```
fun append (xs,ys) =
    if xs=[]
    then ys
    else (hd xs)::append(tl xs,ys)

fun map (f,xs) =
    case xs of
    [] => []
    | x::xs' => (f x)::(map(f,xs'))

val a = map (increment, [4,8,12,16])
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

Programming Languages Dan Grossman

Let Expressions to Avoid Repeated Computation

Avoid repeated recursion

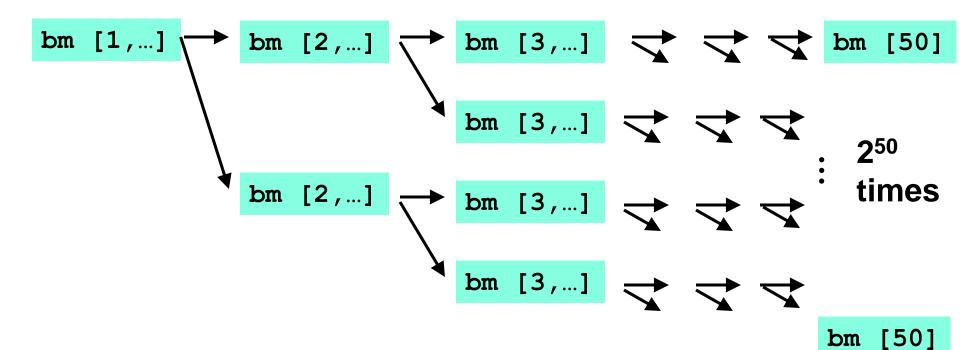
Consider this code and the recursive calls it makes

 Don't worry about calls to null, hd, and tl because they do a small constant amount of work

```
fun bad max (xs:int list) =
    if null xs
    then 0 (* horrible style; fix later *)
    else if null (tl xs)
    then hd xs
    else if hd xs > bad max (tl xs)
    then hd xs
    else bad max (tl xs)
let x = bad max [50, 49, ..., 1]
let y = bad max [1,2,...,50]
```

Fast vs. unusable

if hd xs > bad_max (tl xs)
then hd xs
else bad_max (tl xs)



Math never lies

Suppose one bad_max call's if-then-else logic and calls to hd, null, tl take 10⁻⁷ seconds

- Then bad max [50,49,...,1] takes 50×10^{-7} seconds
- And bad_max [1,2,...,50] takes 1.12 x 108 seconds
 - (over 3.5 years)
 - bad_max [1,2,...,55] takes over 1 century
 - Buying a faster computer won't help much ©

The key is not to do repeated work that might do repeated work that might do...

Saving recursive results in local bindings is essential...

Efficient max

```
fun good max (xs:int list) =
    if null xs
    then 0 (* horrible style; fix later *)
    else if null (tl xs)
    then hd xs
   else
         let val tl ans = good max(tl xs)
         in
             if hd xs > tl ans
             then hd xs
             else tl ans
         end
```

Fast vs. fast

```
let val tl_ans = good_max(tl xs)
in
    if hd xs > tl_ans
    then hd xs
    else tl_ans
end
```

gm [50,...]
$$\rightarrow$$
 gm [49,...] \rightarrow gm [48,...] \rightarrow \rightarrow gm [1]
gm [1,...] \rightarrow gm [2,...] \rightarrow gm [3,...] \rightarrow \rightarrow gm [50]