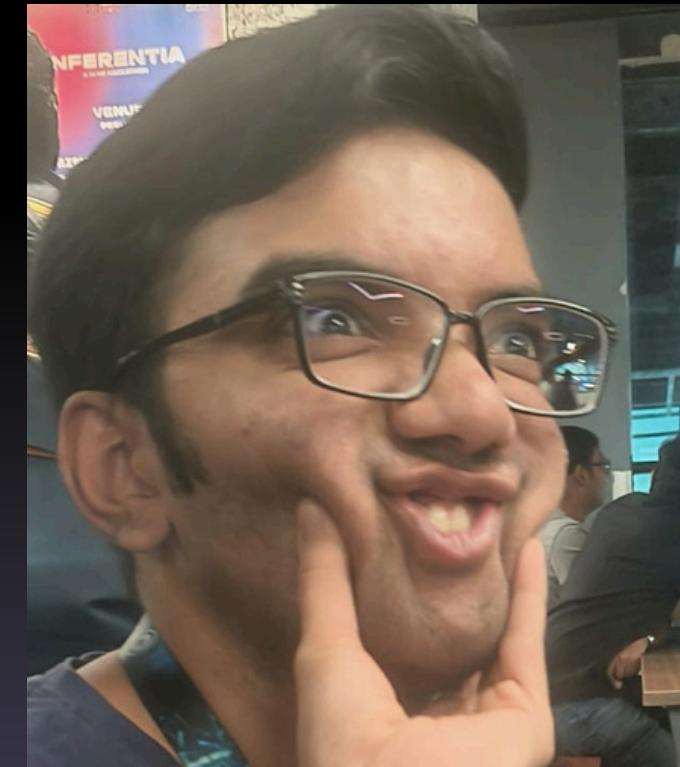


# Introduction to Quantum Post Quantum

# Intro to Quantum Computing



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# Intro to Quantum Crypto



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Teaching assistant  
Professional tryhard :)  
I chain some blocks sometimes



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## quantum shiiii

Classical Computer: “I’ll factor RSA-2048 in 300 trillion years!”

Quantum Computer: “Done. What’s next?”

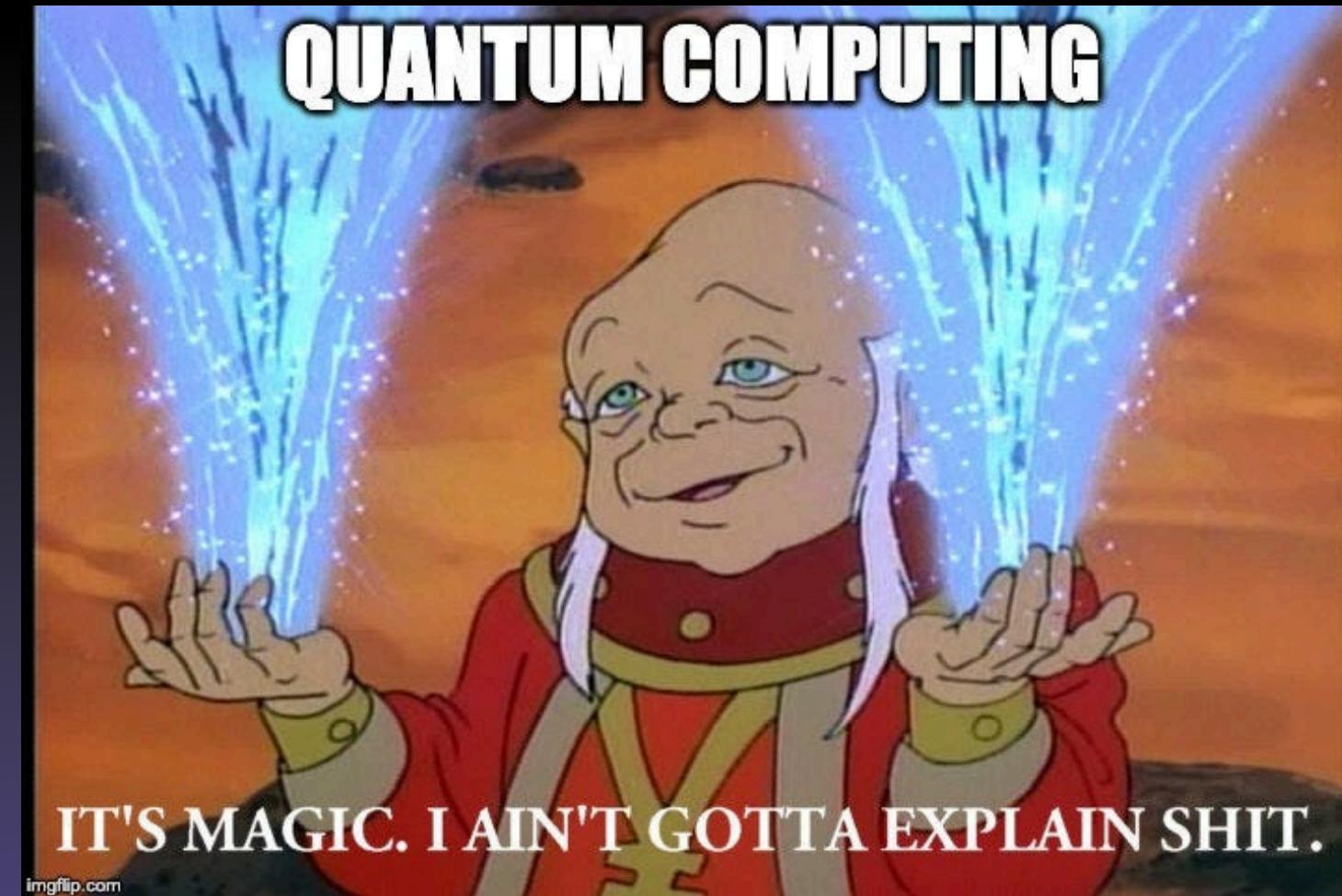
Classical Computer: “...But you didn’t even show your work!”

