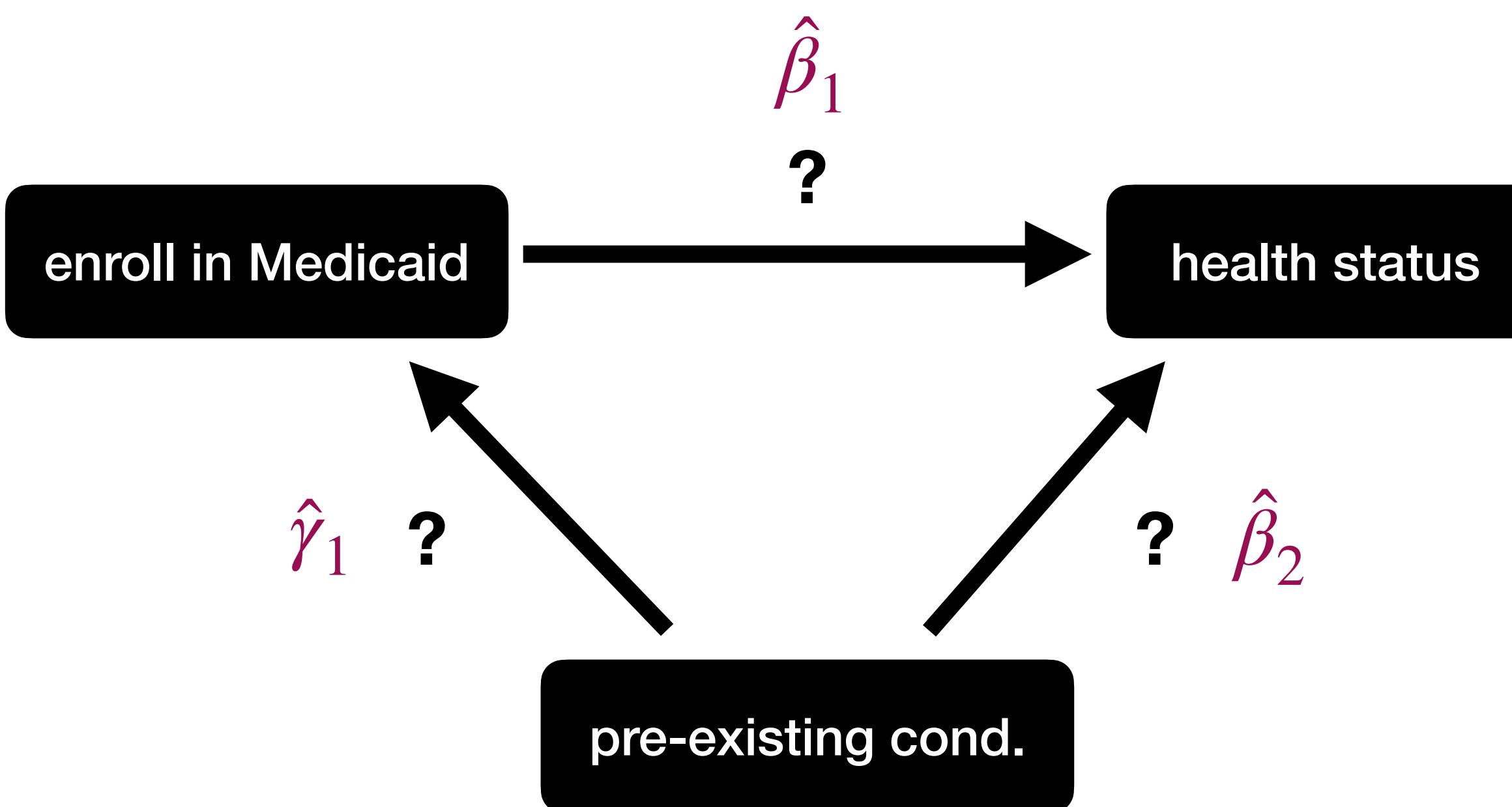
**When we analyze our experiment, whom should we compare?**

# Let's say we just analyze enrollees.

In our short regression, we find that Medicaid = better health.

What if only “sicker” people enrolled?

