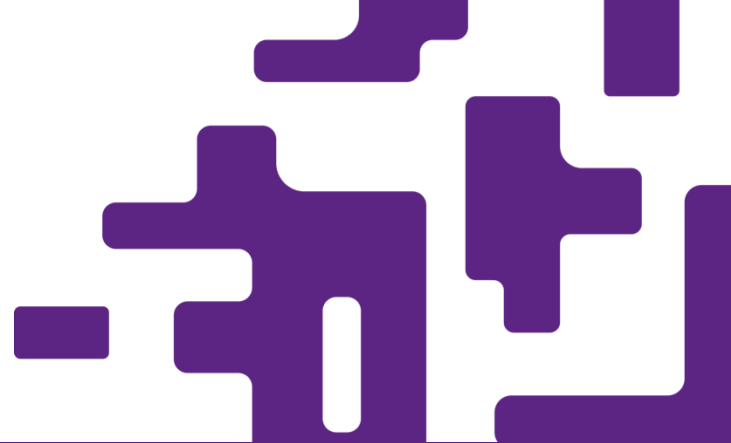




NORMENT

Norwegian Centre for
Mental Disorders Research



Mathematical models of the genetic architecture in complex human disorders

Oleksandr Frei

April 7th 2020

Outline

- **Introduction**
 - NORMENT
 - My background
- **Genetics of Complex Traits**
 - Mendelian vs polygenic inheritance
 - Genome-wide association studies
 - Simple Additive Genetic Model
- **Modeling genetic architecture with MiXeR**
- **MOSTest – multivariate omnibus statistical test**



UiO : **NORMENT: Norwegian Centre for Mental Disorders Research**

Faculty of Medicine

Home

Research

About the centre

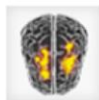
People

Research topics



Genetics

Identify rare genetic variants or expression variation to reveal "missing heritability".



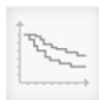
Brain Imaging

Determine new brain imaging phenotypes linking genes and core clinical phenotypes.



Antipsychotic Medication

Define new targets to optimize the ratio of beneficial vs. adverse effects of antipsychotics.



Outcome Predictors

Using genetic and environmental factors to estimate illness course and outcome.



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NORMENT is a Centre of Excellence (CoE) funded by the Research Council of Norway.

Our main goal is to find answers to why some people develop severe mental illness.

[→ Read more about NORMENT](#)

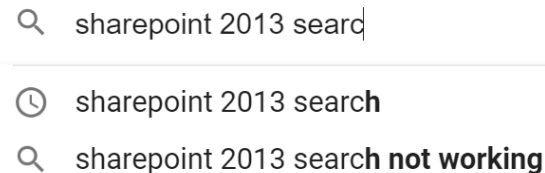
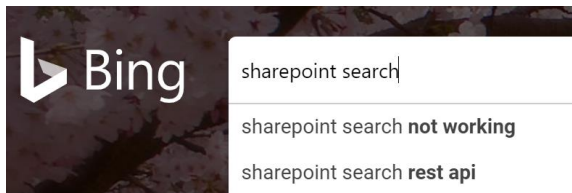
NORMENT in social media

2004 – 2013

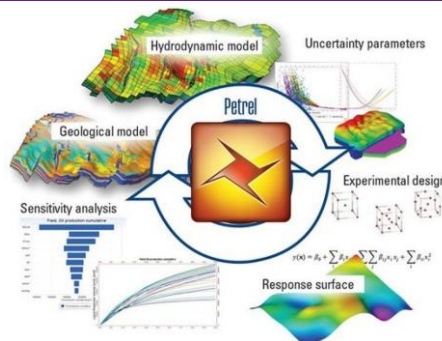
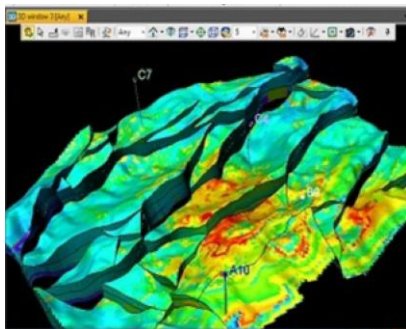