Quantum Computer: “I showed ALL my work. Simultaneously”

**Classical:**  $O(2^{(\log N)^{1/3}})$  time — basically forever

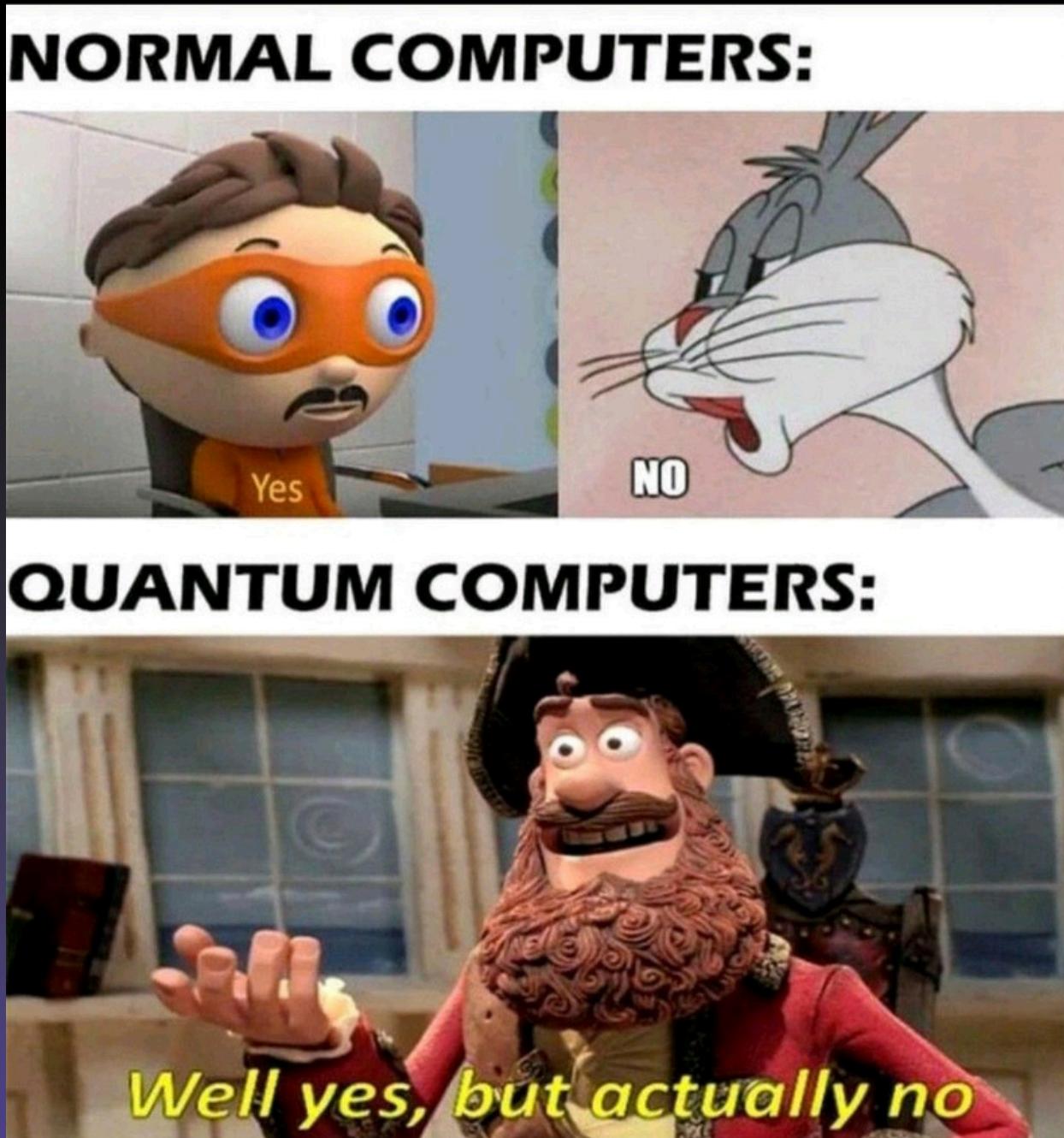
**Quantum:**  $O((\log N)^3)$  time — coffee break

Quantum spins, the cosmos quakes.



# What is Prime Factorization?

- The Problem
- Given: A composite number  $N = p \times q$  (where  $p, q$  are unknown primes)
- Find: The prime factors  $p$  and  $q$
- Easy to verify:  $15 = 3 \times 5$
- Hard to compute: Given 15, find 3 and 5 (trivial). Given RSA-2048, find factors
- (impossible classically).



Quantum computing = math in disguise

- The Naive Approach
- Try dividing  $N$  by every number starting from 2:
- Check if  $N \bmod d = 0$  for  $d = 2, 3, 4, 5, \dots, \sqrt{N}$
- Example: Factoring 143
- 1. Is  $143 \bmod 2 = 0$ ? No (143 is odd)
- 2. Is  $143 \bmod 3 = 0$ ? No ( $1 + 4 + 3 = 8$ , not divisible by 3)
- 3. Is  $143 \bmod 5 = 0$ ? No (doesn't end in 0 or 5)
- 4. Is  $143 \bmod 7 = 0$ ? No ( $143 = 7 \times 20 + 3$ )
- 5. Is  $143 \bmod 11 = 0$ ? Yes! ( $143 = 11 \times 13$ )
- Found factors: 11 and 13

# Pollard's Rho

- A Better Classical Approach
- Don't check every divisor. Use randomization and cycle-finding:

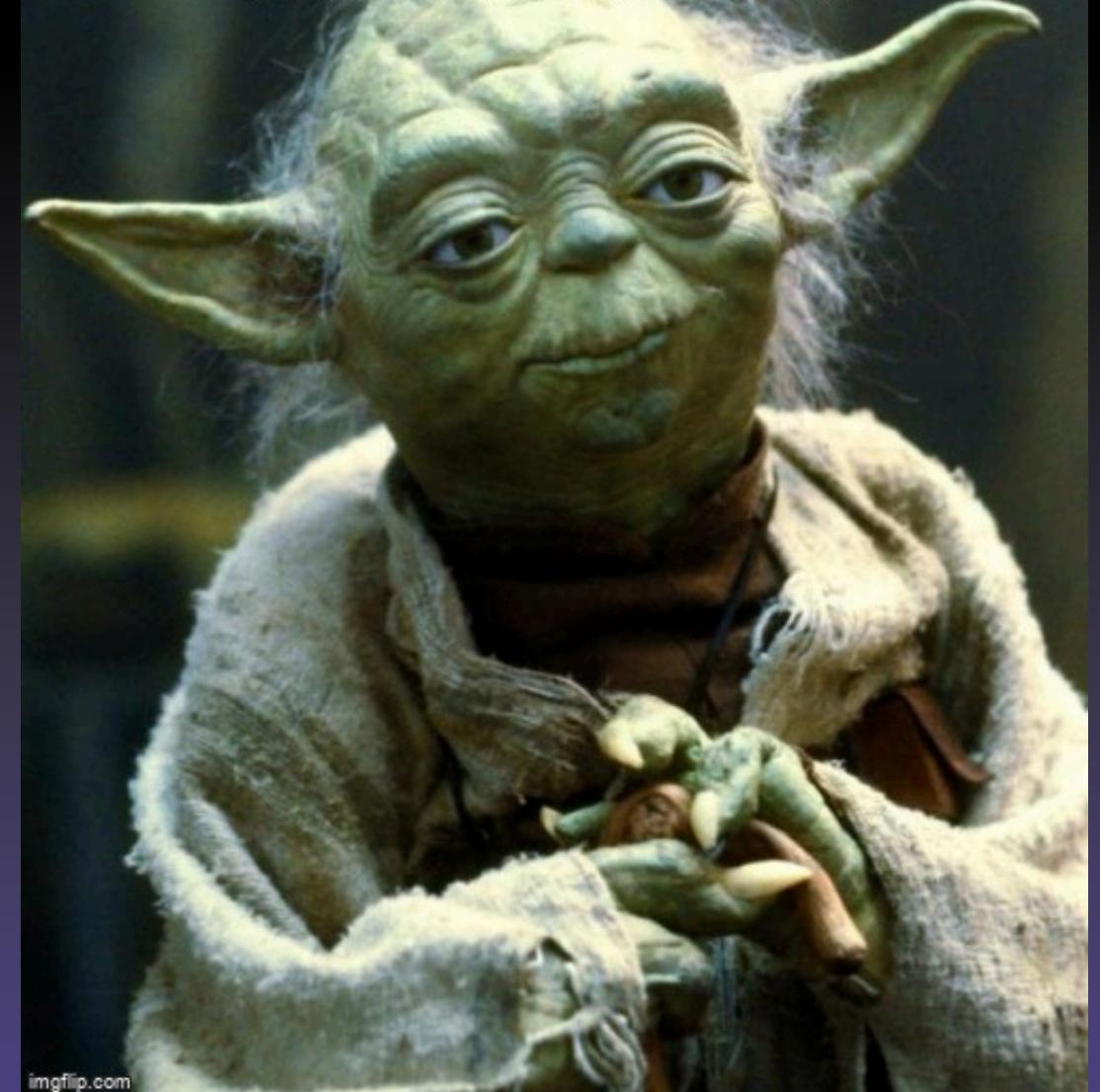
1. Start with  $x_0 = 2$  and iterate:  $x_i = (x_{i-1}^2 + 1) \bmod N$
2. Compute  $\gcd(|x_i - x_j|, N)$  for various  $i, j$
3. If  $\gcd > 1$  and  $\gcd < N$ : Found a non-trivial factor!
4. If stuck: restart with different random seed

