

RS Chapter 6 Simple Linear Regression

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1 Example 6.2

1.1 Data Table, ex6₂

| y | x |
|----|----|
| 95 | 96 |
| 80 | 77 |
| 0 | 0 |
| 0 | 0 |
| 79 | 78 |
| 77 | 64 |
| 72 | 89 |
| 66 | 47 |
| 98 | 90 |
| 90 | 93 |
| 0 | 18 |
| 95 | 86 |
| 35 | 0 |
| 50 | 30 |
| 72 | 59 |
| 55 | 77 |
| 75 | 74 |
| 66 | 67 |

1.2 Analysis in R

1.2.1 Estimation of B₀, B₁

The prediction equation is:

$$\hat{y} = 10.73 + 0.87x$$

1.2.2 (Example 6.3) t-test

We want to test the hypothesis H₀: $\beta_1 = 0$.

Our t-value is 8.8. It is 0.999999921465578

1.2.3 95% confidence interval for β_1

$$\hat{\beta}_1 \pm t_{.025,16} \frac{s}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2}}$$

$$0.87 \pm 0.21$$

This gives a range of β_1 from 0.66 to 1.08.

1.2.4 Coefficient of determination r^2 (Example 6.4)

The coefficient of determination, r^2 is defined as

$$r^2 = \frac{\text{SSR}}{\text{SST}} = \frac{\sum_{i=1}^n (\hat{y}_i - \bar{y})^2}{\sum_{i=1}^n (y_i - \bar{y})^2}$$

r^2 gives the proportion of variation in y that is explained by the model (accounted for by regression on x).

r is the *sample correlation coefficient* between x and y , here 0.91