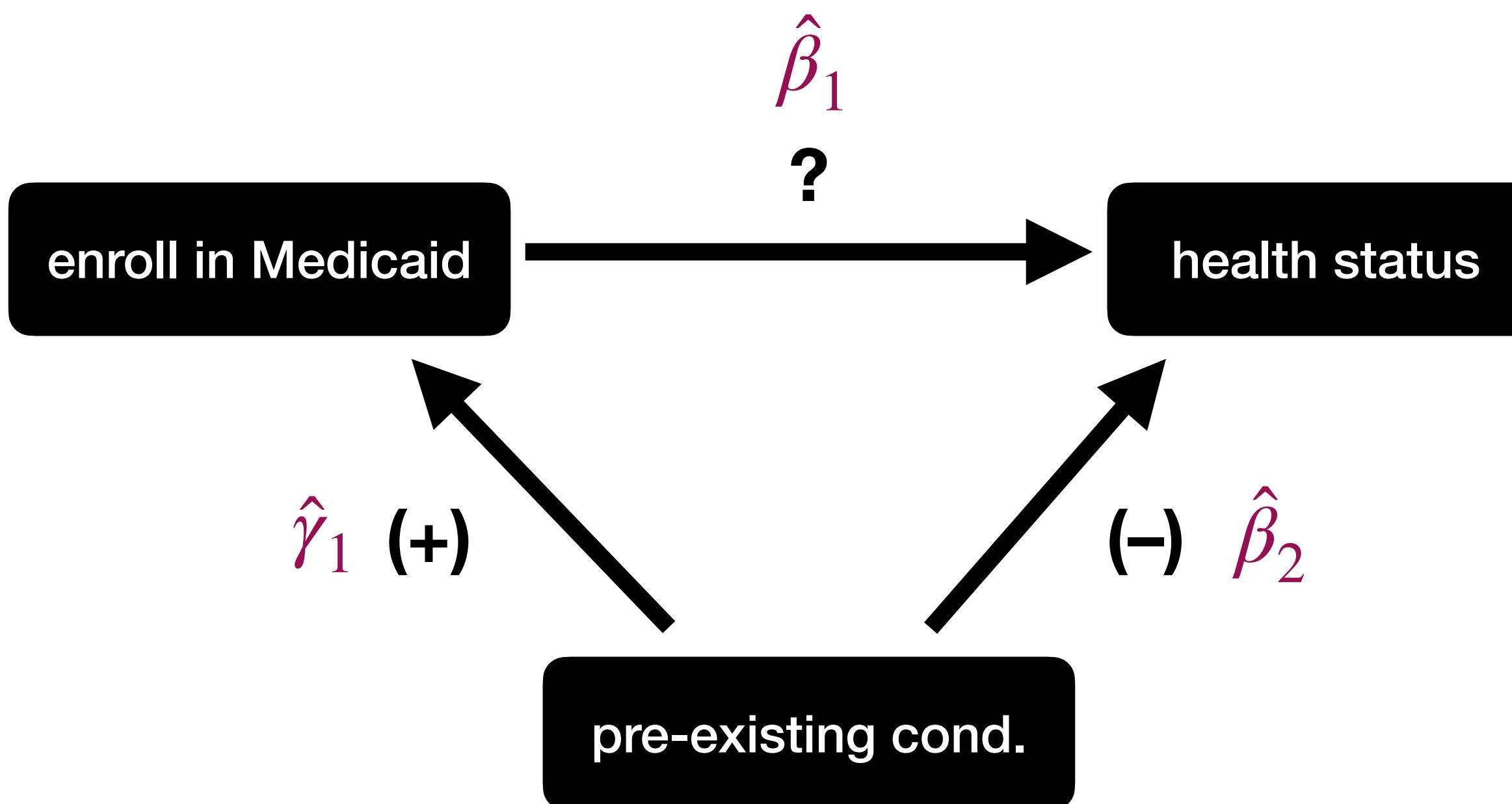
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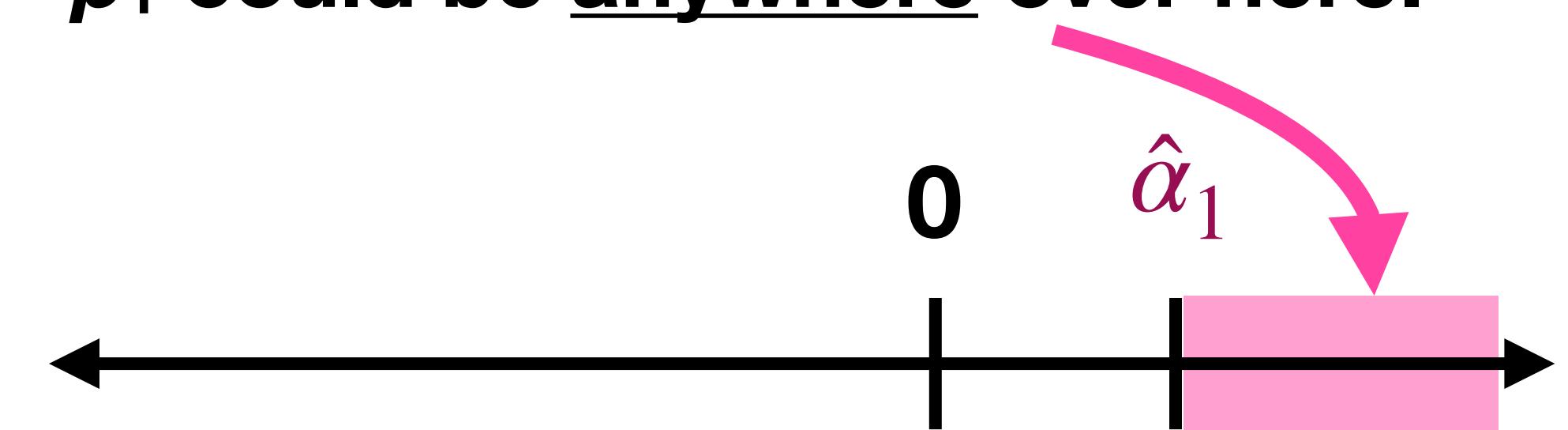
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What if only “sicker” people enrolled?



$$\hat{\alpha}_1 > 0$$

$\hat{\beta}_1$  could be anywhere over here.



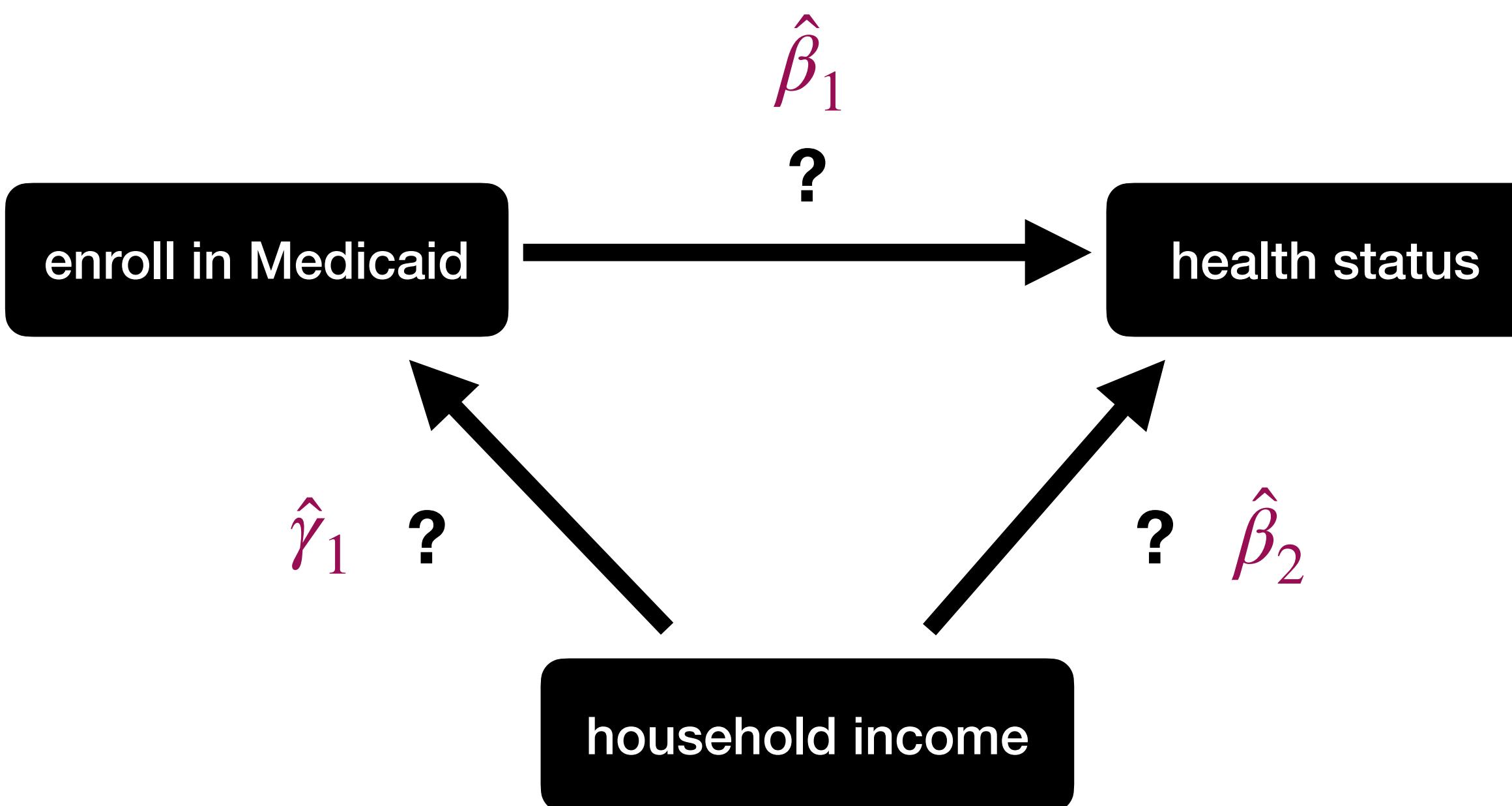
Our bias is negative, so  $\hat{\alpha}_1$  must be to the left of  $\hat{\beta}_1$ .