- Why It Works (Intuition)
  - ▶ By the pigeonhole principle,  $x_i \bmod p$  will repeat before  $x_i \bmod N$  repeats
  - ▶ Where  $p$  is a factor of  $N$
  - ▶ When the sequences diverge,  $\gcd(x_i - x_j, N)$  catches the factor
  - ▶ Much faster than trial division! her classical loser.

# Setting Up Your Quantum Workspace

Algorithm	Time Complexity	Practical for RSA-2048?
Trial Division	$O(\sqrt{N})$	No (impossible)
Pollard's Rho	$O(N^{1/4})$	No (impossible)
Quadratic Sieve	$O(e^{\sqrt{\log N \log \log N}})$	Maybe (2 weeks)
Number Field Sieve	$O(e^{(\log N)^{1/3}})$	Hardest known (16 years)

WHY IS PRIME-FACTORIZATION-FUNCTION  
NOT WORKING PROPERLY?



imgflip.com

Quantum spins, the cosmos quakes.

# Shor's Insight

- Don't factor directly. Instead:
  1. Reduce factorization to the period-finding problem
- Given  $N$ , pick random  $1 < a < N$ , find the smallest  $r$  where:  
$$ar \equiv 1 \pmod{N}$$

This  $r$  is called the order or period.

2. Extract factors from the period
- Once you have  $r$ , use algebra to compute the factors.

Quantum spins, the cosmos quakes.

# Why This Helps

- Classical: Finding period needs  $O(\sqrt{r})$  time, where  $r$  can be  $O(N) \rightarrow$
- exponential
- Quantum: Finding period needs  $O((\log N)^3)$  time  $\rightarrow$  polynomial!
- This is the exponential speedup
- By shifting the problem, quantum gets its advantage

Quantum spins, the cosmos quakes.

# Why This Helps

Why Period  $\Rightarrow$  Factors? (The Magic Trick)

Once you have period  $r$ , use this algebra:

$$a^r - 1 = (a^{r/2} - 1)(a^{r/2} + 1)$$

Since  $a^r \equiv 1 \pmod{N}$ , we know  $N$  divides  $a^r - 1$ .

Therefore:

$$\gcd(a^{r/2} \pm 1, N) = \text{factors of } N$$

**Plot twist:** This math works classically too! Finding  $r$  is the bottleneck.

# Why This Helps

## Step 1: Quantum Superposition — The Grand Entrance

$$|\psi_0\rangle = |0\rangle \xrightarrow{\text{Hadamard}^{\otimes n}} \frac{1}{\sqrt{2^n}} \sum_{x=0}^{2^n-1} |x\rangle$$

Apply Hadamard gates to create superposition of ALL possible inputs at once.  
It's like opening every door simultaneously instead of trying each key one by one.

**Classical:** "Let me try  $x = 0$ , then  $x = 1$ , then  $x = 2\dots$ "

**Quantum:** "I'm already in all states. Catch up."

## Step 2: Modular Exponentiation — The Quantum Flex

$$|\psi_1\rangle = \frac{1}{\sqrt{2^n}} \sum_{x=0}^{2^n-1} |x\rangle |a^x \bmod N\rangle$$

Compute  $f(x) = a^x \bmod N$  for ALL values of  $x$  simultaneously using quantum gates.  
No loops. No waiting. No sequential computation. Just pure quantum showing off.

This is called **quantum parallelism** and it's why quantum computers are unfairly good at this.

Quantum spins, the cosmos quakes.

# Why This Helps

## Step 3: Measure Ancilla Register — The Collapse

Measure the second register (the  $|a^x \bmod N\rangle$  part).

Let's say we measure some value  $y_0 = a^{x_0} \bmod N$ .

The first register collapses to periodic superposition:

$$|\psi_2\rangle = \frac{1}{\sqrt{r}} \sum_{j=0}^{\lfloor n/r \rfloor} |x_0 + jr\rangle$$

Now the state *encodes* the period  $r$  in the spacing between terms!

But we can't just read  $r$  directly (quantum mechanics is passive-aggressive like that).

## Step 4: Quantum Fourier Transform — The Secret Weapon

Apply QFT to the periodic state:

$$\text{QFT } |\psi_2\rangle \approx \frac{1}{\sqrt{r}} \sum_{k=0}^{r-1} |k \cdot 2^n / r\rangle$$

Creates sharp probability peaks at multiples of  $2^n / r$ .

It's like the quantum computer is playing "Hot and Cold" and suddenly shouts "**BURNING HOT!**"

The QFT transforms *periodicity in position* into *peaks in frequency*. Pure magic (actually Fourier analysis).

es.

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SHOR'S ALGORITHM



# Why This Helps

## Step 5: Measurement & Classical Post-Processing

**Measure** the first register after QFT.

You'll get some value  $\approx k \cdot 2^n / r$  for some integer  $k$ .

### Classical computation:

1. Use continued fractions to extract  $r$  from measured value
2. Compute  $\gcd(a^{r/2} \pm 1, N)$  to get factors
3. If you get 1 or  $N$ , try again with different  $a$  (rare failure case)
4. Otherwise: Congrats! You factored  $N$ . RSA is dead.