My background

2010 – 2013



2014 – 2016



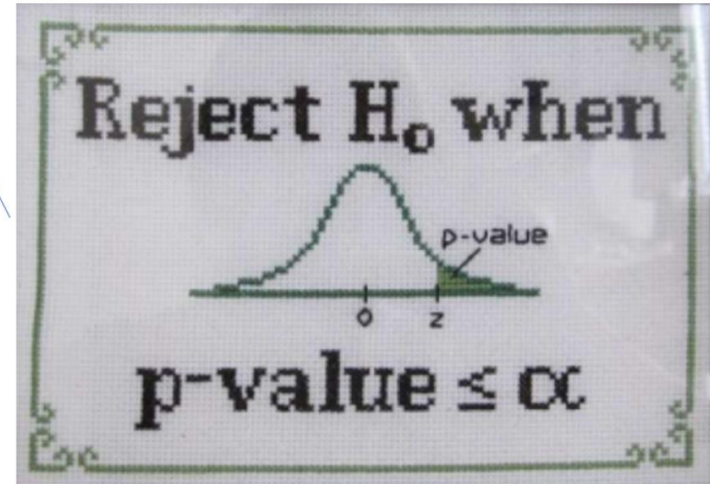
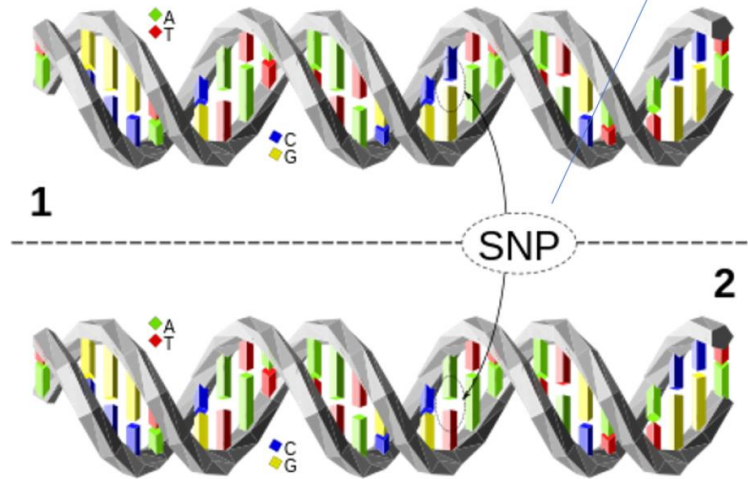
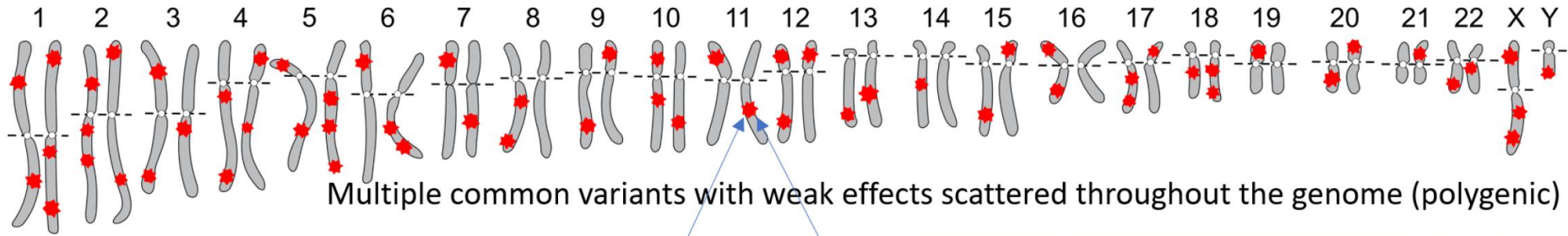
2016 - Today

