

Refrigeration & Air Conditioning

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28/11/2016

Book

P.L. Ballaney.

RAC

open system

- ① steady state
- ② $\Delta K.E. = 0$ & $\Delta P.E. = 0 \swarrow$

S.P.E.E.

Polytropic ($PV^n = c$)

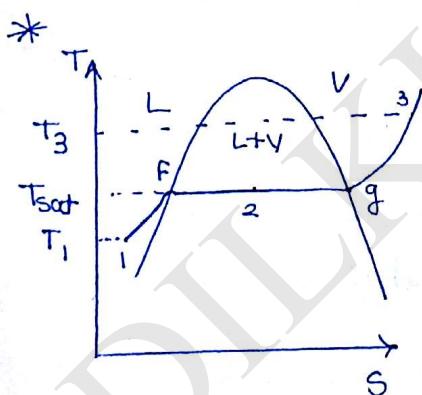
$$h_1 + q = h_2 + w_{c.v.}$$

Adiabatic $\begin{cases} \text{Rev.} \\ \text{Irrv.} \end{cases} \Rightarrow \left\{ \begin{array}{l} q = 0 \\ w_{c.v.} = h_1 - h_2 \end{array} \right.$

$$w_{c.v.} = - \int v dp$$

$$w_{c.v.} = \frac{n}{n-1} (P_1 V_1 - P_2 V_2)$$

$$w_{c.v.} = h_1 - h_2$$



① Sub cooled Region

$$h_f - h_L = C_p e_{iq} (T_{sat} - T_L)$$

$$s_f - s_L = C_p e_{iq} \ln \frac{T_{sat}}{T_L}$$

② Wet Region.

$$h_2 = h_f + x_2 h_{fg} \quad s_g - s_f = \frac{L.H.}{T_{sat}}$$

$$s_2 = s_f + x_2 s_{fg} \quad s_g - s_f = \frac{h_g - h_f}{T_{sat}}$$

$$L.H. Q_p = h_g - h_f$$

$$L.H. = h_g - h_f$$

③ super heated (ideal gas)

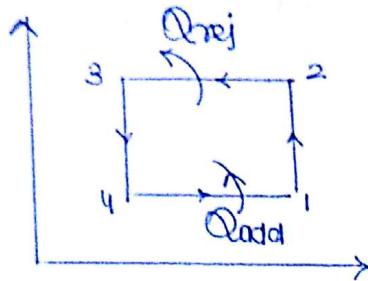
$$h_3 - h_g = Q_v (T_3 - T_{sat})$$

$$s_3 - s_g = C_p \ln \frac{T_3}{T_{sat}} - R \ln \frac{P}{P_{sat}}$$

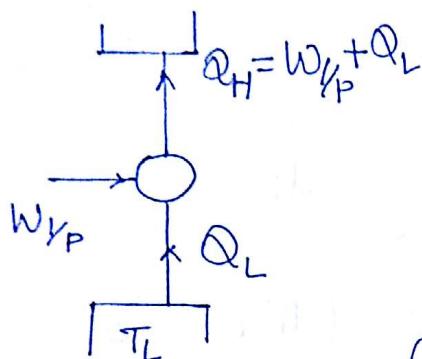
$$s_3 - s_g = C_p \ln \left(\frac{T_3}{T_{sat}} \right)$$

Ideal cycle for Refrigeration:-

(Reversed Carnot Cycle)



- 1-2 isentropic comp.
- 2-3 isoth heat rej
- 3-4 isentropic exp.
- 4-1 isoth. heat add.



$$(COP)_{Ref} = \frac{Q_L}{W_{HP}}$$

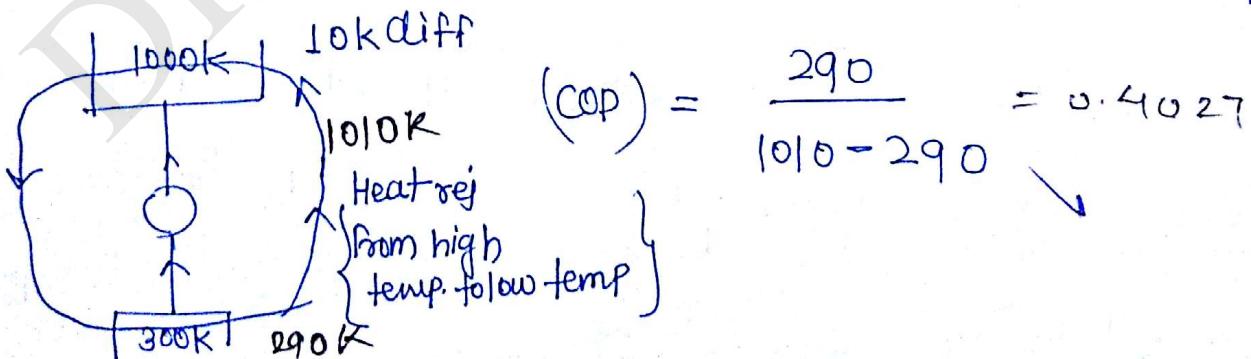
$$(COP)_{HP} = \frac{Q_H}{W_{HP}}$$

$$(COP)_{ref} = (COP)_{HP} - 1$$

$$(COP)_{HP} - (COP)_{ref} = 1$$

$$*(COP)_{ref} = \frac{T_L}{T_H - T_L} \quad (COP)_{HP} = \frac{T_H}{T_H - T_L}$$

e.g. if 10K diff b/w temp. of working substance and sink
 $COP = ?$



$$(COP) = \frac{290}{1010 - 290} = 0.4027$$

$$\frac{1000}{1010 - 300} = 0.4285$$

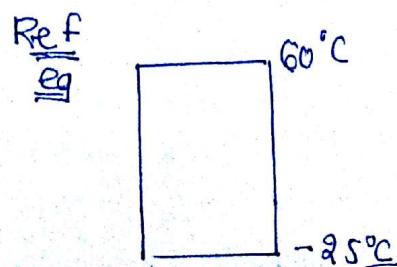
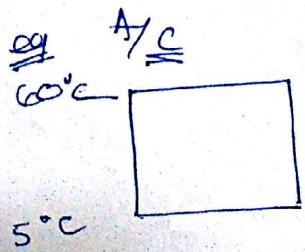
- * The expressions developed in term of temp. can be used when
 - The cycle is internally rev. (may or may not be externally rev.)
 - Heat add. and heat rej. should be isothermal.
 - Temp. should be temp. of working fluid.
- * The eff. (η) of an engine increases by increasing T_H and by decreasing T_L . but increment is more when the T_L is decrease.
- * COP of heat pump & ref. increases by decreasing T_H and by increasing T_L . Here increasing T_L is more beneficial.

* The COP of AC ~~and~~ is more than COP of ref. but the electricity bill of AC is more because the total heat removed i.e. desired effect is more as compare to ref., since

- Reasons
- total space to cool is more
 - Heat gen. ~~sources~~ ^{Sources} are present (fan, light people)
 - Fan, fan Heat leakage from outside

$$\text{Suppose } (\text{COP})_{AC} = 2 = \frac{\text{P.E.}}{W_{IP}} \rightarrow 100 \quad W_{IP} = 50$$

$$(\text{COP})_{ref} = 1 = \frac{\text{D.E.}}{W_{IP}} \rightarrow 10 \quad W_{IP} = 10$$



$$* \quad (\text{COP})_{\text{ref}} = \frac{\text{R.E.}}{W_{Y_p}} = \frac{\text{R.C.}}{W_{Y_p}}, \quad (\text{COP})_{\text{HP}} = \frac{\text{H.E.}}{W_{Y_p}} = \frac{\text{H.C.}}{W_{Y_p}}$$

Ref.
Capacity

Heat Cap.

 Q_L From lower temp.

- The amount of heat absorbed to Maintain a space at a lower temp. is called refrigeration effect. The rate of heat absorption is called refrigeration capacity.

- The amount of heat rejected is called heating effect and the rate of heat rejection is called heating capacity.

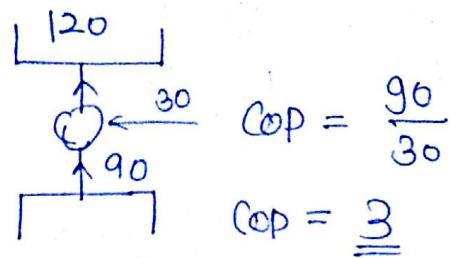
* 1 Ton of Refrigeration: (LTR)

$$\begin{aligned} \text{LTR} &= 3.5167 \text{ kW} \\ &= 211 \text{ kJ/min} \\ &= 50.4 \text{ kcal/min} \end{aligned}$$

It is the amount of heat which has to be removed to convert 1 ton of water at 0°C into 1 ton of ice at 0°C in 24 hrs. hence ton of refrigeration represents heat transfer rate.

Q. 6
P.g. 41
WB

$$COP = \frac{30}{120 - 30} = \frac{1}{3}$$



Q. 10

$$\frac{T_L}{T_H} = 0.8$$

$$(COP)_{ref.} = \frac{T_L}{T_H - T_L}$$

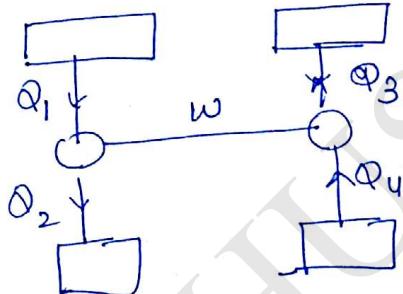
$$\left(\frac{1}{COP}\right)_{ref} = \frac{T_H}{T_L} - 1 = \frac{10}{0.8} - 1$$

$$\left(\frac{1}{COP}\right)_{ref} = 1.25 - 1$$

$$(COP)_{ref} = 4$$

$$(COP)_{HP} = 5$$

Q. 11



$$\eta_{FE} = \frac{Q_1 - Q_2}{Q_1} = 0.4$$

$$1 - \frac{Q_2}{Q_1} = 0.4$$

$$Q_2 = 0.6 Q_1$$

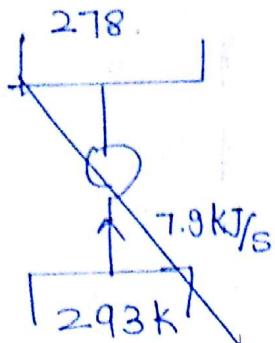
$$Q_2 + Q_4 = 3Q_1$$
$$(COP) = \frac{Q_4}{Q_3 - Q_4} = \frac{\cancel{Q_2} + 3Q_1 - Q_2}{Q_1 - \cancel{Q_2}}$$

$$(COP) = \frac{3Q_1 - 0.6Q_1}{Q_1 - 0.6Q_1}$$

$$= \frac{2.4}{0.4}$$

$$\underline{COP} = 6$$

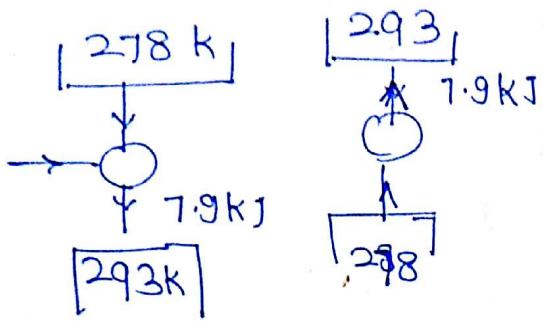
Q.17



$$\frac{Q_L}{Q_H - Q_L} = \frac{T_L}{T_H - T_L}$$

$$\frac{7.9 \times 5}{293} = \omega$$

Heat pump

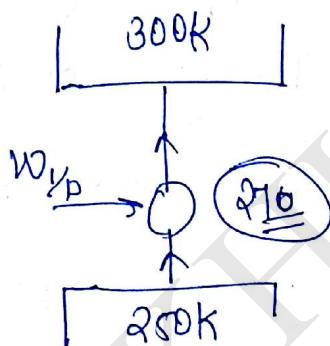


$$\frac{Q_H}{Q_H - Q_L} = \frac{T_H}{T_H - T_L} = \frac{293}{15}$$

$$Q_H - Q_L = \omega = \frac{7.9 \times 15}{293}$$

$$\omega = 0.4045 \text{ kJ} =$$

Q.18



$$m = 3600 \text{ kg}$$

$$t = 10 \text{ hrs}$$

$$C_{p_f} = 2.0 \text{ kJ/kg K} \quad \text{above } -3^\circ\text{C}/270\text{K}$$

$$C_{p_f} = 0.5 \text{ kJ/kg K} \quad \text{below } 270\text{K}$$

$$LH = 230 \text{ kJ/kg}$$

$$(COP)_{\text{ideal}} = 2 (COP)_{\text{act}}$$

$$\text{Heat removed} = m(c_{\text{d}}dT + LH + c_{\text{d}}dT)$$

$$Q = 3600(2 \times 30 + 230 + 0.5 \times 30)$$

$$\frac{5 \times 280}{50} = 2 (COP)_{\text{act}}$$

$$3600 \times (0.5 \times 30 + 230 + 2 \times 30)$$

$$(COP)_{\text{act}} = 9.5 = \frac{Q_L}{Q_H - Q_L} =$$

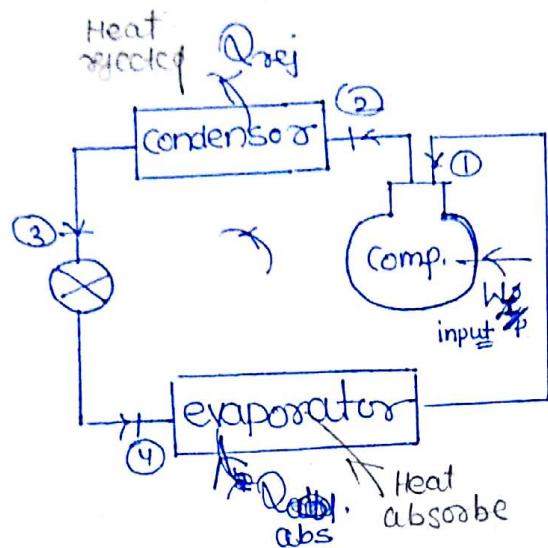
$$\dot{Q} = \frac{Q}{10 \times 3600} = \frac{1080000}{360000}$$

$$9.5 = \frac{30}{w_{IP}}$$

$$w_{IP} = 12 \text{ kW}$$

$$\dot{Q} = 30 \text{ kW}$$

Vapour Compression Refrigeration System (VCRS)



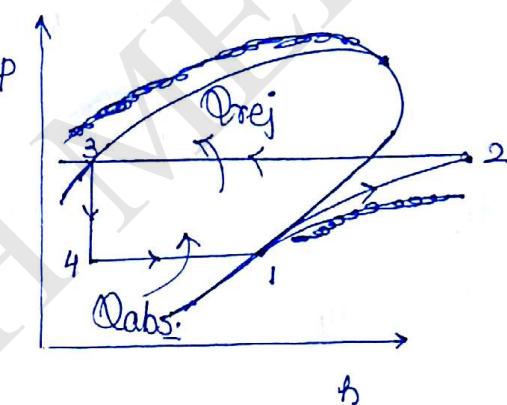
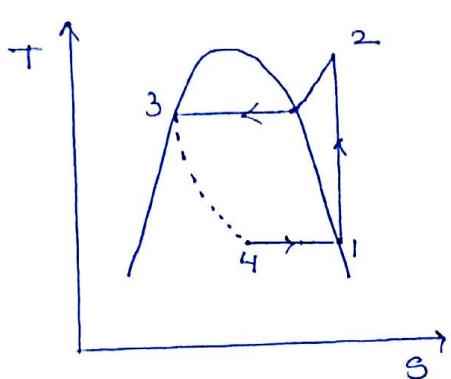
1 → 2 isentropic Comp.

2 → 3 isobaric heat rej.

3 → 4 throttling

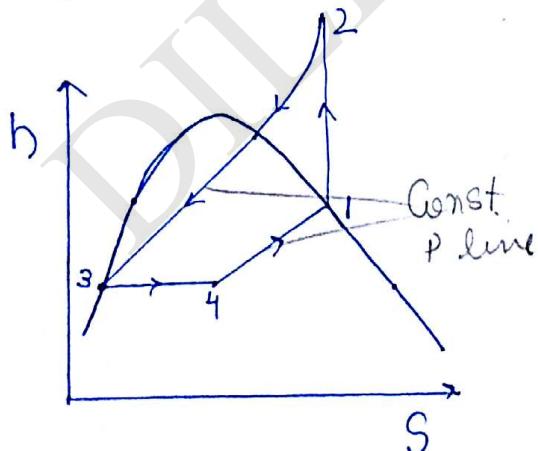
4 → 1 isobaric heat ab.

* In actual unit the ref. leaving the evaporator is superheated



{ Simple V-C cycle
or ideal V-C cycle

{ 1. Sat. vap.
3. Sat. liq.



$$TdS = dh - Vdp \quad \text{---} \quad 6$$

$$\left(\frac{dh}{ds}\right) = T$$

{ 1. Sat. vapour
3. Sat. liquid

⇒ Applying steady state flow energy eqn in various stages

- steady state

$$\Delta KE = \Delta P.E. = 0$$

$$h_i + q = h_e + w_{c.v.}$$

① Compressor

isentropic ($Q=0$)

$$\therefore w_{c.v.} = h_i - h_e$$

$$w_{i/p} = h_e - h_i = h_2 - h_1$$

$$w_{i/p} = h_2 - h_1$$

② Condenser ($w_{c.v.} = 0$)

$$q = h_e - h_i$$

$$Q_{ref} = h_i - h_e = h_2 - h_3$$

$$Q_{ref} = h_2 - h_3$$

③ Throttling

$$h_3 = h_4$$

④ Evaporator $w_{c.v.} = 0$

$$h_i + q = h_e$$

$$Q_{ab} = h_1 - h_4$$

*
$$COP = \frac{R.E.}{w_{i/p}} = \frac{h_1 - h_4}{h_2 - h_1} = \frac{h_1 - h_3}{h_2 - h_1}$$

Ref. Capacity, $(R.E.C) = \dot{m} \times (R.E.)$

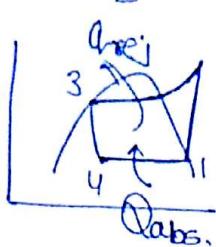
$$\dot{W}_{i/p} = \dot{m} \times (w_{i/p})$$

Q.16

P.g 45°
WB

$$R.C = 5 \text{ kW}$$

$$h_3 = 75 \text{ kJ/kg} = h_4$$



$$h_1 = 183 \text{ kJ/kg.}$$

$$h_2 = 210 \text{ kJ/kg.}$$

$$COP = \frac{R.E}{W_{iwp}} = \frac{h_4 - h_1}{h_2 - h_1}$$

$$(COP) = \frac{183 - 75}{210 - 183} = 4$$

$$W_{iwp} = \text{Power} = \dot{m} (W_{in})$$

$$(R.E) \times \dot{m} = R.C.$$

$$= \dot{m} (h_2 - h_1)$$

$$(h_1 - h_4) \dot{m} = 5$$

$$P_{iwp} = \frac{5}{108} (210 - 183)$$

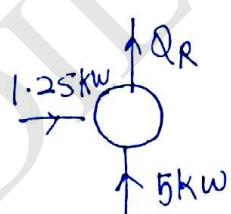
$$\dot{m} = \frac{5}{108} \text{ kg/s.}$$

$$P_{iwp} = 1.25 \text{ kW}$$

$$\text{Heat transrate} = \frac{5}{108} (h_3 - h_2) = \frac{5}{108} (210 - 75)$$

$$= 6.25 \text{ kW}$$

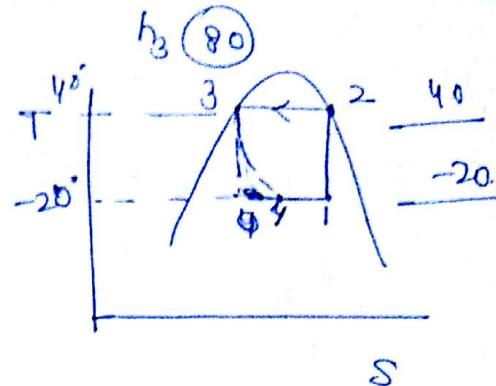
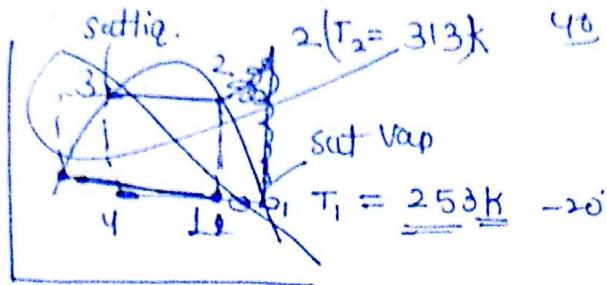
or $COP = \frac{R.C}{W_{iwp}}$ $\Rightarrow W_{iwp} = \frac{5}{4} = 1.25 \text{ kW.}$



$$Q_R = 1.25 + 5$$

$$= 6.25 \text{ kW}$$

Q. 19



$$\text{COP} = \frac{h_1 - h_3}{h_2 - h_1} = \frac{180 - 80}{200 - 180} = 5$$

$$\text{COP} =$$

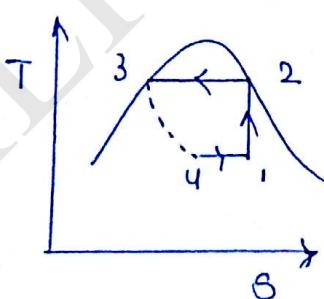
$$h_1 = h_f + x h_{fg} \Big|_{20^\circ\text{C}} \\ = 20 + 160 \times 0.9$$

$$h_1 = 164 \text{ kJ/kg}$$

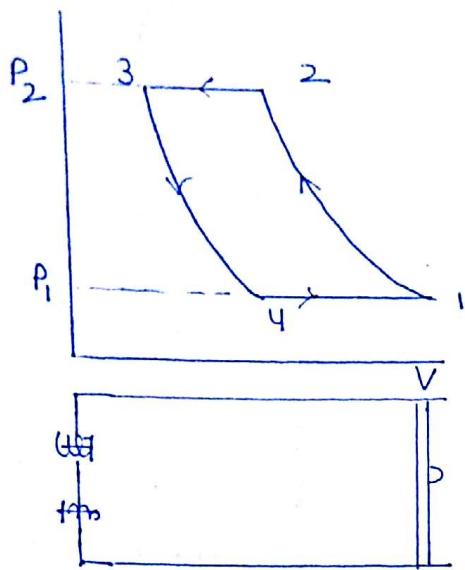
$$\text{COP} = \frac{164 - 80}{200 - 164} = 2.33$$

$$\text{R.E.} = m(h_1 - h_A) = 0.025(164 - 80)$$

$$\underline{\text{R.E.}} = 2.1 \text{ kW}$$



Volumetric efficiency in reciprocating compression:-



$$\eta_v = \frac{\text{Vol. entering}}{\text{Vol. swept}}$$

$$\eta_{u_1} = \frac{v_1 - v_4}{v_1 - v_3}$$

$$\eta_u = 1 + c - c \left(\frac{P_2}{P_1} \right)^{\frac{1}{n}}$$

Refer power plant notes
for deriv.

$$c = \frac{v_3}{v_1 - v_3} \quad \text{clearance ratio.}$$

n - polytropic index.

$$\begin{aligned} \eta_u &= \frac{\dot{m} \times 60 \times v_1}{\sum D^2 L \times N \times K} \\ &= \frac{\dot{m} \times 60 \times v_1}{v_s \times N \times K} \end{aligned}$$

$\xrightarrow{*}$

\dot{m} - kg/min
 v_1 - m³/kg.
 D - m
 L - rev/min
 N - No. of Cylinder.

$$\begin{aligned} \frac{Q_g}{p_g u_B} & C = 0.03 \\ \eta_v &= 1 + c - c \left(\frac{P_2}{P_1} \right)^{\frac{1}{n}} \\ &= 1 + 0.03 - 0.03 \left(\frac{7.45}{1.5} \right)^{1.5} \\ \eta_v &= 0.942 \\ 0.942 &= \frac{\dot{m} \times 60 \times 0.089}{v_s \times N \times K} \end{aligned}$$

$$ITR = 3.561 \text{ KW}$$

Ques

$$\eta_v = 1 + c - c \left(\frac{P_2}{P_1} \right)^{1/n}$$

$$\eta_v = 1 + 0.03 - 0.030 \left(\frac{7.45}{1.5} \right)^{1/15}$$

$$\eta_v = 0.9091$$

$$\eta_v = \frac{\text{Vol. entering}}{\text{Vol swept}} = \dot{m} \times v_1$$

$$\text{R.C.} = \dot{m} \cdot \text{R.E.}$$

$$2 \times 3.5167 = \dot{m}(h_1 - h_u) = \dot{m}(h_1 - 65)$$

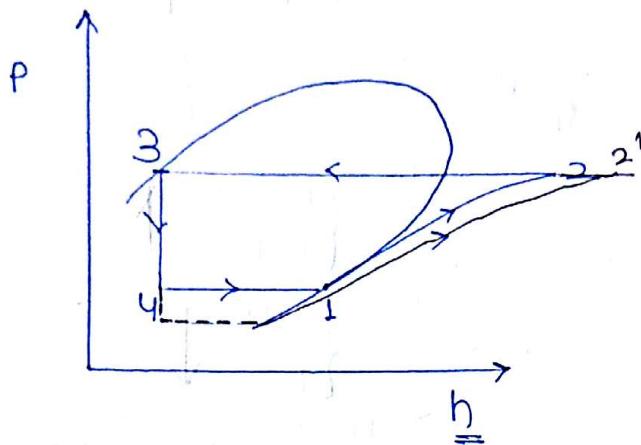
$$\dot{m} = 0.06336 \text{ kg/sec.}$$

$$(V)_{\text{actual}} = \frac{0.06336 \times 0.1089}{0.9091}$$

$$V_{\text{act.}} = 7.58 \times 10^{-3} \text{ m}^3/\text{s.}$$

Effect of Variation of various properties on the performance of VC cycle.

