## In[166]:= MαDMixedFinalAPhy MαDMixedFinalphiPhy MαDMixedFinalAphiPhy

$$\begin{split} \cos |\cos i| &= \left( \left( H \, W_V^2 \, \left( \vec{a} \, \vec{a}_C \, \left( \vec{b}^2 + 2 \, H \, W_V^2 \, \right)^4 + H \, \left( \vec{b}^2 + 2 \, H \, W_V^2 \, \right)^2 \right) + 4 \, \vec{\sigma}_C \, \left( 1 + \vec{\sigma}_N \, \right) \, \left( \vec{b}^2 + 2 \, H \, W_V^2 \, \right)^2 + \vec{\sigma}_V \, \left( - \vec{b}^4 - 4 \, \vec{b} \, \vec{b} \, H \, W_V^2 + 2 \, \vec{b} \, W_V^2 \, \right)^2 + \vec{\sigma}_V \, \left( - \vec{b}^4 - 4 \, \vec{b} \, \vec{b} \, H \, W_V^2 + 2 \, H \, W_V^2 \, \right)^2 + \vec{\sigma}_V \, \left( - \vec{b}^4 - 4 \, \vec{b} \, \vec{b} \, H \, W_V^2 + 2 \, H \, H \, \left( 1 + \vec{\sigma}_N \, \right) \, H \, H_V^2 \, \right) \, W_V^2 - 4 \, \left( 2 \, \dot{H}^2 - \dot{H} \, H + \left( 1 + \vec{\sigma}_N \, \right) \, \dot{H} \, H_V^2 \, \right) \, W_V^2 - 4 \, \left( 2 \, \dot{H}^2 - \dot{H} \, W_V^2 \, \right)^2 \, \left( \vec{b}^4 + 4 \, \vec{b} \, \vec{b} \, \dot{H} \, W_V^2 \, \right) - 2 \, \left( \vec{b} \, H \, \left( 1 + 2 \, \vec{\sigma}_N \, \right) \, H^2 \, \right) \, W_V^2 - 4 \, \left( 2 \, \dot{H}^2 - \dot{H} \, H \, H + \left( 1 + \vec{\sigma}_N \, \right) \, \dot{H} \, H^2 \, \right) \, W_V^2 - 2 \, \left( 3 \, \dot{H}^2 - \dot{H} \, \dot{H} \, \dot{H} \, \right)^2 \, \left( 3 \, \dot{H}^2 - \dot{H} \, \dot{H} \, \dot{H} \, \right)^2 \, \left( 3 \, \dot{H}^2 - \dot{H} \, \dot{H} \, \dot{H} \, \right)^2 \, \left( \dot{H}^2 \, \dot{H} \, \dot{H} \, \dot{H}^2 \, \left( - \vec{b}_N \, \dot{H}^2 \, \dot{H}^2 \, \dot{H} \, \dot{H}^2 \, \right) \, W_V^2 + 4 \, \left( 3 \, \dot{H}^2 \, \dot{H}^2 \, \dot{H}^2 \, \dot{H}^2 \, \dot{H}^2 \, \left( - \vec{b}_N \, \dot{H}^2 \, \dot{H}^2 \, \dot{H}^2 \, \dot{H}^2 \, \left( - \vec{b}_N \, \dot{H}^2 \, \dot{H}^2 \, \dot{H}^2 \, \dot{H}^2 \, \dot{H}^2 \, \left( - \vec{b}_N \, \dot{H}^2 \, \dot{H}^2 \, \dot{H}^2 \, \dot{H}^2 \, \dot{H}^2 \, \dot{H}^2 \, \left( - \vec{b}_N \, \dot{H}^2 \, \dot{H}^2 \, \dot{H}^2 \, \dot{H}^2 \, \dot{H}^2 \, \left( - \vec{b}_N \, \dot{H}^2 \, \dot{H}^2 \, \dot{H}^2 \, \dot{H}^2 \, \dot{H}^2 \, \dot{H}^2 \, \left( - \vec{b}_N \, \dot{H}^2 \, \dot{H$$

