

EMR = perpendicular electric and magnetic fields



$$v = c = 3.0 \times 10^8 \text{ m/s}$$

$$v = f\lambda \rightarrow c = f\lambda \quad c \text{ is constant for all EMR}$$

All EMR has accelerating charges, which cause the fields to form  
↳ different sources

#### PARTICLE

- Straight lines
- Travels through vacuum
- Reflection

#### WAVE

- Diffraction
- Non-sharp shadows
- Wavelets
- Refraction (incident = ref + refl)
- Double slit experiment

Evidence of wave-particle duality (both are true)

#### Maxwell's predictions

- EMR is produced when a charge accelerates
- Frequency of charge moving = wave frequency
- All EMR travels at  $c$ , the speed of light
- Electric and magnetic components are perpendicular to each other as well as the direction of travel
- EMR follows all wave equations ( $c = f\lambda$ , etc)

Hertz proved these by switching the direction of an circuit (AC). This created a EMR wave, and used the hand rules to determine that the two components are perpendicular

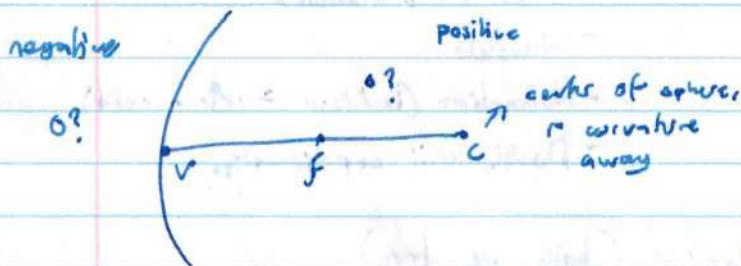
- He also created a standing wave by using a reflection, which allowed him to measure  $\lambda$  and  $c$

## Speed of light

- Galileo: two people turning on lamps a known distance apart
- Römer: calculating the delay between two planets at different distances from the earth
- Fizeau-Foucault: Spinning mirror. If the spinning mirror's frequency aligned with the (known) distance and speed, the light would always be visible
  - ↳ First accurate measure
  - ↳ Michelson: 8-sided mirror turning

## Reflection

- Incident = Reflected (regular surface)
- Flat mirrors create virtual images



- Rays coming in parallel to the mirror go through the focus (and  $\Rightarrow$ )

- Rays going through the center go through the center

$$\frac{1}{f} = \frac{1}{d_o} + \frac{1}{d_i}$$

Focus point is halfway between vertex and center

$$m = \frac{h_i}{h_o} = -\frac{d_i}{d_o}$$

$m > 1$  enlarged  
 $0 < m < 1$  diminished  
 $m < 0$  inverted

## Refraction

Snell's law

$$\frac{\sin \theta_1}{\sin \theta_2} = \frac{n_2}{n_1} = \frac{\lambda_1}{\lambda_2} = \frac{v_1}{v_2}$$

$n$  is refraction index

refraction can change

$$\begin{aligned} n_{\text{air}} &= 1 \\ v_{\text{air}} &= c \end{aligned}$$

the color of light bc  $\lambda$  can change ( $f$  stays constant)





## Prisms

Critical angle = angle where the angle of refraction is  $90^\circ$   
(light ray is trapped)

→ changes with different media

→ If incident angle > critical angle, the ray will reflect

→ fibre-optic cable

Different wavelengths reflect at different angles

→ shorter wavelengths reflect more

→ the prism effect

## Lenses

Use refraction to diver light rays

→ Diverging and converging lenses

→ Real images on other side of the lens, virtual on same side

Lensmaker's equation  $\frac{1}{f} = (n-1) \left( \frac{1}{R_1} - \frac{1}{R_2} \right)$

## Diffraction

- Waves are made of many point sources which have concentric waves producing from each point

- Diffraction: curving of light around openings (because of wavelets)

- Supports wave theory

- Double slit → interference caused by diffraction (creates orders of light lines)

Small angles:  $\lambda = \frac{x d}{n L}$

Resolve formula:  $\lambda > \frac{d \cdot \sin \theta}{n}$

Diffraction grating: many small slits (more precision for measuring  $\lambda$ )