1) Reduction in evaporator pressure:-



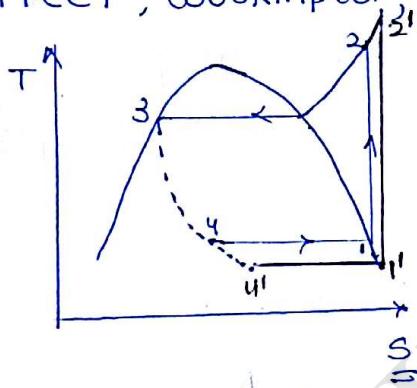
(i) R.E. ↓

(ii) W_{Vp} ↑

$$(iii) \downarrow COP = \frac{R.E. \downarrow}{W_{Vp} \uparrow}$$

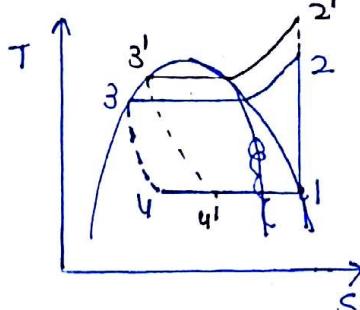
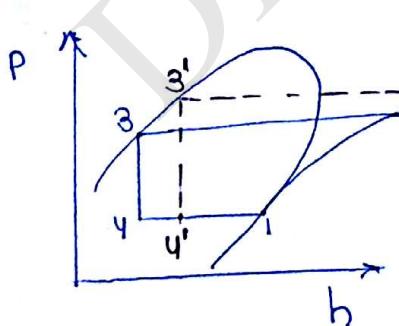
$$(iv) \downarrow \eta_v = 1 + c - c \left(\frac{P_2}{P_1} \right)^{\gamma_m}$$

→ Reduction in evaporator pressure decrease the Refrigeration effect, workinput, COP and Volumetric efficiency.



→ The evaporator pressure depends on the temp. of the evaporator, which depends on the desired effect of the machine. (i.e. Air conditioning or ice making)

2) Increase in Condenser pressure:



(i) R.E. ↓

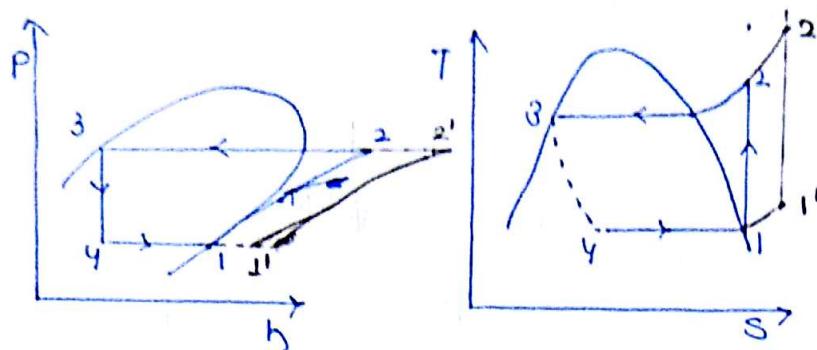
(ii) W_{Vp} ↑

$$(iii) \downarrow COP = \frac{R.E. \downarrow}{W_{Vp} \uparrow}$$

$$(iv) \downarrow \eta_v = 1 + c - c \left(\frac{P_2}{P_1} \right)^{\gamma_m}$$

→ The condenser pressure depends on the condenser temp. which further depends on the ambient temperature.

3) Superheating of the Suction vapour to the Compressor:-



- (i) R.E. ↑
- (ii) $W_{IP} \uparrow$
- (iii) $COP = \frac{R.E.}{W_{IP}}$

For:

R-134a	↑
R-12	

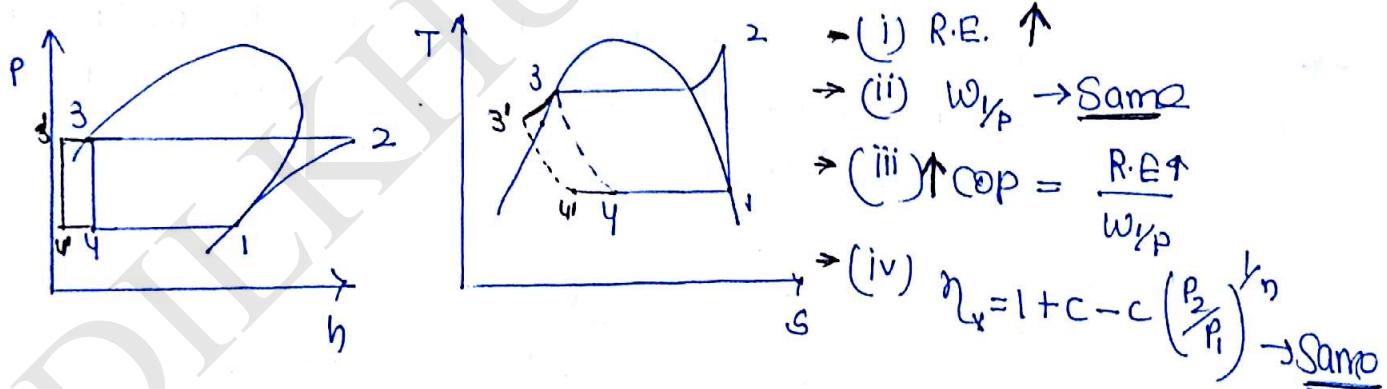
NH ₃	↓
R-22	

- (iv) $\eta_u = \underline{\text{remain same}}$

→ Work input increases due to superheating because superheating increase the volume of the fluid.

Since both R.E and W_{IP} increases hence COP may increase, decrease or remain constant. In case of R-134a and R-12 COP increases with superheating whereas in case of R-22 & NH₃, decrease with superheating COP.

4) Subcooling of liquid in the Condensor:



- (i) R.E. ↑
- (ii) $W_{IP} \rightarrow \underline{\text{Same}}$

→ (iii) $\uparrow COP = \frac{R.E. \uparrow}{W_{IP}}$

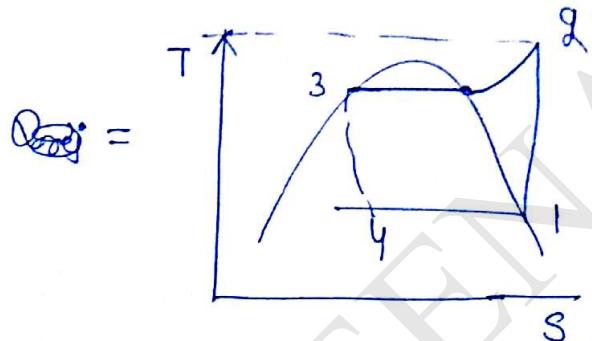
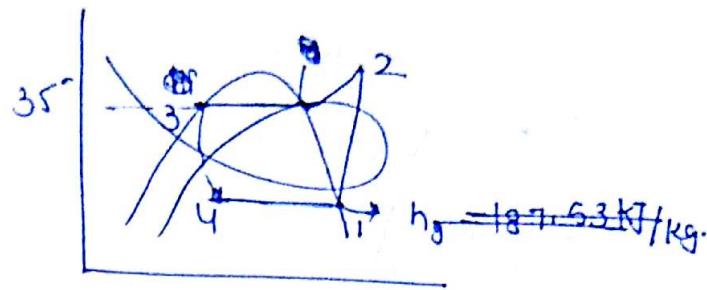
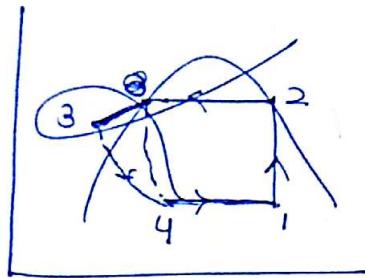
→ (iv) $\eta_u = 1 + c - c \left(\frac{P_2}{P_1} \right)^{k_n} \rightarrow \underline{\text{Same}}$

Q.18

$$COP = 6.5$$

$$\left. \begin{array}{l} h_f = 69.55 \text{ kJ/kg} \\ h_g = 201.50 \text{ kJ/kg} \end{array} \right\}$$

$$C_p = 0.6155 \text{ kJ/kg.}$$



$$h_2 = h_g + C_p \cdot \frac{T_2 - T_3}{T_3} (T_2 - T_3)$$

$$h_2 = 201.5 + 0.6155 (T_2 - 308)$$

$$COP = \frac{\text{R.E.}}{W_{I/P}}$$

$$6.5 = \frac{h_1 - h_4}{h_2 - h_1}$$

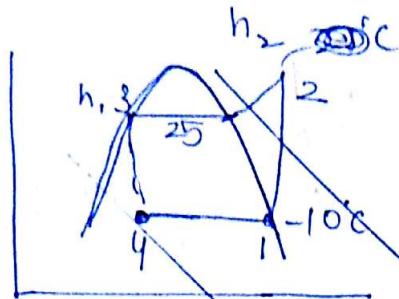
$$6.5 = \frac{201.5 - 69.55}{h_2 - 201.5}$$

$$h_2 = 205.68 \text{ kJ/kg.}$$

$$205.68 = 201.5 + 0.6155 (T_2 - 308)$$

$$T_2 = 41.79^\circ\text{C}$$

Q.17



$$COP = \frac{h_1 - h_4}{h_2 - h_1}$$

$$COP =$$

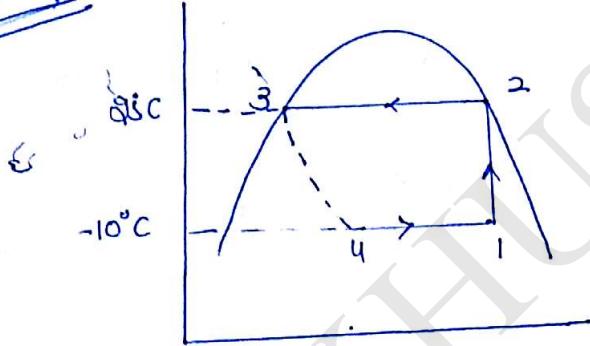
~~$$COP = \frac{1465.84 - 298.9}{-1433.05}$$~~

~~$$COP = \frac{1433.05 - 298.9}{-1433.05}$$~~

$$h_3 = h_4 = h_f + x P_f x$$

$$S_2 = S_g \Big|_{-10^\circ C} = S_g + C_v \ln \left(\frac{T_2}{T_3} \right)$$

Q.17



$$h_2 = 1465.84$$

$$h_3 = h_4 = 298.9$$

$$S_1 = S_2$$

$$S_f + x(S_g - S_f) \Big|_{-10^\circ C} = S_g \Big|_{25^\circ C}$$

@ 25°C

$$S_{fg} = \frac{h_g - h_f}{T_{sat}}$$

$$S_g - S_f = S_g - 1.125 = \frac{1465.84 - 298.9}{298}$$

$$S_g = 5.046 \text{ at } 25^\circ C$$

(@ -10°C) $S_g - S_f = \frac{h_g - h_f}{T_{sat}} \Rightarrow S_g - S_f = \frac{1433.05 - 135.37}{263}$

$$S_{fg} = 4.934$$

Now

$$0.5443 + x(4.934) = 1.1242$$
$$x = 0.91$$

So $h_1 = h_f + x_1 h_{fg}$ at -10°C

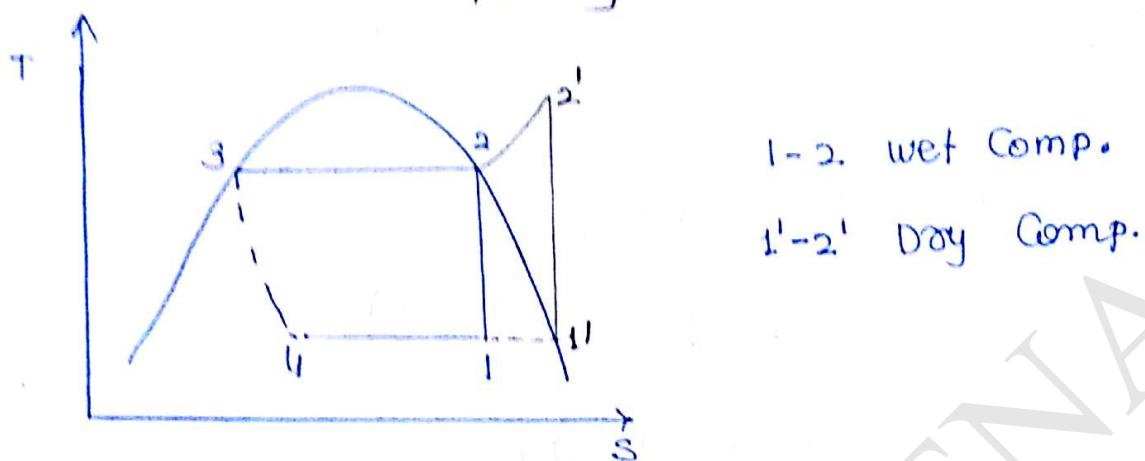
$$= 138.37 + 0.91(1433.5)$$

$$h_1 = 1317.57 \text{ kJ/kg}$$

$$\text{COP} = \frac{h_1 - h_4}{h_2 - h_1} = \frac{1317.54 - 298.9}{1465.84 - 1317.54}$$

$$\text{COP} = 6.8 \text{ Au}$$

Wet Compression Vs Dry Compression:-



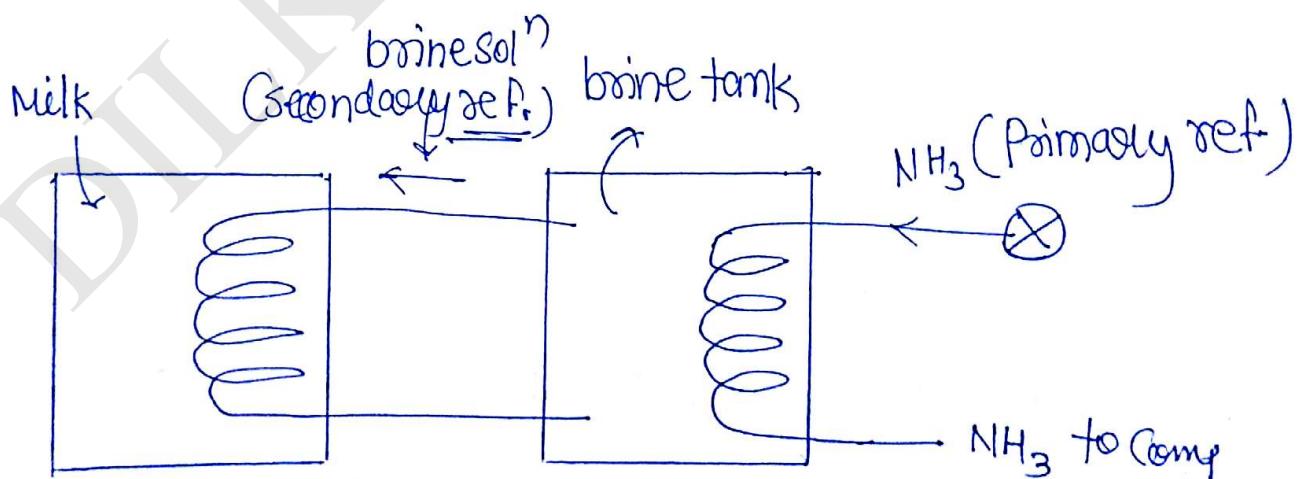
- In wet compression the refrigeration effect is less than the dry compression due to incomplete vapourisation of refrigerant.
- In wet compression the work input is also less as compared of dry comp. because of lower specific volume.
- Generally the COP is more with wet comp. but whenever reciprocating compressor is used wet compressor is not preferred because
 - (i) liquid particles in the refrigerant wash away the lubricating oil hence increase wear and tear of the compressor
 - (ii) ~~leak.~~ ~~oil~~ damage the valves in the reciprocating compressor.

Secondary Refrigerant and Primary Refrigerent:-

- The refrigerant which flows through the refrigeration equipment is called primary refrigerant.
- Secondary refrigerant which absorbs heat from the refrigerated space and rejects to the primary refrigerant.
- Secondary refrigerant used in milk chilling plants, is brine solution. (water + salt)
In Air conditioning the secondary refrigerant is air.

Use of secondary refrigerant helps in

(i) Saving the cost associated with the amount of primary refrigerant.
(ii) It facilitates the use of a primary refrigerant having good thermodynamic properties irrespective of its toxic nature. (eliminate direct mixing)



Q.20



$$\begin{aligned} Q &= m \left\{ C_w dT + L.H. + C_{\text{ice}} dT \right\} \\ &= 8640 (4.18 \times 35 + 334.72 + 2.26 \times 8) \end{aligned}$$

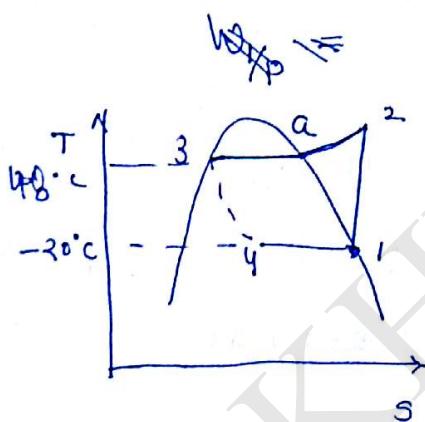
$$Q = 43122.2 \text{ kJ}$$

$$\dot{Q} = \frac{Q}{24 \times 3600} = 49.91 \text{ kW} \quad P.$$

$$\begin{aligned} \text{R.C.} &= \dot{Q} \times 1.1 \\ &= 49.91 \times 1.1 \end{aligned}$$

$$\text{R.C.} = 54.901 \text{ kW}$$

primary ref. remove
this amount of heat.



$$h_1 = 178.74 \text{ kJ/kg}$$

$$h_4 = h_3 = 82.83 \text{ kJ/kg}$$

$$s_3 = s_1 = s_2$$

$$0.7087 = s_g + C_p \ln \left(\frac{T_2}{T_{\text{sat}}} \right)$$

$$0.7078 = 0.6802 + 0.82 \ln \left(\frac{T_2}{321} \right)$$

$$T_2 = 331.9 \text{ K}$$

$$h_2 - h_a = C_p (T_2 - T_a)$$

$$h_2 = 205.83 + 0.82 (331.9 - 321)$$

$$h_2 = 215.135 \text{ kJ/kg}$$

$$COP = \frac{h_1 - h_4}{h_2 - h_1} = 2.63$$

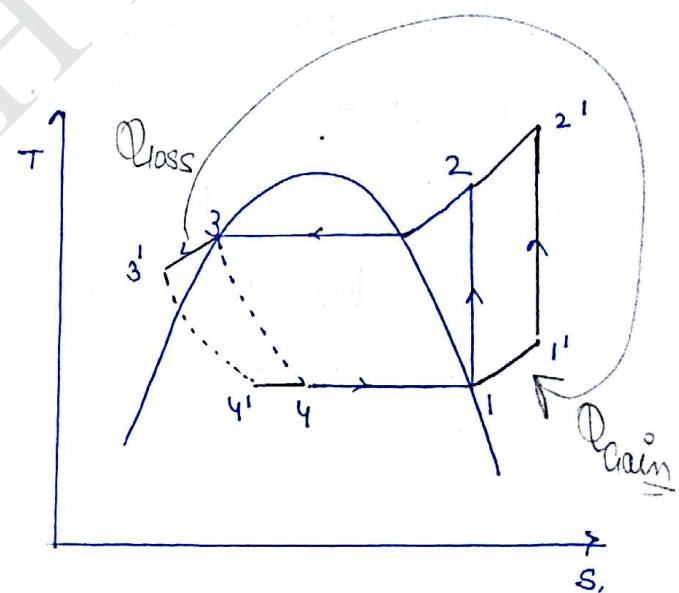
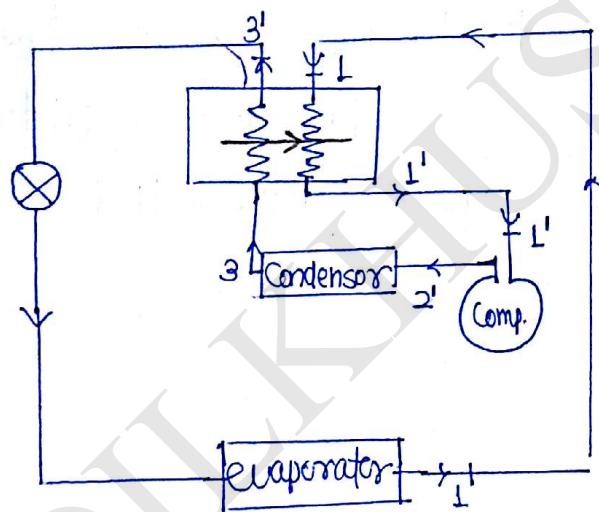
$$2.63 = \frac{R_c}{W_{Y_p}}$$

$$W_{Y_p} = \frac{54,901}{2.63}$$

$$W_{Y_p} = 20.84 \text{ kW}$$

Use of Regenerative heat exchanger

* (Liquid line heat exchanger or Sub cooling H.E.)



$$\therefore Q_{\text{lost}} = Q_{\text{gain}} \quad R.P = (h_1 - h_4) + (h_u - h_{u'})$$

$$h_3 - h_{3'} = h_{1'} - h_1$$

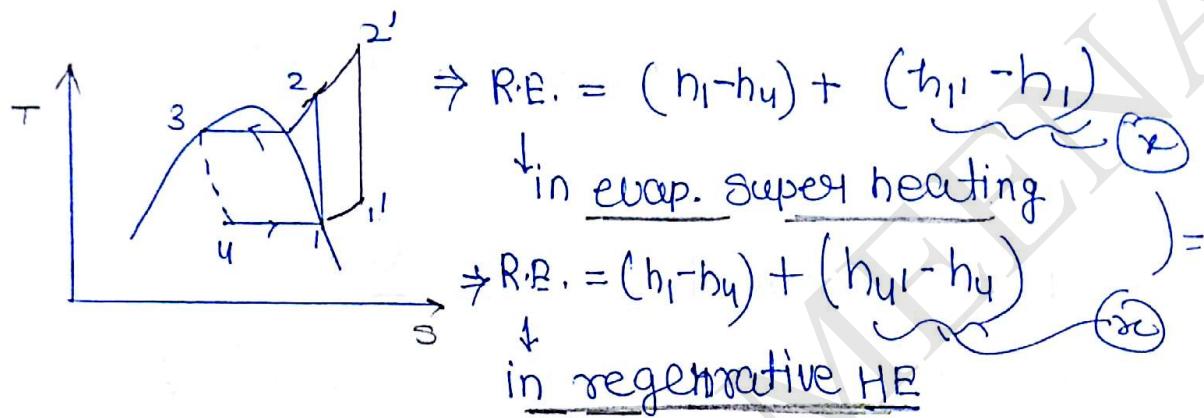
$$C_{P_{\text{Liq}}} (T_3 - T_{3'}) = C_{P_v} (T_{1'} - T_1)$$

Degree of
Subcooling

Degree of
superheating

→ In regenerative heat exchanger Heat loss is equal to heat gained by degree of subcooling is not equal to degree of superheating because specific heat of liquid & vapour is different.

