

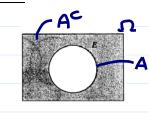
p. 3-10

• Proposition: If A is an event in a sample space Ω and A^c is the complement of A, then $P(A^c) = 1 - P(A)$.

Proof.
$$A^{c} \cup A = \Omega$$
, $A^{c} \cap A = \phi$

$$I = P(\Omega) = P(A^{c} \cup A) = P(A^{c}) + P(A)$$

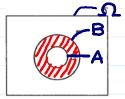
$$I = P(\Omega) = P(A^{c} \cup A) = P(A^{c}) + P(A)$$



• Proposition: If \underline{A} and \underline{B} are events in a sample space Ω and $\underline{A} \subset \underline{B}$, $P(A) \le P(B)$ and P(B - A)then $P(A) = P(B \cap A^c) = P(B) - P(A).$

$$\frac{P \operatorname{roof}}{B} = A \cup (B \cap A^{c}) \qquad \text{by } (A \times I)$$

$$\underline{P(B)} = \underline{P(A)} + \underline{P(B \cap A^{c})} \ge \underline{P(A)}$$



☼ Example (摘自"快思慢想", Kahneman).

琳達是個三十一歲、未婚、有話直說的聰明女性。她主修 哲學,在學生時代非常關心歧視和社會公義的問題,也參 與過反核遊行。下面那一個比較可能?

■ 琳達是銀行行員。AI

Aı∩A₂ ■ 琳達是銀行行員,也是活躍的女性主義運動者。

p. 3-11

 \mathbf{O} Proposition: If A is an event in a sample space Ω , then

Recall.

馬路三審 example

(LNp.1-8)

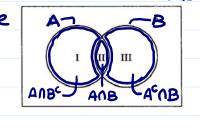
$$0 \le P(A) \le 1. = P(\Omega) & A \subset \Omega$$

• Proposition: If A and B are two events in a sample space Ω , then

$$P(\underline{A \cup B}) = P(A) + P(B) - P(A \cap B).$$

proof. AUB = IUIUII and

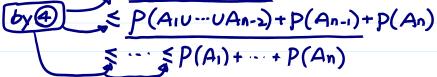
I, II, III mutually exclusive remove $P(A \cup B) = P(I) + P(II) + P(III)$ P(A) = P(I) + P(III) P(B) = P(II) $P(A \cap B) = P(II)$ by disjoint codition



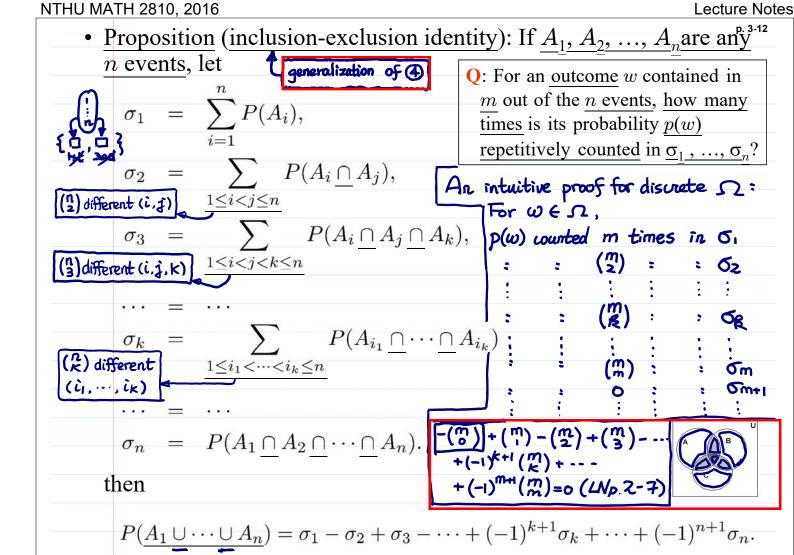
• Proposition: If $A_1, A_2, ..., A_n$ are events in a sample space Ω , then

$$P(\underline{A_1 \cup \dots \cup A_n}) \le P(A_1) + \dots + P(A_n) \stackrel{\mathbf{c.f.}}{\longleftrightarrow} \mathbf{2} \mathbf{\&} \mathbf{4}$$

<u>proof.</u> $P((A_1 \cup \dots \cup A_{n-1}) \cup A_n) \leq P(A_1 \cup \dots \cup A_{n-1}) + P(A_n)$



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