## Polarization

Reducing an EMR wave to just one component by only letting that part through





## Quantum mechanics

- Blackbody: body that absorbs all EMR (emits as blackbody radiation)
- Difference between intensity and frequency of blackbodies
  - Cannot be explained by classical physics
- Planck: minimum amount of energy (per  $f$ ) can be transferred by EMR
  - $E = hf$  ( $h$  = Planck's constant) (smallest piece = quanta)
  - energy is quantized, not continuous (particle model) (light particle = photon)
- Photoelectric effect: photons can knock electrons off of metal plates
  - elastic collision where photon is destroyed
  - threshold frequency ( $f_0$ ): smallest frequency that causes the effect
  - energy needed to "snap off"  $e^-$  = work function (different for each metal)
  - $E = hf$  →  $W = hf_0$
  - Threshold  $\lambda$  instead of  $f$ : convert using  $c$  = speed of light
  - Photoelectric effect can be used to ~~detect~~ create a current
  - $E_{k, \max}(\text{electron}) = q(\text{elementary}) \cdot V_{\text{stop}}$  (voltage needed to stop current)
  - Photoelectric formula:  $hf = E_{k, \max} + W = E_{k, \max} + hf_0$
  - Energy-frequency graph: y-int = work function, x-int = threshold  $f$ , slope = Planck's constant

## Compton

- Momentum of photons:  $p = \frac{h}{\lambda} = \frac{hf}{c}$
- X-rays scatter electrons when they hit metals (Compton effect) (momentum)
- $\Delta\lambda (\text{x-ray}) = \frac{h}{mc} (1 - \cos \theta)$

## De Broglie

- Combined wave and particle formulae
- $\lambda = \frac{h}{mv}$  (De Broglie wavelength of a moving particle)
- Turn "solid" calculations into  $\lambda, f$



### 13.4.1 Diagrammes de rayons [miroirs]

Image virtuelle = image de laquelle les rayons semblent provenir

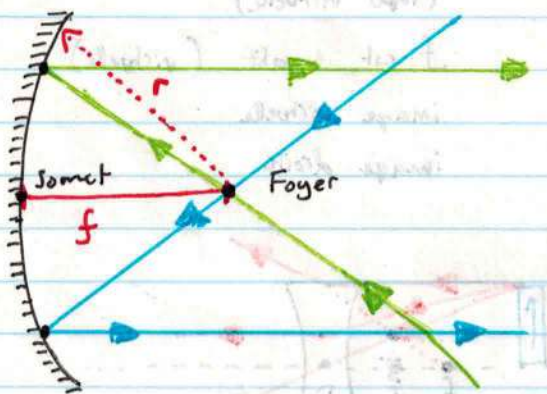
Image réel = image de laquelle les rayons proviennent

↳ peut être formé sur un écran

$m = h_i / h_o$  ( $m$  = grossissement,  $h_i$  = hauteur de l'image,  $h_o$  de l'objet)

↳ Orientation = inversée ou droite

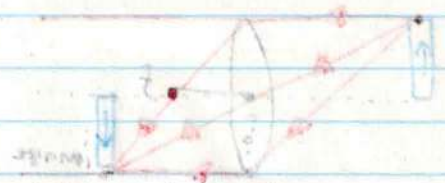
↳ Magnification négatif = changement d'orientation



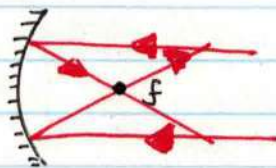
Miroir Convergente

$f$  = distance focale

$r$  = rayon de courbure



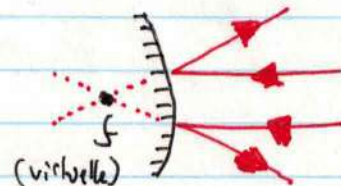
Miroir divergente



$f$  est positif (avant)

image réel crée

image est inversée  
(hauteur négatif)



(virtuelle)

$f$  est négatif (arrière)

image virtuelle crée

image droite  
(hauteur positif)