$$\begin{split} &4\left(4\,\dot{H}^3+(-4\,\ddot{\alpha}_N+4\,\ddot{\alpha}_T+\ddot{\alpha}_N)\,\dot{H}^2\,\dot{H}^2-\ddot{\alpha}_N\,\dot{H}\,\dot{H}^3-\ddot{\alpha}_N\,\dot{H}\,\dot{H}^3\right)\,\dot{M}_N^{2\,3}\right) +\\ &+\left(-4\,\ddot{\alpha}_N\,H\,\dot{M}_N^{2\,2}\left(\ddot{\phi}^2+2\,\dot{H}\,\dot{M}_N^2\right)\left(\dot{\phi}^2+2\,\dot{H}\,\dot{H}^2-\ddot{\alpha}_N\,\dot{H}\,\dot{H}^3\right)\,\dot{M}_N^2\right)+\ddot{\alpha}_N^2\,\dot{H}^2\,\dot{M}_N^2\left(-\dot{\phi}^4+4\,\ddot{\phi}_N\,\dot{H}\,\dot{M}_N^2+2\,\dot{\phi}^2\left(-3\,\dot{H}+\dot{H}^2\right)\,\dot{M}_N^2+4\left(-2\,\dot{H}^2+\dot{H}\,\dot{H}+\left(1+\ddot{\alpha}_N\right)\,\dot{H}\,\dot{H}^2\right)\,\dot{M}_N^2^2\right) +\\ &4\,\ddot{\alpha}_N\left(\dot{\phi}^6+\dot{\phi}^4\left(5\,\dot{H}+\left(-1-3\,\ddot{\alpha}_N+2\,\ddot{\alpha}_T\right)\,\dot{H}^2\right)\,\dot{M}_N^2+4\left(\ddot{\alpha}_N-\ddot{\alpha}_T\right)\,\dot{\phi}\,\dot{\phi}\,\dot{\phi}\,\dot{H}^2\,\dot{M}_N^2^2\right) +\\ &2\,\ddot{\phi}^2\left(4\,\dot{H}^2+\left(-2-7\,\ddot{\alpha}_N+5\,\ddot{\alpha}_T\right)\,\dot{H}^2\,\dot{H}^2+\dot{H}^2\left(-\ddot{\alpha}_C+\dot{H}\left(-\ddot{\alpha}_N+\ddot{\alpha}_T+\ddot{\alpha}_N\,\dot{H}-\ddot{\alpha}_T\,\dot{H}\right)\right)\right)\\ &-\dot{M}_N^{2\,2}+4\left(\dot{H}^3-\left(1+4\,\ddot{\alpha}_N-3\,\ddot{\alpha}_T\right)\,\dot{H}^2\,\dot{H}^2+\dot{H}^2\left(-\ddot{\alpha}_C+\dot{H}\left(-\ddot{\alpha}_N+\ddot{\alpha}_T+\ddot{\alpha}_N\,\dot{H}-\ddot{\alpha}_T\,\dot{H}\right)\right)\right)\right)\\ &-\dot{M}_N^{2\,2}+4\left(\dot{H}^3-\left(1+4\,\ddot{\alpha}_N-3\,\ddot{\alpha}_T\right)\,\dot{H}^2+\dot{H}^2+\left(\ddot{\alpha}_N-\ddot{\alpha}_T\right)\,\dot{H}\right)\right)\right)\,\dot{M}_N^{2\,3}\right)\right)+\\ &2\,\ddot{\alpha}_A\left(\dot{\phi}^2+2\,\dot{H}\,\dot{M}_N^2\right)\left\{2\,\ddot{\alpha}_C\left(\dot{\phi}^6+2\,\dot{\psi}\,\dot{\psi}^3\,\dot{H}\,\dot{M}^2\right)\,\dot{\phi}^2+2\,\dot{q}^2\,\dot{q}^2\,\dot{q}^2\,\dot{q}^2\,\dot{q}^2\right)\right\}\\ &4\,\ddot{\phi}\,\dot{\psi}\,\dot{H}\,\dot{H}^2+2\left(1+\ddot{\alpha}_N\right)\,\dot{H}^2\right)\dot{M}_N^2+2}\\ &2\,\dot{\psi}\,\dot{\psi}\,\dot{H}\,\dot{H}^2+2\left(1+\ddot{\alpha}_N\right)\,\dot{H}^2\right)\dot{M}_N^2+2\,\dot{q}^2+4\left(\ddot{\alpha}_N+\dot{$$