**Bias formula**  $\hat{\alpha}_1 - \hat{\beta}_1 = \hat{\beta}_2 * \hat{\gamma}_1 = (+)(-) = (-)$

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In our short regression, we find that Medicaid = better health.

What if only “richer” people enrolled?



$$\hat{\alpha}_1 > 0$$

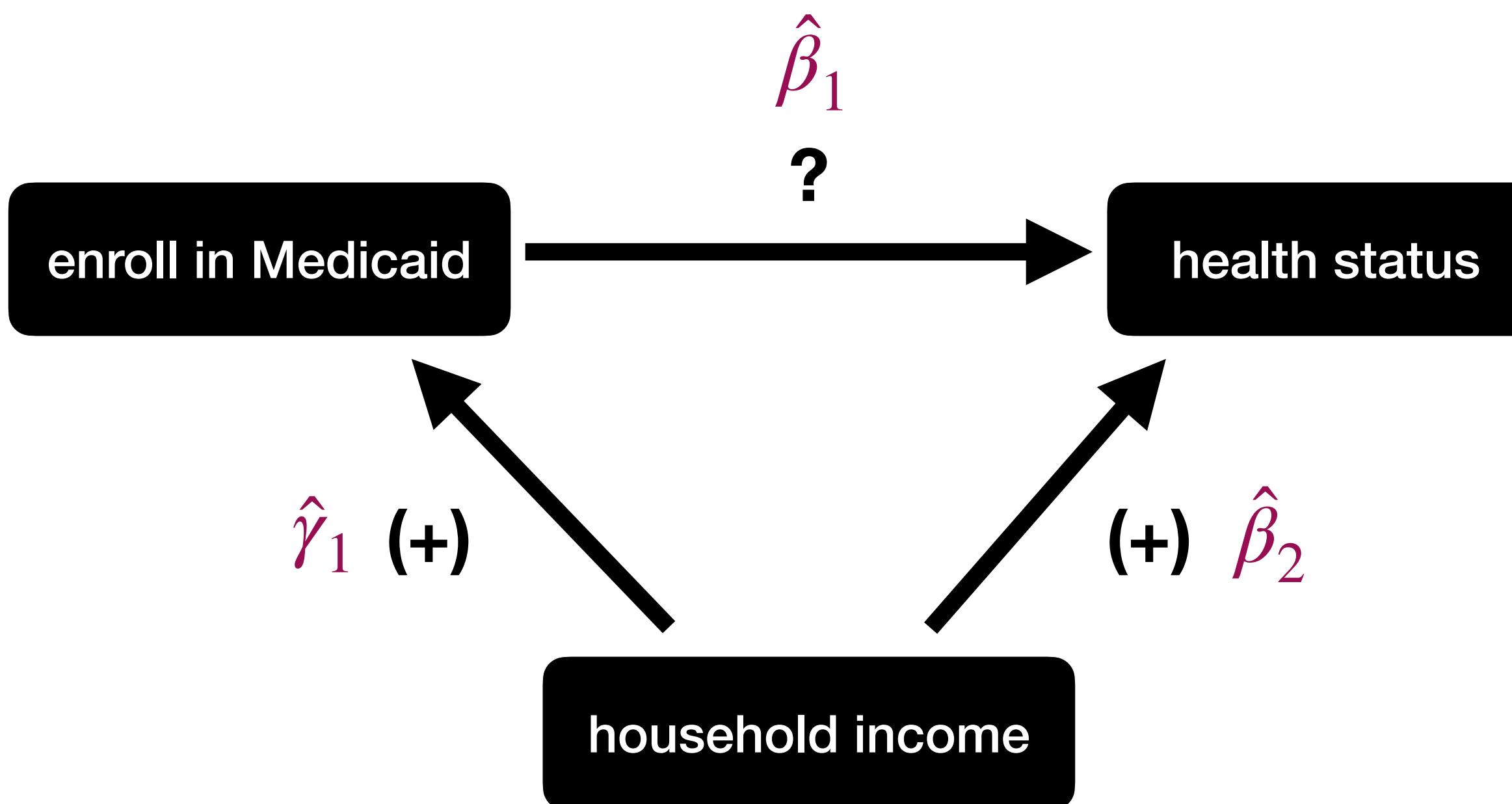


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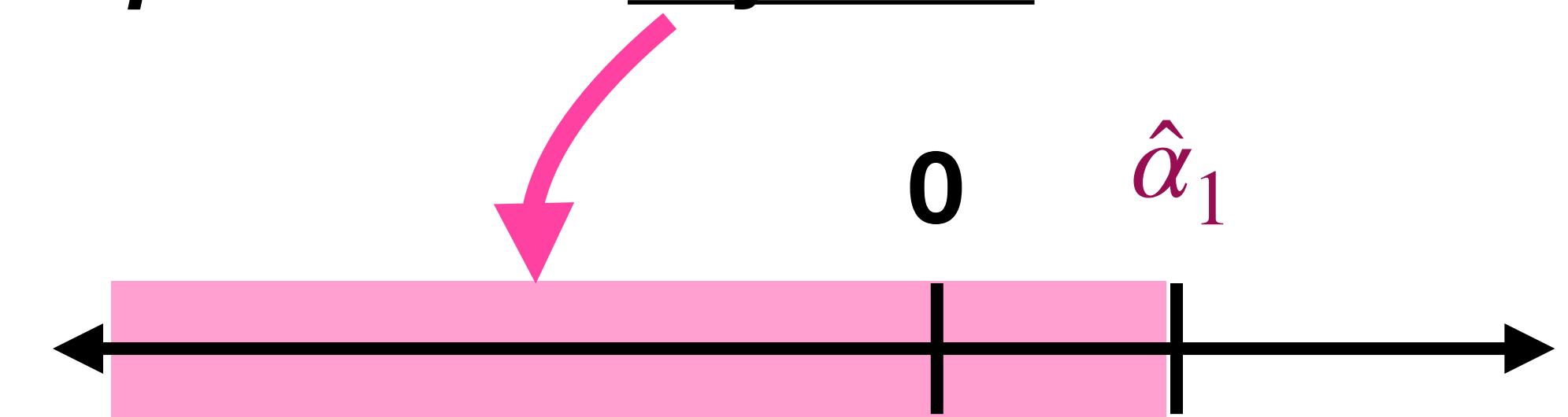
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Our bias is positive, so  $\hat{\alpha}_1$  must be to the right of  $\hat{\beta}_1$ .