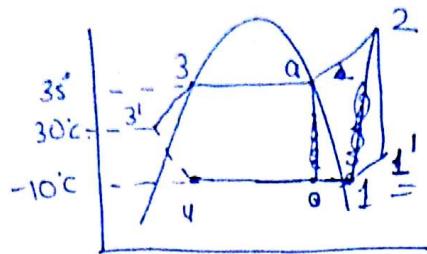
Use of Regenerative heat exchanger V/S superheating in evaporator



* In both the cases the ~~same~~ R.E., work input and hence COP comes out to be same but the increased refrigeration effect is obtained at a lower temp. in regenerative H.E.
Compare to evaporator.

(22)

$$R.C. = 50 \text{ kW}$$



$$\begin{aligned} R.C. &= \dot{m}(R.E.) \\ &= \dot{m}(h_1 - h_4) \end{aligned}$$

$$h_1 = 1488.57 \text{ kJ/kg.}$$

$$h_3 = \underline{366.07} \text{ kJ/kg.}$$

$$h_3' = h_3 - C_p \ln\left(\frac{T_3}{T_3'}\right) (T_3 - T_3')$$

$$h_3' = 366.07 - 4.556 \ln\left(\frac{308}{303}\right)(308 - 303)$$

$$h_4 = \underline{h_3'} = \underline{343.29} \text{ kJ/kg}$$

$$S_g|_{35} = S_f + x S_{fg}|_{-10}$$

$$5.2086 = 0.82965 + x()$$

$$x = 0.88$$

$$\begin{aligned} h_1 &= h_f + x h_{fg} \\ h_1 &= \underline{1294.68} \end{aligned}$$

$$\begin{aligned} 50 \text{ kJ/s} &= \dot{m} (1294.68 - 343.29) \\ \dot{m} &= g \end{aligned}$$

$$\begin{aligned} W &= 0.6525 (1488.57 - 1294.68) \\ &= \underline{16.18 \text{ kW}} \end{aligned}$$

$$L = 1.2 \underline{D}$$

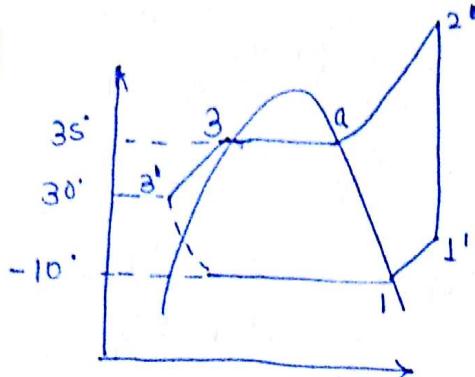
$$V = V_f + x V_{fg}$$

$$=$$

$$\begin{aligned} V &= \frac{\pi}{4} D^2 L \\ &= \frac{\pi}{4} (D^2) 1.2 \underline{D} \end{aligned}$$

$$D = 0.67 \underline{m}$$

Q.22



$$h_1 = 1450.22$$

$$h_3 = 366.07$$

$$h_a = 1488.07$$

$$h_{3'} - h_{31} = \frac{C_p}{4.556} \left(T_3 - T_{31} \right)$$

$$h_{3'} = 343.29 \text{ kJ/kg.}$$

$$Q_{\text{loss}} = Q_{\text{gain}}$$

$$h_3 - h_{31} = h_1 - h_1'$$

$$366.07 - 343.29 = h_1' - 1450.22$$

$$h_1' = 1473.$$

$$h_{11} - h_1 = \frac{C_p}{2.492} \left(T_{11} - T_1 \right)$$

$$T_{11} = 272.14 \text{ K.}$$

$$S_{11} = S_1 + C_p \ln \frac{T_{11}}{T_1} = 5.755 + 2.492 \ln \frac{272.14}{263}$$

$$\therefore S_{11} = 5.840 \text{ kJ/kg K}$$

$$S_1' = S_{11} = S_a + C_p \ln \frac{T_{11}}{T_a}$$

$$5.2086 = 5.2086 + 2.4903 \ln \frac{T_{11}}{308}$$

$$T_{11}' = 382.84 \text{ K}$$

$$h_{21} - h_a = C_p v (T_2 - T_a)$$

$$h_{21} = 1488.57 + 2.903(382.84 - 308)$$

$$h_{21}' = 1705.86$$

$$COP = \frac{R.E.}{W_{IP}} = \frac{h_1 - h_{u1}}{h_{21}' - h_1}$$

$$COP = 4.75$$

$$COP = \frac{Re}{W_{IP}} = 4.75 = \frac{50}{W_{IP}}$$

$$W_{IP} = 10.51 \text{ kW}$$

$$\eta_v = \frac{(\dot{m} \times 60) \varphi_1'}{\frac{\pi}{4} D^2 L \times N \times K} \quad \eta_v = \underline{\underline{1}} \quad (\text{let})$$

$$R.C. = \dot{m} \times R.E.$$

$$\dot{m} = \frac{50}{(h_1 - h_{u1})}$$

$$\dot{m} = 0.045 \text{ kg/s.}$$

$$L = 1.2D, K = \underline{\underline{1}}$$

$$\frac{v_1}{T_1} = \frac{v_1'}{T_1'} \quad \Rightarrow$$

$$\frac{0.041749}{0.63} = \frac{v_1'}{272.14}$$

$$v_1' = 0.4319$$

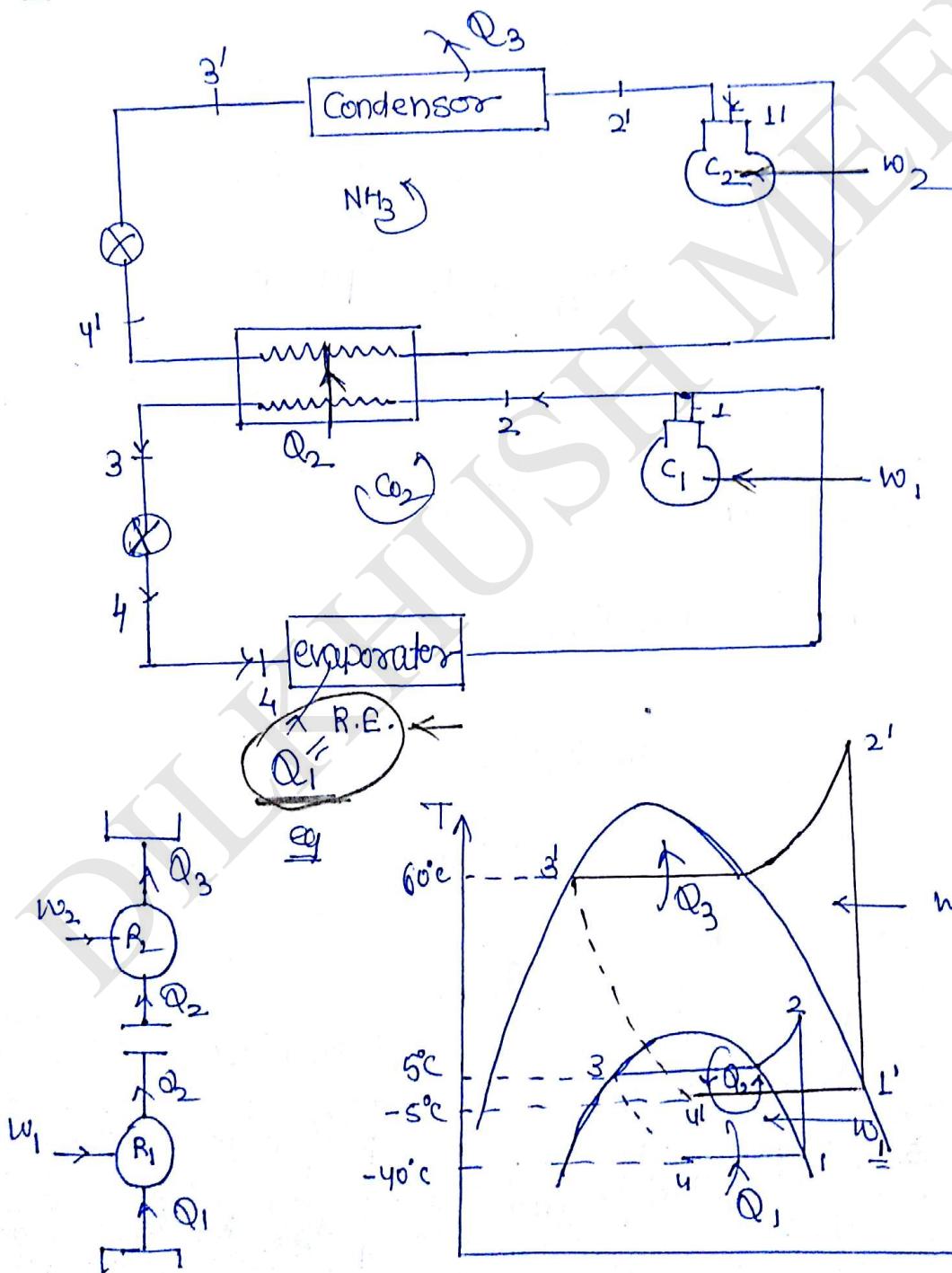
$$\frac{(0.045 \times 60) \times 0.4319}{\frac{\pi}{4} D^2 \times 1.2D \times 1000 \times 1} = 1$$

$$D = 107.49 \text{ mm}$$

$$L = 128.9 \text{ mm}$$

Cascade Refrigeration System:-

- * For producing very low temp the corresponding pressure ratio becomes very high hence the volumetric efficiency becomes very low therefore cascading of refrigeration system is done.
- * It is used in medical industry.



$$COP_1 = \frac{Q_1}{W_1}, \quad COP_2 = \frac{Q_2}{W_2}$$

$$\boxed{COP = \frac{Q_1}{W_1 + W_2}}$$

To prove

$$COP = \frac{COP_1 \cdot COP_2}{1 + COP_1 + COP_2}$$

$$COP = \frac{\frac{Q_1}{W_1 + W_2}}{=} \frac{\frac{Q_1}{\frac{Q_1}{COP_1} + W_2}}{=} \frac{COP_1 \times Q_1}{Q_1 + W_2 COP_1}$$

$$COP = \frac{COP_1}{1 + \frac{W_2}{Q_1} \times COP_1}$$

$$\boxed{Q_1 + W_1 = Q_2}$$

$$COP_2 = \frac{Q_2}{W_2}$$

$$1 + \frac{W_1}{Q_1} = \frac{Q_2}{Q_1}$$

$$1 + \frac{1}{COP_1} = \frac{Q_2}{Q_1}$$

$$COP = \frac{COP_1}{1 + \frac{COP_2}{Q_1} \times \frac{Q_2}{COP_2}} = \frac{COP_1}{1 + \frac{COP_1}{COP_2} \cdot \frac{Q_2}{Q_1}}$$

$$\boxed{COP = \frac{COP_1 \cdot COP_2}{1 + COP_1 + COP_2}}$$

Q. A cascade refrigeration system of 100 TR capacity used NH_3 & CO_2 . The evaporating & condensing temp. of CO_2 are -40°C and 5°C respectively. The evaporating temp. for NH_3 is -7°C . Power supplied to NH_3 compressor is 96.5 kW. Both CO_2 and NH_3 cycles are simple VC cycles. Calculate

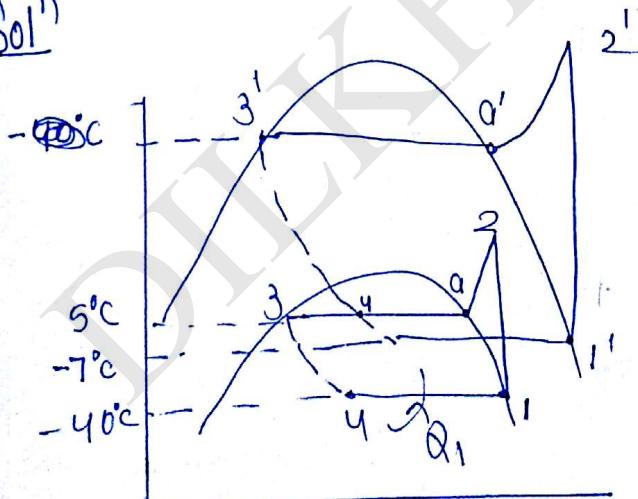
(i) Mass flow rate of refrigerant CO_2 (kg/s)

(ii) COP of the ref. system.

$$\text{For } \text{CO}_2 \quad C_{p,\text{e}} = 0.85 \text{ kJ/kgK}$$

$t(\text{C})$	$P(\text{bar})$	h_f	h_g	s_f	s_g
-40°C	10.05	332.7	652.8	3.8531	5.2262
5°C	39.7	431.0	649.8	4.2231	5.0037

Solⁿ



$$Q_1 = R \cdot E = 100 \text{ TR}$$

$$R \cdot E = 351.67 \text{ kW}$$

$$h_1 = 652.8 \text{ kJ/kg}$$

$$h_3 = 431. \text{ kJ/kg} = h_4$$

$$\underline{P_C} = \dot{m}(h_1 - h_2)$$

$$351.67 = \dot{m}(652.8 - 431)$$

$$\dot{m} = 1.58 \text{ kg/s}$$

$$(COP)_1 = \frac{h_1 - h_4}{h_2 - h_1}$$

$$h_2 = h_a + C_{p,g} (T_2 - T_a)$$

$$s_2 = s_1$$

$$s_1 = s_a + C_{p,g} \ln \frac{T_2}{T_a}$$

$$\frac{s.0037}{5.2262} = s.0037 + 0.85 \ln \frac{T_2}{278}$$

$$T_2 = \underline{\underline{374.7}} \text{ K}$$

$$h_2 = 649.8 + 0.85 \left(\frac{374.7 - 278}{361.18} \right)$$

$$\cancel{h_2 = 712 \text{ kJ/kg}} \quad h_2 = 720.503 \text{ K}$$

$$(COP)_1 = \frac{625.652.8 - 431}{720.503 - 652.8} = \underline{\underline{3.27}}$$

$$\frac{Q_1}{W_1} = 3.97 \Rightarrow W_1 = \frac{1.58 (652.8 - 431)}{3.27}$$

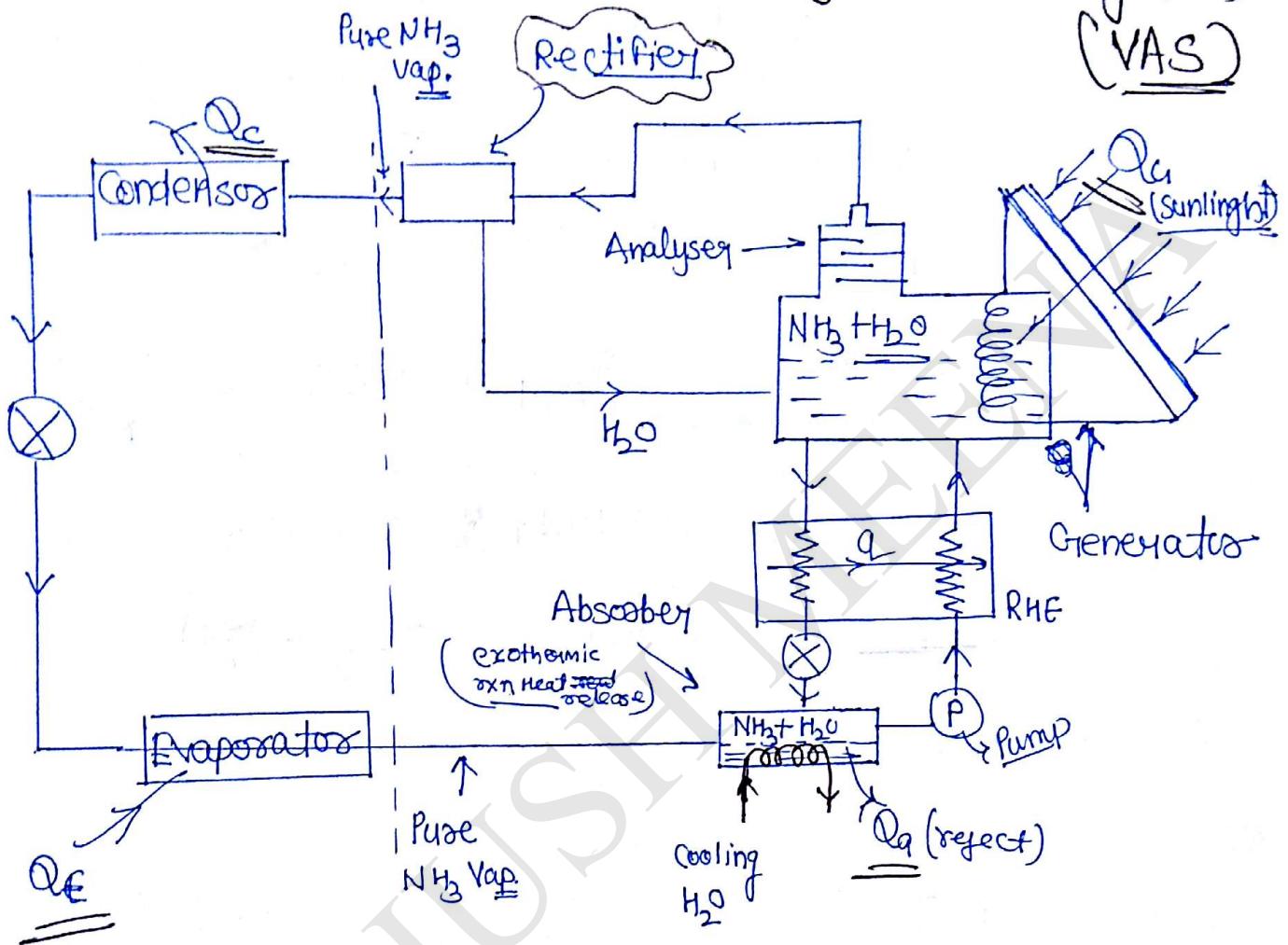
$$W_1 = \underline{\underline{93.7 \text{ kW}}} \quad W_1 = \underline{\underline{106.97}}$$

$$W_2 = \underline{\underline{96.5 \text{ kW}}}$$

$$\boxed{COP = \frac{Q_1}{W_1 + W_2}} = \frac{1.58 (652.8 - 431)}{903.47}$$

$$COP = 1.72$$

* Vapour Absorption Refrigeration System (VAS)



→ Pure NH_3 vapour enters the absorber where it is absorbed in water (H_2O). The reaction is exothermic and the solubility of NH_3 is inversely proportional to temp. of solution. Cooling water is continuously circulating to maintain a low temp. of solution to facilitate absorption of NH_3 . Solution rich in NH_3 is pumped to Generator via Regenerative heat exchanger in Generator this solution absorbs heat and NH_3 separates

forming high pressure NH_3 vapour.

- In RHE solution absorbs some heat from the water moving towards absorber. This reduces the need for heat absorption in generators.
- High pressure NH_3 vapour is passed through analyser where water vapour condenses. For complete removal of water vapour present with NH_3 vapour rectifier is installed.
- * I_h later vapour is presence is undesirable because it may freeze at the exit of the throttling valve because of low temp. thus chocking the system.

* Important Points.

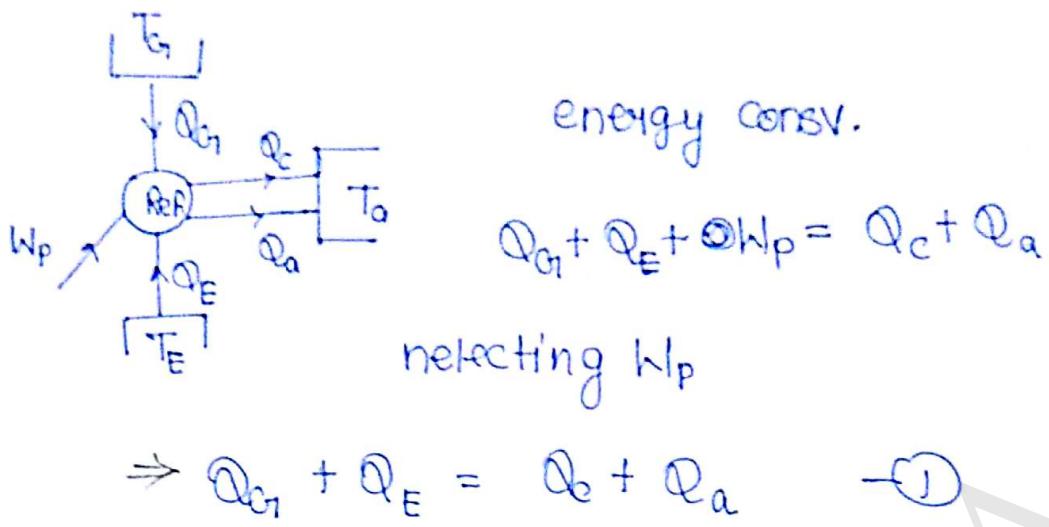
- ① VAS works on low grade energy (Heat) whereas VCRS works on high grade energy (work). hence COP of VAS is very less (0.3 to 0.5).
- ② Most popular VAS is $\text{NH}_3 - \text{H}_2\text{O}$ system. In this water is absorbent and NH_3 is refrigerant. Other popular system are $\text{H}_2\text{O} - \text{LiCl}$ & $\text{H}_2\text{O} - \text{LiBr}$. In these two water is the refrigerant hence used for Air Conditioning purpose.