$$\begin{split} 12 \, \bar{\alpha}_T \, H - 12 \, \bar{\alpha}_M \, \bar{\alpha}_T \, H + \bar{\alpha}_M \, \bar{\alpha}_M \, H + \bar{\alpha}_M \, \bar{\alpha}_M \, H \Big) \Big) \, M_V^{23} \Big) \Big) - \\ \Big( -2 \, \dot{\phi}^2 - 4 \, \dot{H} \, M_V^2 + H \, \Big( 4 \, \dot{\alpha}_C + \Big( 4 \, \dot{\alpha}_M + 4 \, \dot{\alpha}_C \, \Big( 1 + \bar{\alpha}_M \Big) - 4 \, \bar{\alpha}_T + \bar{\alpha}_M \Big) \, H \Big) \, M_V^2 \Big) \\ \Big( -2 \, \bar{\alpha}_C \, \dot{\bar{\alpha}}_K \, \Big( \dot{\phi}^2 + 2 \, \dot{H} \, M_V^2 \Big)^2 + 4 \, \dot{\bar{\alpha}}_C^2 \, H \, \Big( \dot{\phi}^4 + 4 \, \dot{H} \, \dot{\phi}^2 \, M_V^2 + 4 \, \dot{H} \, \Big( \dot{H} - \Big( 1 + \bar{\alpha}_M \Big) \, H^2 \, \Big) \, M_V^2^2 \Big) + \\ 4 \, \bar{\alpha}_C \, H \, M_V^2 \, \Big( 2 \, \dot{H} \, \dot{\phi}^2 + 4 \, \dot{H}^2 \, M_V^2 + \dot{H} \, H \, \Big( 2 \, \dot{\bar{\alpha}}_A - 4 \, \dot{\bar{\alpha}}_C + \Big( -4 \, \dot{\bar{\alpha}}_M + 4 \, \dot{\alpha}_T + \bar{\alpha}_V \Big) \, H \Big) \, M_V^2 + \\ \dot{\bar{\alpha}}_A \, H \, \Big( \dot{\phi}^2 - 2 \, \Big( 1 + \bar{\alpha}_M \Big) \, H^2 \, M_V^2 \Big) + \dot{\alpha}_V \, H^2 \, \Big( \dot{\phi}^2 - \Big( 1 + \bar{\alpha}_M \Big) \, H^2 \, M_V^2 \Big) \Big) + \\ H^2 \, M_V^2 \, \Big( 4 \, \ddot{\bar{\alpha}}_A \, \Big( \dot{\phi}^2 + 2 \, \dot{H} \, M_V^2 \Big) + 2 \, H \, \Big( -\dot{\phi}^2 - 2 \, \dot{H} \, M_V^2 + 2 \, H \, \Big( \dot{\alpha}_C + \Big( \bar{\alpha}_M - \bar{\alpha}_T \, H \Big) \Big) \, M_V^2 \Big) - \\ \dot{\bar{\alpha}}_V \, \Big( \dot{\alpha}_K \, \Big( \dot{\phi}^2 + 2 \, \dot{H} \, M_V^2 \Big)^2 \, \Big( \Big( -1 + \bar{\alpha}_C \Big) \, \dot{\phi}^2 + 2 \, \Big( -1 + \bar{\alpha}_C \Big) \, \dot{H} \, M_V^2 + 4 \, \Big( 2 \, \ddot{\alpha}_C + \Big( 2 \, \ddot{\alpha}_M + 2 \, \ddot{\alpha}_C \, \Big( 1 + \bar{\alpha}_M \Big) \, H^2 \, M_V^2 + 2 \, H \, \Big( 2 \, \dot{\alpha}_C + \Big( 2 \, \dot{\alpha}_M + 2 \, \ddot{\alpha}_C \, \Big( 1 + \bar{\alpha}_M \Big) \, H^2 \, M_V^2 + 4 \, \Big( 1 + \bar{\alpha}_M \, H \, \Big) \, M_V^2^2 + 4 \, \Big( 2 \, \dot{H}^3 - 3 \, \Big( 1 + \bar{\alpha}_M \Big) \, \dot{H}^2 \, H^2 + 2 \, \dot{\alpha}_M \, \dot{H}^3 - \Big( 1 + \bar{\alpha}_M \, H \, \Big) \, M_V^2^2 + 4 \, \Big( 2 \, \dot{H}^3 - 2 \, \Big( \dot{H}^3 \, \dot{H} + \Big( 1 + \bar{\alpha}_M \, \Big) \, \dot{H}^3 \, H^3 + 2 \, \Big( 1 + \bar{\alpha}_M \, H \, \Big) \, M_V^2^2 + 4 \, \Big( 2 \, \dot{H}^3 - 2 \, \Big( \dot{H}^3 \, \dot{H} + \Big( 1 + \bar{\alpha}_M \, \Big) \, \dot{H}^3 \, H^3 - \Big( 1 + \bar{\alpha}_M \, H \, \Big) \, M_V^2^2 + 4 \, \Big( 2 \, \dot{H}^3 - 2 \, \Big( \dot{H}^3 \, \dot{H}^3 \, H \, \Big) \, \dot{H}^3 \, H^3 + 2 \, \bar{\alpha}_M \, H^3 - 2 \, \Big( 1 + \bar{\alpha}_M \, H \, \Big) \, M_V^2^2 + 4 \, \Big( 2 \, \dot{H}^3 \, \dot{H}^3 \, H^3 \, \Big) \, \dot{H}^3 \, H^3 + 2 \, \bar{\alpha}_M \, H^3 \, H^3 \, \Big( 1 + \bar{\alpha}_M \, H \, \Big) \, M_V^2^2 + 4 \, \Big( 2 \, \dot{H}^3 \, \dot{H}^3 \, H^3 \, H^3 \, \Big) \, \dot{H}^3 \, H^3 \, \Big( 1 + \bar{\alpha}_M \, H \, \Big) \, \dot{H}^3 \, H^3 \, \Big( 1 + \bar{\alpha}_M \, H \, \Big) \, \dot{H}^3 \, \Big( 1 + \bar{\alpha}_M \, H \, \Big) \, \dot{H}^3 \, \Big( 1 + \bar$$