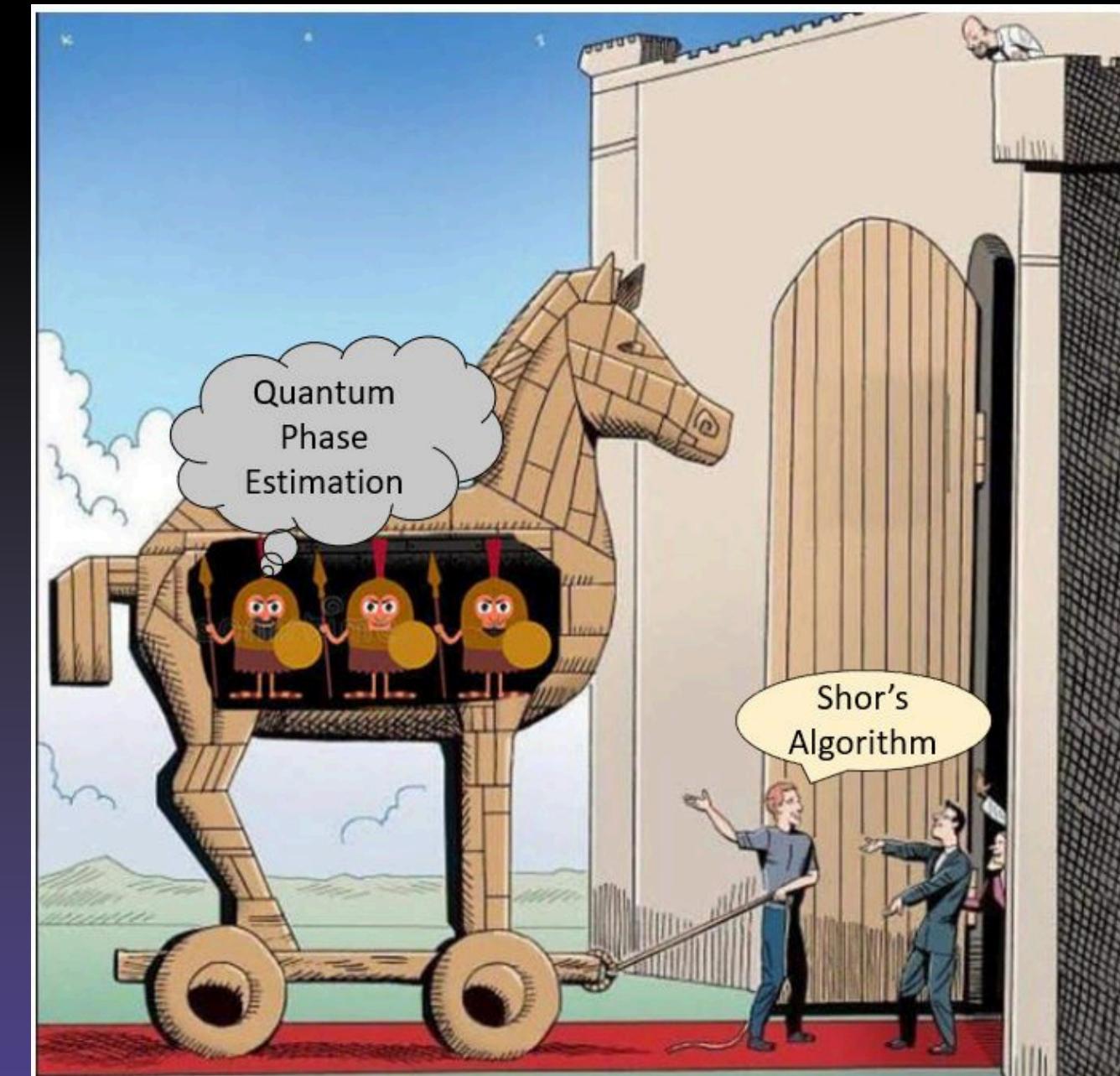
### Success Probability

Each run has good probability of success ( $> 50\%$ ).

If it fails, just run again with different random  $a$ .

Expected number of runs:  $O(1)$  (constant!)

**Bottom line:** Polynomial time with high probability. Game over for RSA.



# Why This Helps

## What QFT Does Mathematically

The Quantum Fourier Transform on  $n$  qubits transforms:

$$|x\rangle \rightarrow \frac{1}{\sqrt{2^n}} \sum_{y=0}^{2^n-1} e^{2\pi i xy/2^n} |y\rangle$$

For a periodic state with period  $r$ :

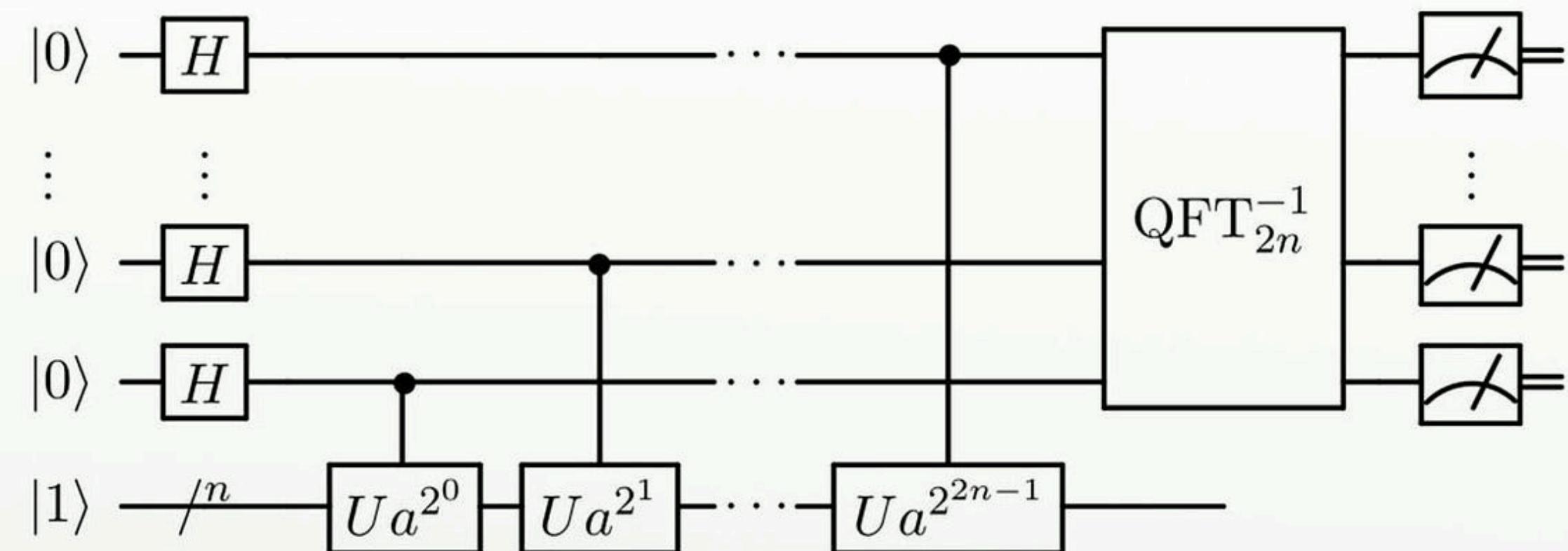
$$\frac{1}{\sqrt{r}} \sum_{j=0}^{r-1} |x_0 + jr\rangle \xrightarrow{\text{QFT}} \text{peaks at } |k \cdot 2^n / r\rangle$$

The periodicity in the input becomes peaks in the output!