**Bias formula**

$$\hat{\alpha}_1 - \hat{\beta}_1 = \hat{\beta}_2 * \hat{\gamma}_1 = (+)(+) = (+)$$



# This is why intention to treat matters.

We only have “balance” in our original, randomized sample.

Analyzing just enrollees breaks this balance since we now have a different sample that people selected into based on omitted variable(s).

Intention-to-treat analyses preserve the original randomization.

We just have a different interpretation: the effect of winning the lottery.

# Can experiments have other biases?

**Yes!**

**We are especially concerned about:**

- 1. Attrition** (which is like an omitted variable – hence, intention to treat)
- 2. Failures in randomization** (also like an omitted variable!)
- 3. Spillover** (also like an omitted variable!)

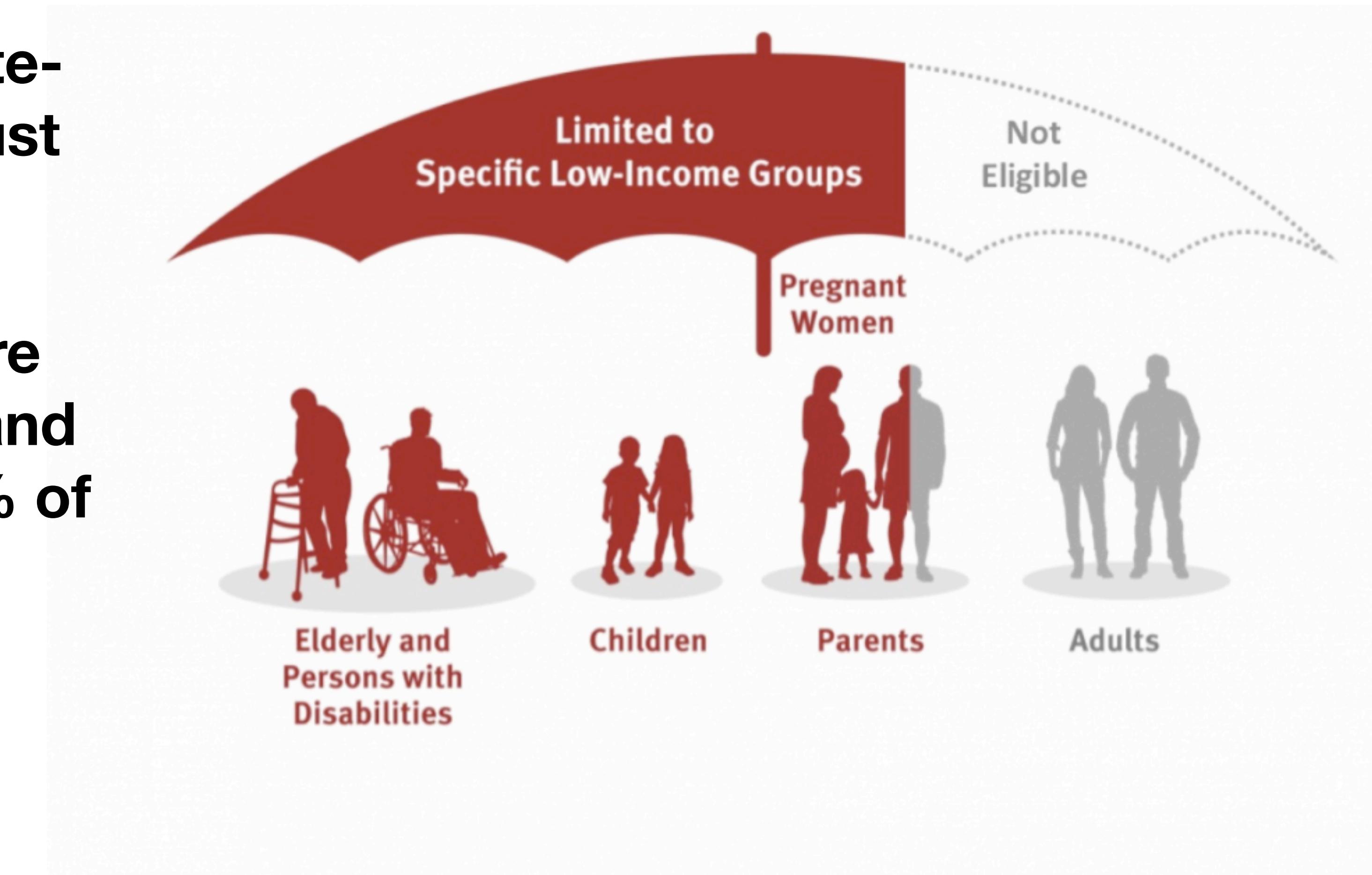
**Also, experiments can be expensive, impractical, or unethical.**

# What about a “natural experiment”?

Medicaid used to be a state-level insurance program just for specific populations.

In 2014, the Affordable Care Act allowed states to expand it to all citizens up to 138% of the federal poverty level.

In 2026, 138% FPL for a family of 4 is \$45,540.