- ③ VAS are used where large waste heat is available or the cost of electricity is very high. \S
Solar refrigeration system and Geothermal refrigeration system are based on VAS.
- ④ Heat is absorbed in generator and evaporator and heat is rejected in condenser & absorber.
- ⑤ Electrolux refrigeration system is a VAS. It is three fluid system. ($\text{NH}_3 - \text{H}_2\text{O} - \text{H}_2$)
- Here NH_3 is the refrigerant, H_2O is absorbent and H_2 is used to create low partial pressure of NH_3 .
- No pump is used in this system and the fluid flows under the action of gravity due to density difference.

$$\text{COP} = \frac{Q_{\text{Evaporator}}}{Q_G + W_p} \quad Q_u > W_p$$

$$\boxed{\text{COP} = \frac{Q_E}{Q_G}}$$

For $(\text{COP})_{\text{max}}$ Refrigerator — Reversible.



$$\text{2nd law} \Rightarrow \oint_{\text{rev.}} \frac{dQ}{T} = 0$$

$$\Rightarrow \frac{Q_{G1}}{T_{G1}} + \frac{Q_E}{T_E} - \frac{Q_a + Q_c}{T_o} = 0 \quad \rightarrow \textcircled{2}$$

from eqn ① & ②

$$\frac{Q_{G1}}{T_{G1}} + \frac{Q_E}{T_E} - \frac{Q_{G1} + Q_E}{T_o} = 0$$

$$Q_E \left[\frac{1}{T_E} - \frac{1}{T_o} \right] = Q_{G1} \left[\frac{1}{T_o} - \frac{1}{T_{G1}} \right]$$

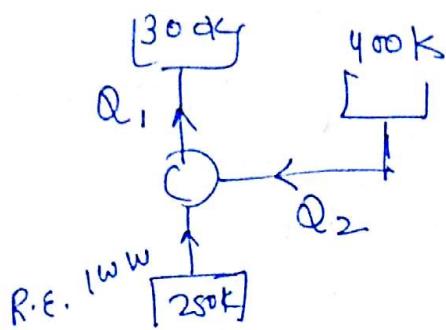
$$Q_E \left[\frac{T_o - T_E}{T_o T_E} \right] = Q_{G1} \left[\frac{T_{G1} - T_o}{T_o T_{G1}} \right]$$

$$\frac{Q_E}{Q_{G1}} = \frac{T_E(T_{G1} - T_o)}{T_{G1}(T_o - T_E)}$$

$$\boxed{\frac{(COP)_{\max}}{} = \frac{T_E(T_{G1} - T_o)}{T_{G1}(T_o - T_E)}}$$

Pg. 49

Q. 13
w.b.



$$\frac{Q_1}{3\omega} = \frac{Q_2}{4\omega} + \frac{\frac{2}{5}Q_2}{\frac{250}{5}}$$

$$Q_1 = 100 + Q_2$$

$$\frac{100 + Q_2}{3\omega} = \frac{Q_2}{4\omega} + \frac{2}{5}$$

$$\frac{1}{3} + \frac{Q_2}{3\omega} = \frac{Q_2}{4\omega} + \frac{2}{5}$$

$$\frac{\frac{1}{3} - \frac{2}{5}}{\frac{5-6}{15}} = Q_2 \left(\frac{4\omega - 3\omega}{4\omega \times 3\omega} \right)$$

~~ref~~ $Q_2 = -80W$

(T1)

$$T_a = 360K$$

$$T_b = 310K$$

$$T_e = 260 \rightarrow 250K$$

$$COP = \frac{T_e(T_a - T_b)}{T_a(T_b - T_e)}$$

$$COP = \frac{260(50)}{360 \times 50} = \frac{250(T_a - 310)}{T_a(310 - 250)}$$

$$\frac{13}{18} = \frac{250 T_a - 250 \times 310}{T_a \times 310 - T_a \times 250}$$

$$T_a = 374.9K$$

$$(12) \quad \text{CoP} = \frac{T_E(T_{G1} - T_0)}{T_{G1}(T_0 - T_E)} =$$

$$\underline{\text{CoP}} = \frac{258(383 - 328)}{383(328 - 258)} = 0.529$$

$$(11) \quad \text{CoP} = \frac{270(360 - 300)}{360(300 - 270)} = \frac{270 \times 60}{360 \times 30}^2 \\ \text{CoP} = 1.5$$

Ques In $\text{NH}_3\text{-H}_2\text{O}$ absorption system heat is supplied to generator by condensing steam at 0.2 MPa. The initial state of steam is at a dryness fraction of 0.9 and the final state of the steam after condensing is saturated liquid. The temp. to be maintained in evaporator is -10°C and the surrounding temp is 30°C

- Find $(\text{CoP})_{\text{max}}$
- If the actual CoP is 40% of max CoP and refrigeration load is 20 TR, what will be the required steam flow rate (kg/sec) at 0.2 MPa

$T_{\text{sat.}} \\ 120.2^\circ\text{C} \quad h_f = 2201.9 \frac{\text{kJ}}{\text{kg}}$

SOL

$$\begin{aligned} (\text{COP})_{\max} &= \frac{T_E (T_G - T_o)}{T_G (T_o - T_E)} \\ &= \frac{263 (128.2 - 30)}{120.393.2 (30 + 10)} \end{aligned}$$

$$(\text{COP})_{\max} = 1.508$$

$$R.E. = R E \times \dot{m}$$

$$\cancel{Q_0 \times 3.51} = \cancel{(h_1 - h_4)} \times \dot{m}$$

$$(\text{COP})_{act} = 0.4 (\text{COP})_{\max}$$

$$\textcircled{1} \quad \frac{RE}{w_{IP}} = 0.4 \times 1.508 = 0.603$$

$$RE = \cancel{U_{2.34}} = \dot{m} (h_1 - h_4)$$

$$\cancel{U_{2.34}} = \dot{m} (h_f + x h_{fg} - h_f)$$

$$\dot{m} =$$

$$\frac{RC}{\dot{Q}_G} = 0.603 = \frac{\cancel{Q_0 \times 3.5167}}{\dot{m} \times x \times h_{fg}}$$

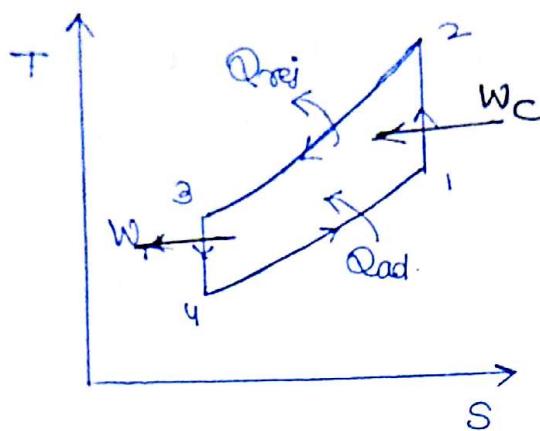
$$\dot{m} = 0.058 \frac{\text{kg}}{\text{s}}$$

29/11/2016

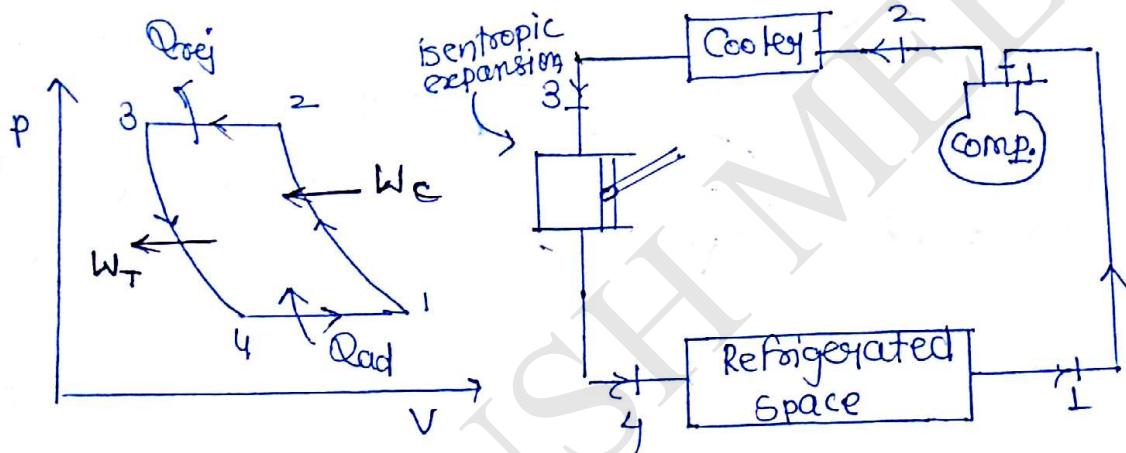
* Gas Refrigeration Cycle (Revised Brayton)

→ (Air craft - air conditioning cycle)

{ - Gas liquefaction cycle
- Bell Coleman cycle.



- $1 \rightarrow 2$ isentropic comp.
- $2 \rightarrow 3$ isobaric heat rej.
- $3 \rightarrow 4$ isentropic exp.
- $4 \rightarrow 1$ isobaric heat addition



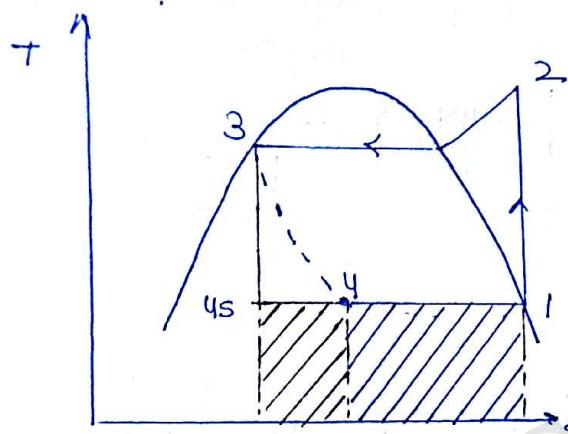
- This cycle is used for air craft air conditioning because of it's low weight per ton of refrigeration.
- Air conditioning is done for the cooling of the air-craft because since the air craft moves at high velocity due to skin friction a lot of heat is generated.

→ Isentropic expander v/s throttling :-

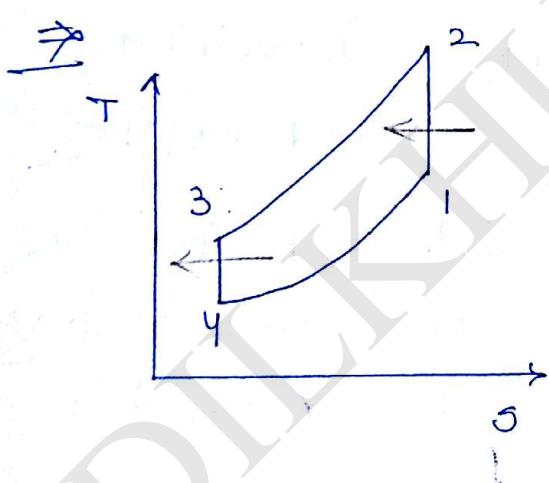
- In gas refrigeration cycle since air is used as refrigerant which behaves as ideal gas hence throttling does not result in any temp. drop. Moreover use of isentropic expander gives some work

output which reduces the work input from outside.

→ In NCRS we don't use isentropic expander because the refrigerant remain liquid during most of its expansion hence the work obtained is very less this does not justify the cost of the isentropic expander. Hence throttling is used since it is very cheap device.



(Area) $4s-4$ → extra R.E.
due to
isentropic
expander



expression for COP = ?

$$COP = \frac{R.E.}{W_c - W_T}$$

$$R.E. = h_1 - h_4$$

$$= C_p(T_1 - T_4)$$

$$W_c = h_2 - h_1 = C_p(T_2 - T_1)$$

$$\therefore W_T = h_3 - h_4 = C_p(T_3 - T_4)$$

$$COP = \frac{(T_1 - T_4)}{(T_2 - T_1) - (T_3 - T_4)}$$

$$COP = \frac{T_1 - T_4}{(T_2 - T_3) - (T_1 - T_4)}$$

$$COP = \frac{\frac{1}{\frac{T_2 - T_3}{T_1 - T_4} - 1}}{\frac{1}{\frac{T_2}{T_1} \left(1 - \frac{T_3}{T_2}\right)} - 1}$$
①

\therefore Comp & exp. are isentropic.

$$\therefore \frac{T_2}{T_1} = \left(\frac{P_2}{P_1}\right)^{\frac{r-1}{r}} = \gamma_p^x$$

$$\text{let } \frac{r-1}{r} = x$$

$$\rightarrow \frac{T_3}{T_4} = \gamma_p^x$$

$$\text{Since } \frac{T_2}{T_1} = \frac{T_3}{T_4} \Rightarrow \frac{T_4}{T_1} = \frac{T_3}{T_2}$$

$$1 - \frac{T_4}{T_2} = 1 - \frac{T_3}{T_2}$$

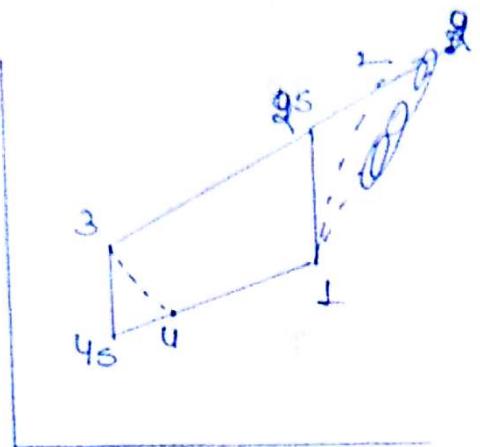
From ①

$$COP = \frac{1}{\frac{T_2}{T_1} - 1}$$

$$COP = \frac{1}{\gamma_p^x - 1}$$

$$COP = \frac{1}{\gamma_p^x - 1}$$

$$COP = \frac{1}{\frac{r-1}{r} \gamma_p^x - 1}$$



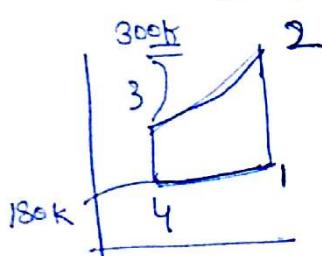
$$\eta_{isc,C} = \frac{T_{2S} - T_1}{T_2 - T_1}$$

$$\eta_{isc,T} = \frac{T_3 - T_4}{T_3 - T_{4S}}$$

Q. 3

$$COP = \frac{1}{\left(\gamma_p\right)^{\frac{r-1}{r}} - 1} = \frac{1}{\frac{T_2}{T_1} - 1}$$

$$COP = \frac{1}{\frac{300}{180} - 1} = 1.5$$



$$\left(\frac{P_3}{P_4}\right)^{\gamma} = \frac{T_3}{T_4} = \left(\frac{P_2}{P_1}\right)^{\gamma} = \frac{T_2}{T_1} = \frac{300}{180}$$

$$P_1 = 0.1 \text{ MPa}$$

$$P_2 = 0.3 \text{ MPa}$$

$$\eta_{isc,C} = 72\%, \eta_{isc,T} = 78\%$$

$$T_1 = 277 \text{ K}$$

$$T_3 = 328$$

$$\frac{T_3}{T_{4S}} = \frac{T_{2S}}{T_1} \rightarrow$$

$$T_{4S} = 379.14$$

$$0.72 = \frac{T_{2S} - T_1}{T_2 - T_1}$$

$$0.72 = \frac{379.14 - 277}{T_2 - 277} \Rightarrow T_2 = \underline{\underline{418.86 \text{ K}}}$$

$$W_{isc,T} = 0.78 = \frac{T_3 - T_4}{T_{30} - T_{4s}} \quad \frac{T_3}{T_{4s}} = (3)^{\gamma_f}$$

$$T_{4s} = 239.63$$

$$0.78 = \frac{328 - T_4}{328 - 239.63}$$

$$T_4 = \underline{328 - 259.07} \text{ K}$$

$$\text{COP} = \frac{T_1 - T_4}{(T_2 - T_1) - (T_3 - T_4)}$$

$$= \frac{277 - 259.07}{(418.86 - 277) - (328 - 259.07)}$$

$$\text{COP} = \underline{0.245 \text{ hr}}$$

$$RC = 3 TR = \dot{m} \times R.E.$$

$$3 \times 3.51 = \dot{m} \times (1.005(T_1 - T_4))$$

$$3 \times 3.51 = \dot{m} (1.005(277 - 259.07))$$

$$\dot{m} = 0.584 \text{ kg/s.}$$

$$\text{COP} = \frac{RC}{W_{input}}$$

$$W_{IP} = \frac{3 \times 3.51}{0.245} = \underline{42.97 \text{ kW}}$$

Refrigerants:-

Naming of Refrigerants:-

① saturated hydrocarbon :- (single bond)



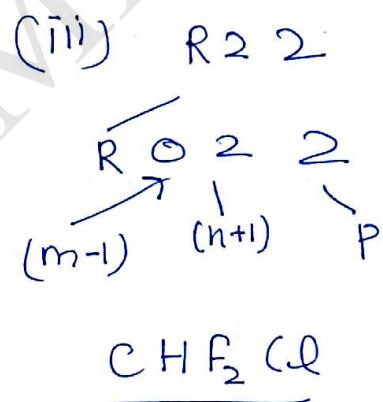
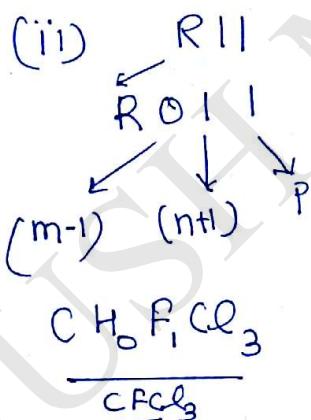
$$m+q = n+p+q \quad (\text{saturated})$$

$$\Rightarrow R(m-1)(n+1)P$$



$$\begin{aligned} m &= 1, m-1 = 0 \\ n &= 0, n+1 = 1 \\ p &= 2 \end{aligned}$$

$$\underline{R O I 2 \Leftrightarrow R I 2}$$

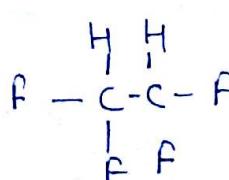
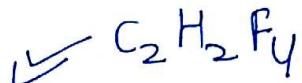
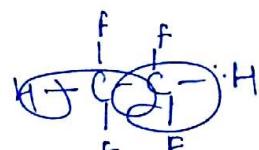
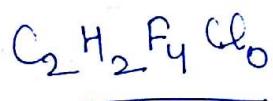


$$\begin{aligned} m &= 2 \\ n &= 0 \\ p &= 3 \end{aligned}$$

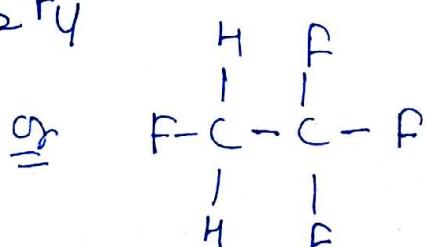
$$\underline{R O R I I 3}$$



$$\begin{aligned} m-1 &= 1, m = 2 \\ n+1 &= 3 \quad n = 2 \\ p &= 4 \end{aligned}$$

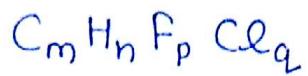


Symmetric



Asymmetric R134a

② Unsaturated hydrocarbon (double bond)



$$2m = n + p + q$$

$$\rightarrow R \downarrow (m-1)(n+1) \cancel{p-p}$$

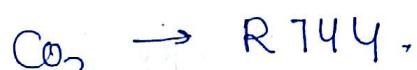


$$R \downarrow (2-1)(4+1)0$$

$$\underline{\underline{R \downarrow 150}}$$

③ Inorganic

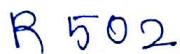
$$R (700 + \text{mol. mass})$$



④ Azeotrope:-

(as a pure substance)

$$R - (500 + \text{random No.})$$



↳ ingredient Sec butyls

- * The mixture of refrigerent behaving as pure substance is called azeotrope.

Properties of the Refrigerent

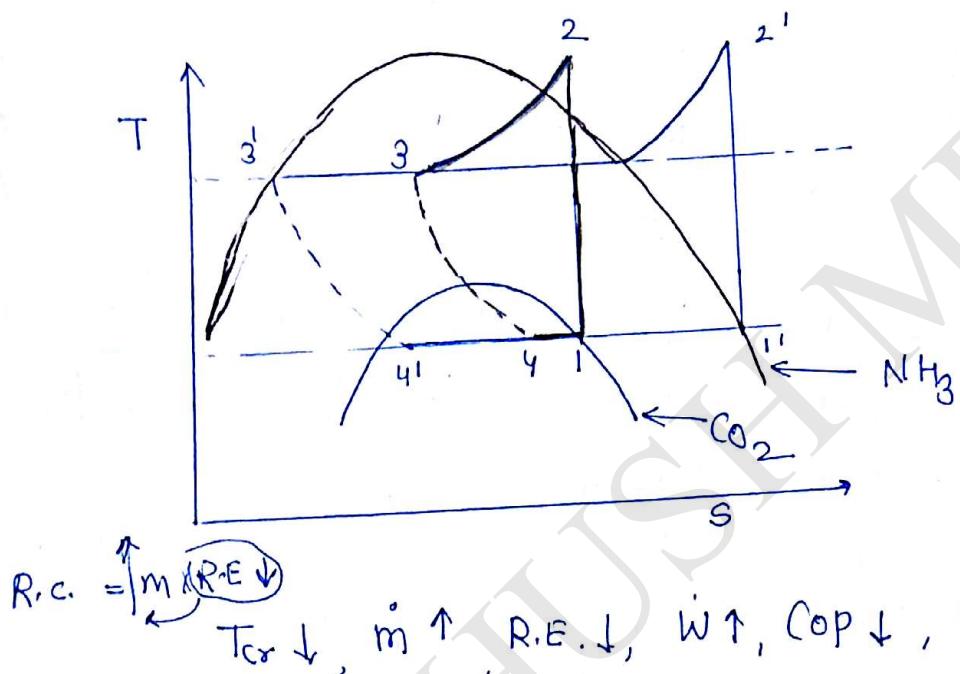
Properties of the Refrigerent.

1) Normal Boiling Point (NBP) :-

- The minimum pressure in the cycle is desired to be above atmospheric pressure. This is because if the leakage occurs, we don't want air to leak inside the system because it will bring water vapour with it self which may freeze at low temp. hence chocking the system.
- If the evaporator pressures are close to atmospheric pressure then for the refrigerant to boil at very low temp. the normal boiling point should be lower than the desired temp. Hence low NBP refrigerent are desirable.
- * low NBP refrigerent are high pressure refrigerants a high NBP refrigerents are low pressure refrigerents.

Note: The air if enters in the system get trapped in the condenser. It increase condenser pressure, compressor power and cooling water temp. The removal of trapped air in the condenser is called 'purgging'.

② Critical Point temperature:-



R.c. \Rightarrow $m \propto R.E \downarrow$
 $T_{cr} \downarrow, m \uparrow, R.E. \downarrow, w \uparrow, \text{Cop} \downarrow, \text{Vol} \uparrow$

The critical temp. of the refrigerant should be sufficiently more than the condenser temp., to facilitate heat transfer during phase change. CO_2 and ethylene have very low critical temp hence they are undesirable.

→ Water has one of the highest critical temp among the commonly used refrigerant.

Note:- Since heat transfer in Bell Coleman Cycle is sensible hence the COP of this cycle is less than VCRS.

(3) Latent heat and Specific heat:-

latent heat of the refrigerant should be high as it result in lower mass flow rate specific heat should be low in liquid phase and high vapour phase.

$$\text{R.C.} = \frac{m}{\tau_{LHT}} (R.E \uparrow)$$

(4) Freezing point:- Freezing point should be lower than the required temp. to avoid freezing of refrigerent.

→ water has good thermodynamic property but because of its high freezing point it is not used for refrigeration.

(5) Viscosity: The viscosity of refrigerant should be low to eliminate viscous loss.

(6) Pressure Ratio:- we should select a refrigerant which gives low pressure ratio corresponding to the required evaporator and condenser temp.

$$n_v \doteq n_h = 1 + c \cdot c \left(\frac{P_2}{P_1} \right)^{1/n}$$

⑦ Specific Volume at the inlet to the Compressor:

The specific volume at the compressor inlet should be less because ~~high specific volume result in large size compressor.~~ P_0

→ R11 & R113 have high specific volume hence they are used with centrifugal compressor.

⑧ Compressor discharge temperature!:-

Compressor discharge temp. should be low, high compressor discharge temp. increase compressor damage.

⑨ → Since NH_3 has high compressor discharge temp. hence NH_3 compressors are water cooled.

Note:- NH_3 has a high latent heat of vaporisation

⑨ Toxicity and flammability!:- The refrigerant should be non toxic and non flammable.

→ NH_3 has very good thermodynamic properties but is not used in domestic application because of its toxic and flammable nature.

(10) Action with the lubricating oil:-

(i) Completely immiscible:- refrigerants like NH_3 and CO_2 which are completely immiscible with the lubricating oil are separated with the help of an oil separator installed b/w compressor and condenser. The separated oil brought back to the compressor.

(ii) Completely miscible: Refrigerant like R11 & R22 which are completely miscible with the lubricating oil do not present much problem because the ~~separated~~ oil is brought the oil which is washed away by the refrigerant is brought back in the compressor.

(iii) partially miscible:- The refrigerant like R22 present problem because the lubricating oil is washed away by the refrigerant gets deposited it in the evaporator this leads to reduction in lubricating oil in the compressor hence weay & tear of compressor.

→ In such cases we use synthetic oil in place of lubricating oil.

⑩ Action with material of Construction:-

- NH₃ reacts with copper hence whenever NH₃ is used as refrigerent copper is not used as material of construction instead wrought iron or steel is used.
- Freon's react with Al hence whenever Freon's are used as refrigerent Al is not used instead Cu is used as material of construction

leak detection test:-

- ① Halide torch test: it is used to detect the leakage of p Freon's. In presence of Freon' the blue flame of hydrocarbon changes to bluish green.
- ② Sulphur Stick or Sulphur ribbon method:- it is used to detect the leakage of NH₃. White fumes of (NH₄)₂S Amoniam sulphide are formed when sulphure stick brought close to leaking NH₃.
- ③ Ammonia swab test:- A cloth dibbed in NH₃ is passed over leaking Sulphur dia oxide(SO₂) white fumes of (NH₄)₂S are formed.
- ④ soap bubble test:- Soap water is used to identify the leakage of hydrocarbon.

Recent trend in Refrigeration:-

Cl element present in the refrigerant dissociates in presence of sunlight and reacts with O_3 which is situated in stratosphere.