$$2 H \left( (\tilde{\Delta}_R - \tilde{\Delta}_T) H^2 \left( -\tilde{\Delta}_V + 4 \left( 1 + \tilde{\Delta}_N \right) \left( \tilde{\Delta}_H - \tilde{\Delta}_T \right) H \right) + \tilde{\Delta}_V \left( -\tilde{H} + H \left( \tilde{\Delta}_C + H \left( \tilde{\Delta}_R - \tilde{\Delta}_T + \left( 1 + \tilde{\Delta}_R \right) \left( \tilde{\omega}_R - \tilde{\omega}_T \right) H \right) \right) \right) M_V^{22} \right) \right) \right) \right)$$

$$\Rightarrow A_R^{-12} \Rightarrow^2 \bigg/ \left( 4 \left( \tilde{\omega}_K \left( \tilde{\omega}^2 + 2 \tilde{H} M_V^2 \right)^2 - 2 H^2 M_V^2 \left( 2 \left( -1 + \tilde{\omega}_R \right) \tilde{\omega}^2 + 4 \left( -1 + \tilde{\omega}_A \right) \tilde{H} M_V^2 + H \left( 4 \tilde{\omega}_C + \left( 4 \tilde{\omega}_R + 4 \tilde{\omega}_C \left( 1 + \tilde{\omega}_R \right) - 4 \tilde{\omega}_T + \tilde{\omega}_V \right) H \right) M_V^2 \right) \right)^2 \right)$$