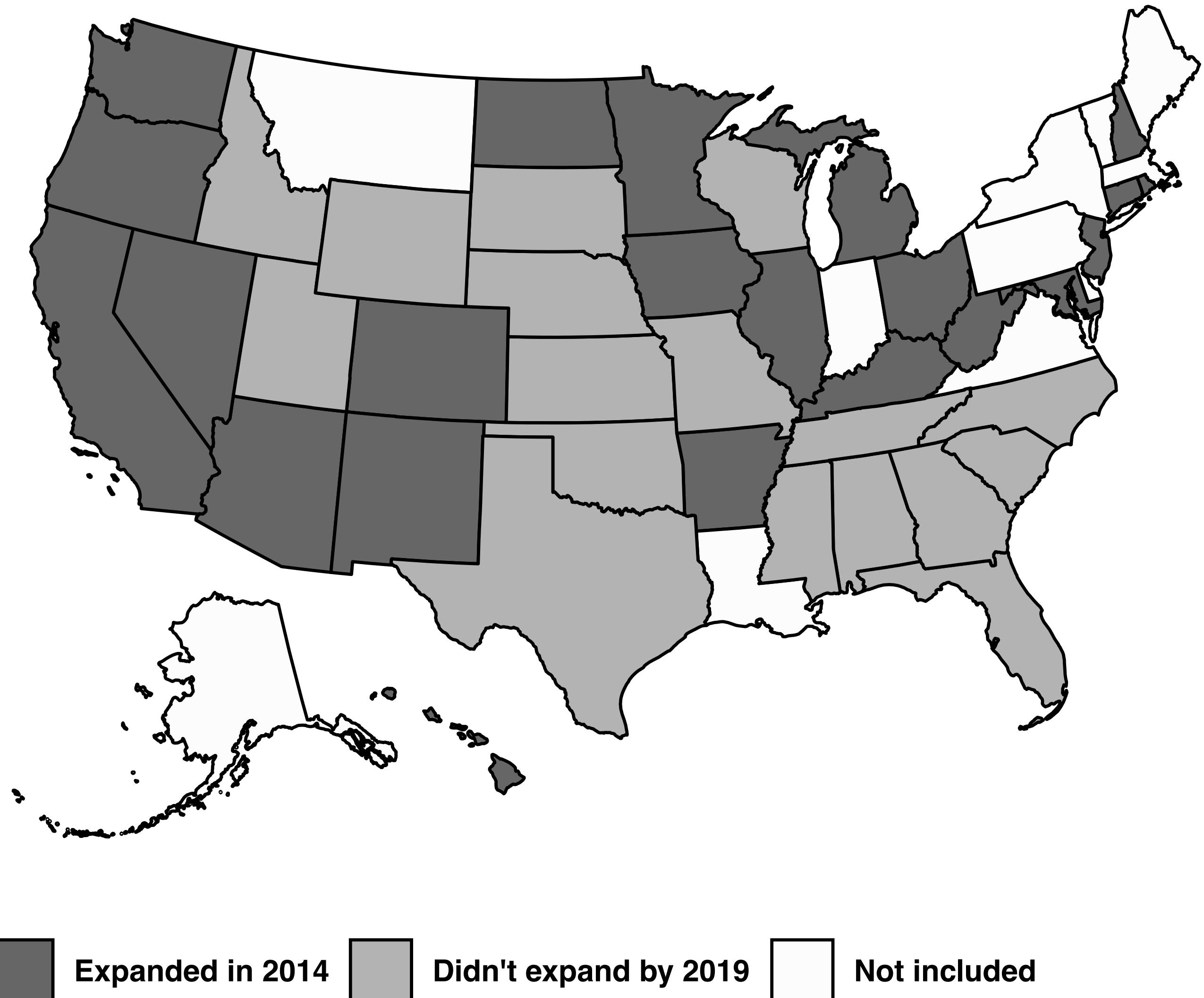


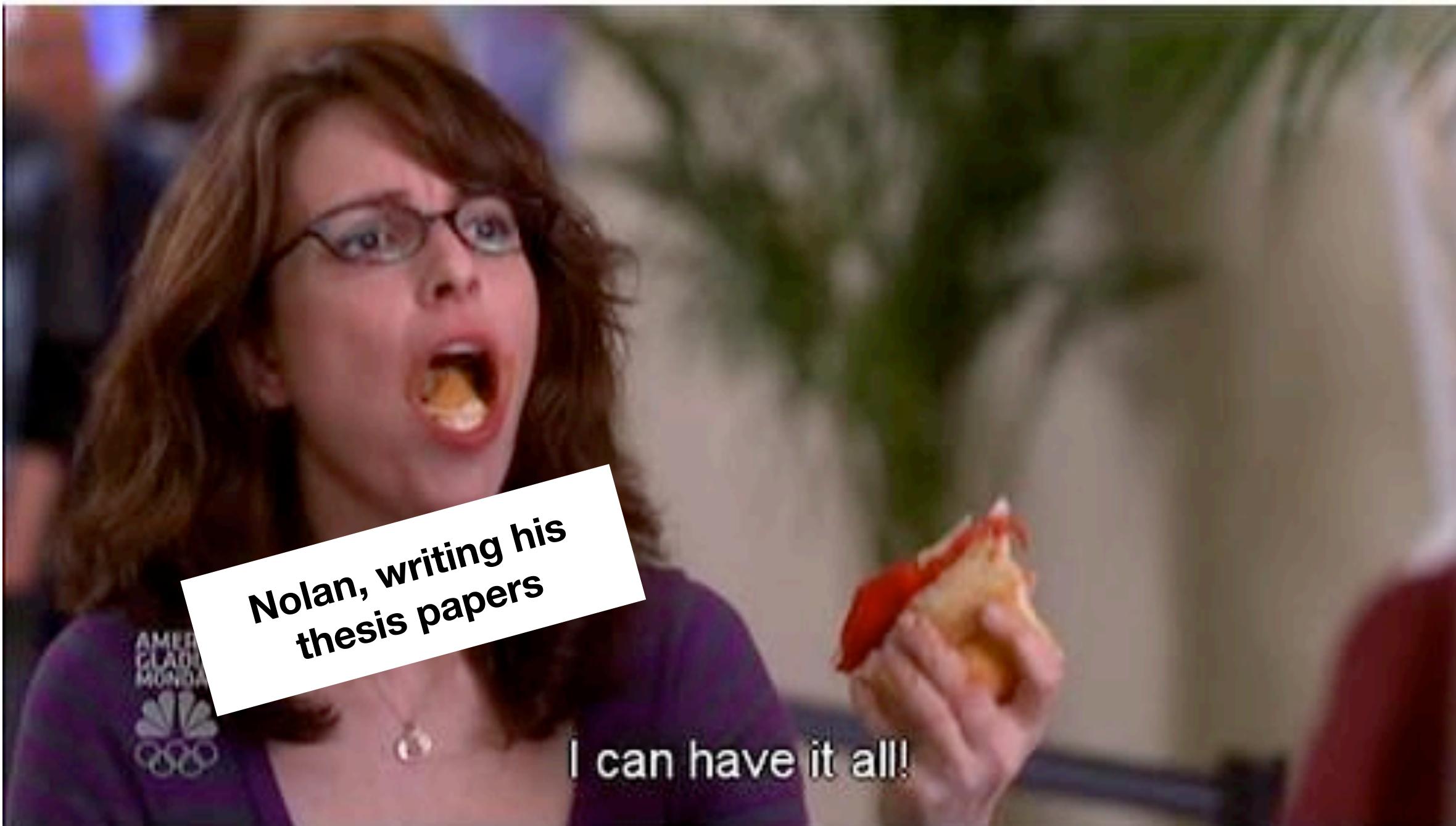
# What about a “natural experiment”?

