matching_plot_constelation

April 27, 2017

```
In [1]: load_ext autoreload
In [2]: autoreload 2
In [24]: import numpy as np
         import pyphi
         import random
         import makegridslibrary as me
         import matplotlib
         import matplotlib.pyplot as plt
         import itertools
         from pypci import pci
         import pickle
         from tsne import tsne
         import bitarray as bit
         from IPython.core.display import display, HTML
         def i_to_bitlist(o):
             if not o:
                 return [0]
             shifts = list( range( int( np.ceil(np.log2(o)) + 1 ) )
             shifts.reverse() # little endian
             return [(o >> shift) & 1 for shift in shifts]
In [4]: # Load results from matching_LB.py
        temp = 0
        \# temp = .2
        # Old measure
        # results_filename = '/data/nsdm/pyphi/fivenodes_barVSshuffled_gridVSrandor
        results_filename = '/data/nsdm/pyphi/fivenodes_barVSshuffled_gridVSrandom_r
        print('EMD results')
        with open(results_filename, 'rb') as f:
            results = pickle.load(f)
```

```
big_results_bar = results[2]
big_results_shuffled = results[3]
# for network in big results bar:
network = 'Grid'
print(network)
print('\tT : ', temp)
print('\tfor the bar')
for input_stim in big_results_bar[network][temp]:
    print('\t', input_stim)
    this_result = big_results_bar[network][temp][input_stim]
    bar_emd_big_phi = this_result[0]
    bar_emd_concepts = this_result[1]
print('\tfor the shuffled')
for input_stim in big_results_shuffled[network][temp]:
    print('\t', input_stim)
    this_result = big_results_shuffled[network][temp][input_stim]
    shu_emd_big_phi = this_result[0]
    shu_emd_concepts = this_result[1]
print('done.')
# New measure
# results_filename = '/data/nsdm/pyphi/fivenodes_barVSshuffled_gridVSrandor
# results_filename = '/data/nsdm/pyphi/fivenodes_barVSshuffled_gridVSrandon
# results_filename = '/data/nsdm/pyphi/fivenodes_barVSshuffled_gridVSrandor
results_filename = '/data/nsdm/pyphi/fivenodes_barVSshuffled_gridVSrandom_I
print('\nNew cut + entropy distance results')
with open (results filename, 'rb') as f:
    results = pickle.load(f)
big_results_bar_new = results[2]
big_results_shuffled_new = results[3]
# for network in big_results_bar_new:
print(network)
print('\tT : ', temp)
print('\tfor the bar')
for input_stim in big_results_bar_new[network][temp]:
    print('\t', input_stim)
    this_result = biq_results_bar_new[network][temp][input_stim]
```

```
bar_new_big_phi = this_result[0]
            bar_new_concepts = this_result[1]
        print('\tfor the shuffled')
        for input_stim in big_results_shuffled_new[network][temp]:
            print('\t', input_stim)
            this_result = big_results_shuffled_new[network][temp][input_stim]
            shu_new_big_phi = this_result[0]
            shu_new_concepts = this_result[1]
        print('done.')
EMD results
Grid
        T : 0
        for the bar
         (0, 0, 0, 1, 1)
        for the shuffled
         (0, 0, 1, 0, 1)
done.
New cut + entropy distance results
Grid
        T : 0
        for the bar
         (0, 0, 0, 1, 1)
        for the shuffled
         (0, 0, 1, 0, 1)
done.
In [196]: # preprocess: build masks, labels, etc
          def copy_and_mask(X):
              Y = X.copy()
              Y_invalid = Y == -1
              Y[Y_invalid] = 0
              Y_big_invalid = np.any(Y_invalid, axis=0)
              return(Y, Y_invalid, Y_big_invalid)
          # Use EMD
          [bar_concepts, bar_big_phi, shu_concepts, shu_big_phi] = [bar_emd_concept
          # Use new cuts and distances
          # [bar_concepts, bar_big_phi, shu_concepts, shu_big_phi] = [bar_new_conce
          (bar, bar_invalid, bar_big_phi_invalid) = copy_and_mask(bar_concepts)
          (shu, shu_invalid, shu_big_phi_invalid) = copy_and_mask(shu_concepts)
```

```
N = int(np.ceil(np.log2(bar.shape[0])))
# Generate mechanisms labels
mechanisms_orders = np.array([sum(i_to_bitlist(m)) for m in range(2**N)])
# null mechanism is impossible
# mechanisms orders = mechanisms_orders[1:]
# created a sorted index
mo_sorted_idx = np.argsort(mechanisms_orders)