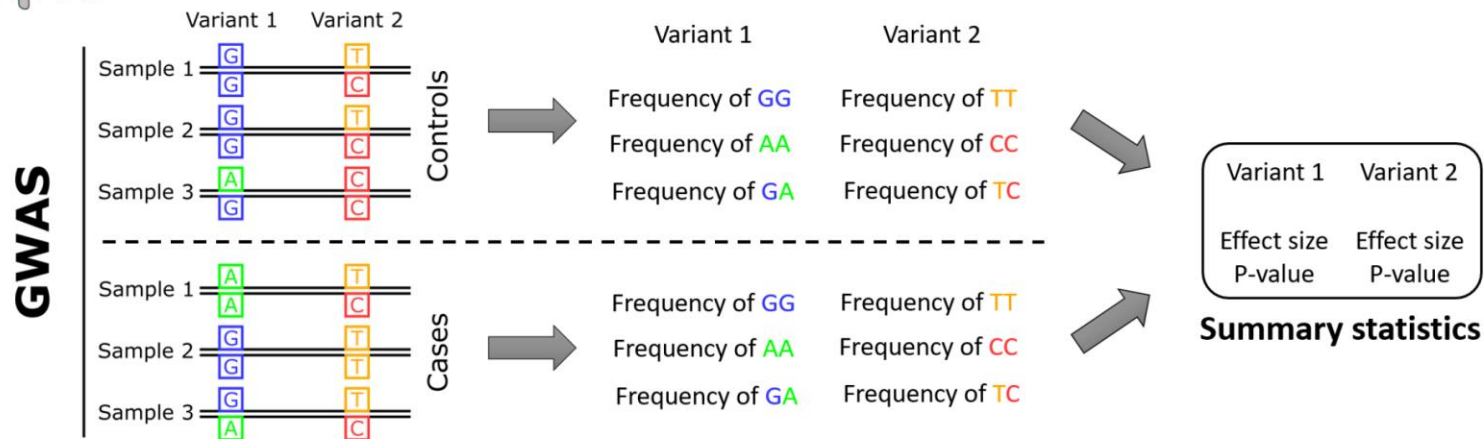
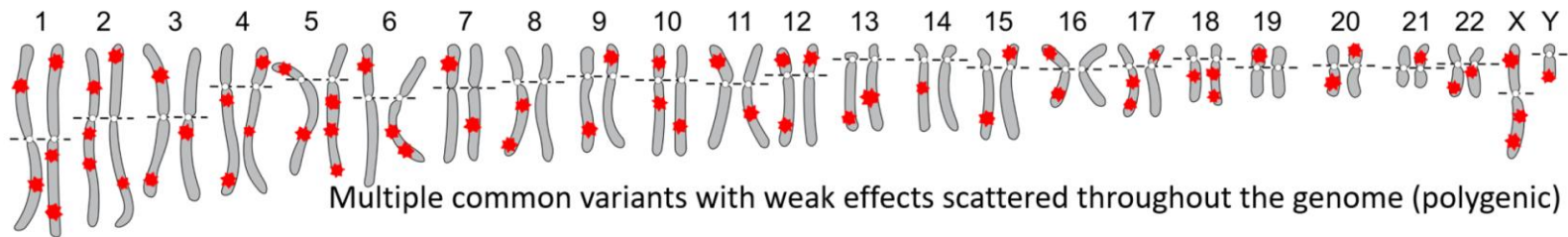