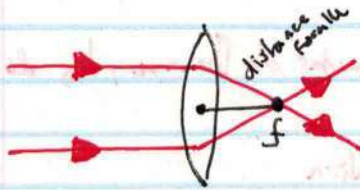
$$\frac{1}{f} = \frac{1}{d_o} + \frac{1}{d_i} \quad (\text{les lentilles minces})$$

$$m = \frac{h_i}{h_o} = -\frac{d_i}{d_o} \quad (\text{les lentilles minces})$$

# Les diagrammes à rayons [lentilles]

$$\frac{1}{f} = \frac{1}{d_o} + \frac{1}{d_i}, \quad m = \frac{h_i}{h_o} = -\frac{d_i}{d_o}$$

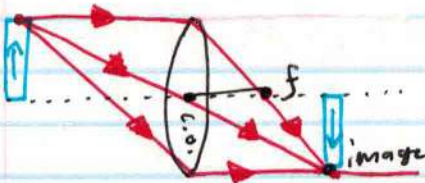
Lentille convergente



$f$  est positif (réel)

image réel

image inversé



Lentille divergente

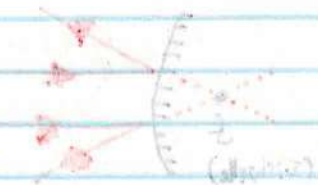
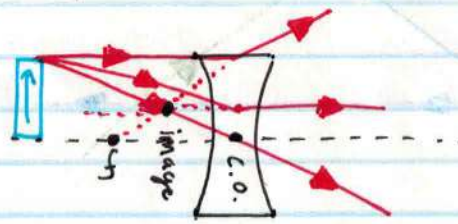


(foyer virtuelle)

$f$  est négatif (virtuelle)

image virtuelle

image droite

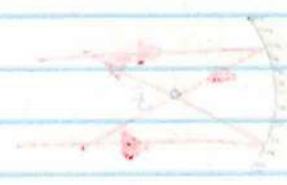


(image virtuelle)

image virtuelle

image droite

(l'objet est à gauche)



(image virtuelle)

image virtuelle

image est inversé

(l'objet est à droite)

$$\frac{1}{f} = \frac{1}{d_o} + \frac{1}{d_i}$$

$$m = \frac{h_i}{h_o} = -\frac{d_i}{d_o}$$

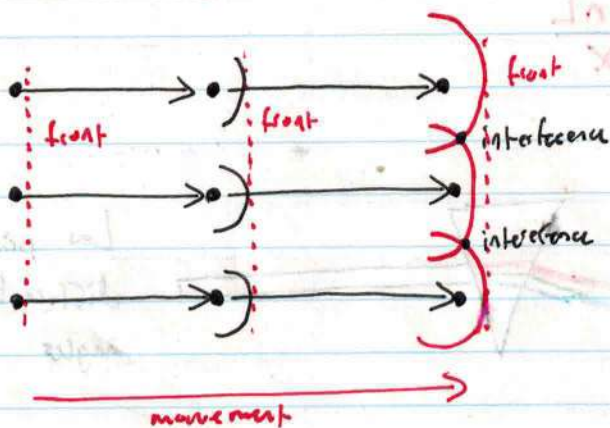


## Diffraction et interference

Ventre - point d'interaction entre les ondes [positif / constructif]

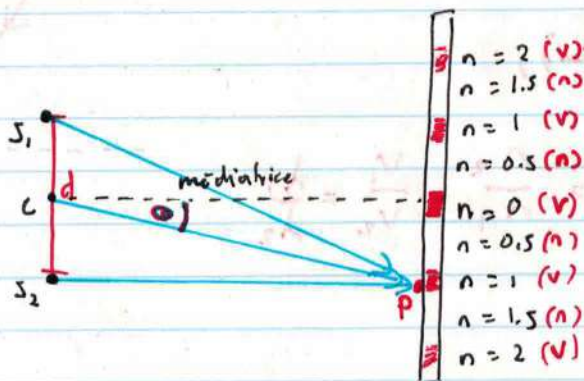
Noeud - point d'interaction entre les ondes [negatif / destructif]

### Principe de Huygens



Quand une onde se propage, les ondettes (ondes secondaires) se propagent d'une manière concentrique. Ils peuvent interférer avec eux-mêmes.

