

Q Given a boolean function  $f(x) = w \cdot x$ ;  
 where,  $x$  &  $w$  are  $n$ -bits of binary string.  
 Give a classical algo to find  $w$ .

(A) Suppose,  $x = (x_1, x_2, \dots, x_n)$ , &  $w = (w_1, \dots, w_n)$   
 $\hookrightarrow f(x) = \sum_{i=1}^n x_i w_i$

Evaluate,

$$f(x^{(i)}) \quad \forall i \in \{1, 2, \dots, n\}$$

$$x^{(i)} = (0, 0, \dots, \underset{\substack{\text{ith} \\ \text{entry}}}{1}, \dots, 0).$$

$$\therefore f(w) = (f(x^{(1)}), f(x^{(2)}), \dots, f(x^{(n)}))$$