$$\Rightarrow A_R^{-12} \Rightarrow^2 \bigg/ \left( 4 \left( \tilde{\omega}_K \left( 4 \tilde{H} \tilde{\omega}^2 + \tilde{U}^2 H \left( 4 \tilde{\omega}_C + \left( 4 \tilde{\omega}_R + 4 \tilde{\omega}_C \left( 1 + \tilde{\omega}_R \right) - 4 \tilde{\omega}_T + \tilde{\omega}_V \right) H \right) + 8 \tilde{H}^2 M_V^2 \right) - 2 H^2$$

$$= \left( -(-2 + \tilde{\omega}_A)^2 \tilde{\omega}^2 + 8 \left( -1 + \tilde{\omega}_A \right) \tilde{H} M_V^2 + 2 H \left( 4 \tilde{\omega}_C + \left( 4 \tilde{\omega}_R + 4 \tilde{\omega}_C \left( 1 + \tilde{\omega}_R \right) - 4 \tilde{\omega}_T + \tilde{\omega}_V \right) H \right) M_V^2 \right) \right)$$

$$\Rightarrow O_V^{22} \Rightarrow^2 \bigg/ \left( 4 \tilde{\omega}_K \left( \tilde{\omega}^2 + 2 \tilde{H} M_V^2 \right)^2 - 8 H^2 M_V^2 \right)$$

$$\left( 2 \left( -1 + \tilde{\omega}_A \right) \tilde{\omega}^2 + 4 \left( -1 + \tilde{\omega}_A \right) \tilde{H} M_V^2 + 2 H \left( 4 \tilde{\omega}_C + \left( 4 \tilde{\omega}_R + 4 \tilde{\omega}_C \left( 1 + \tilde{\omega}_R \right) - 4 \tilde{\omega}_T + \tilde{\omega}_V \right) H \right) M_V^2 \right) \right)$$

$$\Rightarrow O_V^{22} \Rightarrow^2 \bigg/ \left( 8 \tilde{\omega}^2 + 2 \tilde{H} M_V^2 \right) \left( 8 \tilde{H}^3 \tilde{\omega} M_V^2 - 2 \tilde{H} M_V^2 \right) \right)$$

$$\Rightarrow \left( -4 \tilde{\omega}^3 - 4 \tilde{\omega}^2 \tilde{H} M_V^2 + 2 \tilde{H} M_V^2 + 2 \tilde{H} M_V^2 \right) \left( 2 \left( -1 + \tilde{\omega}_A \right) \tilde{\omega}^2 + 4 \left( -1 + \tilde{\omega}_A \right) \tilde{H} M_V^2 + 4 \tilde{\omega}^2 + 4 \tilde{\omega}$$