### Expérience de Young

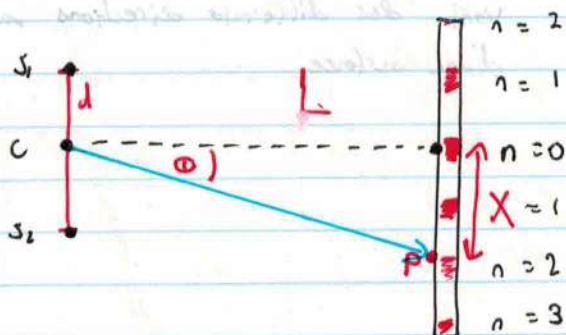


Quand il y a de l'interférence constructive, une lumière forte est projetée sur l'écran (destructif = pas de lumière)

$$\lambda = \frac{d \cdot \sin(\theta)}{n}$$

$n - \frac{1}{2}$  si destructif

### → Approximation



$$\lambda \approx \frac{Xd}{nL}$$



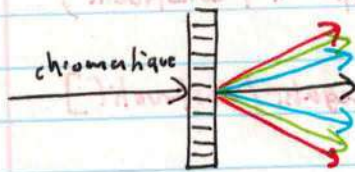
Plus fort  
d est pr  
a 1

Ceci est assuré par le principe de Huygens

Diffraction = Les rayons courbent quand ils passent par un trou



## Réseau de diffraction



Un réseau de diffraction comprend une surface avec beaucoup de lignes parallèles espacées également (comme grating, mais plus de trous)

$$\lambda = \frac{x d}{n L} \rightarrow d = \frac{\lambda n L}{x}$$

## Prismes (réfraction)

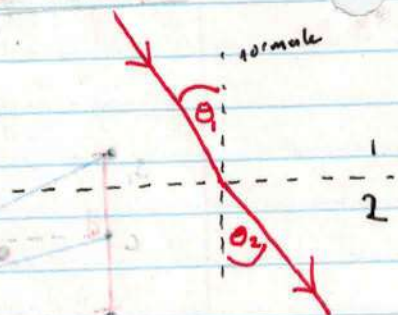


Les prismes réfractent les différents  $\lambda$  à différents angles

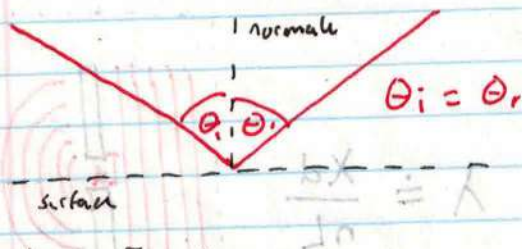
## Réfraction

$$n = \frac{c}{v} \quad (n = \text{indice de réfraction})$$

$$\frac{\sin \theta_i}{\sin \theta_r} = \text{constante}, \quad \frac{\sin \theta_1}{\sin \theta_2} = \frac{n_2}{n_1} = \frac{v_1}{v_2} = \frac{\lambda_1}{\lambda_2}$$



## Réflexion



Sur presque toute les surfaces, les rayons vont des différentes directions au cours d'une surface

## Autre Formules

$$f = \frac{c}{\lambda} \rightarrow \text{vitesse de la lumière}$$



## Mechanique Quantique

Corps noir - une corps celeste qui absorbe toute energie electromagnetique qui entre en contacte

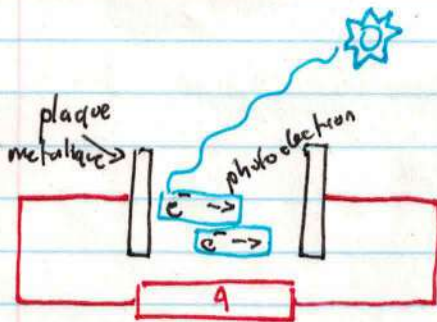
Quantum - plus petit quantite d'energie que possede une rayonnement d'une  $\lambda$  donnee

↳ photon - un quantum de REM (particule lumineuse)  $\frac{N}{s} = \frac{N}{q} \cdot \Delta \lambda$

Loi de Planck :  $E = nhf$

( $E$  = energie,  $n = 1, 2, 3$  etc;  $h$  = constante de Planck;  $f$  = frequence)