sorted_mechanisms_orders = mechanisms_orders[mo_sorted_idx]
# Generate states labels
gs = np.array(list(itertools.product((0, 1), repeat=N)))
# print(grid_states)
# print(np.abs(np.diff(grid_states, axis=1)))
def neighbor(i,N,d):
    j = i + d
    # cycle right
    while j > N-1:
        j = j-N
    # cycle left
    while j < 0:
        j = j+N
    return j
def state_label_cont(s):
    if not np.sum(s) or np.sum(s) == len(s):
        label = 'full'
    else:
        second\_order = [s[i] + s[neighbor(i,N,1)]  for i in range(N)]
        n1 = np.sum(1*[s2 == 1 for s2 in second_order])
        n2 = np.sum(1*[s2 == 2 for s2 in second_order])
          print(n2, s)
        if n2 == 0:
            label = 'shuffled'
        elif n2 == 1:
              if n1 > 0
            label = 'mixed'
        elif n2 == 2:
            label = 'bigbar2'
        elif n2 == 3:
            label = 'bigbar3'
            raise ValueError('Invalid state')
    return label
def state_label_acti(s):
      s = [s[i] + s[neighbor(i, N, 1)]  for i in range(N)]
```

```
s = [s[neighbor(i,N,-1) + s[i] + s[neighbor(i,N,1)] for i in range
                s = [1*(si > 1) \text{ for } si \text{ in } s]
                s = [1*(si != 1) for si in s]
              s = [1 * (s[neighbor(i,N,-1)] == s[i]) + 1 * (s[neighbor(i,N,1)] == s[i])
              return np.sum(s)
          states_labels = [state_label_cont(s) for s in qs]
          # states_labels = [state_label_acti(s) for s in qs]
          sl_sorted_idx = np.argsort(states_labels)
          sorted_states_labels = [states_labels[s1] for s1 in s1_sorted_idx]
In [197]: s=gs[6]
          ss = [1*(s[neighbor(i,N,-1)] == s[i]) + 1*(s[neighbor(i,N,1)] == s[i]) 
          # print(s)
          # print(ss)
          print(np.sum(ss))
          plt.figure(figsize=(10,10))
          print(states_labels)
          plt.plot(states_labels, list(range(2**N)))
          plt.yticks(range(2**N), gs)
          plt.show()
          plt.figure(figsize=(10,4))
          plt.hist(states_labels)
          plt.show()
['full', 'shuffled', 'mixed', 'shuffled', 'shuffled', 'mixed', 'bigbar2
        ValueError
                                                   Traceback (most recent call last)
        <ipython-input-197-db10d8ffea54> in <module>()
         10 print(states_labels)
    ---> 11 plt.plot(states_labels, list(range(2**N)))
         12 plt.yticks(range(2**N), gs)
```

```
13 plt.show()
    /home/leonardo/anaconda3/envs/nsdm-pyphi/lib/python3.4/site-packages/matplo
   3316
                              mplDeprecation)
   3317
            try:
-> 3318
                ret = ax.plot(*args, **kwargs)
   3319
            finally:
   3320
                ax. hold = washold
    /home/leonardo/anaconda3/envs/nsdm-pyphi/lib/python3.4/site-packages/matplo
   1890
                             warnings.warn(msg % (label_namer, func.__name__),
   1891
                                           RuntimeWarning, stacklevel=2)
-> 1892
                    return func(ax, *args, **kwargs)
  1893
                pre_doc = inner.__doc__
   1894
                if pre_doc is None:
    /home/leonardo/anaconda3/envs/nsdm-pyphi/lib/python3.4/site-packages/matplo
   1405
   1406
                for line in self._get_lines(*args, **kwargs):
-> 1407
                    self.add_line(line)
   1408
                    lines.append(line)
   1409
    /home/leonardo/anaconda3/envs/nsdm-pyphi/lib/python3.4/site-packages/matplo
   1785
                    line.set_clip_path(self.patch)
   1786
                self._update_line_limits(line)
-> 1787
   1788
                if not line.get_label():
   1789
                    line.set_label('_line%d' % len(self.lines))
    /home/leonardo/anaconda3/envs/nsdm-pyphi/lib/python3.4/site-packages/matplo
   1807
                Figures out the data limit of the given line, updating self.dat
   1808
-> 1809
                path = line.get_path()
   1810
                if path.vertices.size == 0:
   1811
                    return
    /home/leonardo/anaconda3/envs/nsdm-pyphi/lib/python3.4/site-packages/matplo
    987
```