$$\begin{array}{c} 4 \; \ddot{\alpha}_{C} \; H + 4 \; \ddot{\alpha}_{T} \; H - \tilde{\alpha}_{V} \; H + 4 \; \ddot{\alpha}_{H} \; \left( \dot{\vec{\alpha}}_{C} - \left( 1 + \tilde{\alpha}_{C} \right) \; H \right) \right) \right) \; M_{V}^{2} \; ^{2} \right) \; ) \right) + \\ 2 \; \ddot{\alpha}_{K} \; H^{2} \; \left( \ddot{\alpha}_{A}^{2} \; \left( \dot{\psi}^{2} + 2 \; \dot{H} \; M_{V}^{2} \right) \; \left( \dot{\psi}^{5} + 3 \; \dot{\psi} \; \dot{\psi}^{2} \; H \; M_{V}^{2} + \dot{\psi}^{3} \; \left( \dot{H} - \left( 1 + 2 \; \tilde{\alpha}_{M} \right) \; H^{2} \right) \; M_{V}^{2} - 2 \; \dot{\psi} \; \dot{\psi}^{4} \; H \; M_{V}^{2} + \dot{\psi}^{3} \; \left( \dot{H} - \left( 1 + 2 \; \tilde{\alpha}_{M} \right) \; H^{2} \right) \; M_{V}^{2} - 2 \; \dot{\psi} \; \dot{\psi}^{4} \; H \; M_{V}^{2} + \dot{\psi}^{3} \; \left( \left( -1 + \tilde{\alpha}_{C} \right) \; \dot{\psi}^{7} - 2 \; \dot{\psi} \; \dot{\psi}^{4} \; H \; M_{V}^{2} + \dot{\psi}^{3} \; \left( \left( -4 + 6 \; \tilde{\alpha}_{C} \right) \; \dot{H} + H \; \left( -\dot{\alpha}_{A}^{2} + 2 \; \dot{\alpha}_{C}^{2} + \left( -2 + 2 \; \tilde{\alpha}_{M} + 2 \; \tilde{\alpha}_{C} \; \left( 1 + \tilde{\alpha}_{M} \right) - 2 \; \tilde{\alpha}_{T} - \tilde{\alpha}_{V} \right) \; H \right) \right) \; M_{V}^{2} - \\ \ddot{\psi} \; \dot{\psi}^{2} \; H \; \left( 8 \; \dot{H} + H \; \left( 4 \; \dot{\alpha}_{C}^{2} + \left( 4 \; \tilde{\alpha}_{M} + 4 \; \tilde{\alpha}_{C} \; \left( 1 + \tilde{\alpha}_{M} \right) - 4 \; \tilde{\alpha}_{T} + \tilde{\alpha}_{V} \right) \; H \right) \right) \; M_{V}^{2} \; + \dot{\psi}^{3} \; \left( 4 \; \left( -1 + 3 \; \tilde{\alpha}_{C} \right) \right) \\ \ddot{H}^{2} \; + \dot{H} \; H \; \left( -4 \; \dot{\alpha}_{A}^{2} + 8 \; \dot{\alpha}_{C}^{2} + \left( -8 + 12 \; \tilde{\alpha}_{M} + 12 \; \tilde{\alpha}_{C} \; \left( 1 + \tilde{\alpha}_{M} \right) - 12 \; \tilde{\alpha}_{T} - 3 \; \tilde{\alpha}_{V} \right) \; H \right) \right) \; M_{V}^{2} \; - \\ \ddot{H}^{2} \; + \dot{H} \; H \; \left( -4 \; \dot{\alpha}_{A}^{2} + 8 \; \dot{\alpha}_{C}^{2} + \left( -4 \; \tilde{\alpha}_{M} + 4 \; \tilde{\alpha}_{C} + 4 \; \left( 1 + \tilde{\alpha}_{C}^{2} \right) \; \dot{\alpha}_{M}^{2} - 4 \; \dot{\alpha}_{C}^{2} + 4 \; \dot{\alpha}_{C}^{2} \; H + 4 \; \tilde{\alpha}_{C}^{2} \; \dot{\alpha}_{M}^{2} + 4 \; \dot{\alpha}_{C}^{2} \; H + 4 \; \ddot{\alpha}_{C}^{2} \; \dot{\alpha}_{M}^{2} + 4 \; \dot{\alpha}_{C}^{2} \; H + 4 \; \ddot{\alpha}_{C}^{2} \; \dot{\alpha}_{M}^{2} + 4 \; \dot{\alpha}_{C}^{2} \; \left( 1 + \tilde{\alpha}_{M}^{2} \right) \; \dot{\alpha}_{M}^{2} + 4 \; \dot{\alpha}_{C}^{2} \; \left( 1 + \tilde{\alpha}_{M}^{2} \right) \; \dot{\alpha}_{M}^{2} + 4 \; \dot{\alpha}_{C}^{2} \; \left( 1 + \tilde{\alpha}_{M}^{2} \right) \; \dot{\alpha}_{M}^{2} + 4 \; \dot{\alpha}_{C}^{2} \; \left( 1 + \tilde{\alpha}_{M}^{2} \right) \; \dot{\alpha}_{M}^{2} + 4 \; \dot{\alpha}_{C}^{2} \; \left( 1 + \tilde{\alpha}_{M}^{2} \right) \; \dot{\alpha}_{M}^{2} + 4 \; \dot{\alpha}_{C}^{2} \; \left( 1 + \tilde{\alpha}_{M}^{2} \right) \; \dot{\alpha}_{M}^{2} + 4 \; \dot{\alpha}_{C}^{2} \; \dot{\alpha}_{M}^{2} + 4 \; \dot{\alpha}_{C}^{2} \; \dot{\alpha}_{$$