Quantum spins, the cosmos quakes.

# Why This Helps

## Shor's algorithm



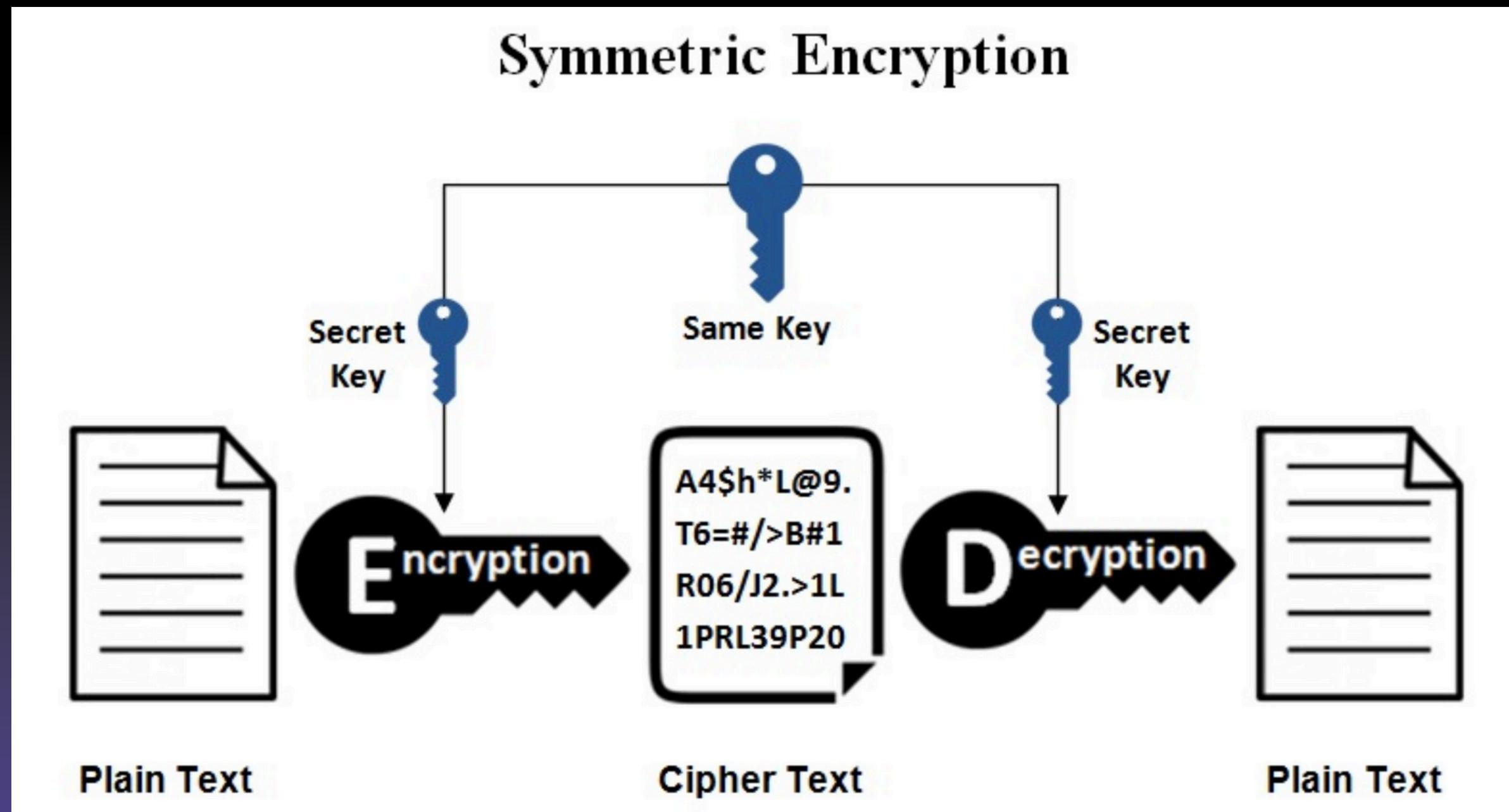
[https://en.wikipedia.org/wiki/File:Shor's\\_algorithm.svg](https://en.wikipedia.org/wiki/File:Shor's_algorithm.svg)

Quantum spins, the cosmos quakes.

# Cryptography time

Quantum spins, the cosmos quakes.

