

```
fun append (xs,ys) =  
  if xs=[]  
  then ys  
  else (hd xs)::append(tl xs,ys)  
  
fun map (f,xs) =  
  case xs of  
    [] => []  
  | x::xs' => (f x)::(map(f,xs'))  
  
val a = map (increment, [4,8,12,16])  
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

Programming Languages

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ML Rules for Expressions (Seen So Far)

A very simple ML program

This program has integers, variables, addition, if-expressions, less-than, subtraction, and calling a pre-defined function

```
(* My first ML program *)

val x = 34;

val y = 17;

val z = (x + y) + (y + 2);

val q = z + 1;

val abs_of_z = if z < 0 then 0 - z else z;

val abs_of_z_simpler = abs z
```

Expressions

- We have seen many kinds of expressions:

**34 true false x $e1+e2$ $e1<e2$
if $e1$ then $e2$ else $e3$**

- Can get arbitrarily large since any subexpression can contain subsubexpressions, etc.
- Every kind of expression has
 1. Syntax
 2. Type-checking rules
 - Produces a type or fails (with a bad error message ☹)
 - Types so far: **int bool unit**
 3. Evaluation rules (used only on things that type-check)
 - Produces a value (or exception or infinite-loop)

Variables

- Syntax:
sequence of letters, digits, _, not starting with digit
- Type-checking:
Look up type in current static environment
 - If not there, fail
- Evaluation:
Look up value in current dynamic environment

Addition

- Syntax:
 $e1 + e2$ where $e1$ and $e2$ are expressions
- Type-checking:
If $e1$ and $e2$ have type `int`,
then $e1 + e2$ has type `int`
- Evaluation:
If $e1$ evaluates to $v1$ and $e2$ evaluates to $v2$,
then $e1 + e2$ evaluates to sum of $v1$ and $v2$

Values

- All values are expressions
- Not all expressions are values
- Every value “evaluates to itself” in “zero steps”
- Examples:
 - **34, 17, 42** have type **int**
 - **true, false** have type **bool**
 - **()** has type **unit**

A slightly tougher one

What are the syntax, typing rules, and evaluation rules for conditional expressions?

Let's write it out...

Now you try one

Syntax, type-checking rules, and evaluation rules for less-than comparisons?