self.recache()

return self._path

if self._invalidy or self._invalidx:

988

990

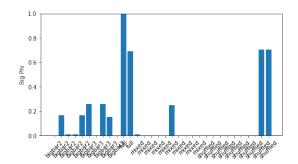
--> 989

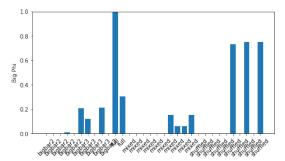
```
/home/leonardo/anaconda3/envs/nsdm-pyphi/lib/python3.4/site-packages/matplo
                       674
                                                                                x = ma.asarray(xconv, np.float).filled(np.nan)
                       675
                                                                     else:
           --> 676
                                                                                x = np.asarray(xconv, np.float_)
                                                                     x = x.ravel()
                       677
                       678
                                                         else:
                       /home/leonardo/anaconda3/envs/nsdm-pyphi/lib/python3.4/site-packages/numpy/
                       529
                       530
           --> 531
                                             return array(a, dtype, copy=False, order=order)
                       532
                       533
                      ValueError: could not convert string to float: 'full'
In [198]: # [np.sum(sorted_mechanisms_orders==o) for o in np.unique(mechanisms_orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=orders=
                            # print(sl_sorted_idx)
                            mechanisms orders
                             # print (mechanisms_orders)
                             # print(sorted_mechanisms_orders)
                             #print (sorted_states_labels)
Out[198]: array([0, 1, 1, 2, 1, 2, 2, 3, 1, 2, 2, 3, 2, 3, 3, 4, 1, 2, 2, 3, 2, 3,
                                                 4, 2, 3, 3, 4, 3, 4, 4, 5])
In [200]: # Big Phi
                            plt.figure(figsize=(17,4))
                            plt.subplot(1,2,1)
                            plt.ylim([0, 1])
                            Y = bar_biq_phi.copy()
                            Y[bar_big_phi_invalid] = 0
                            plt.bar(range(len(Y)), Y[sl_sorted_idx])
                            plt.xticks(range(len(Y)), sorted_states_labels, rotation=45)
                            plt.ylabel('Big Phi')
                            plt.subplot(1,2,2)
                            plt.ylim([0, 1])
                             # Y = bar_big_phi_new.copy()
                             # Y[bar_big_phi_new_invalid] = 0
```