- ozone layer filters the harmful ultraviolet ray from the sun, hence its depletion is undesirable.
- Therefore the use of refrigerant containing chlorine (cl) has been discouraged and we have replaced R12 in domestic refrigerators with R134a.
- The substitute for chlorofluorocarbon (CFC) is
 - a) hydro carbon
 - b) fluorocarbon
 - c) hydro fluorocarbon

	<u>Name of Ref.</u>	<u>use</u>
1)	R-12	Domestic Ref. (earlier)
2)	R134a	Domestic ref. (Now) & car A/c's
3)	R - 22	window A/c
4)	R - 11	central A/c
5)	NH_3	Industrial Application (ice making)
6)	Air	Air draft + A/c
7)	CO_2	transport refrigeration and direct contact food refrigeration

* Air Conditioning *

Air conditioning :- it is the process of simultaneous control of temp., humidity, velocity and purity of Air.

Psychrometry :- it is the branch of science which deals with the properties of moist air.

→ Moist air is considered as two component hence three variables are required for our study. We have fixed total pressure equal to 1 atm therefore we are able to draw psychrometry chart in 2-D.

	v mas.
O ₂	21%
N ₂	79%

Dry air Water Vapour

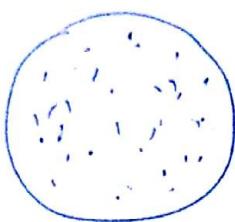
$$* P + F = C + 2$$

$$1 + F = 2 + 2 \Rightarrow F = 3$$

$$\overset{?}{P}_t = \frac{\overset{?}{P}_{\text{atm}}}{\text{---}} + \frac{\overset{?}{P}_{\text{air}}}{\text{---}}$$

$$P_{\text{total}} = 1 \text{ atm} \text{ (const.)}$$

Psychrometric Properties:-



P_t, V
 T, P_a, P_v
 m_v, m_a

$$P_v V = m_v R_v T \quad \text{--- (1)}$$

$$P_a V = m_a R_a T \quad \text{--- (2)}$$

(1) Specific humidity / humidity Ratio / Absolute humidity (w)

$$w = \frac{m_v}{m_a}$$

From eqn (1) & (2)

$$\frac{P_v}{P_a} = \frac{m_v}{m_a} \times \frac{R_v}{R_a} \rightarrow \frac{\bar{R}}{18}$$

~~mass of water vapour in moist air~~

$$\frac{P_v}{P_a} = \frac{m_v}{m_a} \times \frac{29}{18}$$

$$\therefore \frac{m_v}{m_a} = \frac{18}{29} \frac{P_v}{P_a}$$

* mass of water vapour present in moist air per kg of dry air

$$w = 0.622 \frac{P_v}{P_t - P_v}$$

kg v / kg dry air

$$m_t = m_v + m_a$$

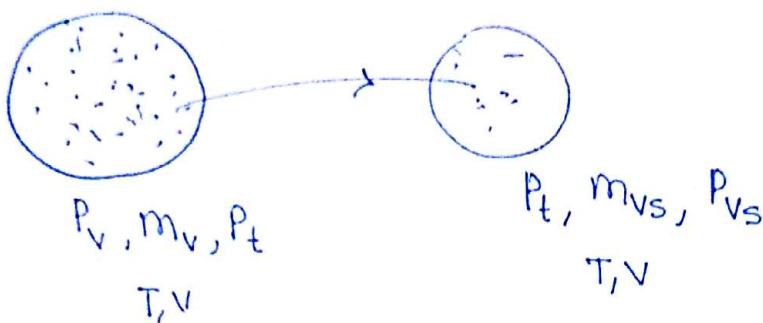
$$\frac{m_t}{m_a} = \frac{m_v}{m_a} + 1$$

$$\frac{m_t}{m_a} = w + 1$$

$$m_a = \frac{m_t}{w+1}$$

m_t
 $= H.W$

② Relative humidity: (ϕ)



$$P_v V = m_v R_v T \quad - \textcircled{1}$$

$$P_{vs} V = m_{vs} R_v T \quad - \textcircled{2}$$

$$\frac{\textcircled{1}}{\textcircled{2}} \quad \frac{P_v}{P_{vs}} = \frac{m_v}{m_{vs}}$$

*
$$\boxed{\phi = \frac{P_v}{P_{vs}} = \frac{m_v}{m_{vs}}} \rightarrow \text{saturated } V.$$

* Relative humidity represent vapour absorption capacity whereas specific humidity represent the actual mass of vapour.

* If the relative humidity is 100%, air is called as saturated air

③ Dry bulb temp. (DBT):- It is the normal temp. measured by an ordinary thermometer.

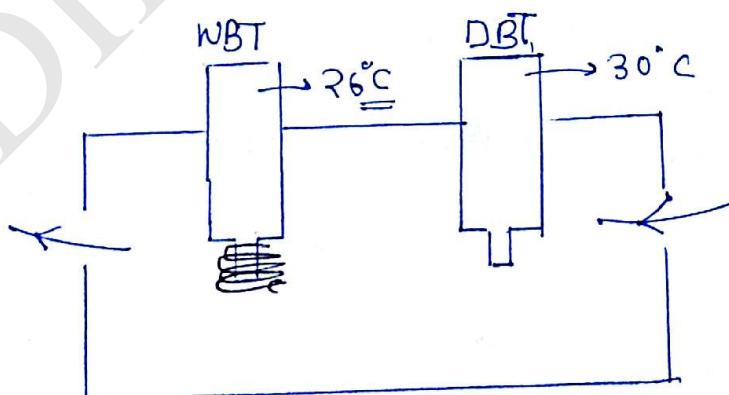
④

④ Wet bulb temp :-(WBT) :-

- it is the minimum temp. achieved by a wet cloth due to evaporation of water.
- it is the temp. measured by a thermometer whose tip is covered with wet cloth.
 - it is the temp. upto which air can be cooled in desert cooler.
 - It is the temp. upto which water can be cooled in cooling towers
 - It is the minimum temp upto which water can be cooled earth & pot.
 - Wet bulb depression (WBD) = DBT - WBT

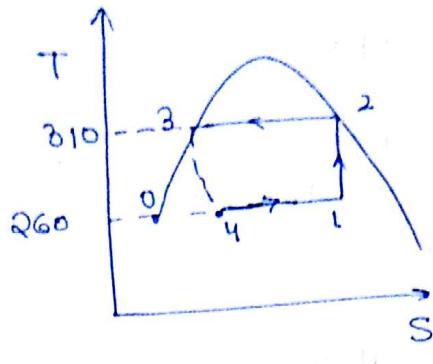
$$\boxed{WBD = DBT - WBT}$$

- Use of desert cooler is beneficial if the WBD is high.
- For saturated air $\boxed{DBT = WBT}$



Q 1.17 Gate book

P-411



$$@ 310 \quad L.H = 1054$$

$$C_{eq} = 4.8$$

$$h_1 - h_0 = ?$$

$$\frac{h_1 - h_0}{260} = s_1 - s_0$$

$$s_2 - s_3 = \frac{h_2 - h_3}{310} = \frac{1054}{310} \quad -\textcircled{1}$$

$$s_3 - s_0 = C_p \ln \frac{T_f}{T_i} = 4.8 \ln \frac{310}{260}$$

$$s_3 - s_0 = 4.8 \ln \frac{310}{260} \quad -\textcircled{2}$$

$\textcircled{1} + \textcircled{2}$

$$s_2 - s_0 = 4.8 \ln \frac{310}{260} + \frac{1054}{310}$$

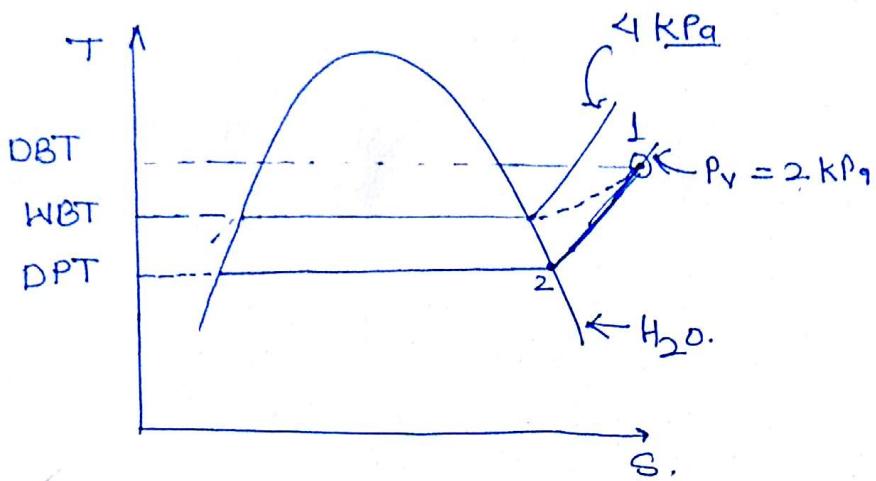
$$s_1 = s_2$$

$$s_1 - s_0 = 4.8 \ln \frac{310}{260} + \frac{1054}{310} = \frac{h_1 - h_0}{260}$$

$$h_1 - h_0 = 260 \left\{ 4.8 \ln \frac{310}{260} + \frac{1054}{310} \right\}$$

$$h_1 - h_0 = 1103.51 \text{ kJ/kg}$$

⑤ Dew point temperature:-



{ unsaturated :- $DBT > WBT > DPT$
 { saturated :- $DBT = WBT = DPT$

- Dew point temp. is the temp. of air at which water vapour present in the air starts condensing when cooled at constant pressure.
- Air is saturated means water vapour is present in air is saturated.
- Air is unsaturated means water vapour is present in the air is superheated.
- ~~Saturation pressure~~ corresponding to ~~dew point temp.~~ is the partial pressure of vapour in air at DBT Conditions.

Q.23

P.g.58

$$P_s = 0.6624 \text{ bar}$$

$$P_{atm} = 1 \text{ bar},$$

DBT 38°

$$\omega = ?$$

$$\phi = 72\%$$

$$\Rightarrow \phi = \frac{m_v}{m_t} = \frac{P_v}{P_t + P_r} \quad P_v = 0.47692$$

$$\omega = 0.622 \quad \frac{P_v}{P_t - P_r}$$

$$\omega = 0.622 \quad \frac{0.47692}{1 - 0.4762}$$

$$\omega = 0.56712 \text{ kg/kgdn} = 567.12 \text{ g/gde}$$

Q.24

$$\omega = 0.01$$

$$m_i = 10.1 \text{ kg/s.}$$

$$m_2 = 0.1 \text{ kgs.}$$

$$\omega = \frac{\dot{m}_1 \omega_1 + \dot{m}_2 \omega_2}{\dot{m}_1 + \dot{m}_2}$$

~~$$\begin{array}{l} m_{t_1} = 10.1 \\ \omega_1 = 0.01 \\ \dot{m}_{a_1} = ? \end{array}$$~~

$$\dot{m}_{v_1} = ?$$

$$\frac{\dot{m}_t}{1+\omega} = \dot{m}_{a_1}$$

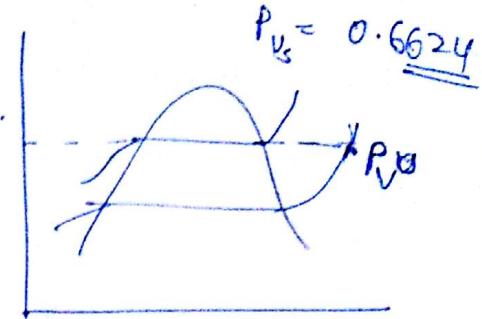
$$\dot{m}_{v_3} = \dot{m}_{v_1} + \dot{m}_{v_2} \quad \dot{m}_{a_1} = \frac{10.1}{1.01} = 10 \text{ kgd.f.s.e.}$$

~~$$\dot{m}_{v_2} = 0.1 \text{ kg/s.}$$~~

$$\dot{m}_{v_1} = 0.1$$

$$\dot{m}_{v_3} = 0.1 + 0.1$$

$$\dot{m}_{a_3} = 10 = \dot{m}_{a_1} \quad \omega_3 = \frac{\dot{m}_{v_3}}{\dot{m}_{v_1}} = \frac{0.2}{10} = 0.02$$



~~$$\begin{aligned} 0.01 &= 0.0160 \frac{P_v}{P_t - P_r} \\ 0.0160(P_t - P_r) &= P_v \\ 0.0160 &= (1+0.016) P_r \\ P_v &= 0.01582 \end{aligned}$$~~

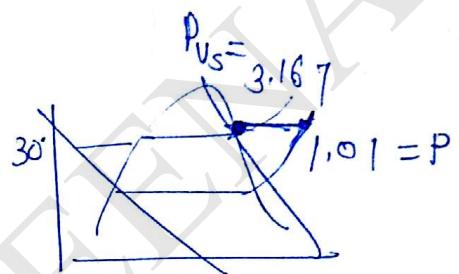
Ques Moist air at 1.013 bar & 30°C contains 10 g of water vapour per kg of dry air.

Saturation pressure of water vapour at 30° is 3.167 kPa find relative humidity of moist air

$$\Rightarrow w = ?$$

$$w = 0.1 \quad m_w = \frac{10 \text{ g}}{\text{kg dry}}$$

$$P_{st} = 3.16$$

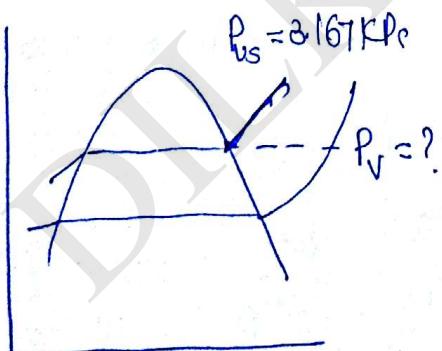


$$w = 0.622 \frac{P_e}{P_t - P_e}$$

$$w = 0.622 \frac{P_e}{P_{st} - P_e} = 0.61$$

$$0.622 \times \frac{3.167}{1.013 - P_e} = 0.61 \Rightarrow P_e = 1.6028$$

$$w = 10 \times 10^{-3} = 0.01 = 0.622 \frac{P_e}{P_t - P_e}$$



$$P_t = 1.013$$

$$0.01 = 0.622 \frac{P_e}{1.013 - P_e}$$

$$P_e = 1.6028$$

$$\phi = \frac{P_v}{P_{vs}} = \frac{1.6028}{3.167} \times 100\% = 50.61\%$$

Q. Atmospheric air at 100 kPa & 30°C has a relative humidity of 70%. The saturation pressure of vapour at 30°C is 4.25 kPa then find the partial pressure of dry air

$$\underline{\phi} = \frac{P_v}{P_{vs}} = 0.70$$

$$P_v = 0.70 \times 4.25 = 2.975$$

$$P_t = P_v + P_a$$

$$P_a = 100 - 2.975 \\ = 97.025$$

Enthalpy of Moist Air!—

Moist air

$$H = H_a + h_v$$

$$H = m_a h_a + m_v h_v \quad - \textcircled{A}$$

Dry air

$$dh_a = C_p a dt$$

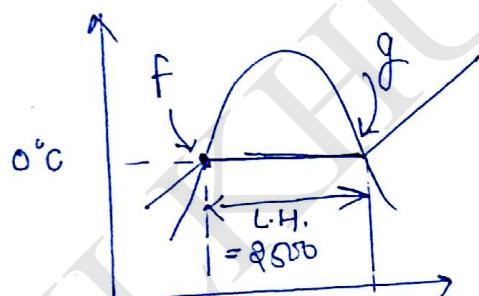
$$\text{at } t = 0^\circ\text{C} \quad \text{let } h_a = 0$$

$$t = t^\circ\text{C} \quad \text{let } h_a = h_a$$

$$(h_a - 0) = C_p a (t - 0)$$

$$\boxed{h_a = C_p a t}, \quad t \text{ is in } \underline{\underline{^\circ\text{C}}}$$

water vapour



$$\text{at } 0^\circ\text{C}, h_f = 0$$

$$h_v = 2500 + C_p v (t - 0)$$

$$h_v = 2500 + 1.88t$$

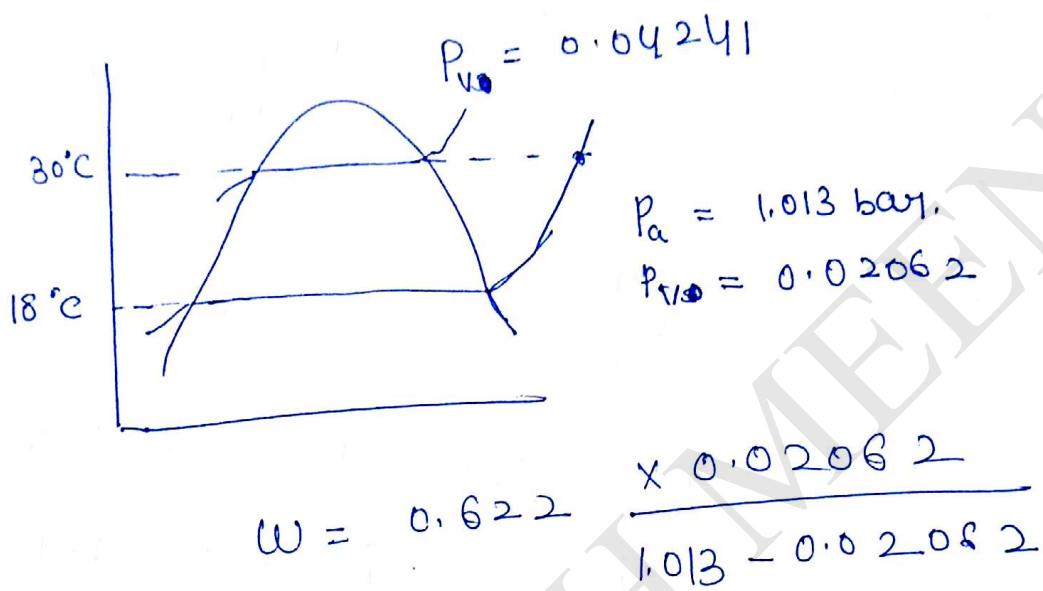
From \textcircled{A} $H = m_a \times C_p a t + m_v (2500 + 1.88t)$

$$h = \frac{H}{m_a} = 1.005t + \frac{m_v}{m_a} (2500 + 1.88t)$$

$$\checkmark \quad h = 1.005 t + w(2500 + 1.88t) \quad \frac{\text{kJ}}{\text{kg d.a.}}$$

$$m_a = 1 \\ m_v = w$$

Q.2



$$w = 0.01291$$

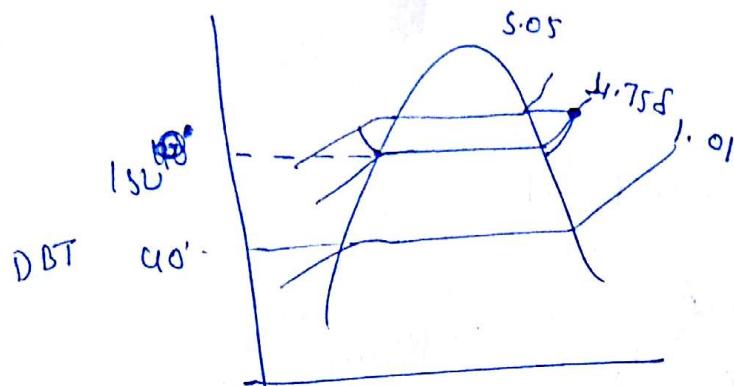
$$h = 1.005 t + 0.0129 (2500 + 1.88 t)$$

$$= 1.005 \times \cancel{30} + 0.0129 (2500 + 1.88 \times \cancel{30})$$

$$h = 63.1 \underline{\underline{59}}$$

Q.20

$$\phi = 0.50 = \frac{P_v}{P_{vs}}$$



$$P_{sat}|_{1.01} = 7.38 \text{ kPa}$$

$$P_{sat}|_{4.75} = 4.758$$

$$\phi = \frac{P_v}{P_{vs}} = 0.50$$

$$P_v = 0.50 \times 7.38 = 3.69 \text{ kPa}$$

$$P_v = 3.69 \text{ kPa}$$

$$w = 0.622$$

$$w = \left(0.622 \times \frac{3.69}{101 - 3.69} \right) \times 1000$$

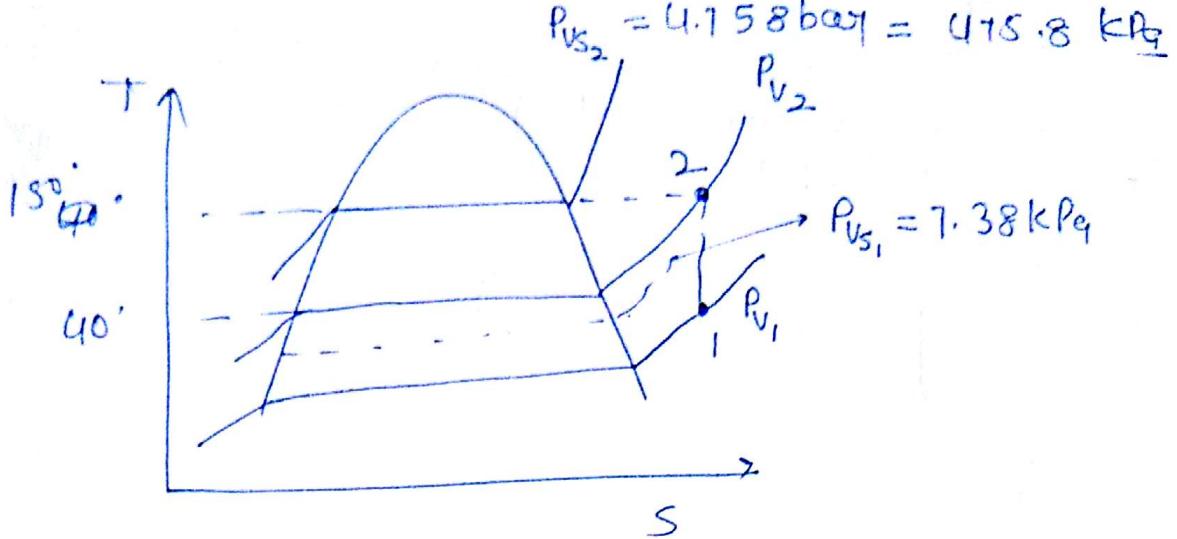
$$w = 23.58 \text{ g/kg dry air}$$

$$P_{vs} = 4.758 \text{ kPa}$$

$$w = \frac{\frac{P_v}{P_v - P_{vs}}}{0.622} = 0.236$$

$$P_v = 0.316$$

$$\phi = \frac{P_v}{P_{vs}}$$



$$0.5 = \phi_1 = \frac{P_{V_1}}{P_{VS_1}} = \frac{P_V}{7.38}$$

$$P_V = 3.69 \text{ kPa}$$

$$\omega_1 = 0.622 \frac{\rho_{\phi_1}}{P_{t_1} - P_{V_1}} = 0.622 \frac{3.69}{101 - 3.69}$$

$$\omega_1 = 23.6 \times 10^{-3} \text{ kg u / kg da}$$

$$\frac{P_{t_2}}{P_{t_1}} = \frac{P_{V_2}}{P_{V_1}} \Rightarrow \frac{\rho_{\phi_2}}{101} = \frac{3.69}{3.69}$$

$$\rho_{\phi_2} = 18.48 \text{ kPa}$$

$$\phi_2 = \frac{P_{V_2}}{P_{VS_2}} = \frac{18.48}{475.8} = 0.0388$$

$$\phi_2 = 3.9 \%$$

Degree of saturation :- (μ)
Percent humidity

$$\star \boxed{\mu = \frac{w}{w_s}} = \frac{0.622 \frac{P_v}{P_t - P_v}}{0.622 \frac{P_{vs}}{P_t - P_{vs}}}$$

$$\therefore \mu = \frac{P_v}{P_{vs}} \left(\frac{P_t - P_{vs}}{P_t - P_v} \right)$$

$$\mu = \phi \left(\frac{P_t - P_{vs}}{P_t - P_v} \right)$$

* Ap John Formula :-

$$\boxed{P_v = P_{v'} - \frac{1.8 p(t - t')}{9700}} *$$

- P_v = Partial pressure of Vap.

- $p_{v'}$ = Sat. pressure Corresponds to. WB T

- p = total pressure

- t = DBT

- t' = WB T.