### Effet photoelectrique



Une rayonnement d'haute intensite peut causer les electrons de se separer d'une metal

Seuil de frequence: le plus petit frequence une onde peut avoir pour causer l'effet  
↳ Energie d'ionisation = energie minimale

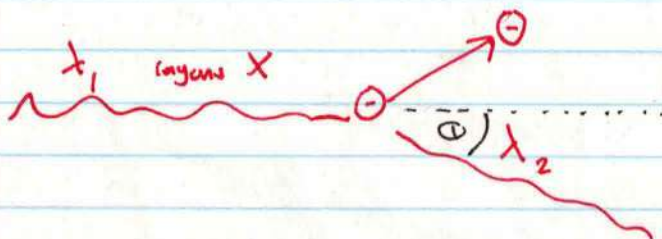
$$E = hf = E_c + W \quad \rightarrow \quad E_{c \text{ max}} = qV$$

travailcharge

### Effet Compton

Diffusion Compton : diffusion de rayons X par des electrons

Effet compton: Variation de  $\lambda$  des rayons X diffracts



$$p = \frac{h}{\lambda} \quad (\text{quantite de mouvement des rayons X})$$

$$\Delta \lambda = \lambda_f - \lambda_i = \frac{h}{mc} (1 - \cos \theta)$$

↳ Quantite de mouvement applique

$\theta$  = angle de diffusion

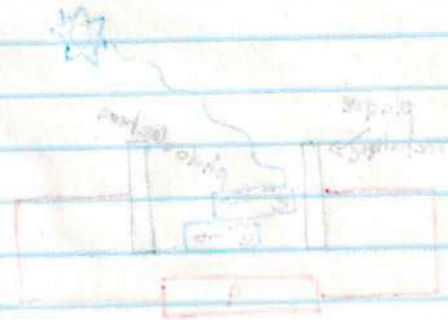
## De Broglie Hypothesis

$$\lambda = \frac{h}{p} = \frac{h}{mv} \quad \text{pour les electrons ?}$$

## Principe de Heisenberg

$$\Delta x \Delta p = \frac{h}{2} \rightarrow \text{On ne peut pas savoir la quantité de mouvement et la position d'une photon}$$

On peut représenter le REM comme particule et/ou onde



$$E = hf = E_{\text{kin}} + W$$

$$p = \frac{h}{\lambda}$$

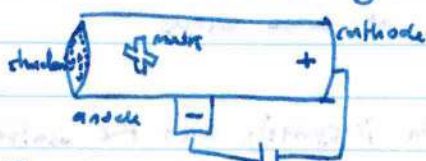
$$\Delta \lambda = \lambda - \lambda_0 = \frac{h}{mc} (1 - \cos \theta)$$





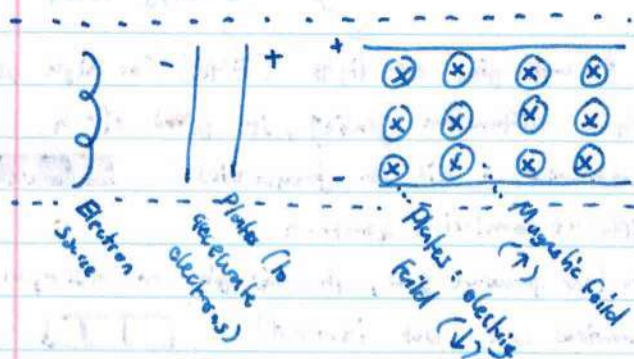
## Atomic physics

- 1803: John Dalton proposed that everything is made of atoms
  - ↳ Used to explain chemistry
  - ↳ Solid sphere model: atoms cannot be subdivided
- Late 1800s: cathode rays showed that negatively charged particles were going from the cathode to the anode (if a high voltage was applied)
  - ↳ Cathode: Metal ray tube:



→ Metal tube would gain a negative charge (proved 1895)

- J. J. Thompson cathode ray experiments
  - ↳ Proved that cathode rays were made up of negative charges
  - ↳ Showed that cathode rays could be deflected by magnetic fields
  - ↳ Charge to mass ratio: used a special CRT