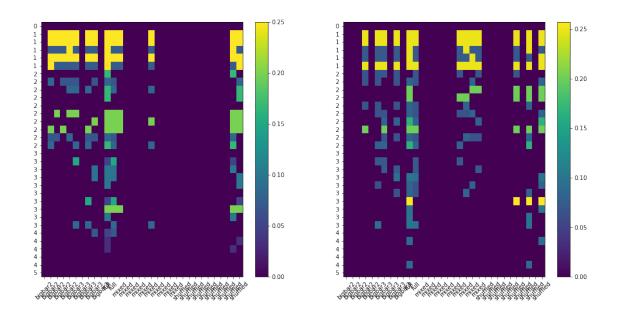
```
Y = shu_big_phi.copy()
Y[shu_big_phi_invalid] = 0
plt.bar(range(len(Y)), Y[sl_sorted_idx])
plt.xticks(range(len(Y)), sorted_states_labels, rotation=45)
plt.ylabel('Big Phi')
plt.show()
# All concepts
def norm_min_max(Y):
    Z = (Y-min(Y.flatten()))/(max(Y.flatten())-min(Y.flatten()))
    return Z
plt.figure(figsize=(17,8))
plt.subplot (1,2,1)
# Y = X[sl sorted idx, :]
# Why numpy, why...
# Y = bar[mo_sorted_idx, sl_sorted_idx].copy()
bar_sorted = bar[mo_sorted_idx, :].copy()[:, sl_sorted_idx]
# bar_sorted[bar_invalid[mo_sorted_idx, :][:, sl_sorted_idx]] = 0
# bar_sorted = np.ma.masked_where(X_invalid[sl_sorted_idx, :], X[sl_sorted_idx]
# bar_sorted = norm_min_max(Y)
plt.imshow(bar_sorted, aspect='auto')
plt.yticks(range(len(mo_sorted_idx)), sorted_mechanisms_orders)
plt.xticks(range(len(sl_sorted_idx)), sorted_states_labels, rotation=45)
# plt.xticks(range(len(sl_sorted_idx)), range(len(sl_sorted_idx)), rotate
plt.colorbar()
plt.subplot(1,2,2)
# Y = X_new[sl_sorted_idx, :]
# shu_sorted = shu[mo_sorted_idx, sl_sorted_idx].copy()
shu_sorted = shu[mo_sorted_idx, :].copy()[:, sl_sorted_idx]
# shu_sorted[shu_invalid[mo_sorted_idx, :][:, sl_sorted_idx]] = 0
# shu_sorted = np.ma.masked_where(X_new_invalid[sl_sorted_idx, :], X_new
# shu_sorted = norm_min_max(Y_shu)
```

```
plt.imshow(shu_sorted, aspect='auto')
plt.yticks(range(len(mo_sorted_idx)), sorted_mechanisms_orders)
plt.xticks(range(len(sl_sorted_idx)), sorted_states_labels, rotation=45)
# plt.xticks(range(len(sl_sorted_idx)), range(len(sl_sorted_idx)), rotation=45)
plt.colorbar()
```







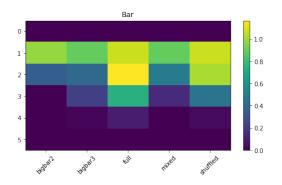


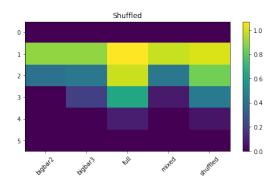
```
In [201]: # number_only = 1
          \# number_only = 0
          for number_only in range(2):
              display(HTML("<center><h1 style='font-size: %dpx;height: 100;'>%s</h1
                      ((40, '# of concepts') if number_only else (50, 'Σ &ph:
              # unique mechanisms
              unique_mechanism_orders = np.unique(sorted(sorted_mechanisms_orders))
              # unique and states
              unique_states_labels = np.unique(sorted(sorted_states_labels))
              nstates = len(unique_states_labels)
              # BAR
              # find all the concepts for the bar
              if number_only:
                  bar\_sorted\_n = 1. * (bar\_sorted > 0)
              else:
                  bar_sorted_n = bar_sorted
              # sum all the mechanisms for a given order, per state
              bar_sorted_cpmo = np.array([np.sum(bar_sorted_n[sorted_mechanisms_order])
                                           for o in unique_mechanism_orders])
              # remove invalid states
```

