

- Find the solutions of  $\left(\frac{dy}{dx}\right)^2 + y = x^2$  with initial value  $y(0) = 0$

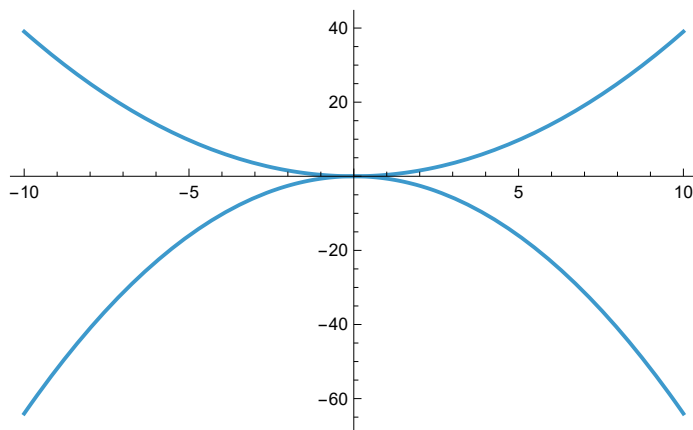
```
In[ ]:= NDSolve[{(y'[x])^2 + y[x] == x^2, y[0] == 0},
  y, {x, -10, 10}]
```

Out[ ]:=

```
{ {y → InterpolatingFunction[
  {+ [plot] Domain: {{-10., 10.}}
  Output: scalar ] },
  {y → InterpolatingFunction[
  {+ [plot] Domain: {{-10., 10.}}
  Output: scalar ] } ] }
```

```
In[ ]:= Plot[y[x] /. %, {x, -10, 10}]
```

Out[ ]:=



```
sol = NDSolve[{(y'[x])^2 + y[x] == x^2, y[0] == 0},  
y, {x, -10, 10}];
```

```
Table[{x, y[x] /. sol[[1]]},  
{x, -10, 10, 1}] // TableForm
```

*Out[ ]//TableForm=*

|     |           |
|-----|-----------|
| -10 | 39.0388   |
| -9  | 31.6214   |
| -8  | 24.9848   |
| -7  | 19.129    |
| -6  | 14.054    |
| -5  | 9.75971   |
| -4  | 6.24621   |
| -3  | 3.51349   |
| -2  | 1.56155   |
| -1  | 0.390388  |
| 0   | 0.        |
| 1   | -0.640388 |
| 2   | -2.56155  |
| 3   | -5.76349  |
| 4   | -10.2462  |
| 5   | -16.0097  |
| 6   | -23.054   |
| 7   | -31.379   |
| 8   | -40.9848  |
| 9   | -51.8714  |
| 10  | -64.0388  |

```
In[*]:= Grid[Table[{x, y[x] /. sol[[1]]}, {x, -10, 10, 1}], Frame → All]
```

```
Out[*]=
```

|     |           |
|-----|-----------|
| -10 | 39.0388   |
| -9  | 31.6214   |
| -8  | 24.9848   |
| -7  | 19.129    |
| -6  | 14.054    |
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| 5   | -16.0097  |
| 6   | -23.054   |
| 7   | -31.379   |
| 8   | -40.9848  |
| 9   | -51.8714  |
| 10  | -64.0388  |

```
sol = NDSolve[{(y'[x])^2 + y[x] == x^2, y[0] == 0},  
y, {x, -10, 10}];
```

```
Table[{x, Abs[y[x] /. sol[[1]]]},  
{x, -10, 10, 1}] // TableForm
```

*Out[ ]//TableForm=*

|     |          |
|-----|----------|
| -10 | 39.0388  |
| -9  | 31.6214  |
| -8  | 24.9848  |
| -7  | 19.129   |
| -6  | 14.054   |
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| -4  | 6.24621  |
| -3  | 3.51349  |
| -2  | 1.56155  |
| -1  | 0.390388 |
| 0   | 0.       |
| 1   | 0.640388 |
| 2   | 2.56155  |
| 3   | 5.76349  |
| 4   | 10.2462  |
| 5   | 16.0097  |
| 6   | 23.054   |
| 7   | 31.379   |
| 8   | 40.9848  |
| 9   | 51.8714  |
| 10  | 64.0388  |