**However, not every state chose to expand Medicaid.**

**We might call this a “natural experiment” and evaluate it as if it were randomized\*!**

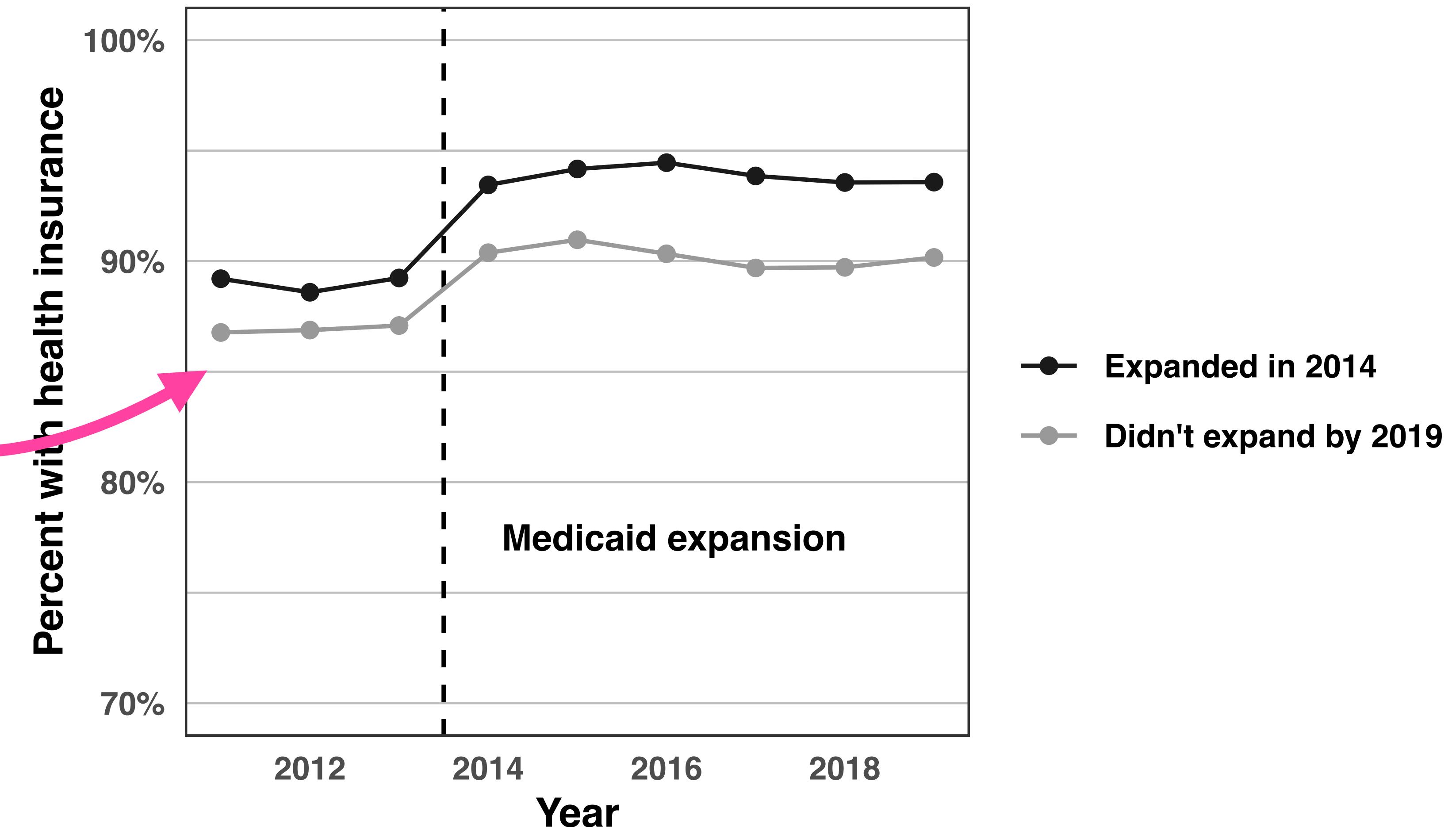
**\*Each state’s choice to expand isn’t really random, but if our difference-in-difference assumptions hold, we can pretend like it is!**





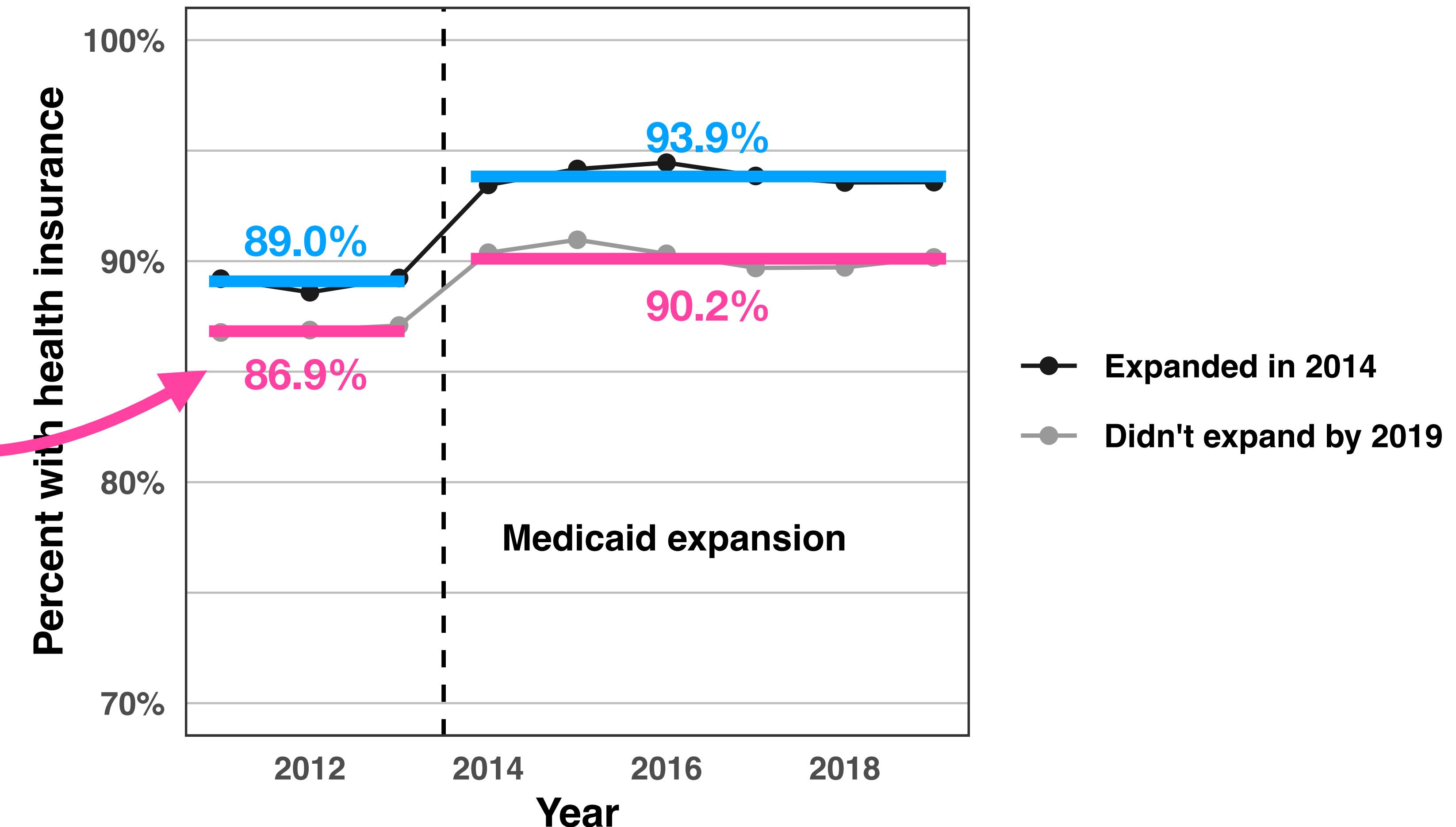
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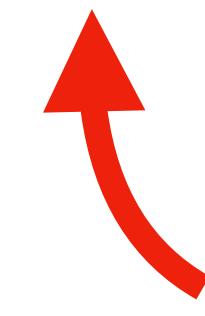
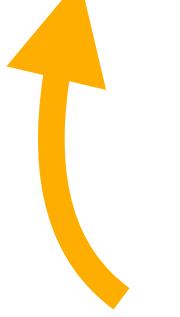
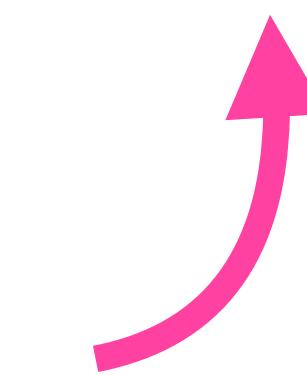
# Let's do a difference-in-differences!