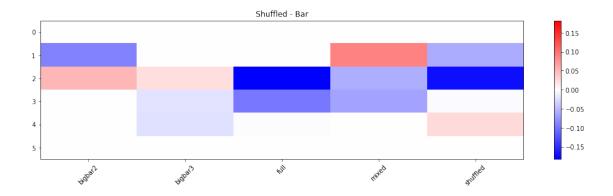
```
invalid_bar_states = np.all(bar_invalid[mo_sorted_idx, :][:, sl_sorted_idx)
sorted_bar_states_labels_noinv = np.delete(sorted_states_labels, np.v
bar_sorted_cpmo_noinv = np.delete(bar_sorted_cpmo, np.where(invalid_k)
# take the mean and std accross valid states
bar_sorted_cpmosc = np.array([np.mean(bar_sorted_cpmo_noinv[:, [ss ==
                        for s in unique_states_labels]).T
bar_sorted_cpmosc_std = np.array([np.std(bar_sorted_cpmo_noinv[:, [ss
                        for s in unique_states_labels]).T
# SHUFFLED
# find all the concepts for the shuffled
if number_only:
    shu\_sorted\_n = 1. * (shu\_sorted > 0)
else:
    shu\_sorted\_n = shu\_sorted
# sum all the mechanisms for a given order, per state
shu_sorted_cpmo = np.array([np.sum(shu_sorted_n[sorted_mechanisms_order)])
                             for o in np.unique(sorted(mechanisms_orde
# remove invalid states
invalid_shu_states = np.all(shu_invalid[mo_sorted_idx, :][:, sl_sorted_idx, :]
sorted_shu_states_labels_noinv = np.delete(sorted_states_labels, np.v
shu_sorted_cpmo_noinv = np.delete(shu_sorted_cpmo, np.where(invalid_s
# take the mean and std accross valid states
shu_sorted_cpmosc = np.array([np.mean(shu_sorted_cpmo_noinv[:, [ss ==
                        for s in unique_states_labels]).T
shu_sorted_cpmosc_std = np.array([np.std(shu_sorted_cpmo_noinv[:, [ss
                        for s in unique_states_labels]).T
plt.figure(figsize=(17,4))
plt.subplot (1, 2, 1)
plt.imshow(bar_sorted_cpmosc, aspect='auto')
plt.xticks(range(len(unique_states_labels)), unique_states_labels, re
plt.colorbar()
plt.title('Bar')
plt.subplot (1, 2, 2)
plt.imshow(shu_sorted_cpmosc, aspect='auto')
plt.xticks(range(len(unique_states_labels)), unique_states_labels, ro
plt.colorbar()
plt.title('Shuffled')
plt.show()
```

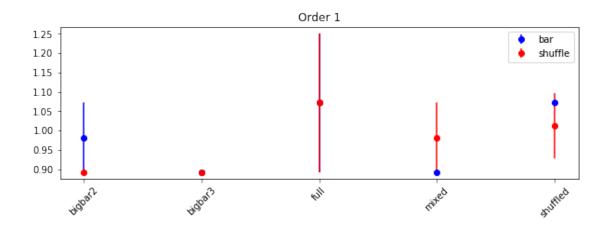
```
plt.figure(figsize=(17,4))
the_diff = shu_sorted_cpmosc-bar_sorted_cpmosc
the_diff_max = max(abs(the_diff.flatten()))
plt.imshow(the_diff, aspect='auto', cmap='bwr', vmin=-the_diff_max, v
plt.colorbar()
plt.xticks(range(len(unique_states_labels)), unique_states_labels, re
plt.title('Shuffled - Bar')
plt.show()
for o in range(1, len(unique_mechanism_orders)):
    plt.figure(figsize=(10,3))
   hb = plt.errorbar(range(nstates), bar_sorted_cpmosc[o, :], yerr=h
    hs = plt.errorbar(range(nstates), shu_sorted_cpmosc[o, :], yerr=s
    plt.legend([hb, hs], ['bar', 'shuffle'])
    plt.xticks(range(len(unique_states_labels)), unique_states_labels
    plt.title('Order %d' % o)
    plt.show()
```