- Alignment Circle is a pt on psychrometric Chart

$$DBT = 26^\circ C$$

$$\phi = \underline{50\%}$$

CP. 6 WB
Q.1 Pg. 57

$$u = \frac{P_v}{P_{vs}} \left(\frac{P_t - P_{vs}}{P_t - P_v} \right)$$

$$0.24 = \frac{P_v}{4} \left(\frac{100 - 4}{100 - P_v} \right)$$

$$0.24 \times 4 (100 - P_v) = 100 P_v \times 96$$

$$P_v = 0.990 \quad \cancel{120} = \cancel{P_{vs}} = 1230 \text{ kPa}$$

$$\phi = \frac{P_v}{P_{vs}} = \frac{0.990}{4} \times 100$$

$$\phi = 24.75$$

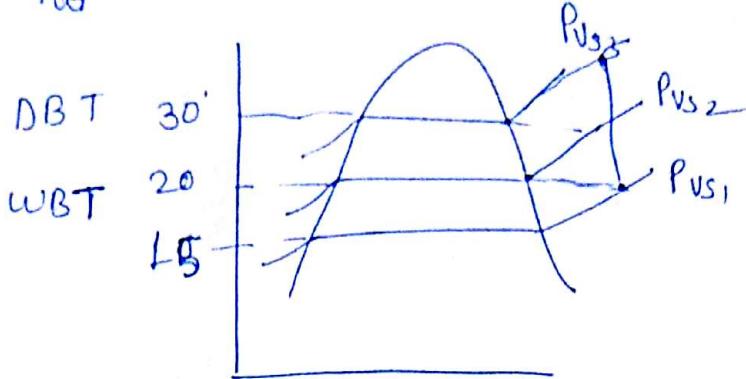
$$\omega = 0.622 \frac{P_v}{P_t - P_v}$$

$$\omega = 0.622 \frac{1}{99}$$

$$\omega = 0.0062$$

Q 26

$$P_{at} = 740 \text{ mm Hg.} = \cancel{100.624 \text{ kPa}}$$



$$P_{VS_3} = 0.04242$$

$$P_{VS_2} = 0.02337$$

$$\underline{P_{VS_1} = 0.01679}$$

$$P = 740 \text{ mm of Hg}$$

$$760 \rightarrow 1.013$$

$$740 = \frac{1.013}{760} \times 740$$

$$P = 0.9869$$

bc

(i) ~~P_V~~ = $P_V' - \frac{1.8 P (t - t')}{2730}$

$$P_V = 0.02337 - \frac{1.8 \times 0.9869 (30 - 20)}{2730}$$

$$P_V = \underline{0.01679} \quad DP = 15^{\circ}\text{C}$$

(ii) $\omega = 0.622 \times \frac{0.01679}{0.9869 - 0.01679}$

$$\omega = \underline{0.01077}$$

(iii) $RH = \phi = \frac{P_V}{P_{VS} \text{ at } \underline{DBT}} = \frac{0.01679}{0.04242} = 39.5\%$

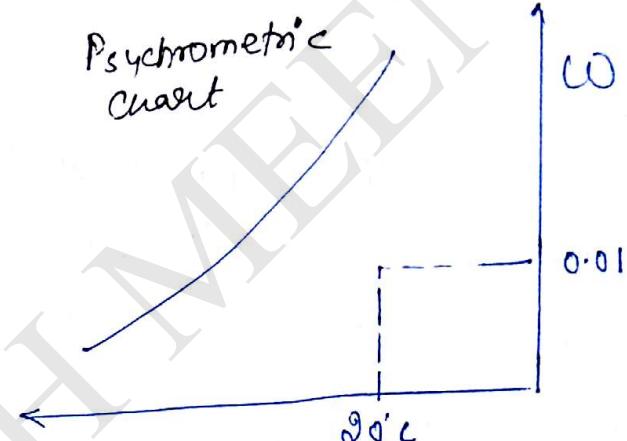
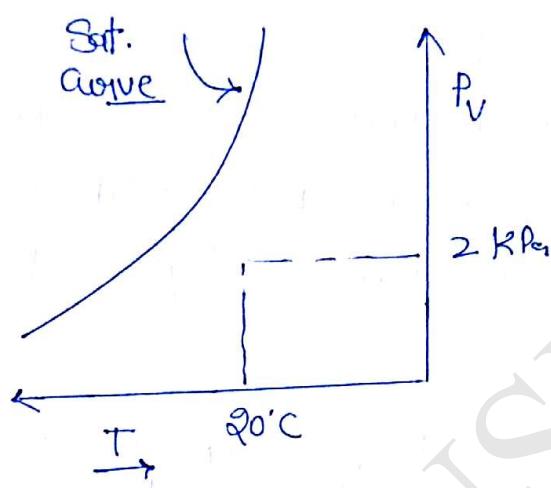
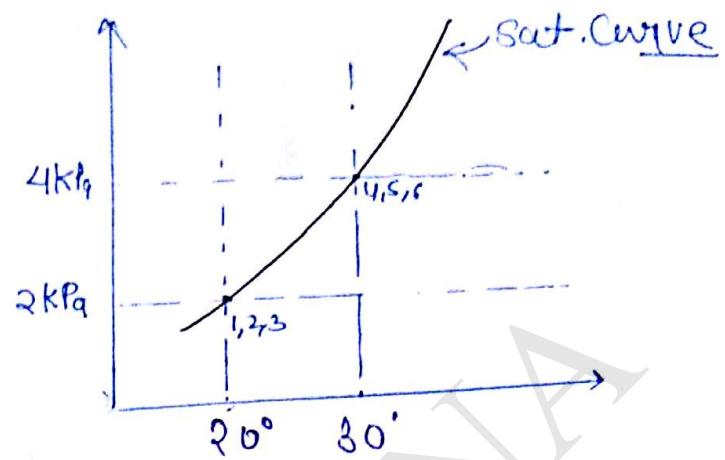
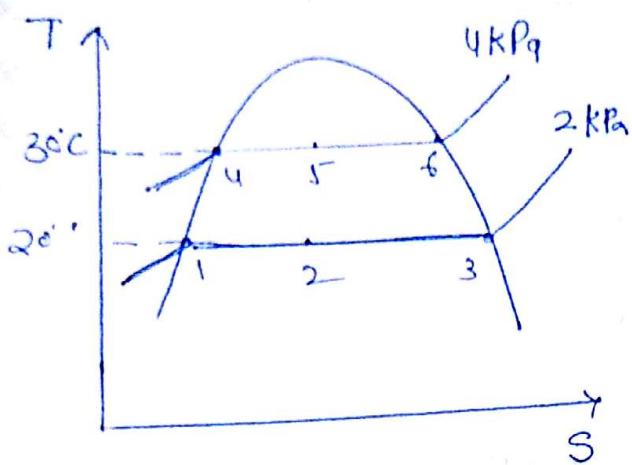
(iv) $P_V V = m_V R T$

$$P_V = \gamma R T$$

$$\gamma = \frac{P_V}{R T} = \frac{0.01679 \times 100}{8.314 \times 303}$$

$$\gamma = 0.0119 \text{ kg/m}^2$$

Development of Psychrometric chart:-



$$w = 0.622 \frac{R_g}{P_f - P_v} = f(P_v)$$

↓
let L atm

$$w @ P_v = 2 \text{ kPa} \quad \text{let } \underline{\underline{0.01}}$$

* humidity ratio is the function of P_v

Q25

$$\phi = 60\% = \frac{P_v}{P_{vs}}$$

$$P_{atm} = 0.1 \text{ MPa} = 0.1 \times 10^6 \text{ Pa} = 100 \text{ kPa}$$

$$P_v = 0.60 \times 5.63$$

$$w = 0.622 \times \left(\frac{0.60 \times 5.63}{100 - 0.60 \times 5.63} \right) \times 1000$$

$$w = 21.24 \text{ gram/kg day A}$$

Ques if the volume of moist air with 50% relative humidity is isothermally reduced to half of the original val the relative humidity of moist air will become ?

Soln

$$\phi = 0.50 = \frac{P_{v1}}{P_{vs}}$$

$$P_{v1} V_1 = m R_v T$$

$$P_{v1} = \frac{m R_v T}{V_1}$$

~~$$P_{vs} = \frac{P_{v1}}{0.5}$$~~

$$V_2 = \frac{V_1}{2}$$

Now

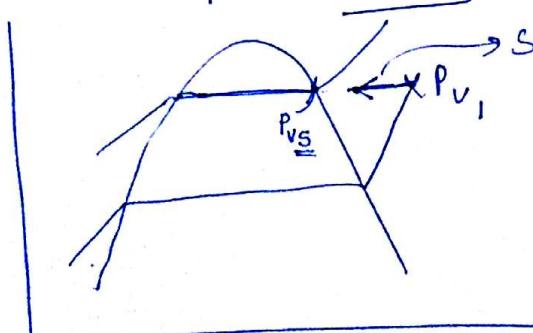
$$\phi = \frac{2 P_{v1}}{P_{vs}/0.5}$$

$$P_{v2} = 2 \left(\frac{m R_v T}{V_1} \right)$$

$$P_{v2} = 2 P_{v1}$$

$$\frac{P_{v1}}{P_{v2}} =$$

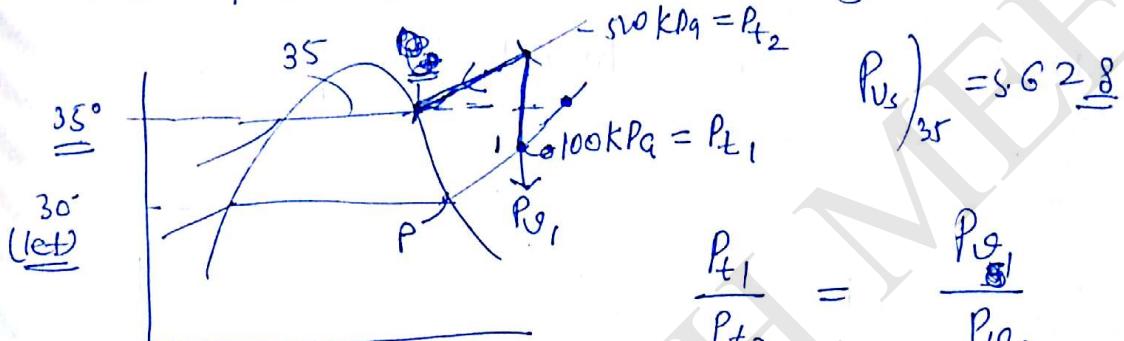
$$\phi = 100\%$$



Same temp

 P_{vs} const. (isothermally)

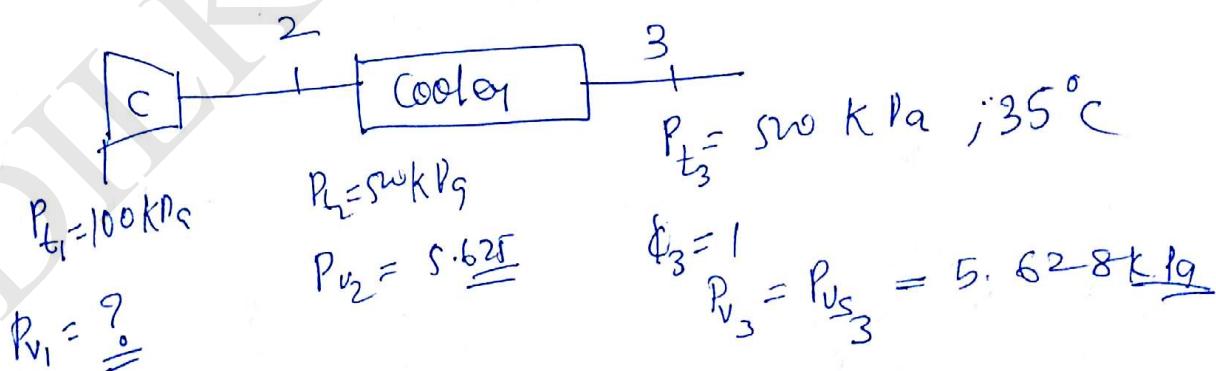
P Moist air at a pressure of 100 kPa is compressed to 500 kPa and then cooled to 35°C in a cooler at const. pressure (there is no condensation). The air at the entry to the cooler is unsaturated and becomes just saturated at the exit of cooler. The saturation pressure of vapour at 35°C is 5.628 kPa, find partial pressure of vapour in moist air entering the compressor.



$$\frac{P_{t_1}}{P_{t_2}} = \frac{P_{t_1}}{P_{v_2}}$$

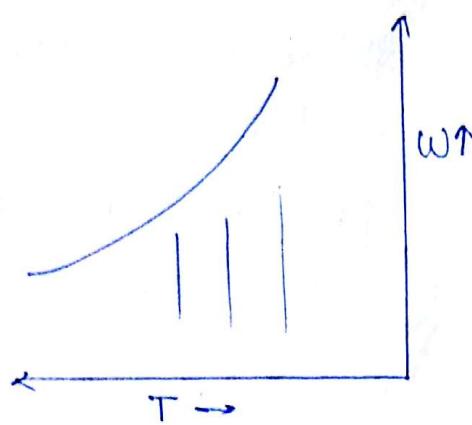
$$\frac{100}{500} = \frac{P_{t_1}}{P_{v_2}} \frac{5.628}{5.628}$$

$$P_{v_1} = 1.1256 \text{ kPa}$$

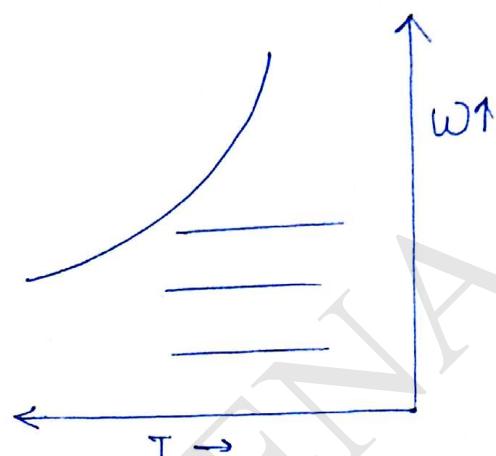


Various lines on Psychrometric chart:-

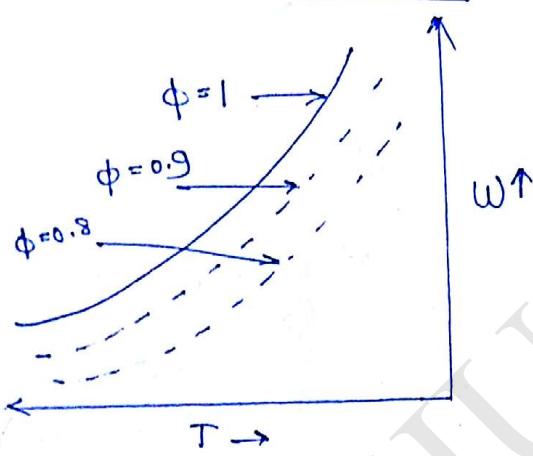
① Constant DBT lines



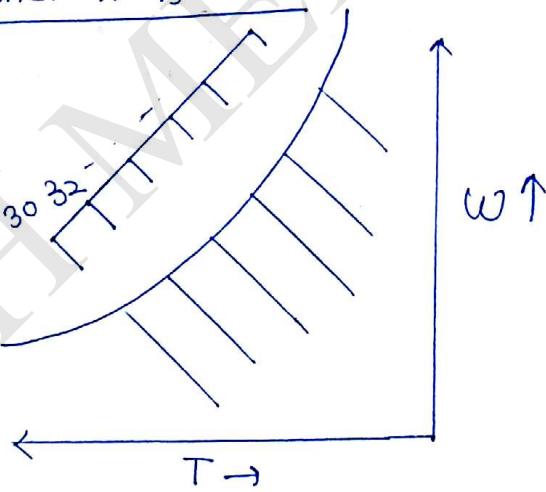
② Constant 'w' lines



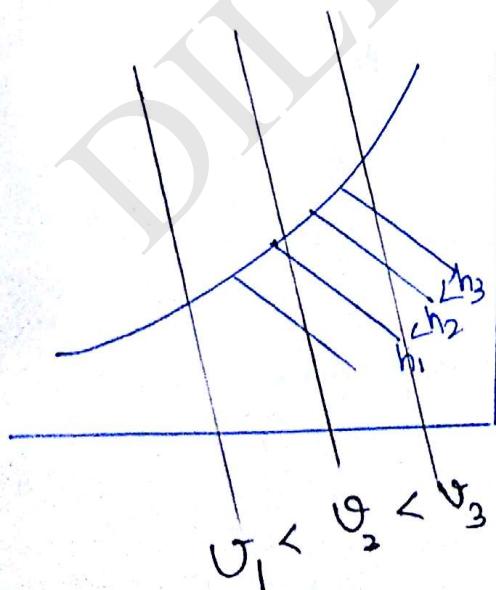
③ Constant R.H. (φ) lines



④ Constant 'b' lines



⑤ Const 'V' lines:



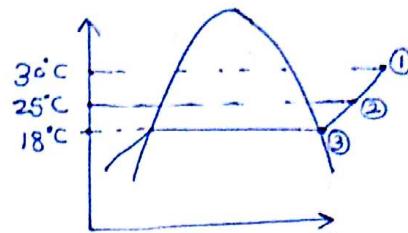
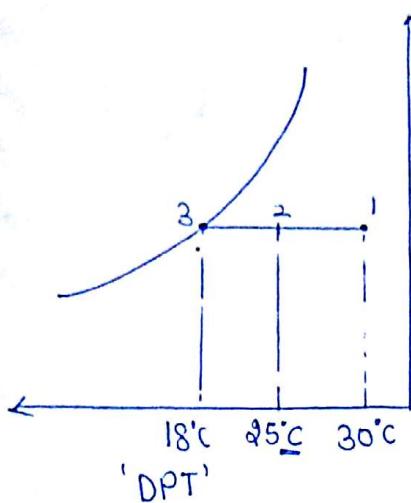
Specific Vol.

$$V = \frac{V}{m_a} \left(\frac{m^3}{kg d.a} \right)$$

$$m_a = \frac{V}{V}$$

dry air mass remain same

② Constant 'DPT' lines



→ if ' P_0 ' is same, 'DPT' is same

→ $w = f(P_0 \text{ only})$

if ' P_0 ' is same

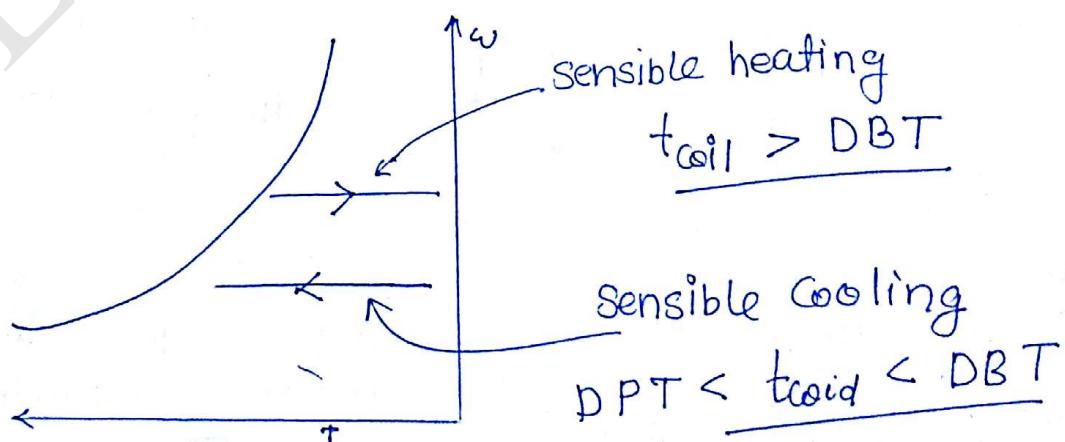
$\therefore w$ is same

* Constant DPT lines follow constant 'w' line and are horizontal lines on psychrometric chart.

① WBT line: Though there is slight deviation between constant WBT lines and constant enthalpy lines but for all practical purposes these lines are taken to be same.

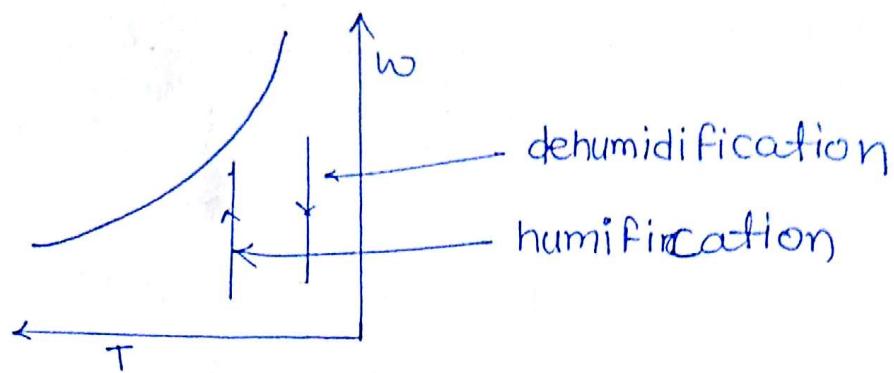
Various processes on psychrometric chart:-

① Sensible Cooling & sensible Heating:-

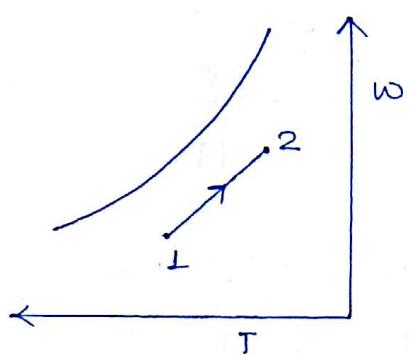


The process followed in the electrical room heater is sensible heating

② Humidification & Dehumidification:-



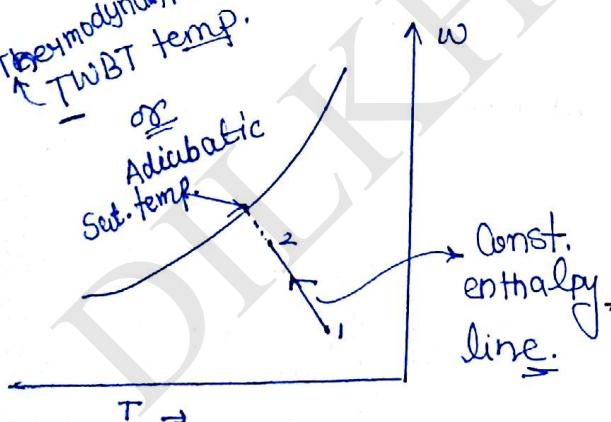
③ Heating and Humidification:-



e.g.: steam spray in air

~~Adiabatic saturation~~

Thermodynamic
TWBT temp.
or
Adiabatic
sat. temp.



eq:- Desert cooler follow \xrightarrow{T} adiabatic saturation process.

⇒ if cooling and humidification occurs when air interact with water in the absence of a cooling coil then the process is called Adiabatic Saturation.

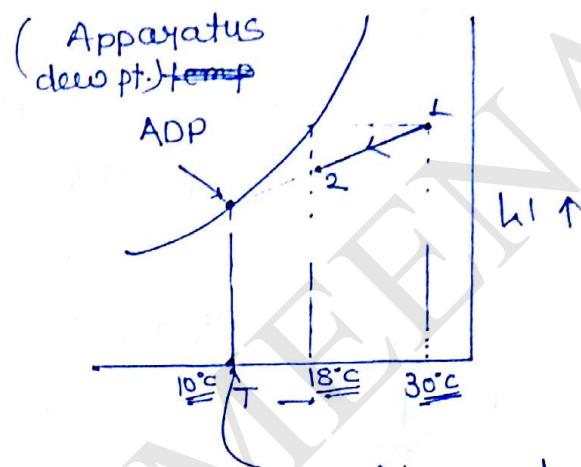
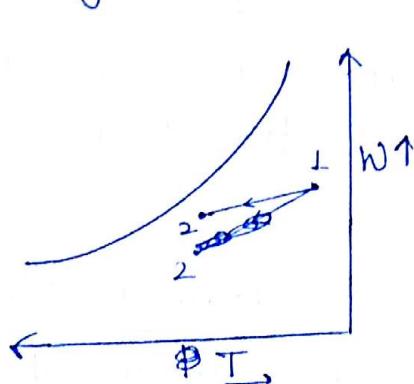
Adiabatic saturation lines are isenthalpic lines and also const. WBT lines.