2013-2018
<http://bigartm.org/>



Complex polygenic traits, e.g. height





Think of the naïve bayes classifier

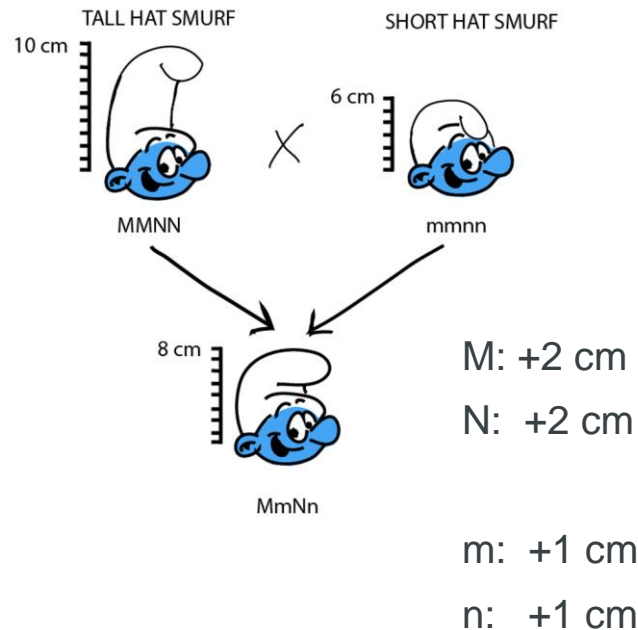
- genetic variants = features
- human trait = output

Simple additive genetic model

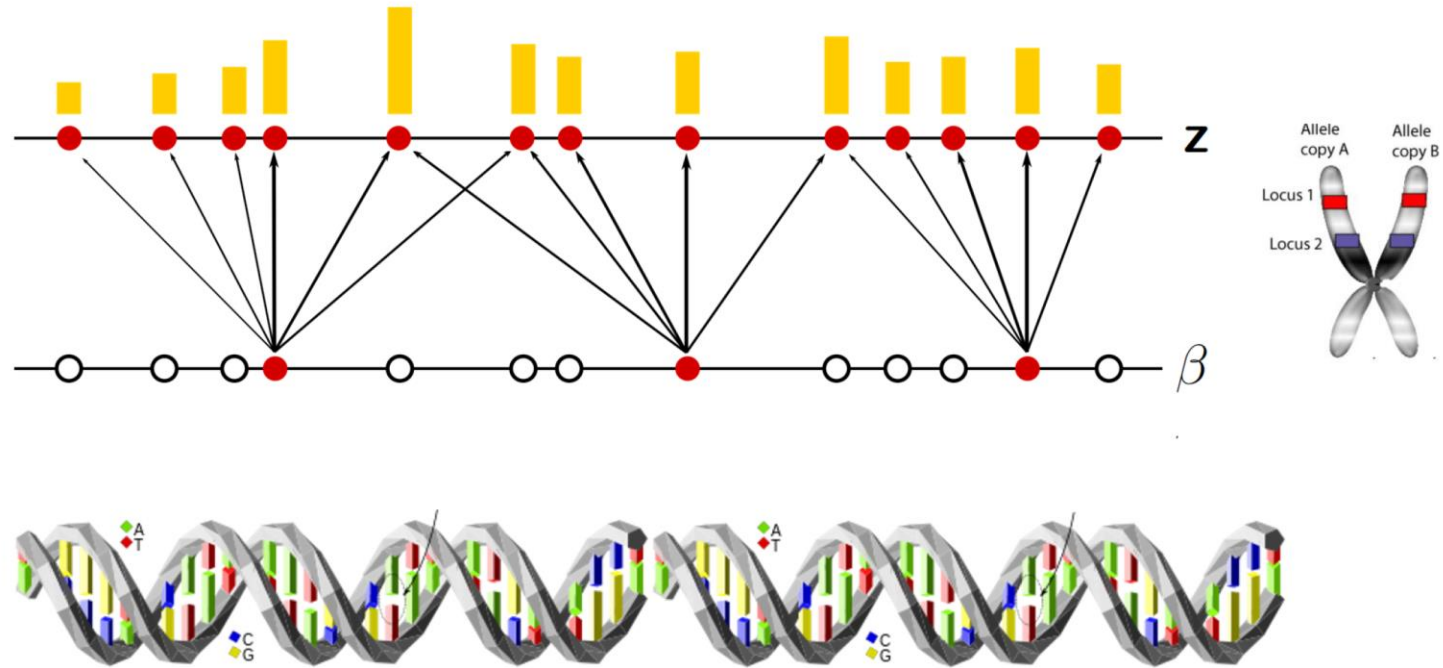
$$y_k = \sum_{i=1}^M g_{ki}\beta_i + e \quad \leftrightarrow \quad \mathbf{y} = \mathbf{G}\boldsymbol{\beta} + \mathbf{e}$$