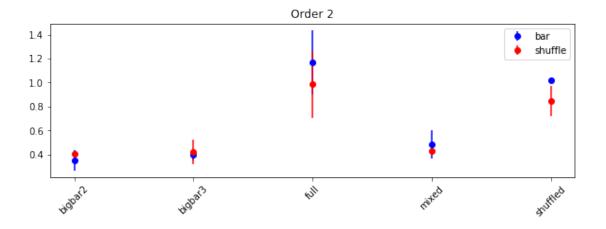
<IPython.core.display.HTML object>

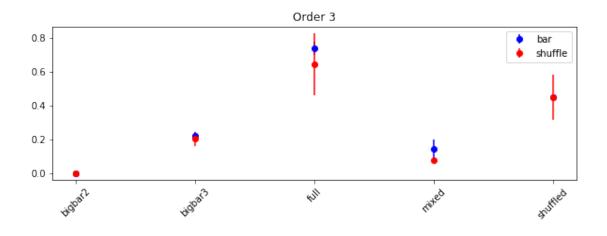


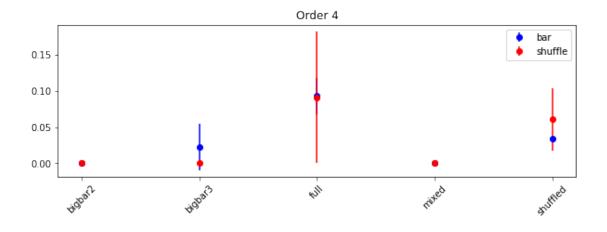


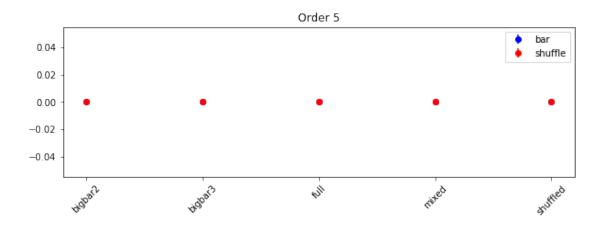




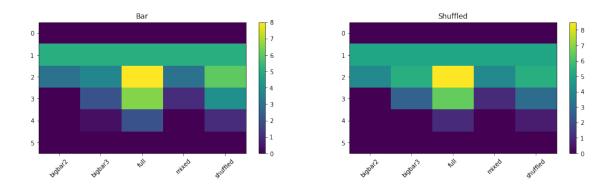


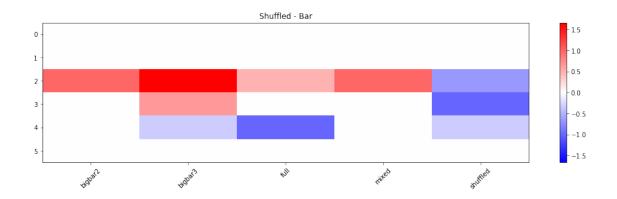


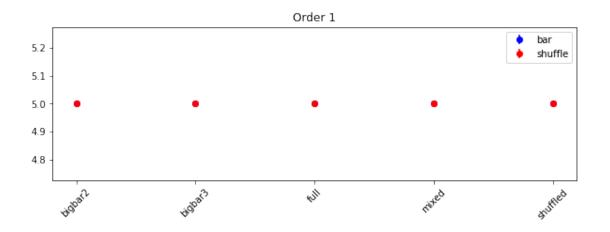


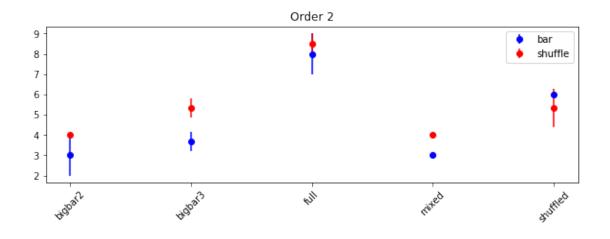


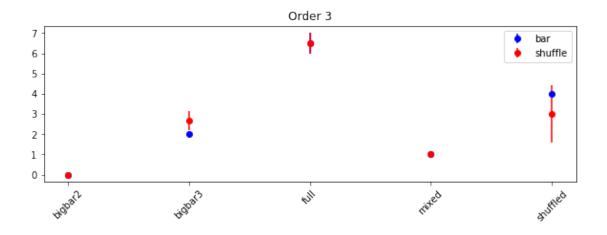
<IPython.core.display.HTML object>

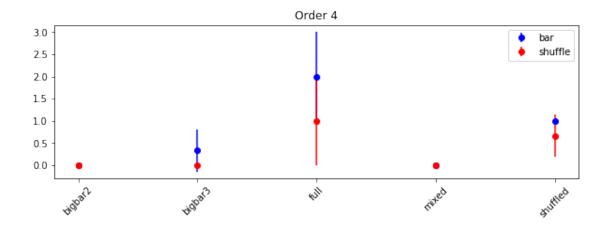


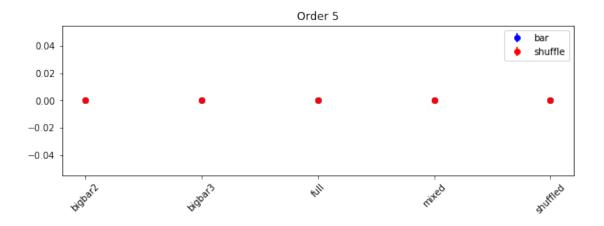












```
In [208]: # State labels
          X = bar.T.copy()
          # continuity
          # labels = states_labels.copy()
          # unique_labels_values = np.unique(labels)
          # unique_labels = unique_labels_values
          # bar vs shuffled
          # labels = states_labels.copy()
          # labels_to_int = {'full': 1, 'shuffled': 2, 'mixed': 3, 'bigbar2': 4, 'k
          # labels = np.array([labels_to_int[s] for s in labels])
          # unique_labels_values = list(labels_to_int.values())
          # unique_labels = labels_to_int.keys()
          # Mechanism labels
          X = bar.copy()
          labels = mechanisms_orders.copy()
          unique_labels_values = np.unique(labels)
          unique_labels = unique_labels_values
          \# X = np.loadtxt("./tsne/mnist2500_X.txt");
          # labels = np.loadtxt("./tsne/mnist2500_labels.txt");
          Y = tsne.tsne(X, 2, 50, 20.0)
Preprocessing the data using PCA...
Computing pairwise distances...
Computing P-values for point 0 of 32 ...
```

Mean value of sigma: 0.232840008782

```
10 : error is
                          10.8421054037
Iteration
Iteration
           20 : error is
                          10.5130750976
           30 : error is
                          10.1467157004
Iteration
Iteration 40 : error is
                          10.4974449252
                          9.60596882615
Iteration
           50 : error is
                          9.56683722161
Iteration
           60 : error is
Iteration
          70 : error is
                          10.6079576952
Iteration
           80 : error is
                          10.3190645416
                          10.4364399743
Iteration
           90 : error is
Iteration 100 : error is
                           9.42144935303
Iteration 110 : error is
                           0.981397460112
                           0.869544627301
Iteration 120 : error is