If the magnetic and electric fields were equal, the electron would not move up or down

$$F_e = F_m \rightarrow v = \frac{E}{B}$$

→ where  $v$  is speed of electron

$$\frac{q}{m} = \frac{E}{B^2 r} \dots \text{very high, because electrons have lots of charge}$$

- Thompson's plum pudding model: Small, negatively charged [electrons] floating in a clump of positively charged material

- Millikan's oil drop experiment: measuring the fundamental charge

→ Some of the oil drops would fall through the hole in the positive plate and strike the



→ They would usually accelerate to the negative plate if charged positively (as per usual)

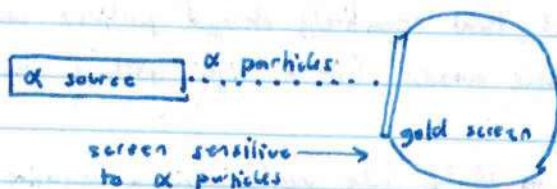
→ However, if they were charged negatively, they might enter a situation where  $F_g = F_e$

→ Derived to  $q = mgd/V$

→ The experiment showed all  $q$  was a multiple of one charge:  $1.6 \times 10^{-19} \text{ C}$



- Alpha particles ( $\alpha^{2+}$ ) ( $\text{He}^{2+}$ ) are released by some radioactive materials
  - ↳ These particles move at high speeds ( $2.5 \times 10^7 \text{ m/s}$ )
- Gold foil experiment: alpha particles scatter when they pass through gold foil. The scatter at different frequencies at different angles



- If Thompson's model was correct, there would be minimal scattering.
- However, some of the particles scatter at large angles

- Rutherford's planetary model: accounts for the irregularity with the scattering



- $\alpha^{2+}$  might get repelled by  $+$  at the exterior
- However, it wasn't compatible with Maxwell's EMR theory
- The electrons aren't creating EMR (which they should be if accelerating)

Because electrons change energy level

- Spectroscopy: if a gas is heated, it will give off light (EMR) (or high voltage)
  - ↳ If this light goes through a diffraction grating, it gives off a discrete spectrum (not continuous): discrete frequencies



- ↳ Every element has a different emission spectrum

- ↳ If light shines through a low pressure gas, it will give an absorption spectrum (same as the previous one, but inverted)



- Bohr's formula:  $\frac{1}{\lambda} = R_H \left( \frac{1}{n_f^2} - \frac{1}{n_i^2} \right)$

- ↳  $\lambda$  = wavelength,  $R_H$  = Rydberg's hydrogen constant,  $n_f$  and  $n_i$  = energy level
- ↳ Thus, electrons have energy levels: amounts of energy at particular positions
- ↳ EMR is released when an electron loses power (goes down a level)
- ↳ EMR is absorbed when an electron gains a power level
- ↳ When an electron goes down many power levels, more energized UV radiation is emitted
- ↳ When it goes down less, less energized infrared radiation is emitted
- ↳ Rutherford figured out the radius of H ( $n=1$ ) and the energy to ionize hydrogen
- ↳  $r_n = n^2 r_1$ , where  $r$  is radius and  $n$  is power level
- ↳  $E_n = \frac{1}{n^2} E_1$ , where  $E$  is energy and  $n$  is power level
- ↳ Can be used with  $E = \frac{hc}{\lambda}$  and  $E = hf$



