# STAT PHYS SCIENCE Midterm Cheat Sheet

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# 1 Measure of Central Ten- 3 Measurement of Variation dency or Dispersion

1.1 Mean

$$\mu = \frac{\sum_{i=1}^{N} x_i}{N}$$

$$\bar{x} = \frac{\sum_{i=1}^{n} x_i}{n}$$

1.2 Median

$$M = x_{\left(\frac{N+1}{2}\right)}$$

- 2 Quantiles
- 2.1 Quartiles

$$Q_i = x_{(i(\frac{N+1}{4}))}$$

2.2 Deciles

$$D_i = x_{(i(\frac{N+1}{10}))}$$

2.3 Percentiles

$$P_i = x_{\left(i\left(\frac{N+1}{100}\right)\right)}$$

3.1 Range

$$(1) R = x_{max} - x_{min} (7)$$

 $_{(2)}$  3.2 Average Deviation (A.D.)

$$A.D. = \frac{\sum_{i=1}^{n} |x_i - \mu|}{n}$$
 (8)

- (3) 3.3 Standard Deviation (S.D.)
  - 3.3.1 Standard Deviation (Population)

$$\sigma = \sqrt{\frac{\sum_{i=1}^{N} (x_i - \mu)^2}{N}} = \sqrt{\frac{\sum_{i=1}^{N} x_i - N\mu^2}{N}}$$
 (9)

 $^{(4)}$  3.3.2 Standard Deviation (Sample)

(5) 
$$s = \sqrt{\frac{\sum_{i=1}^{n} (x_i - \mu)^2}{n-1}} = \sqrt{\frac{\sum_{i=1}^{n} x_i - N\mu^2}{n-1}}$$
 (10)

3.4 Quatile Deviation

$$Q.D. = \frac{Q_3 - Q_1}{2} \tag{11}$$

## 3.5 Skewness

#### 3.5.1 Skewness (Population)

$$S_k = \sum_{i=1}^{N} \frac{[x_i - \mu]^3}{\sigma^3 N}$$
 (12)

if  $S_k = 0$  the data is normal else if  $S_k > 0$  the data is skwed right else if  $S_k < 0$  the data is skwed left

#### 3.5.2 Skewness (Sample)

$$s_k = \sum_{i=1}^n \frac{[x_i - \bar{x}]^3}{s^3 n} \tag{13}$$

if  $-1 \le s_k \le 1$  the data is normal else if  $s_k > 1$  the data is skwed right else if  $s_k < -1$  the data is skwed left

#### 3.6 Relative Kurtosis

A measure of the peakedness of a distribution

#### 3.6.1 Relative Kurtosis (Population)

$$K = \sum_{i=1}^{N} \frac{[x_i - \mu]^4}{\sigma^4 N} - 3 \tag{14}$$

if K = 0 the data is normal else if K > 0 the data is higher than normal else if K < 0 the data is lower than normal

#### 3.6.2 Relative Kurtosis (Sample)

$$k = \frac{n^2(n+1)}{(n-1)(n-2)(n-3)} \sum_{i=1}^{n} \frac{[x_i - x]^4}{s^4 n} - \frac{3(n-1)^2}{(n-2)(n-3)}$$
 (15)

if  $-1 \le k \le 1$  the data is normal else if k > 1 the data is higher than normal else if k < -1 the data is lower than normal

#### 4 Coefficient of Variation

$$C.V. = \frac{\sigma}{\mu} \times 100\% \tag{16}$$

$$C.V. = \frac{s}{\bar{x}} \times 100\% \tag{17}$$

# 5 Outlier by Box Plot

## 5.1 Inter Quartile Range

$$IQR = Q_3 - Q_1 \tag{18}$$

#### 5.2 Whisker

Whisker is the highest or lowest value not reaching the Inner Fence.

#### 5.3 Fence

Outlier is the value lower or higher than the Outer Fence.

