

All Pairs Shortest Path

procedure **Floyd** (var A:array[1..n,1..n] of real; C:array[1..n,1..n] of real);
{Floyd computes shortest path matrix A given arc cost matrix C }

var

i,j,k : integer;

begin

for i:= 1 to n do *{copy C into A }*

for j:= 1 to n do

A[i,j] := C[i,j];

for i:= 1 to n do *{set distance to self as 0 }*

A[i,i] := 0;

for k:= 1 to n do *{compute shortest paths }*

for i:= 1 to n do

for j:= 1 to n do

if A[i,k] + A[k,j] < A[i,j] then

A[i,j] := A[i,k] + A[k,j];

end; *{Floyd}*

procedure **shortest** (var A:array[1..n,1..n] of real; C:array[1..n,1..n] of real; P:array[1..n,1..n] of integer);

{shortest takes an n X n matrix C of arc costs and produces an n X n matrix A of lengths of shortest paths and an n X n matrix P giving a point in the "middle" of each shortest path }

var

i,j,k : integer;

begin

for i:= 1 to n do *{copy C into A }*

for j:= 1 to n do

begin

A[i,j] := C[i,j];

P[i,j] := 0; *{ set P to zero }*

end

for i:= 1 to n do *{set distance to self as 0 }*

A[i,i] := 0;

for k:= 1 to n do *{compute shortest paths }*

for i:= 1 to n do

for j:= 1 to n do

if A[i,k] + A[k,j] < A[i,j] then

begin

A[i,j] := A[i,k] + A[k,j];

P[i,j] := k

{record the middle point }

end

end; *{Floyd}*

path algorithm on next page ☺

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procedure path ( i, j : integer);
var
    k : integer;
begin
    k := P[i,j];           {set k to midpoint of i → j }

    if k = 0 then          {if there is a direct path then ground the recursion }
        return;

    path(i,k);             {get the midpoint between i → k }

    writeln(k);            {process the midpoint }

    path(k,j);             {get the midpoint between k → j }

end;

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