                           0.797414343533
Iteration
          130 : error is
Iteration 140 : error is
                           0.742332215212
Iteration 150 : error is
                           0.652262402185
                           0.563451187057
Iteration 160 : error is
Iteration 170 : error is
                           0.533495533184
Iteration 180 : error is
                           0.516064522462
Iteration 190 : error is
                           0.507405689709
Iteration
          200 : error is
                           0.500660731866
Iteration 210 : error is
                           0.488217069869
Iteration
           220 : error is
                           0.478906036814
Iteration 230 : error is
                           0.468670871253
Iteration 240 : error is
                           0.464441261938
Iteration 250 : error is
                           0.461782534312
                           0.457934031193
Iteration 260 : error is
Iteration 270 : error is
                           0.452314351276
Iteration 280 : error is
                           0.448374677711
Iteration 290 : error is
                           0.444617747016
Iteration 300 : error is
                           0.441538968758
                           0.437780923505
Iteration
          310 : error is
Iteration 320 : error is
                           0.432649981967
Iteration 330 : error is
                           0.425376737527
Iteration 340 : error is
                           0.414465379722
Iteration 350 : error is
                           0.39847412371
Iteration 360 : error is
                           0.372593376458
                           0.345702571443
Iteration 370 : error is
Iteration
          380 : error is
                           0.325076743765
Iteration 390 : error is
                           0.314441612079
Iteration 400 : error is
                           0.312203191338
Iteration 410 : error is
                           0.311068172773
                           0.310298741795
Iteration 420 : error is
Iteration 430 : error is
                           0.309307825529
                           0.307057359275
Iteration 440 : error is
Iteration
          450 : error is
                           0.299212767555
Iteration 460 : error is
                           0.296661877733
Iteration 470 : error is
                           0.295686901023
Iteration 480 : error is
                           0.295246680407
```