where

- N - the number of individuals in the dataset
- M - the number of genetic variants
- \mathbf{y} - N -vector, “phenotype” (e.g. human height)
- \mathbf{G} - $N \times M$ -matrix
- $\boldsymbol{\beta}$ - M -vector, genetic effects, random variables
- e - non-genetic effects, random variable
- \mathbf{y} , \mathbf{G} - known; $\boldsymbol{\beta}$, e - unknown



LD: Correlation among genetic features



Causal mixture model

$$\mathbf{y} = \mathbf{G}\beta + \mathbf{e}, \text{ or}$$

$$\mathbf{z} = \mathbf{A}\beta + \epsilon$$

MiXeR:

$$\beta_i \sim (1 - \pi_1)N(0, 0) + \pi_1 N(0, \sigma_\beta^2)$$

where

- π_1 - weight in the mixture
- σ_β^2 - variance
- $N(0, 0)$ - probability mass at zero

Bivariate causal mixture model quantifies polygenic overlap between complex traits beyond genetic correlation

Oleksandr Frei , Dominic Holland, Olav B. Smeland, Alexey A. Shadrin, Chun Chieh Fan, Steffen Maeland, Kevin S. O'Connell, Yunpeng Wang, Srdjan Djurovic, Wesley K. Thompson, Ole A. Andreassen & Anders M. Dale 