Suspected Outlier is the value between the Inner Fence and the Outer Fence.

$$Outer\ Fence = Q_1 - 3(IQR) \tag{19}$$

$$Inner\ Fence = Q_1 - 1.5(IQR) \tag{20}$$

$$Inner\ Fence = Q_3 + 1.5(IQR) \qquad (21)$$

$$Outer \ Fence = Q_3 + 3(IQR) \tag{22}$$

# 6 Probability

## 6.1 Permutation

$${}^{n}P_{r} = \frac{n!}{(n-r)!}$$
 (23)

### 6.2 Combination

$${}^{n}C_{r} = \binom{n}{r} = \frac{n!}{r!(n-r)!} \tag{24}$$

#### 6.3 Properties of Probability

- $0 \le P(A) \le 1$
- $P(\emptyset) = 0$
- P(S) = 1
- $P(A \cup B) = P(A) + P(B) P(A \cap B)$
- P(A) = 1 P(A)'

## 6.4 Conditional Probability

$$P(A|B) = \frac{P(A \cap B)}{P(B)} \tag{25}$$

#### 6.5 Joint Probability

$$P(A \cap B) = P(A)P(B|A) \tag{26}$$

$$P(A \cap B) = P(B)P(A|B) \tag{27}$$

$$P(A \cap B \cap C) = P(A \cap B)P(C|(A \cap B)) \quad (28)$$

$$P(A \cap B \cap C) = P(A)P(B|A)P(C|(A \cap B))$$
(29)

# 7 Probability Distribution

## 7.1 Probability Mass Function

$$f(x) \ge 0$$
; for all  $x$  (30)

$$\sum_{x,y,z} f(x) = 1 \tag{31}$$

$$F(x) = P(X \le x) = \sum_{all \ x \in [-\infty, x]} f(x) \qquad (32)$$

$$\mu = E(X) = \sum_{all \ x} x f(x) \tag{33}$$

$$\sigma^2 = V(X) = \sum_{all \ x} x^2 f(x) - \mu^2$$
 (34)

## 7.2 Probability Density Function

$$f(x) \ge 0$$
; for all  $x$  (35)

$$\int_{-\infty}^{\infty} f(x) = 1 \tag{36}$$

$$F(x) = P(X \le x) = \int_{-\infty}^{x} f(y)dy$$
 (37)

$$\mu = E(X) = \int_{-\infty} \infty x f(x) \tag{38}$$

$$\sigma^2 = V(X) = \int_{-\infty}^{\infty} x^2 f(x) - \mu^2$$
 (39)

# 8 Probability Function

## 8.1 Uniform Distribution

$$f(x) = \frac{1}{k} \tag{40}$$

$$\mu = \frac{1}{k} \sum_{i=1}^{k} x_i \ \sigma^2 = \frac{1}{k} \sum_{i=1}^{k} (x_i - \mu)^2$$
 (41)

### 8.2 Binomial Distribution

$$f(x) = {}^{n}C_{x}p^{x}(1-p)^{1-x}; x = 0, 1, 2, ..., n$$
 (42)

$$\mu = np \quad \sigma^2 = np(1-p) \tag{43}$$

# 8.3 Negative Binomial Distribution

$$f(x) = {x-1 \choose r-1} (1-p)^{x-r} p^r$$
 (44)

$$x = r, r + 1, r + 2, \dots$$

$$\mu = E(X) = \frac{r}{p} \tag{45}$$

$$\sigma^2 = V(X) = \frac{r(1-p)}{p^2}$$
 (46)

Geometric Distribution (r=1)

$$f(x) = p(1-p)^{x-1}; x = 1, 2, ...$$
 (47)

$$\mu = E(X) = \frac{1}{n} \tag{48}$$

$$\sigma^2 = V(X) = \frac{(1-p)}{p^2} \tag{49}$$

### 8.4 Poisson Distribution

$$f(x) = \frac{e^{-\mu}\mu^x}{r!} \tag{50}$$

$$\sigma^2 = \mu \tag{51}$$

## 8.5 Hypergeometric Distribution

$$f(x) = \frac{\binom{K}{x} \binom{N-K}{n-x}}{\binom{N}{x}} \tag{52}$$

$$\mu = E(X) = np \tag{53}$$

$$\sigma^{2} = V(X) = np(1-p)\frac{N-n}{N-1}$$
 (54)