- Bohr's model still couldn't explain all of the experimental data
  - ↳ Why "don't" electrons emit EMR in their energy levels
  - ↳ Only works for hydrogen
  - ↳ Brightness and spacing of emission lines
- Bohr's model could be joined with quantum mechanics: de Broglie's equations
  - ↳ Electrons can be thought of like waves where  $\lambda$  is a multiple of the circumference ( $r$  dependent, which is  $n$  dependent)
    - ↳ If not a multiple, the waves would add together (destructive)
  - ↳ Electrons = standing waves
  - ↳ Because it's not accelerating, EMR theory doesn't apply
  - ↳ Quantum model explains all elements: more protons in core  $\rightarrow$  more force on electron  $\rightarrow$  smaller radius  $\rightarrow$  different  $\lambda$
- The nucleus of an atom can determine its properties
  - ↳ Made up of protons (atomic number  $Z$ ) and neutrons (neutron number  $N$ )
  - ↳ Protons have a charge of  $+e$ , neutrons have a charge of  $0$
  - ↳ Each element has a specific number of protons and neutrons ( $\begin{smallmatrix} A \\ Z \end{smallmatrix} X$ )
    - ↳ Elements can have multiple numbers of neutrons (isotopes)
  - ↳ The number of neutrons controls how stable an atom is
  - ↳ The neutron is held together by the strong nuclear force
    - ↳ Counteracts the electrostatic force ( $p^+$  and  $p^+$ )
    - ↳ Only acts over very small distances
  - ↳ Binding energy: Energy it takes to separate the nucleus so that the strong nuclear force doesn't apply
    - ↳ Equation:  $E = mc^2$  (energy in Joules)
    - ↳ Separate nucleons have more mass than ones that are together
    - ↳ The difference between the mass of the nucleus and its components is the mass defect ( $\Delta m$ )
- Atomic masses can be measured using the atomic mass unit ( $u$ )
  - ↳  $1 u = 1/12$  the mass of  $(^{12}_6\text{C})$



- Some (radioactive) elements emit EMR under all conditions
  - ↳ This radiation comes from the nucleus
  - ↳ If the nucleus is unstable, it will decay into a stable nucleus
  - ↳ This can even change the element (transmutation)
- Ernest Rutherford found three types of radioactive decay
  - ↳ Alpha ( $\alpha$ ): deflected as positive in a magnetic field (weak)
  - ↳ Beta ( $\beta$ ): deflected as negative particle in a magnetic field (stronger)
  - ↳ Gamma ( $\gamma$ ): not deflected in a magnetic field (very strong)
- Conservation of nucleons: the number of nucleons stays the same during decay
- Alpha radiation: 2 protons and 2 neutrons leave the nucleus ( $\alpha^{2+}$ )
  - ↳ The same as a Helium nucleus ( ${}^4_2\text{He}$ )
  - ↳ ex.  ${}^{188}_{77}\text{Ir} \rightarrow {}^4_2\alpha + {}^{184}_{75}\text{Re} \dots \rightarrow {}^{184}_{75}\text{Re} = \text{daughter particle}$
  - ↳ The change in mass (products - reactants) is released as energy ( $E = mc^2$ )
  - ↳ Mostly kinetic energy of the atoms
- Beta radiation: A neutron becomes a proton and electron (negative decay)
  - ↳ proton stays in the nucleus, electron ( ${}^0_{-1}\beta$ ) leaves the atom
  - ↳ neutrons are just electrons and protons stuck together
  - ↳  ${}^{46}_{20}\text{Ca} \rightarrow {}^0_{-1}\beta + {}^{46}_{21}\text{Sc} + \bar{\nu}$
  - ↳  $\bar{\nu}$  is a neutral antineutrino (used for conservation of momentum)
- Beta radiation<sup>+</sup>: The antimatter equivalent of negative beta decay ( $\beta^+$ )
  - ↳ Antineutron  $\rightarrow$  positron + antielectron + neutrino
  - ↳ ex.  ${}^{40}_{19}\text{K} \rightarrow {}^0_{+1}\beta + {}^{40}_{18}\text{Ar} + \nu$
- Inverse beta decay: proton-rich nucleus absorbs inner electron
  - ↳  $p^+ + e^- \rightarrow n^0 + \nu$
  - ↳ ex.  ${}^{83}_{37}\text{Rb} + {}^0_{-1}e \rightarrow {}^{83}_{36}\text{Kr} + \nu$
- Gamma decay: releasing energy in form of EMR (no particles)
  - ↳ A gamma burst is produced if the atom needs to let off energy
- If the daughter nucleus is unstable, a decay series can happen
  - ↳ ex.  ${}^{236}_{90}\text{Th} \rightarrow {}^{222}_{88}\text{Ra} \rightarrow {}^{218}_{86}\text{Po} \rightarrow {}^{218}_{84}\text{Fr} \rightarrow {}^{214}_{82}\text{Pb}$
- Radiation is a health risk because it can cause genetic damage and ionize cells
  - ↳ Gamma is the most dangerous, then Beta, then alpha