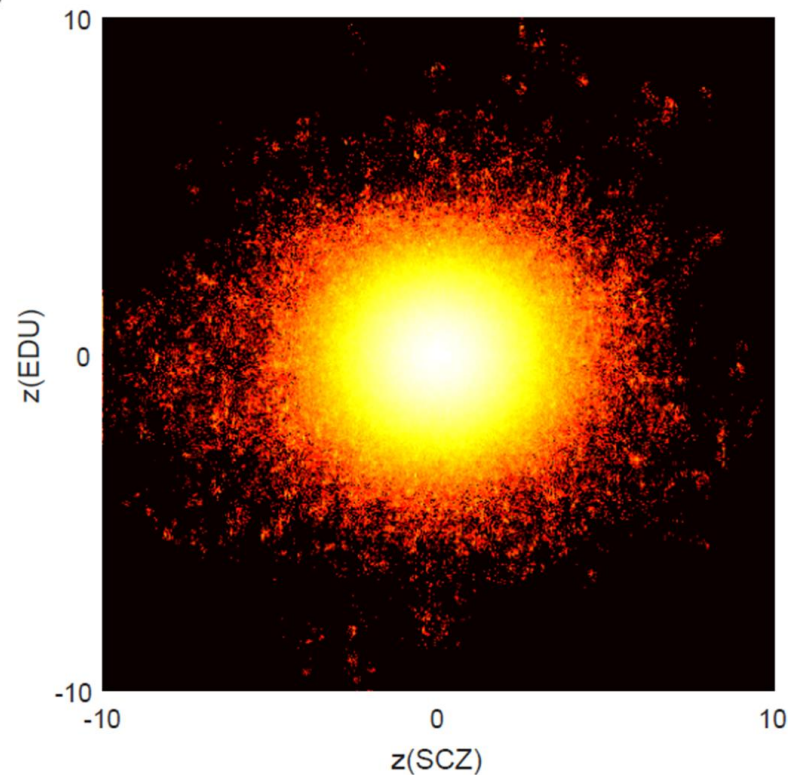
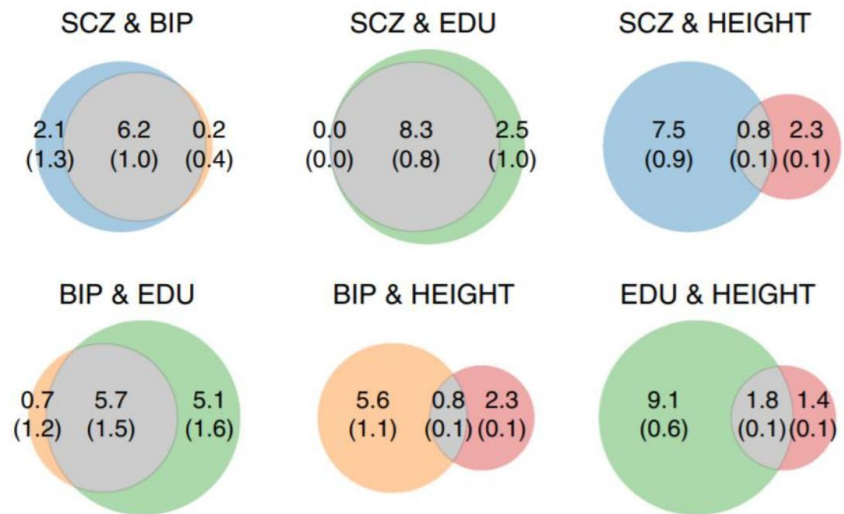
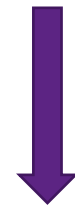
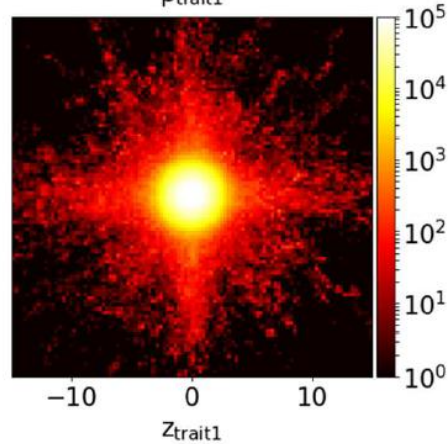
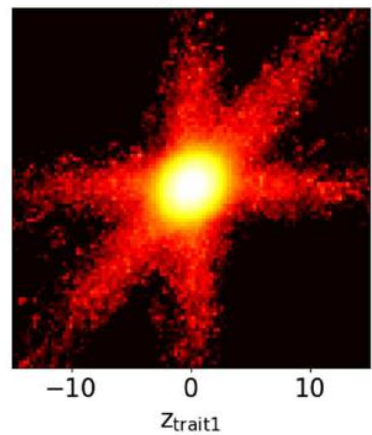
