

STAT PHYS SCIENCE Final Cheat Sheet

Noppakorn Jiravaranon

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1 Measurement of Variation or Dispersion

1.1 Range

$$R = x_{max} - x_{min} \quad (1)$$

1.2 Average Deviation (A.D.)

$$A.D. = \frac{\sum_{i=1}^n |x_i - \mu|}{n} \quad (2)$$

1.3 Standard Deviation (S.D.)

1.3.1 Standard Deviation (Population)

$$\sigma = \sqrt{\frac{\sum_{i=1}^N (x_i - \mu)^2}{N}} = \sqrt{\frac{\sum_{i=1}^N x_i^2 - N\mu^2}{N}} \quad (3)$$

1.3.2 Standard Deviation (Sample)

$$s = \sqrt{\frac{\sum_{i=1}^n (x_i - \mu)^2}{n-1}} = \sqrt{\frac{\sum_{i=1}^n x_i^2 - N\mu^2}{n-1}} \quad (4)$$

1.4 Skewness

1.4.1 Skewness (Population)

$$S_k = \sum_{i=1}^N \frac{[x_i - \mu]^3}{\sigma^3 N} \quad (5)$$

if $S_k = 0$ the data is normal
else if $S_k > 0$ the data is skewed right
else if $S_k < 0$ the data is skewed left

1.4.2 Skewness (Sample)

$$s_k = \frac{n^2}{(n-1)(n-2)} \sum_{i=1}^n \frac{[x_i - \bar{x}]^3}{s^3 n} \quad (6)$$

if $-1 \leq s_k \leq 1$ the data is normal
else if $s_k > 1$ the data is skewed right
else if $s_k < -1$ the data is skewed left

1.5 Relative Kurtosis

A measure of the peakedness of a distribution

1.5.1 Relative Kurtosis (Population)

$$K = \sum_{i=1}^N \frac{[x_i - \mu]^4}{\sigma^4 N} - 3 \quad (7)$$

if $K = 0$ the data is normal
else if $K > 0$ the data is higher than normal
else if $K < 0$ the data is lower than normal

1.5.2 Relative Kurtosis (Sample)

$$k = \frac{n^2(n+1)}{(n-1)(n-2)(n-3)} \sum_{i=1}^n \frac{[x_i - \bar{x}]^4}{s^4 n} - \frac{3(n-1)^2}{(n-2)(n-3)} \quad (8)$$

if $-1 \leq k \leq 1$ the data is normal
else if $k > 1$ the data is higher than normal
else if $k < -1$ the data is lower than normal