## ~~Electrochemistry~~ Half-lives

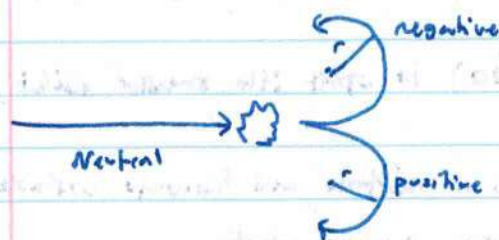
- The half-life of an element is the amount of time it takes for half of the element to transmute into something else
  - ↳ Half-lives can range from  $10^{28}$  s ( $10^{21}$  years) to  $10^{-22}$  s
- The activity of a sample measures the decays / per second
  - ↳ Measured in Becquerels (Bq) = decay/s
  - ↳ This changes as the sample gets older

Half-life formula:  $N = N_0 \left(\frac{1}{2}\right)^n$  where  $n$  is the number of half-lives

- Fission: causing a large nucleus ( $A > 120$ ) to split into smaller nuclei
  - ↳ This releases energy
  - ↳ Can start when a nucleus absorbs a neutron and becomes unstable
  - ↳ Used in nuclear reactors, produces nuclear waste
- Fusion: causing smaller nuclei to stick together into a large nucleus
  - ↳ This releases energy
  - ↳ Makes safe by-products (unlike fission)
- Critical nuclear reaction: where every reaction causes the same reaction once
  - ↳ This is because neutrons are reactants and products
- Supercritical: when every reaction causes the same reaction multiple times
  - ↳ If more ( $> 1$ ) neutrons are produced than consumed
  - ↳ This is the reaction behind atomic bombs and nuclear meltdowns
- Subcritical: The reaction will eventually die out
  - ↳ If less neutrons are produced than consumed
- Nuclear reactors use moderators to slow down the reaction (so the chain can happen) and heavy water so that no neutrons get absorbed
- Proton-proton chain: H and H combine to form He and  $\gamma$  radiation
  - ↳ This is the reaction that takes place in our sun
  - ↳ It is hard to replicate on earth due to the high pressures and temperatures
  - ↳ Uncontrolled fusion is used in thermonuclear bombs
  - ↳ We can perform fusion, but not when  $E_{in} > E_{out}$



- Cloud chamber: a chamber supersaturated with water vapor
  - ↳ Charged particles can ionize some of the water
  - ↳ The path of the particle could be observed this way
- Bubble chamber: a chamber with liquified gas at low pressure
  - ↳ Same concept: path is visible (due to gas-state gas)
- Chambers are often use with electric and magnetic fields
- Chambers can't detect neutral particles
- When particles follow circular tracks, we can use  $F_m = F_c$



- We can use the third hand rule to determine which particle is positive and negative
- The charges have to add up to 0

- Antimatter: same as matter, but charges are reversed ( $e^+$ ,  $p^-$ ,  $\bar{n}$ ,  $\bar{\nu}$ )
  - ↳ When antimatter and matter collide, they annihilate and produce energy
  - ↳ Energy produced is defined by  $E = mc^2$
  - ↳  $e^- + e^+ \rightarrow 2\gamma$

- It turns out that there are many fundamental particles (particle zoo) (categories:
  - ↳ Leptons: don't interact with the strong nuclear force (half-integer spins)
  - ↳ Hadrons: Interact with the strong nuclear force
    - ↳ Mesons: integer spins (bosons)
    - ↳ Baryon: half-integer spins (fermions)
  - ↳ Spin: Quality of particles (similar to momentum)
  - ↳ Mass unit:  $\text{MeV}/c^2$  (from  $E = mc^2$ )

- Quarks: sub-atomic particles with fractional charges ( $1/3$ )
  - ↳ Every particle is made of (3) quarks that add up to its charge
  - ↳ Up =  $2/3 e$ , down =  $-1/3 e$ , strange =  $-1/3 e$ , charm =  $2/3 e$
  - ↳ Conservation of (fractional) charge is still applied w/ quarks
  - ↳ Negative beta decay: down quark  $\rightarrow$  up quark
  - ↳ Positive beta decay: up quark  $\rightarrow$  down quark