$$(insurance)_i = \hat{\beta}_0 + \hat{\beta}_1(expansion)_i + \hat{\beta}_2(post\_2014)_i + \hat{\beta}_3(expansion * post\_2014)_i + \hat{u}_i$$

**dummy for expansion**

1 = Expanded in 2014

0 = Didn't expand by 2019



**dummy for time**

1 = June 1, 2014 or later

0 = Before 2014

**interaction**

i.e. the diff-in-diff

	<b>Before 2014</b> post_2014 = 0	<b>After 6/1/2014</b> post_2014 = 1	<b>Difference</b>
<b>Didn't expand by 2019</b> expansion = 0			
<b>Expanded in 2014</b> expansion = 1			
<b>Difference</b>			

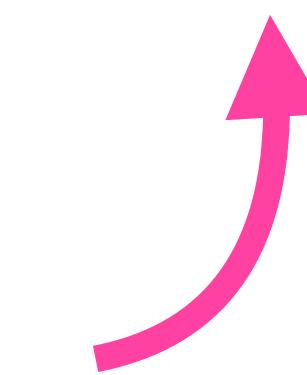
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# What omitted variables are we eliminating?

	<b>Before 2014</b> post_2014 = 0	<b>After 6/1/2014</b> post_2014 = 1	<b>Difference</b>
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<b>Difference</b>	$\hat{\beta}_1$	$\hat{\beta}_1 + \hat{\beta}_3$	$\hat{\beta}_3$

# What omitted variables are we eliminating?

**omitted variables that vary between states but not over time**

e.g. demographics that don't change within a state over time

**What's left? Omitted variables that vary by state and time.**

e.g. changes in state policies that differently affect the groups

**omitted variables that vary over time but are the same between states**

e.g. national economic trends that affect both groups of states

	<b>Before 2014</b> post_2014 = 0	<b>After 6/1/2014</b> post_2014 = 1	<b>Difference</b>
<b>Didn't expand by 2019</b> expansion = 0	$\hat{\beta}_0$	$\hat{\beta}_0 + \hat{\beta}_2$	$\hat{\beta}_2$
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<b>Difference</b>	$\hat{\beta}_1$	$\hat{\beta}_1 + \hat{\beta}_3$	$\hat{\beta}_3$

Diagram illustrating the omitted variable bias: A yellow arrow points from the first column to the second column, indicating the coefficient  $\hat{\beta}_1$ . A red arrow points from the second column to the third column, indicating the coefficient  $\hat{\beta}_3$ .



# Show me the regression already!

	insurance
<b>Intercept</b>	<b>0.869***</b> (0.007)
<b>expansion</b>	<b>0.021*</b> (0.009)
<b>post_2014</b>	<b>0.033***</b> (0.003)
<b>expansion * post_2014</b>	<b>0.016**</b> (0.005)
Num.Obs.	2,253,130
R2	0.008
R2 Adj.	0.008

\*p<0.05, \*\*p<0.01, \*\*\*p<0.001

**Note:** `insurance` was measured as 0–1.

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**The insurance rate in the non-expansion states was 86.9% before 2014.**

(Note: We're comparing groups within the interaction, so we don't have to say "holding time constant" since that's necessarily implied by the interaction terms.)

**The difference is statistically significant.**

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The difference in insurance rates between expansion and non-expansion states before 2014 was 2.1 percentage points (pp).

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The insurance rate in non-expansion states rose by 3.3 pp after 2014.\*

Alternatively, the insurance rate in non-expansion states was 3.3 pp higher after 2014 than it was before 2014.

The difference is statistically significant.

\*This is not a causal statement; it just describes what happened.

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The difference-in-differences for insurance rates was 1.6 percentage points.

That is, the difference in insurance rates over time for expansion states, compared to the difference over time for non-expansion states, was 1.6 pp.

The difference is statistically significant.

Note: **insurance** was measured as 0–1.

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To a policymaker, we could say, “The causal effect of Medicaid expansion was to increase health insurance coverage by 1.6 percentage points in expansion states, relative to non-expansion states.”

The difference is statistically significant.