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Iteration 490 : error is
                           0.294818536377
Iteration 500 : error is
                           0.294183050505
                           0.29244740447
Iteration 510 : error is
Iteration 520 : error is
                           0.290123105781
Iteration
           530 : error is
                           0.289501746518
Iteration 540 : error is
                           0.289309833641
Iteration 550 : error is
                           0.289232088086
Iteration
           560 : error is
                           0.289196393759
Iteration
           570 : error is
                           0.289172760524
Iteration 580 : error is
                           0.289156120085
Iteration 590 : error is
                           0.289145558047
                           0.289139461979
Iteration
           600 : error is
                           0.289136053566
Iteration
           610 : error is
Iteration
           620 : error is
                           0.289133758356
Iteration
           630 : error is
                           0.289131829592
                           0.289129966819
Iteration
           640 : error is
Iteration
           650 : error is
                           0.289127996891
           660 : error is
                           0.289125816518
Iteration
Iteration
                           0.289123370645
           670 : error is
Iteration
           680 : error is
                           0.289120634697
Iteration
           690 : error is
                           0.289117594623
Iteration
           700 : error is
                           0.289114238678
Iteration 710 : error is
                           0.289110553792
Iteration
          720 : error is
                           0.28910652488
Iteration 730 : error is
                           0.289102135268
                           0.289097373856
Iteration
          740 : error is
Iteration 750 : error is
                           0.289092309817
Iteration
          760 : error is
                           0.28908688164
           770 : error is
Iteration
                           0.289081014301
Iteration
          780 : error is
                           0.28907467243
          790 : error is
Iteration
                           0.289067824626
Iteration 800 : error is
                           0.289060479403
Iteration 810 : error is
                           0.289052782585
Iteration 820 : error is
                           0.289044693006
Iteration 830 : error is
                           0.28903599914
Iteration 840 : error is
                           0.289026624569
Iteration 850 : error is
                           0.289016910744
Iteration 860 : error is
                           0.289006613117
Iteration 870 : error is
                           0.288995708
Iteration 880 : error is
                           0.288984641153
                           0.288972997685
Iteration 890 : error is
                           0.288960697502
Iteration
           900 : error is
Iteration
           910 : error is
                           0.288947358275
Iteration
           920 : error is
                           0.28893327515
Iteration
           930 : error is
                           0.288918917261
Iteration
           940 : error is
                           0.288904440792
Iteration
           950 : error is
                           0.288889343742
Iteration 960 : error is
                           0.28887319453
```

```
Iteration 970 : error is 0.288855923795
Iteration 980 : error is 0.288838101773
Iteration 990 : error is 0.288819937401
Iteration 1000 : error is 0.288800558712
In [209]: plt.figure()
          cmap = plt.get_cmap('Accent', len(unique_labels))
         plt.scatter(Y[:,0], Y[:,1], 20, c=labels, label=labels, cmap=cmap,
                      vmin=min(unique_labels_values), vmax=max(unique_labels_values)
          cbar = plt.colorbar(ticks=unique_labels_values)
          cbar.ax.set_yticklabels(unique_labels) # horizontal colorbar
          plt.show()
           60
           40
           20
            0
          -20
                                                             2
          -40
```

- 1

-20

0

20

40

-60

-40

bigbar2 4
mixed 3
full 1