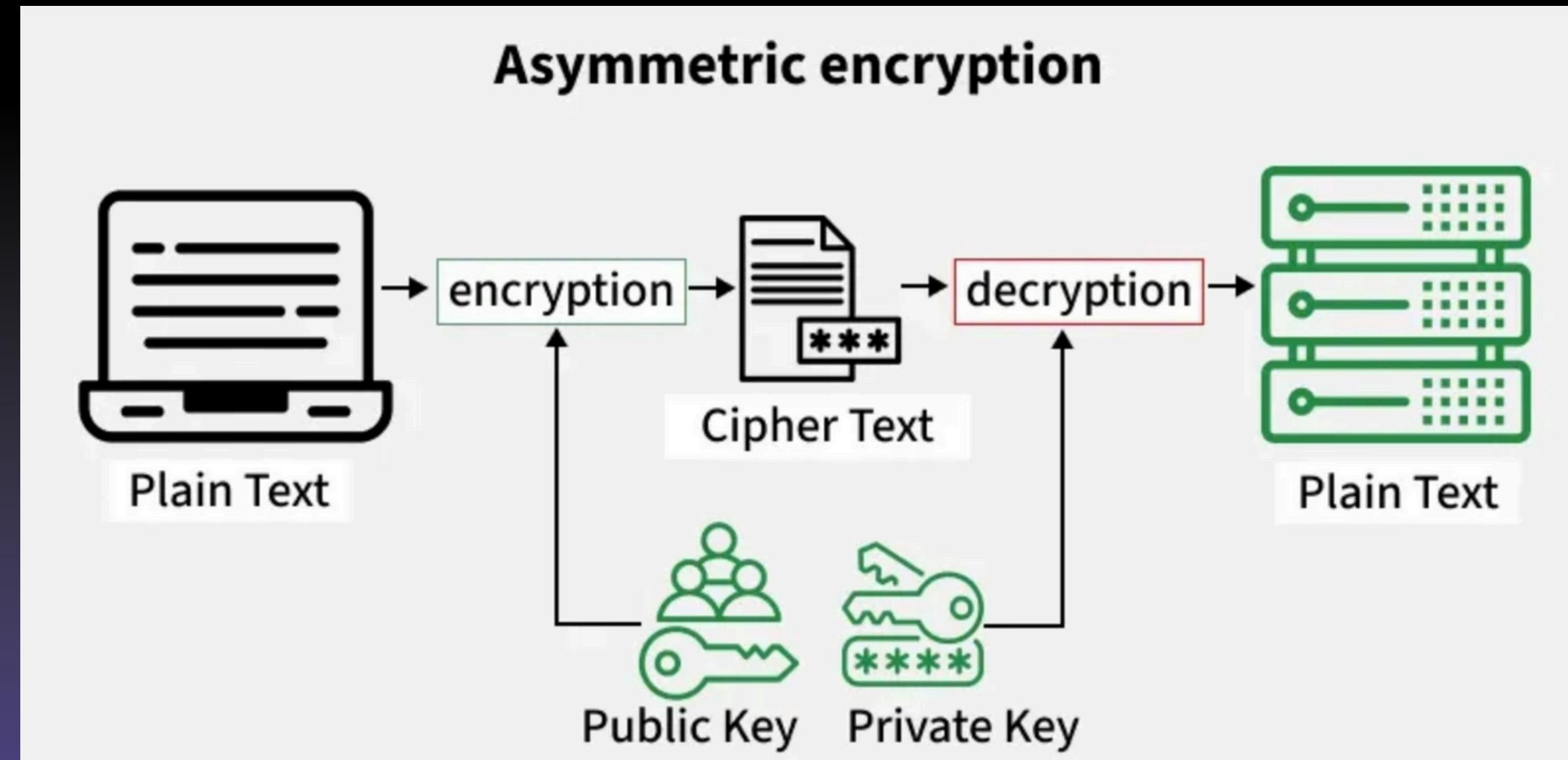
# Symmetric Encryption



# Grovers vs Symmetric

Grover's algo lets a quantum computer brute-force symmetric keys in roughly  $O(\sqrt{n})$  instead of  $O(n)$  time, giving a quadratic speedup.

# Asymmetric Encryption



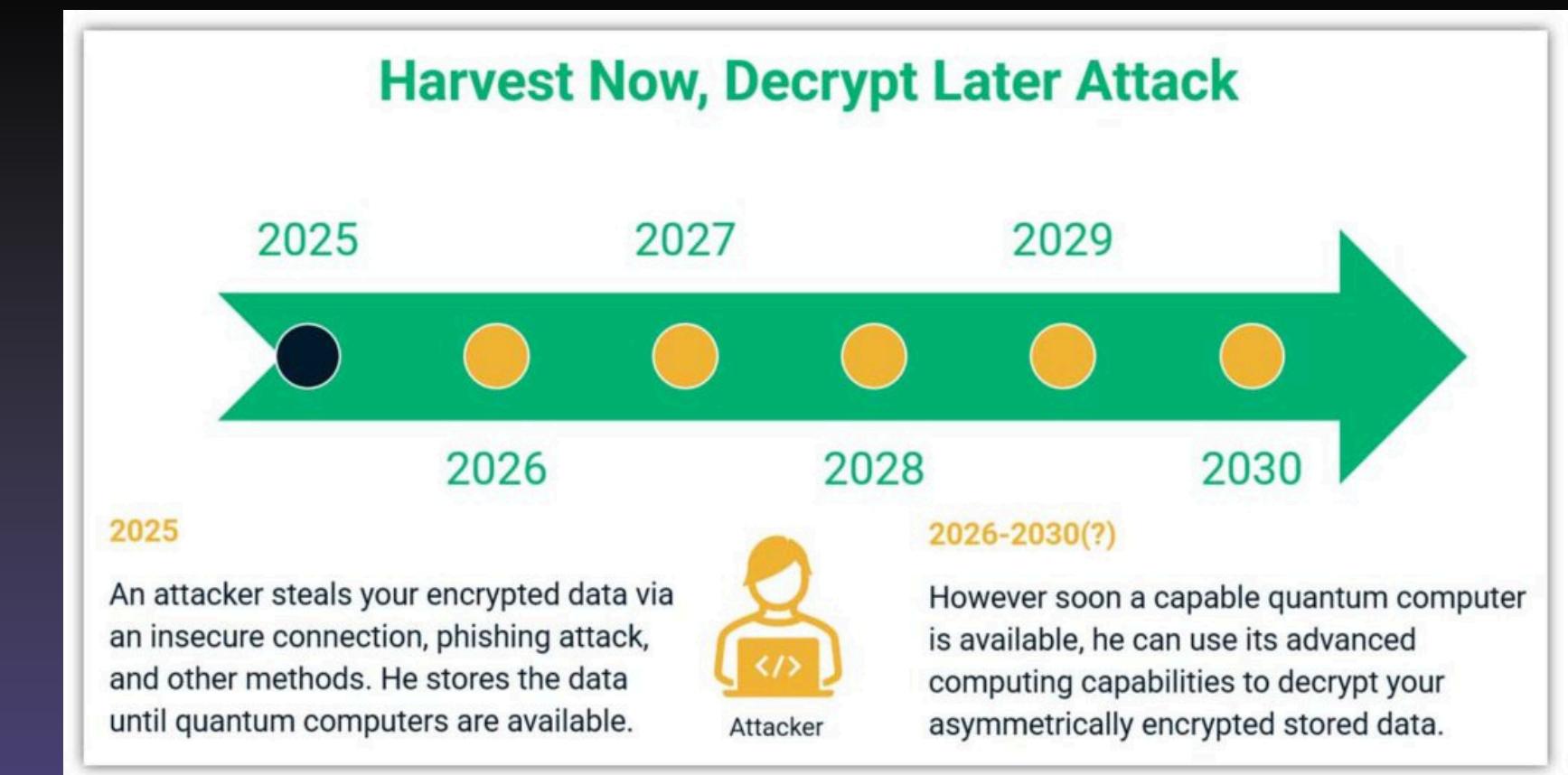
# how do they break

## Asymmetric - Shor's

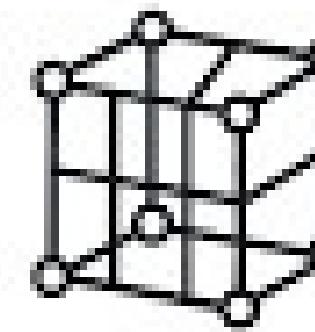
Shor's algorithm efficiently factors large integers and solves discrete logarithms using quantum period finding, breaking the mathematical foundations of RSA, Diffie-Hellman, and ECC.