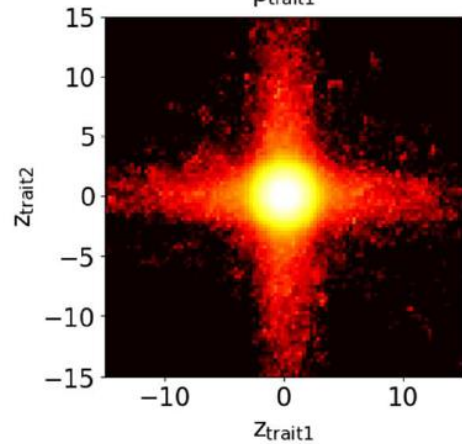
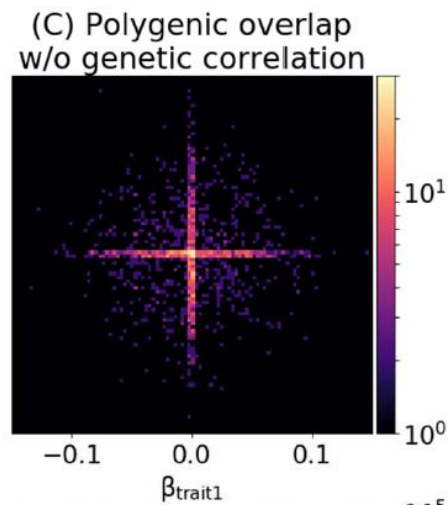
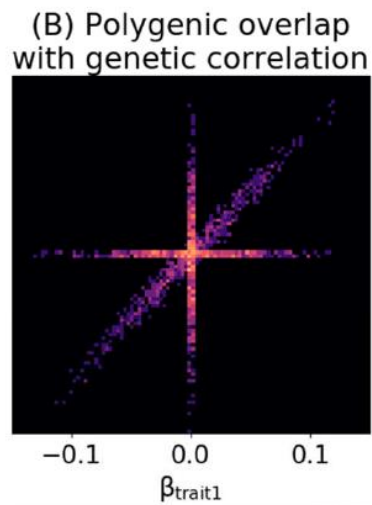
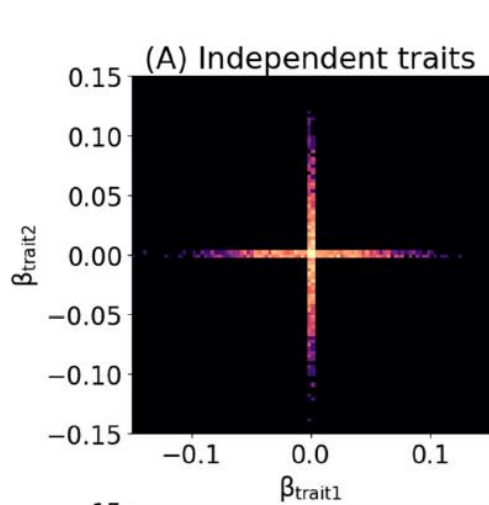
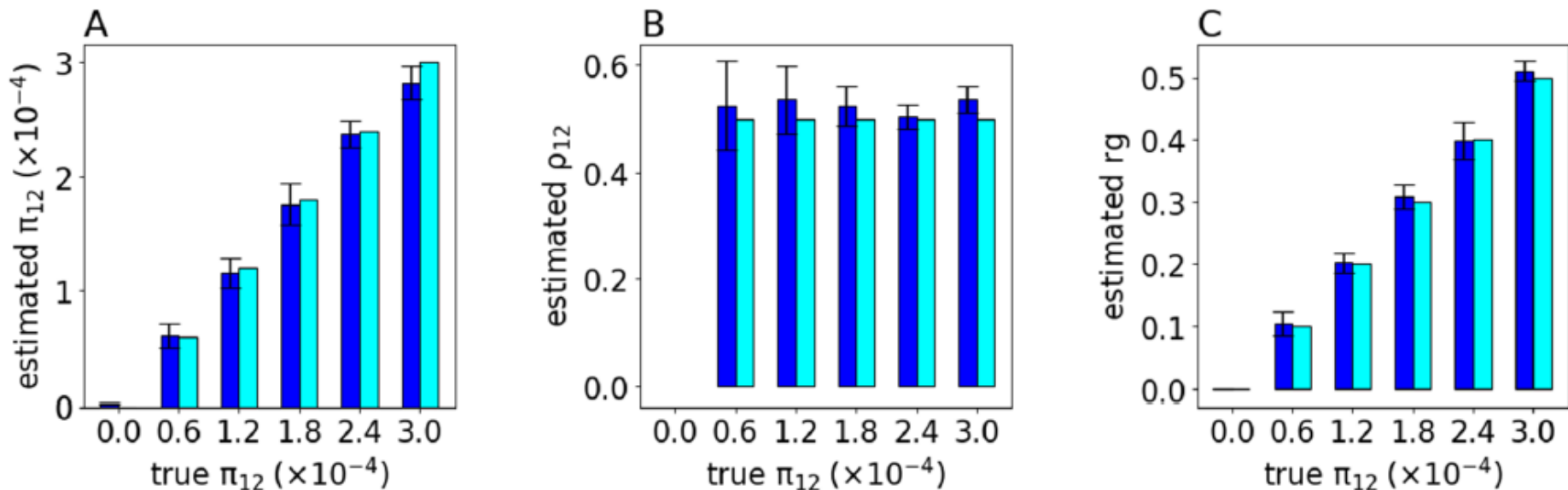