~~Temp. Corresponding to the point where adiabatic sat. line when produced intersects the saturation curve is called Thermodynamic wet bulb temp (TWBT) or adiabatic sat. temp.~~

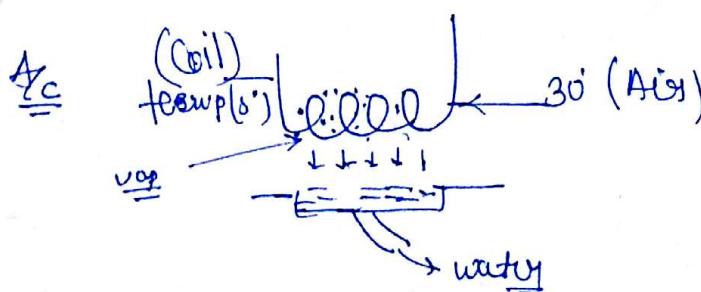
- TWBT is a property of the air whereas WBT is not the property of the air.

$$\cancel{\Rightarrow} * \boxed{TWBT \leq WBT}$$

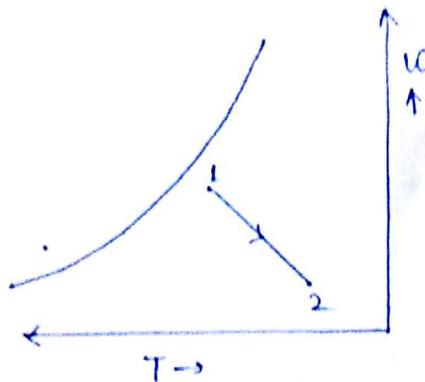
⑤ Cooling and dehumidification:



- ⇒ The cooling and dehumidification lines when produced intersects the saturation curve at the point called as apparatus dew point. The temp. corresponding to this point is the temp of the cooling coil. called as apparatus dew point temp
- The process followed in summer A/c is Cooling and dehumidification.



(6) Heating and dehumidification:-



This process is carried out with the help of chemicals like alumina (Al_2O_3). These chemicals absorb water vapour from the air and ~~not~~ water vapour while leaving the air, condenses and reject latent heat of condensation in the air, hence the temp of air increases.

→ This process is called as adiabatic chemical dehumidification and enthalpy of air remain const during the process.

Ques 5 gram of w. vapour per kg of dry air from atmospheric air is removed and temp of air after removing water vapour become 25°C Find

(i) Relative humidity & enthalpy of air after removal of moisture

② Cooling load on the cooling coil.

Assume the atmospheric condition are 35°C DBT

Q1 and $\phi = 60\%$. Take the mass flow rate of air to 5 kg/ per sec. (dry air basis) and Condenser leaving

the coil at 25°C

~~for $w = 5 \text{ kg/m}^3$~~

t_{d1}

35

25

$P_{vs} (\text{bar})$

0.05733

0.03229,

Soln

$$\omega = \frac{5}{1000} = 0.005$$

$$\omega = 0.622 \quad \frac{P_{\text{at}}}{P_t - P_{\text{at}}}$$

$$\omega = 0.622 \quad \frac{P_{\text{at}}}{1.013 - P_{\text{at}}} = 0.005$$

$$P_{\text{at}} = 8.07 \times 10^{-3} \text{ bar},$$

$$P_{\text{at}} = 8.07 \text{ kPa}$$

$$\phi = \frac{P_{\text{at}}}{P_{\text{vap}}^{\text{sat}}} =$$

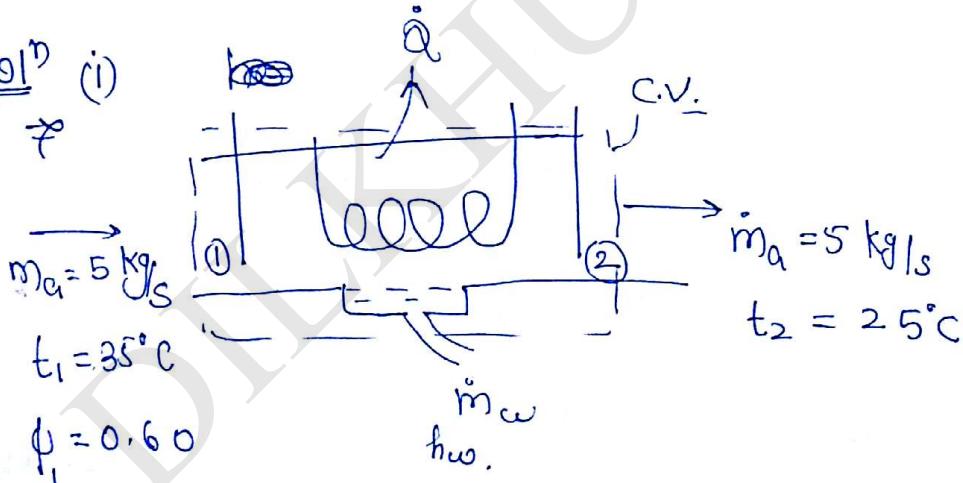
$$\phi = \frac{8.07 \times 10^{-3}}{0.05733 \times 0.03229} = 25.01$$

~~$$\phi = 14.09 \text{ %}$$~~

$$\phi = 25.01 \text{ %}$$

$$h = 1.005 t + \omega(2500 + 1.88 t)$$

Soln (i)



$$\phi_1 = 0.60 = \frac{P_{\text{at}}}{P_{\text{vap}}^{\text{sat}}_1} = \frac{P_{\text{at}}}{0.05733}$$

$$P_{\text{at}} = 0.03439.$$

$$w_1 = 0.622 \frac{P_{V_1}}{P_{t_1} - P_{V_1}}$$

$$w_1 = 0.622 \frac{(0.03439)}{1.013 - 0.03439}$$

$$w_1 = 21.86 \times 10^{-3} \text{ kgv} \cancel{\text{kg da.}}$$

$$\begin{aligned} h_1 &= 1.005 \times t_1 + w_1 (25\omega + 1.88 t_1) \\ &= 1.005 \times 35^\circ + 21.86 \times 10^{-3} (25\omega + 1.88 \times 35) \end{aligned}$$

$$h_1 = 91.36 \text{ kJ/kg d}$$

Now $w_2 = w_1 - u \rightarrow \text{removed}$

$$w_2 = 21.86 \times 10^{-3} - 5 \times 10^{-3}$$

$$w_2 = 16.86 \times 10^{-3} \text{ kgv} \cancel{\text{kg da.}}$$

$$h_2 = 1.005 t_2 + w_2 (25\omega + 1.88 t_2)$$

$$h_2 = 1.005 \times 25 + 16.86 \times 10^{-3} (25\omega + 1.88 \times 25)$$

$$\boxed{h_2 = 68.07 \text{ kJ/kg d.a.}} \text{ Ans}$$

$$w_2 = 0.622 \frac{P_{V_2}}{P_{t_2} - P_{V_2}} = 0.622 \frac{P_{V_2}}{1.013 - P_{V_2}} = 16.86 \times 10^{-3}$$

$$P_{V_2} = 0.0268 \text{ bar.}$$

$$\phi = \frac{0.0268}{0.03229} = 82.8 \%$$

$$(ii) \dot{E}_{in} = \dot{E}_{out}$$

$$\dot{m}_a h_1 = \dot{m}_a h_2 + \dot{Q} + \dot{m}_w h_w$$

↑
Cooling
Coil

$$5 \times 91.36 = 5 \times 68.07 + \dot{Q} + \dot{m}_w h_w$$

$$\begin{aligned}\dot{m}_w &= (w_1 - w_2) \frac{\text{kg v}}{\text{kg d.a}} \times 5 \frac{\text{kg d.a}}{\text{s}} \\ &= 5 \times 10^{-3} \times 5 = 25 \times 10^{-3} \frac{\text{kg}}{\text{s}}$$

$$\begin{aligned}h_w &= C_{pw} \times t_w \leftarrow \text{latent} \\ &= 4.18 \times 25 \quad (\text{in system C.V.})\end{aligned}$$

$$5 \times 91.36 = 5 \times 68.07 + \dot{Q} + 25 \times 10^{-3} \times 4.18 \times 25$$

$$\dot{Q} = 113.8 \frac{\text{kW}}{\text{s}}$$

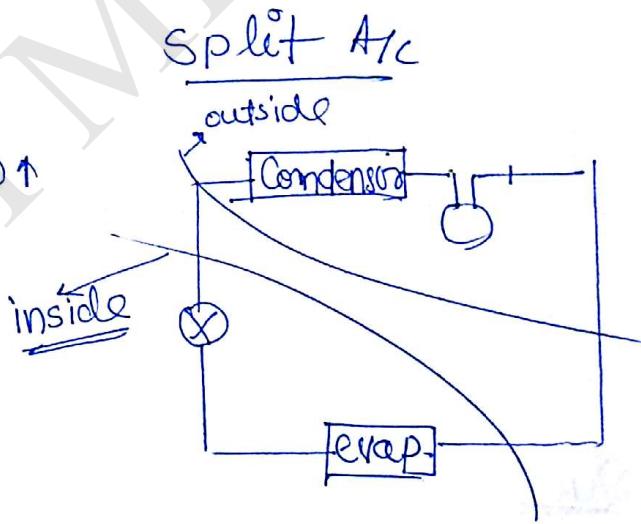
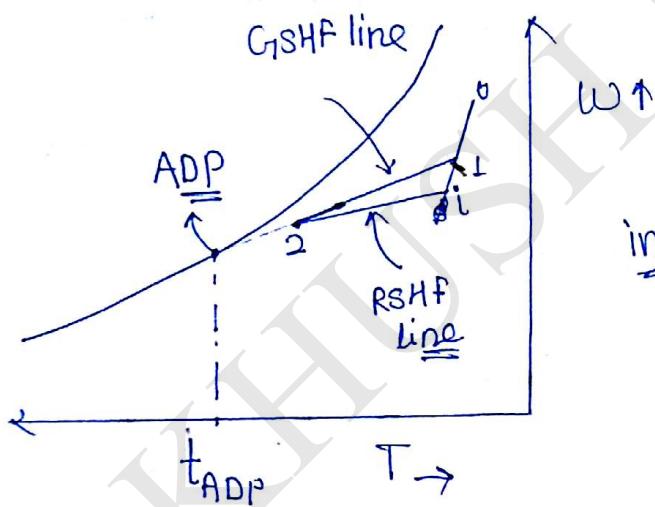
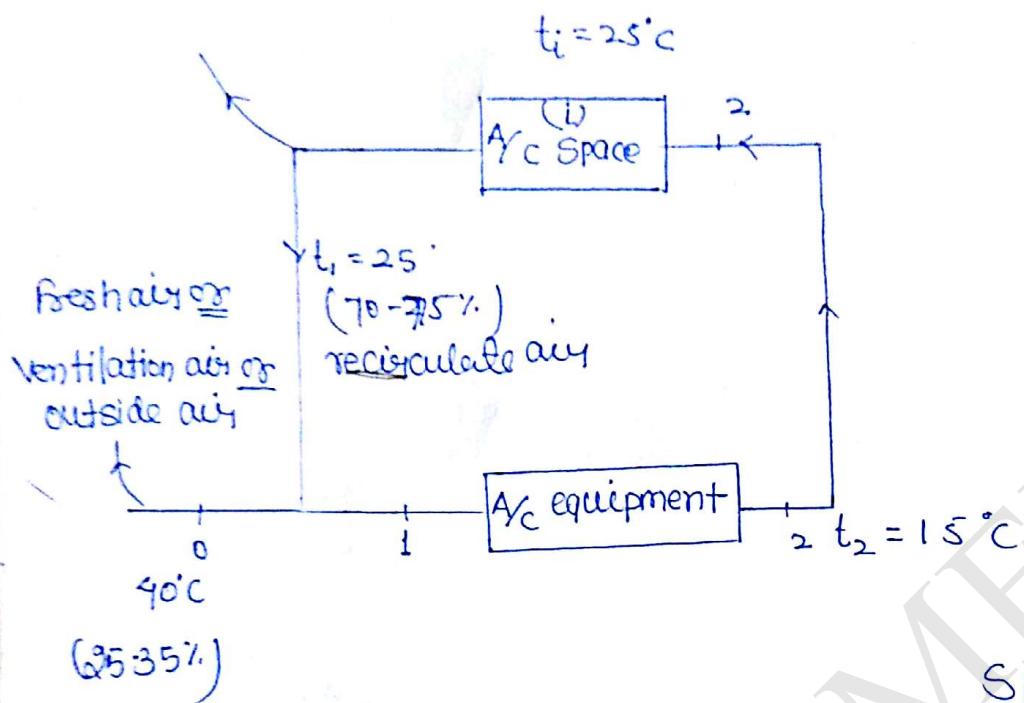
Ques 5
w.B. Sb

$$\begin{aligned}m_a &= 3 \frac{\text{kg}}{\text{s}} & m_a &= 3 \frac{\text{kg}}{\text{s}}, \quad \dot{E}_{in} = \dot{E}_{exit} \\ h_1 &= 85 \frac{\text{kJ}}{\text{kg}} & h_2 &= 43 \frac{\text{kJ}}{\text{kg}} \\ w_1 &= 10 \times 10^{-3} & w_2 &= 8 \times 10^{-3} \\ m_1 h_1 &= m_2 h_2 + m_w h_w + \dot{Q} & \dot{m}_w &= (w_1 - w_2) \times \frac{\text{kg v}}{\text{kg d.a}} \times 3 \frac{\text{kg d.a}}{\text{s}} \\ 3 \times 85 &= 3 \times 43 + \dot{Q} + 3 \times (10 - 8) \times 10^{-3} \times 67\end{aligned}$$

$$\dot{Q} = 123.78 \frac{\text{kW}}{\text{s}}$$

\dot{m}_w = Condenser rate

Summer Air Conditioning with Ventilation A/C



→ line joining the inlet and exit conditions of A/C equipment is called Grand sensible heat factor line.

→ line joining the supply condition to the room with the room inside condition is called Room sensible heat factor line RSHF.

- The intersection of RSHF & GSHF gives the supply conditions to the room.
- The outside air supplied in order to maintain purity of air is called ventilation air or fresh air.
- In hospitals the recirculated air should be zero and ventilation air/fresh should be 100%.

Air changes:-

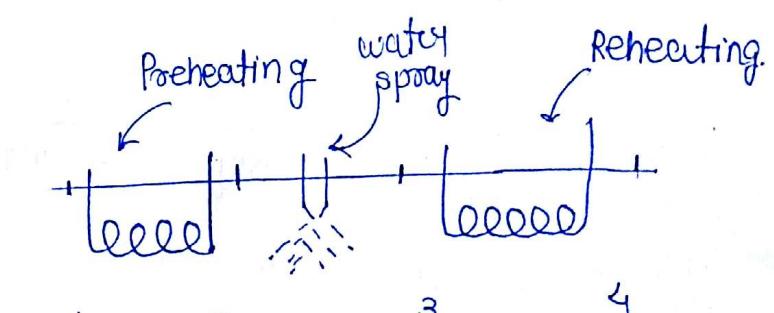
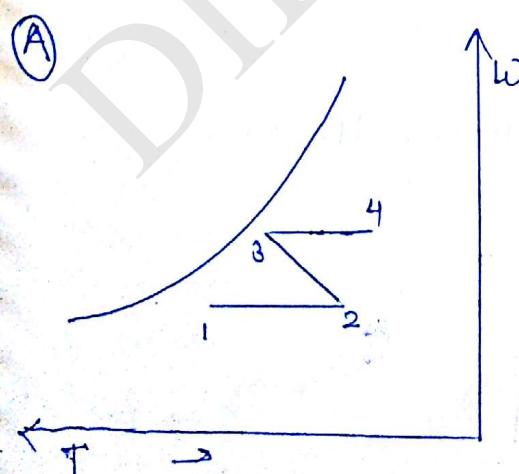
$$\text{Air changes per hour (ACH)} = \frac{V_o \text{ (m}^3\text{/hr)}}{V \text{ (m}^3\text{)}}$$

V_o - outside air
 V → Vol. of A/C Space.

$$\text{Air changes per min} = \frac{V_o \text{ (m}^3\text{/min)}}{V \text{ (m}^3\text{)}}$$

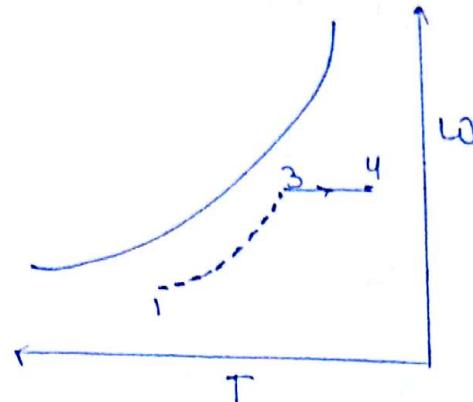
(MM - Cubic meter per min (m^3/min))

Winter Air Conditioning:



$1 \rightarrow 2$ sensible heating
 $2 \rightarrow 3$ Adiabatic Sat.
 $3 \rightarrow 4$ sensible heating.

(B)



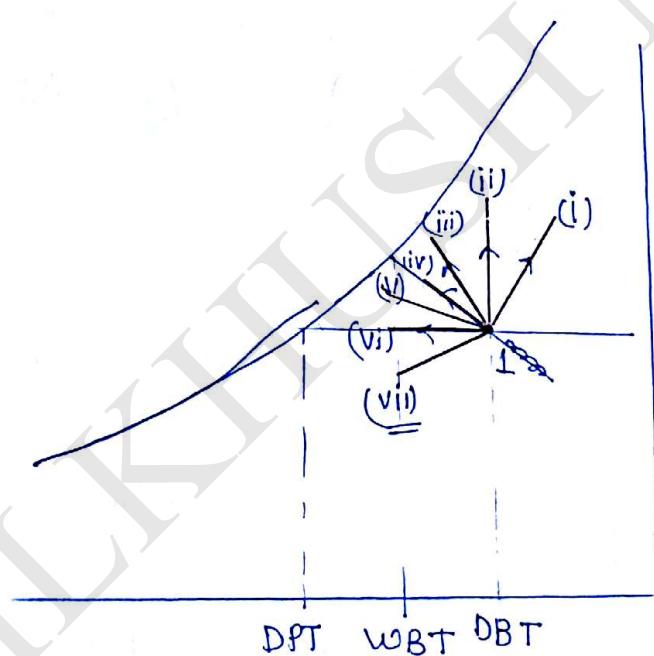
Steam spray

Reheat Coil

1-3 → heat humidification
3-4 → sensible heating

→ In winters the outside air is at low w and low temp. hence heating and humidification of air is required. This can be achieved by one of the above methods.

Air washer:-



(i) $t_w > DBT \rightarrow$ heating & humidification
 \rightarrow heating coil
 $\rightarrow h_a \uparrow$

(ii) $t_w = DBT \rightarrow$ humidification
 \rightarrow heating coil
 $\rightarrow h_a \uparrow$

(iii) $WBT < t_w < DBT$

- cooling and humidification
- heating coil
- $h_a \uparrow$

(iv) $t_w = WBT \rightarrow$ cooling & humidification
→ No coil.
→ $h_a = \text{Const.}$

(v) $DPT < t_w < WBT$

- cooling & humidification
- cooling coil
- $h_a \downarrow$

(vi) $t_w = DPT \rightarrow$ sensible cooling
→ cooling coil
→ $h_a \downarrow$

(vii) $t_w < DPT \rightarrow$ cooling & dehumidification
→ cooling coil
→ $h_a \downarrow$

Human Comfort and Effective temperature:-

- The physical comfort of a human being which can be affected by affecting the temp., humidity, air velocity & purity of air.
 - Effective temp is the temp. of a saturated envt. where the person feel same level of comfort as in the normal ~~at~~ environment.
 - According to the study conducted by American society for heating refrigeration and air condition engineers (ASHRAE), 99% of the ~~adults wearing light cloths~~ adults wearing light cloths involved in light activity (e.g. office work) will experience comfort at $DH \rightarrow 50-60^\circ\text{C}$.

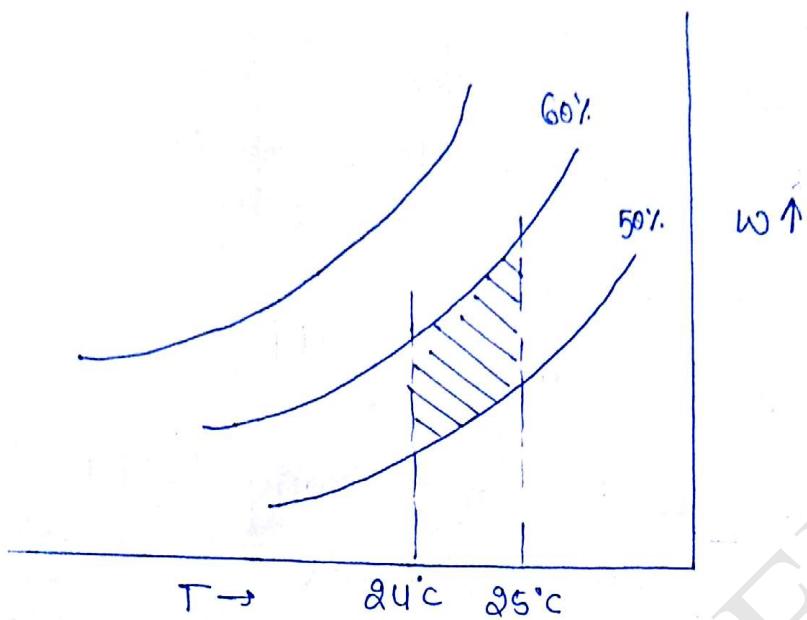
DBT → 24-25°C & RH → 50-60%

Effective temp 21.6°C (summer)
20°C (winter)

Factors affecting human comfort:-

- ① Gender:- man experience comfort at a lower temp. compare to woman.
- ② Age:- Adult experience comfort at a lower temp. compare to children & old age people.
- ③ kind of clothing:- Person wearing light cloths will experience comfort at a relatively higher temp. compare to people wearing heavy cloths.
- ④ kind of activity:- Person involved in heavy physical activity (for ex. gym) will experience comfort at a lower temp. Compared to person involved in light activities (offic work)
- ⑤ climatic condition:- People habitual to cold climate experience comfort at lower temp @ compare to people living in hot climatic condition.
- ⑥ Seasons:- People experience comfort at a lower temp. in winters compare to summer.

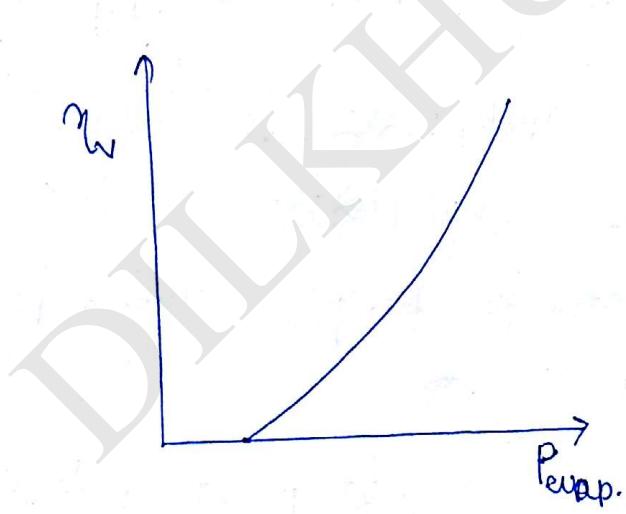
Comfort chart :-



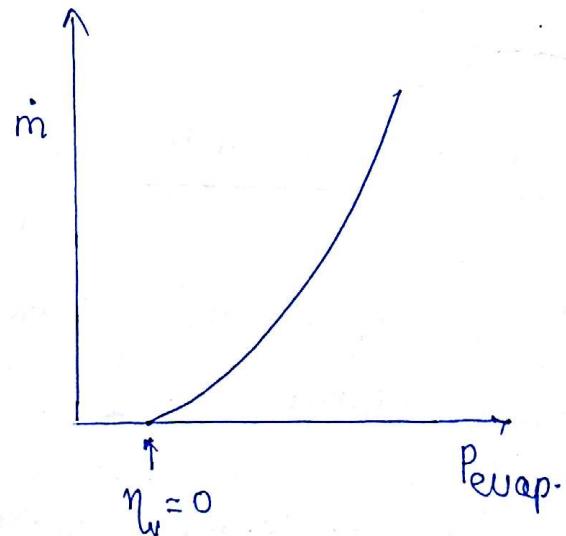
- * The chart representing the year round comfort condition is called as comfort chart.