# harvest now decrypt later

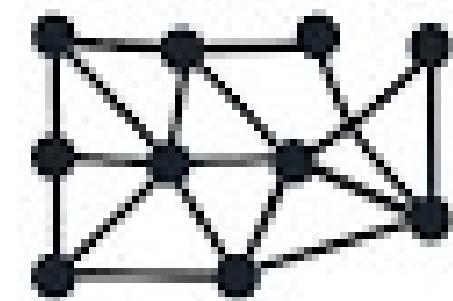
1. Stages of the attack
2. Why is it a serious threat
3. Who is at risk
4. How do we defend



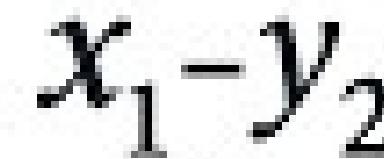
## Families of Post-Quantum Cryptography Algorithms



Lattice-Based



Code-Based



Multivariate  
Polynomial

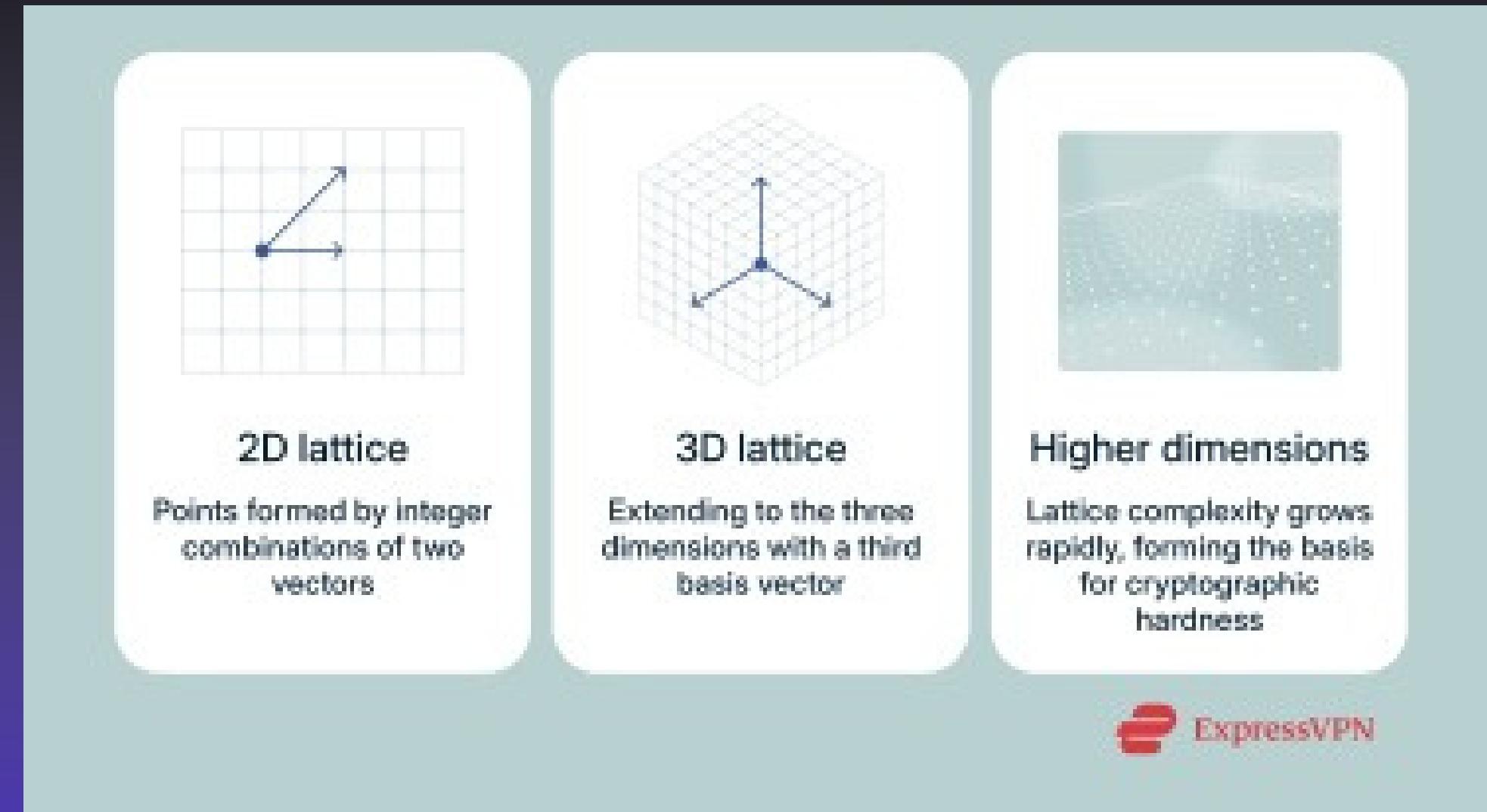


Hash-Based

# Quantum Proof Cryptography

## Lattice-based (Kyber, Dilithium)

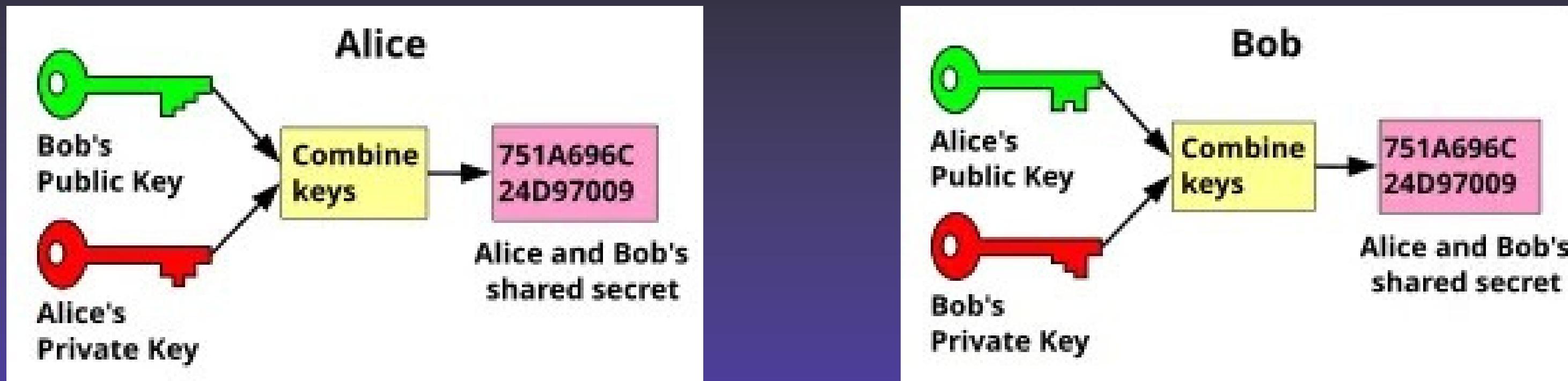
Security from the hardness of solving noisy high dimensional linear equations.