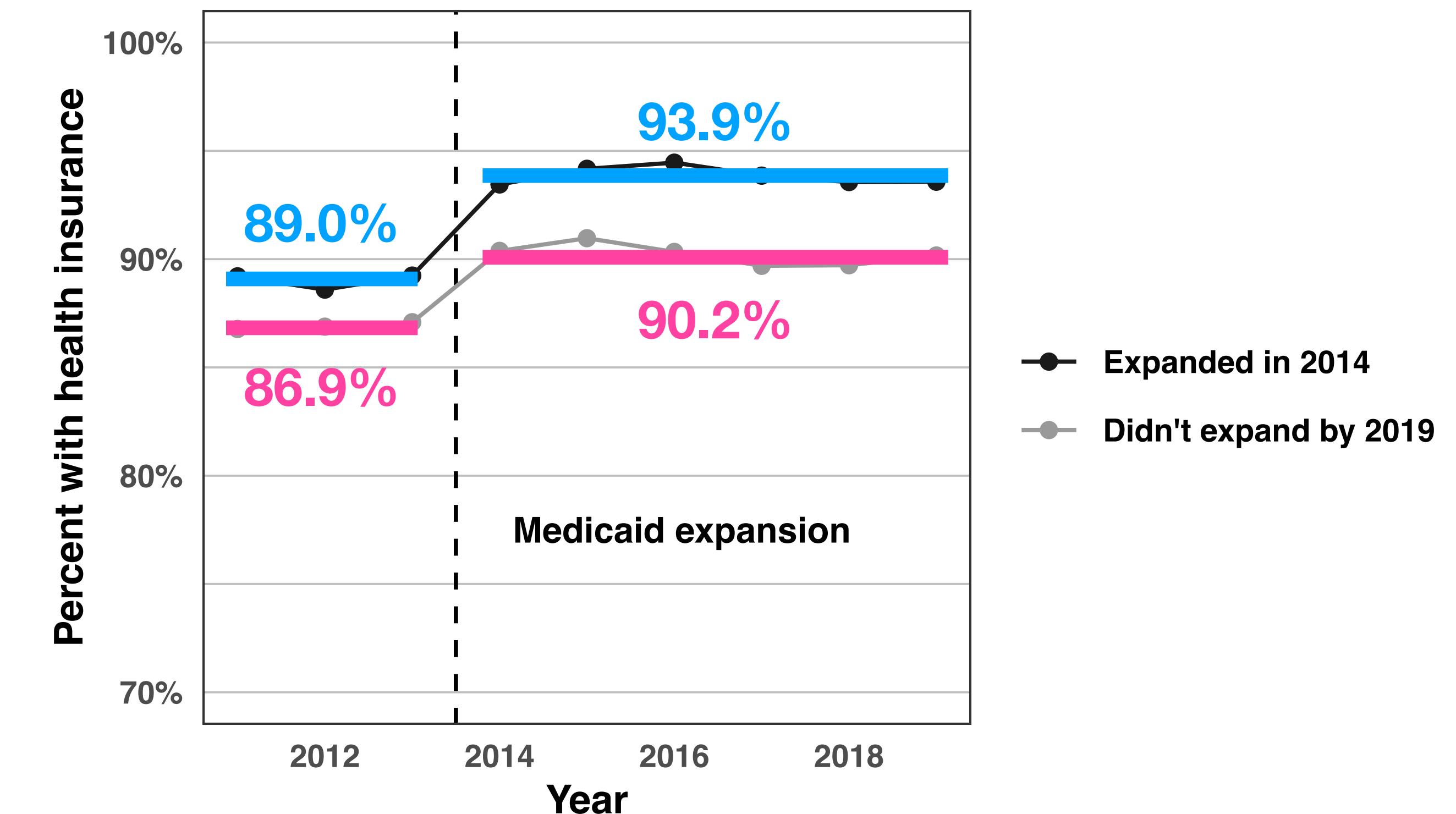
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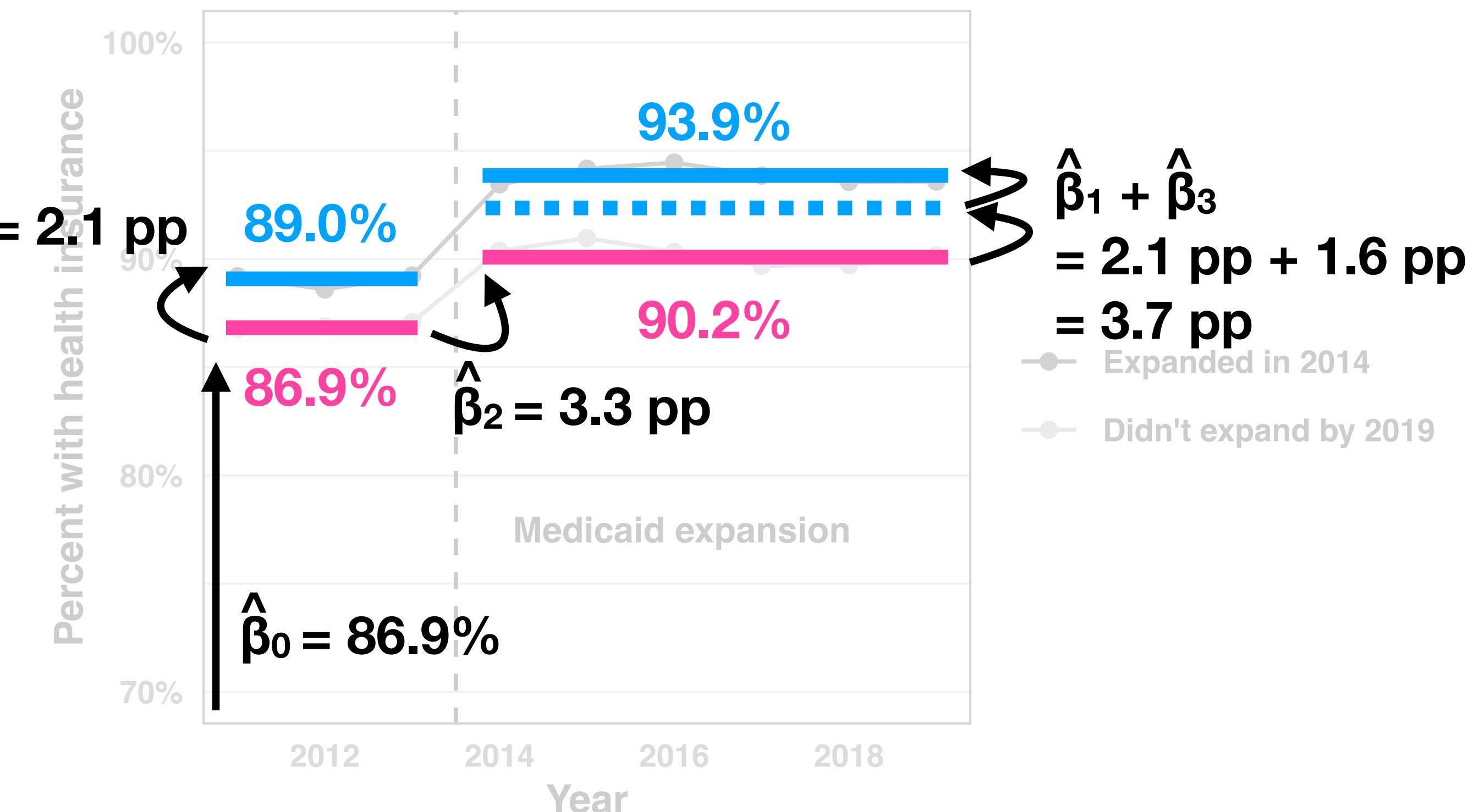


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R2	0.008
R2 Adj.	0.008

\*p<0.05, \*\*p<0.01, \*\*\*p<0.001



$$(insurance)_i = \hat{\beta}_0 + \hat{\beta}_1(expansion)_i + \hat{\beta}_2(post\_2014)_i + \hat{\beta}_3(expansion * post\_2014)_i + \hat{u}_i$$

Note: insurance was measured as 0–1.

# But is it causal?

Again, causality is a spectrum.

We have to evaluate the assumptions.

But here, I would say yes, causal!

...unless we can think of “killer”  
state-variant omitted variables.