* Performance curve:-

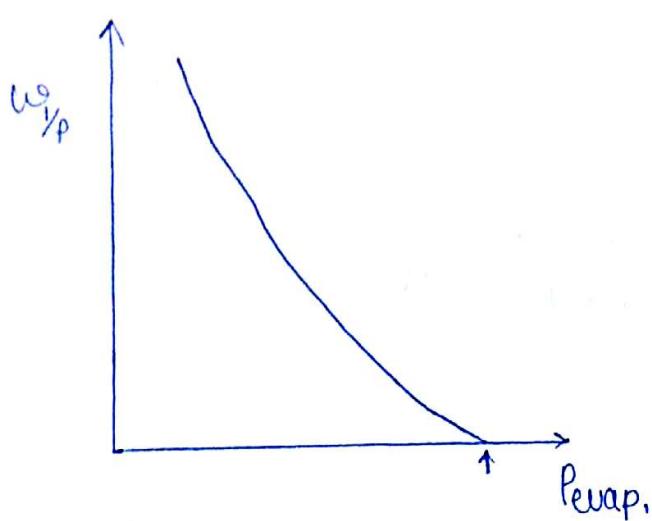
(i) η_w vs $P_{ewap.}$



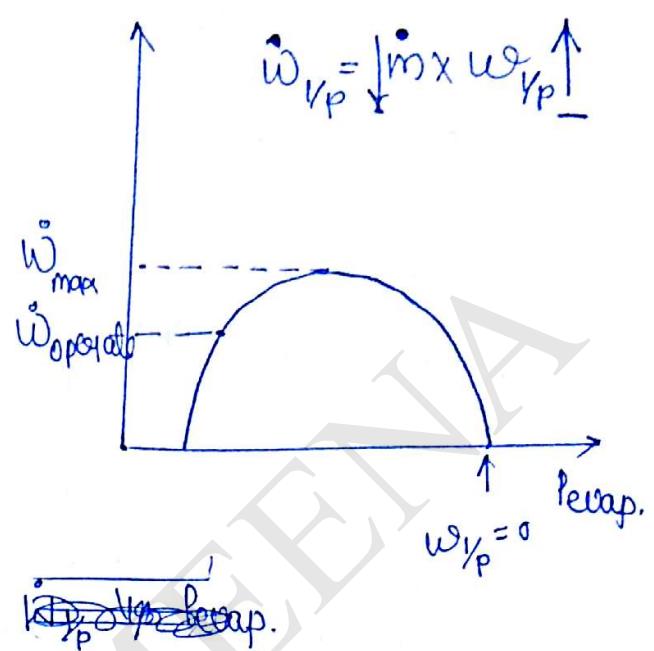
(ii) \dot{m} vs $P_{ewap.}$



(iii) \dot{W}_{Vp} Vs. $P_{evap.}$



(iv) \dot{W}_{Vp} Vs. $P_{evap.}$



* The operating is less than the maximum br power but the compressor motors are designed for maximum power conditions because for reaching the operating power we have to cross the max. power condition.

• Refrigeration Equipment •

Compressor:-

① Hermetically shield compressor:-

- In this the compressor and motor are installed on a steel shell.
- Occupies less space and noise generation is low.
- Used in domestic application.
- Maintenance is difficult and Motor cooling is achieved by rejecting heat to the suction vapour to compressor. This results in super heating of vapour hence increasing work input and decreasing COP of unit

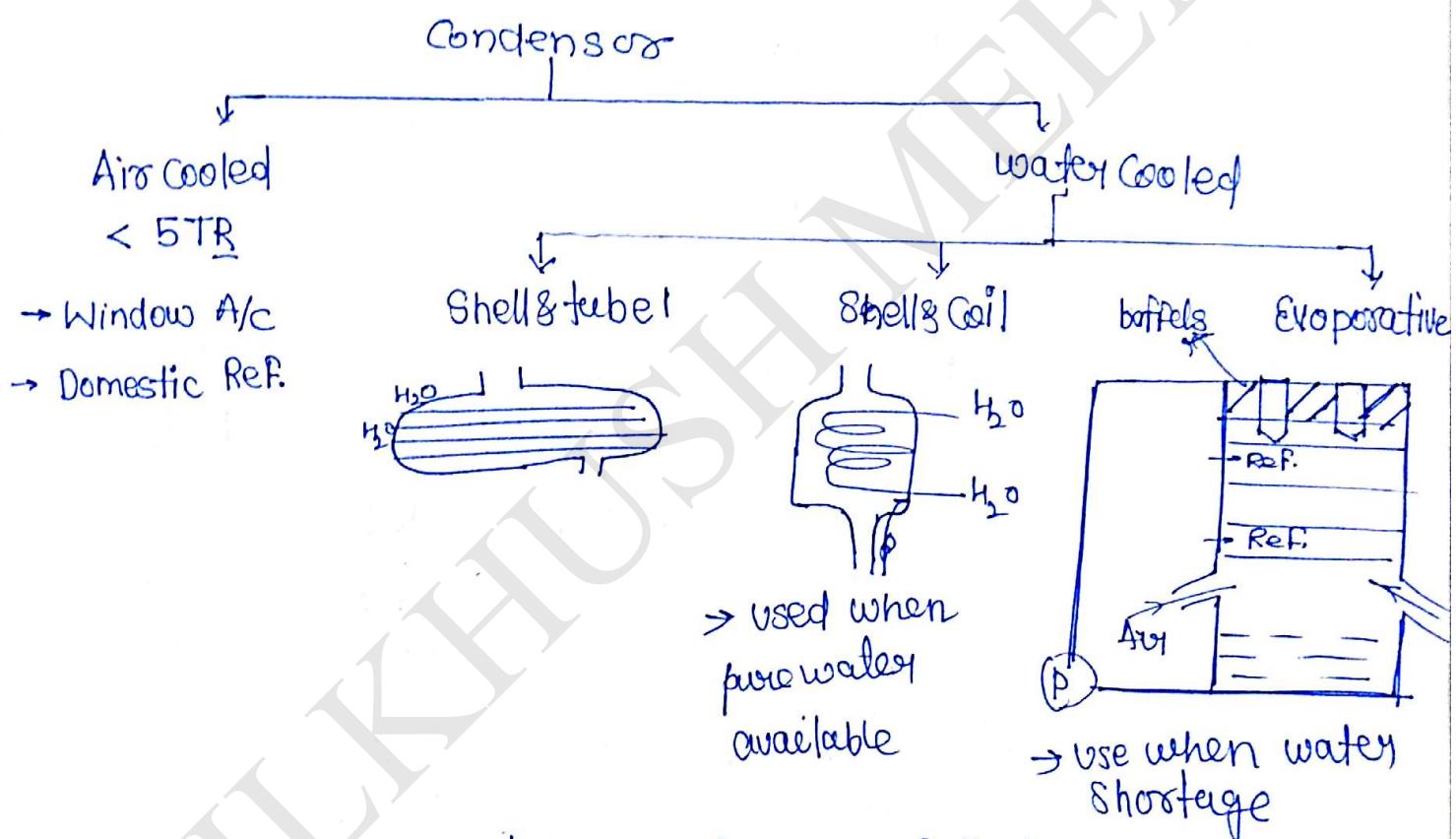
② Open type Compressor:-

- Compressor and motor are install on separate shafts and joined by a belt and pulley arrangement
- Maintenance is easy and motor cools by itself
- Used in Industrial applications.
- Occupies large space & Noise generation is high.

(3) semi hermetic compressor:-

Motors and compressors are installed on separate shaft and shield separately they are connected by belt and pulley arrangement. The ~~merit~~^{demand} and ~~demerit~~ are in b/w the above two compressors.

Condenser



* In both shell and tube and shell & coil type Condenser the refrigerant flows through the shell. The flow through tube is avoided to avoid the pressure loss of refrigerant.

- Shell and coil type condenser can be used only when pure water is available because of scaling problem in the coil.
- Evaporative condenser is used where there is shortage of water. Water absorbs heat from the refrigerant and is further cooled due to evaporative action as it comes in contact with the air.



Heat rejection Factor / Heat rej. ratio :-

$$\text{Heat rejection ratio} = \frac{Q_{\text{Rej}}}{R.E.} = \frac{Q_{\text{Rej}}}{R.E.}$$

$$= \frac{Q_{W_{1/p}} + R.E.}{R.E.}$$

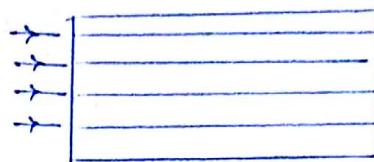
Heat rejection ratio =
$$HRR = \frac{1}{COP} + 1$$

Heat rejection Ratio signifies the size of the condenser. In hermetically shield unit since COP is less, HRR is high hence larger size Condenser are required.

Evaporators :-

coil type: *  window A/c.

Plate type: Domestic Ref.



Expansion devices

expansion devices.

Const. Area type

→ capillary tube
Domestic ref.
window A/c

variable Area.

Automatic
exp. valve

Thermostatic
expansion valve (TEV)

Automatic expansion valve:-

→ maintain const. pressure in the evaporator

→ used when load is almost constant. (for e.g. Milk chilling plants)

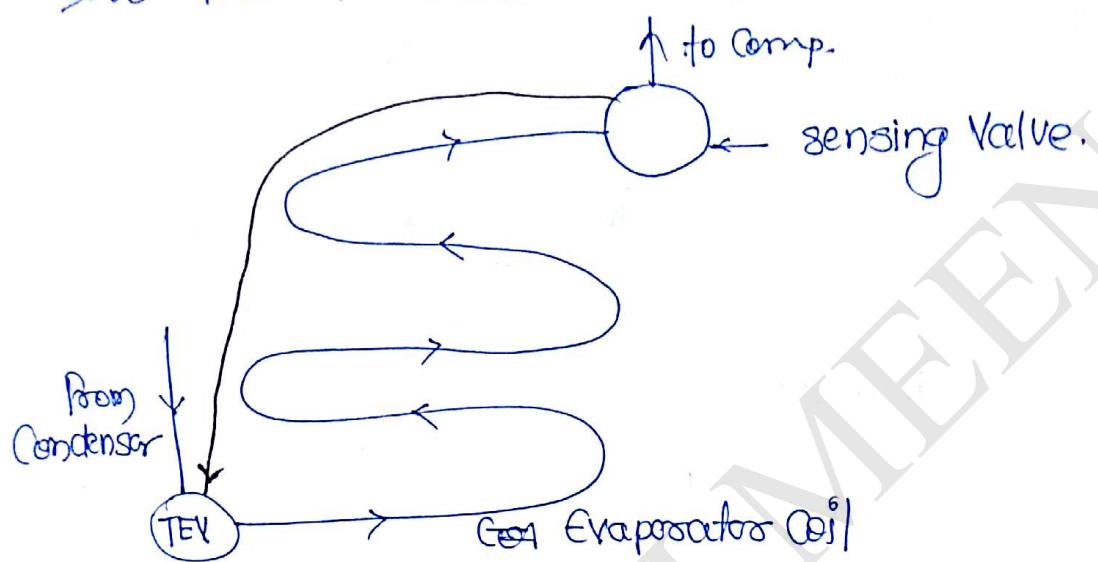
Thermostatic expansion valve:-

→ Maintains constant degree of superheat in evaporator.

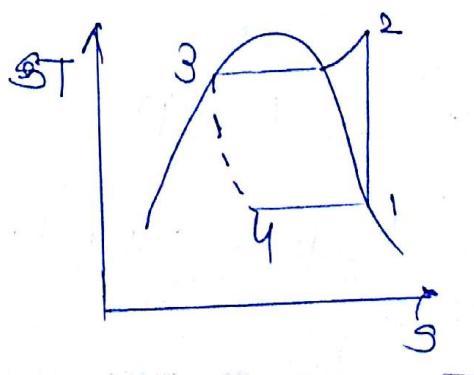
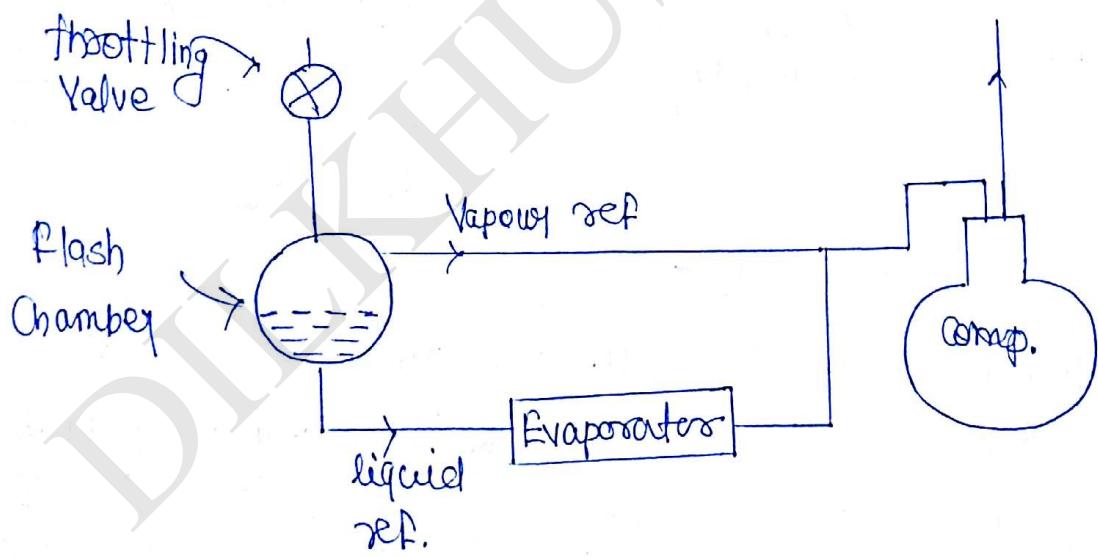
→ used when load is variable (~~constant~~)

* → sensing bulb is located at the exit of evaporator.

→ Alternative overfeeding & starving of refrigerant in the evaporator coil leads to hunting in the thermostatic expansion valve.



Flash chamber:-

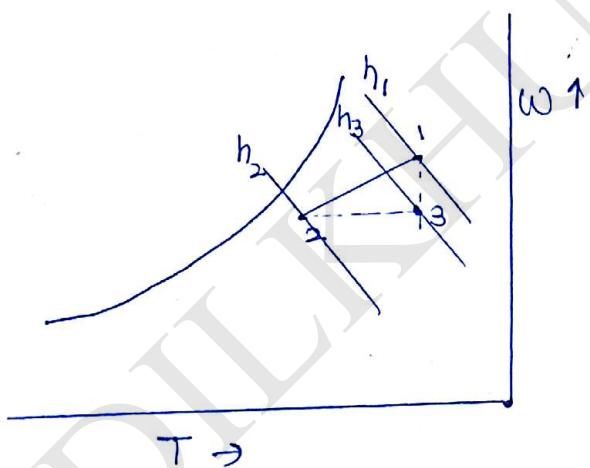


Theoretically there is no improvement in COP but practically as the vapour is bypass the pressure loss during the flow reduces hence COP ~~improve~~ ~~slightly~~ slightly.

Float Valve:-

These valves are used for regulating the level of liquid refrigerant. It is called as high side float valve if used on high pressure side i.e. Condenser. And called as low side float valve if used on low pressure side i.e. evaporator.

Sensible Heat factor & latent heat factor:-



Total heat removed

$$TH = h_1 - h_2$$

$$\text{latent heat } LH = h_1 - h_3$$

$$\text{sensible heat } SHF = h_3 - h_2$$

$$SHF = \frac{h_3 - h_2}{h_1 - h_3}$$

$$LHF = \frac{h_1 - h_3}{h_1 - h_3}$$

~~SHF + LHF = 1~~

$$SHF + LHF = 1$$

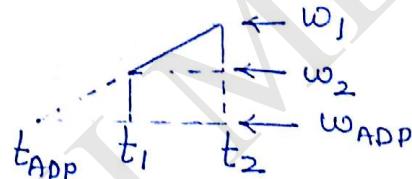
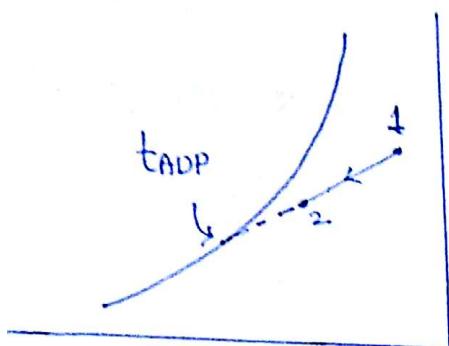
Q.27

Pg.54

~~outside~~
 $m_a = 50 \text{ kg/sec.}$
 $DBT = 45^\circ\text{C}$
 $\phi = 30\%$

~~inside~~
 $t = 25^\circ\text{C}$
 $\phi = 50\%$

By pass Factor & Contact factor (η)
(coil eff.)



$$* BPF = \frac{t_2 - t_{ADP}}{t_1 - t_{ADP}} = \frac{w_2 - w_{ADP}}{w_1 - w_{ADP}} \approx \frac{h_2 - h_{ADP}}{h_1 - h_{ADP}}$$

Contact

factor

$$* \eta = \frac{t_1 - t_2}{t_2 - t_{ADP}} = \frac{\cancel{t_1 - t_2}}{\cancel{t_2 - t_{ADP}}} = \cancel{\frac{t_1 - t_2}{t_2 - t_{ADP}}}$$

$BPF + \eta = 1$

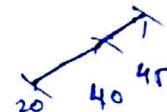
Note ① The by pass factor depends on the placing of the coil. It also depends on the air velocity, as the air velocity increases by pass factor increases.

② latent heat factor is high when the relative humidity is high e.g. during rainy season

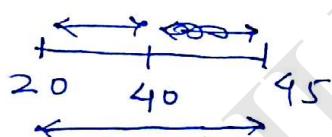
LHF is also high for the place of high occupancy like movie hall, auditorium.

Ques Air at 20°C DBT and 40% RH is heated to 40°C using electric heater. The surface temp. of the coil is 45°C , the bypass factor will be.

$$\text{BF} = \frac{45-40}{45-20}$$



$$\text{BF} = \frac{5}{25} = \frac{1}{5} = 0.2$$



Ques In an air Conditioning process 5 kJ/min of heat is extracted from the room if the SHF = ~~0.8~~, then the latent heat load is

$$\text{SHF} = \frac{SH}{TH}$$

$$SH = \frac{5 \times 0.8}{10} = 4$$

$$\text{SHF LHF} = 1$$

$$CH = 1 - 5 \times 0.8$$

$$LHF = 0.2$$

$$LHF$$

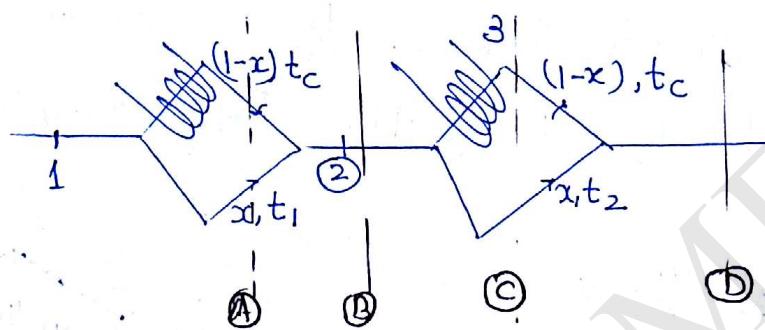
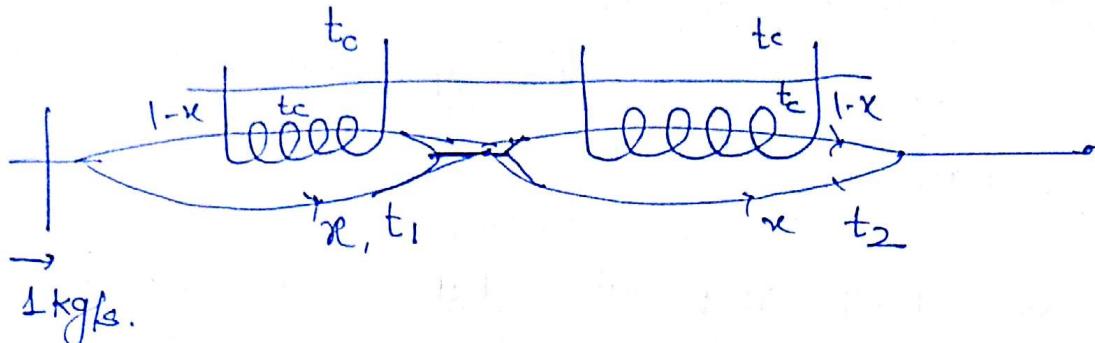
$$SH = 4 \text{ kJ/min}$$

$$LHF = 1 \text{ kJ/min}$$

$$CH = 0.2 \times 5 = 1 \text{ kJ/min}$$

Effective bypass Factors:-

Note: For calculation of effective BF Day Air is Considered



energy Consrv. $\textcircled{A} \rightarrow \textcircled{B}$

$$(1-x)h_c + xh_1 = 1xh_2$$

$$(1-x)C_p t_c + xC_p t_1 = C_p t_2$$

$$(1-x)t_c + x t_1 = t_2 \quad \textcircled{1}$$

Similarly $\textcircled{C} \& \textcircled{D}$

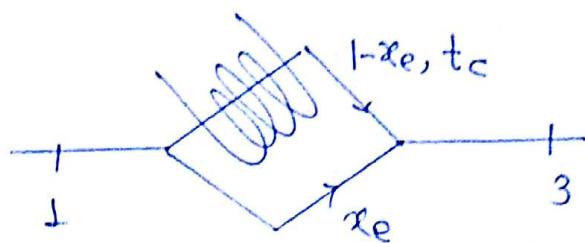
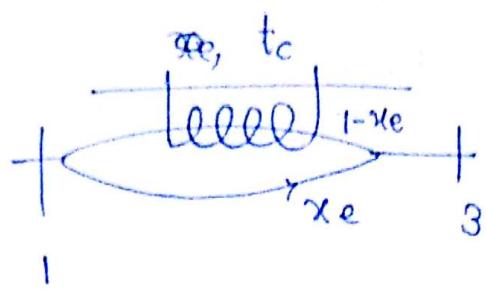
$$(1-x)t_c + x t_2 = t_3 \quad \textcircled{2}$$

From $\textcircled{1} \& \textcircled{2}$

$$(1-x)t_c + x \{(1-x)t_c + x t_1\} = t_3$$

$$t_c - xt_c + xt_c - x^2t_c + x^2t_1 = t_3$$

$$(1-x^2)t_c + x^2t_1 = t_3 \quad \textcircled{3}$$



$$(1-x_e) t_c + x_e t_1 = t_3 \quad -\textcircled{4}$$

$$(1-x^2) t_c + x^2 t_1 = t_3 \quad -\textcircled{3}$$

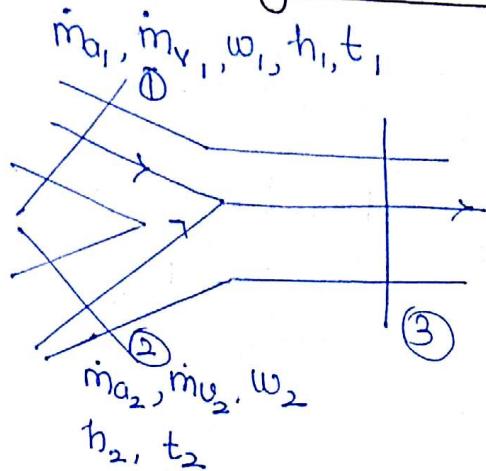
From $\textcircled{3} \& \textcircled{4}$

$$\therefore x_e = x^2$$

For 'n' coils

$$x_e = x^n$$

Adiabatic Mixing of Air streams



① Consrv. of mass

$$(a) \text{ dry} \quad m_{a_1} + m_{a_2} = m_{a_3} \quad - (a)$$

(b) water vapour

$$m_{v_1} + m_{v_2} = m_{v_3} \quad - (b)$$

∴ (No Condensation)

$$\Rightarrow w = \frac{m_v}{m_a}$$

From ④

$$w_1 m_{a_1} + w_2 m_{a_2} = w_3 m_{a_3}$$

$$w_1 m_{a_1} + w_2 m_{a_2} = w_3 m_{a_1} + w_3 m_{a_2}$$

$$\boxed{\frac{m_{a_1}}{m_{a_2}} = \frac{w_3 - w_2}{w_1 - w_3}}$$

Similarly ④ energy cons4.

$$m_{a_1} h_1 + m_{a_2} h_2 = m_{a_3} h_3$$

$$\boxed{\frac{m_{a_1}}{m_{a_2}} = \frac{h_3 - h_2}{h_1 - h_3}}$$