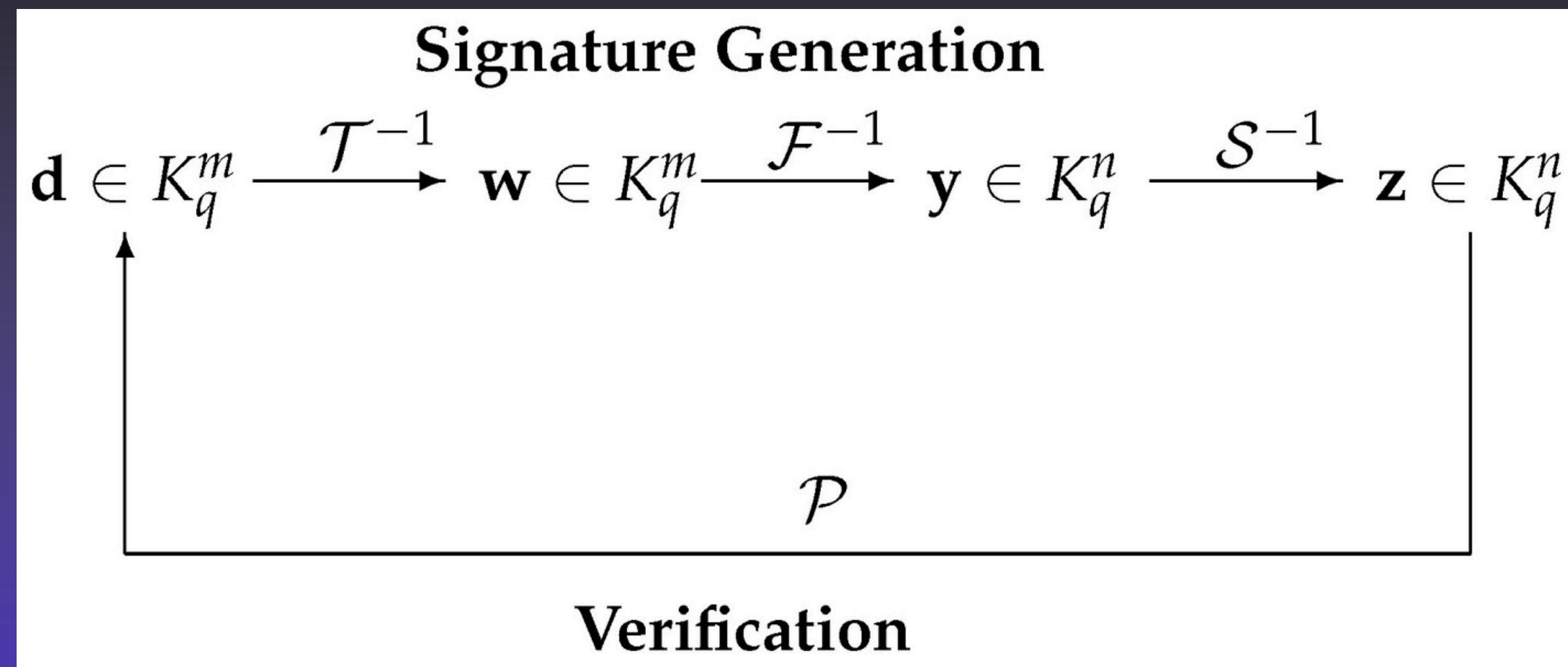
# Quantum Proof Cryptography

## Code-based (Classic McEliece)

Use error-correcting codes, but hide their structure.



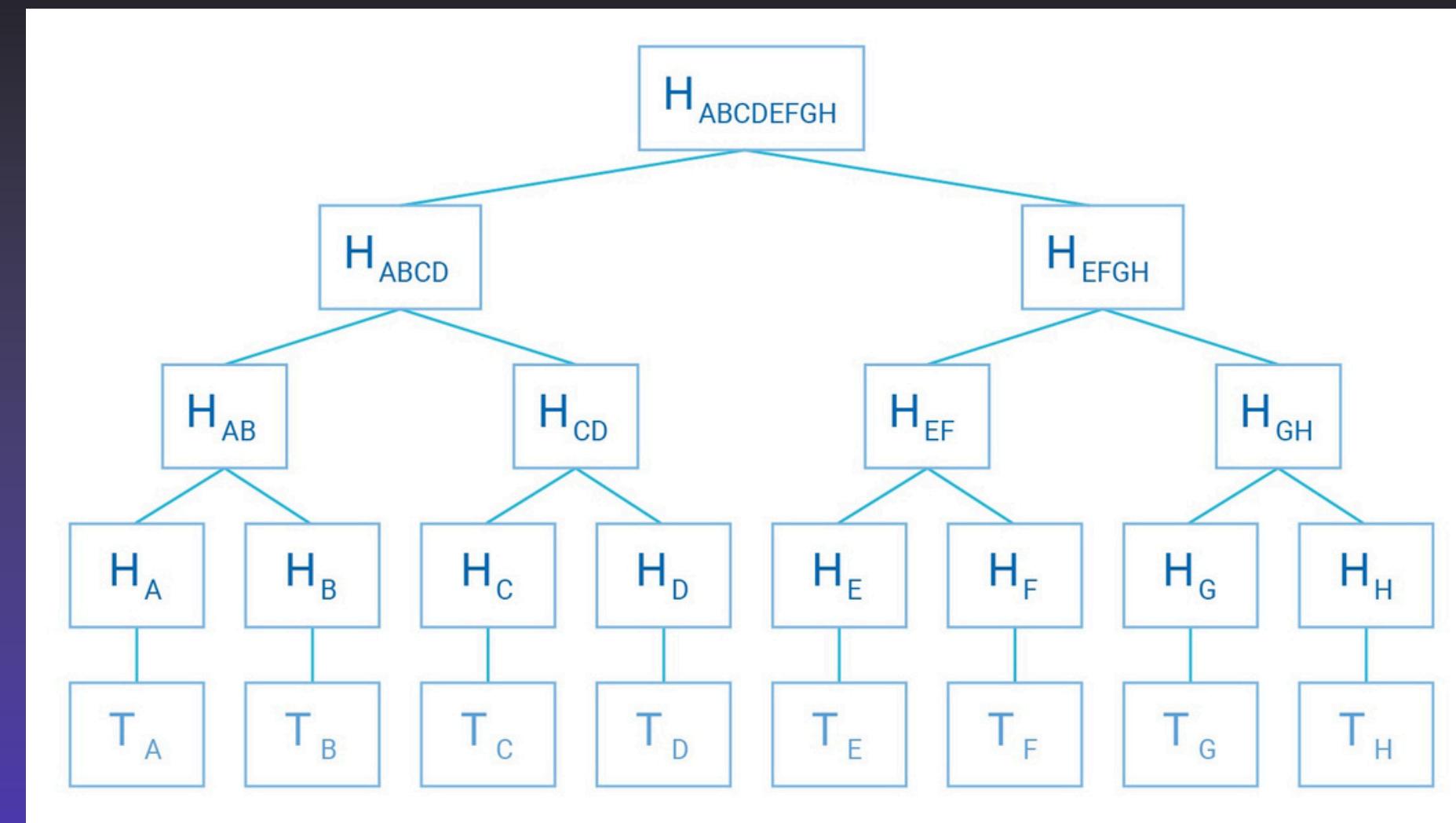
**Multivariate polynomial-based (Rainbow, Gemss)**  
Security from solving systems of multivariate quadratic  
equations (MQ problem).



# Quantum Proof Cryptography

## Hash-based (SPHINCS+)

Security entirely built on the one-way property of cryptographic hash functions.





Thank You