Fig. 3 Venn diagrams of unique and shared polygenic components



Linkage Disequilibrium

Simulations on synthetic data

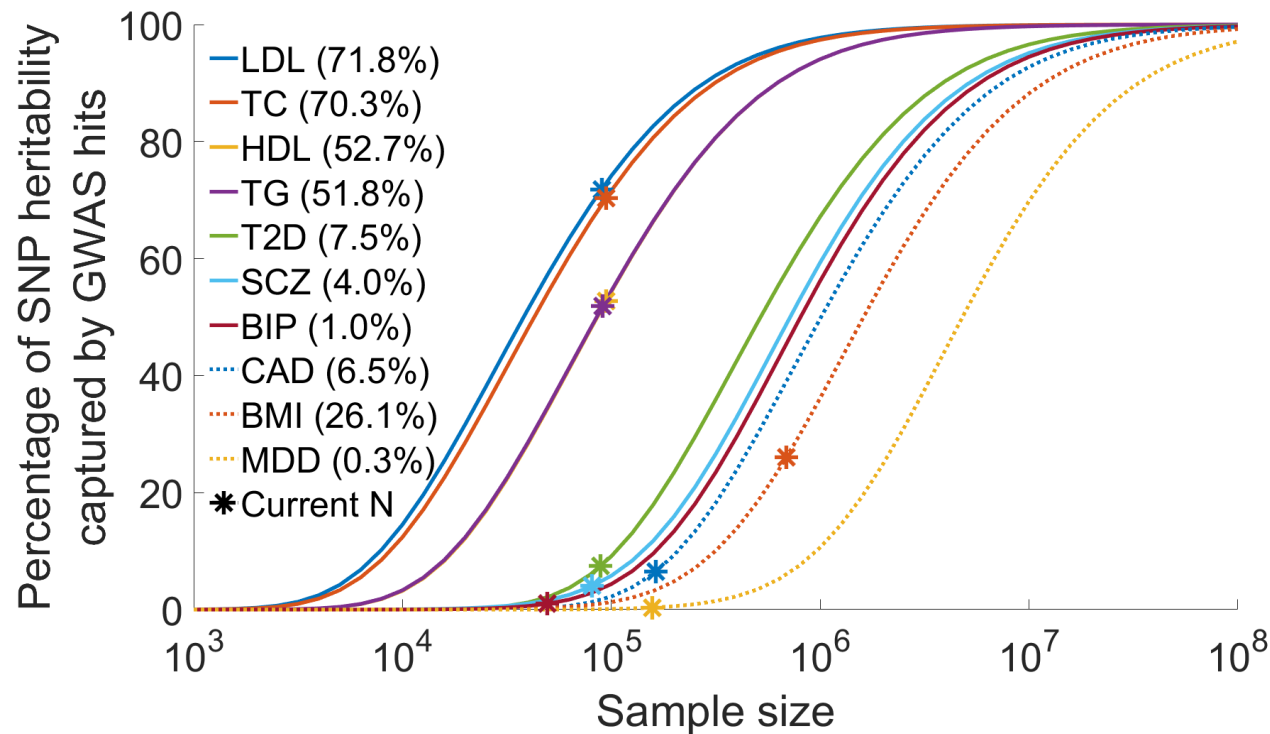


(A) Estimates of polygenic overlap

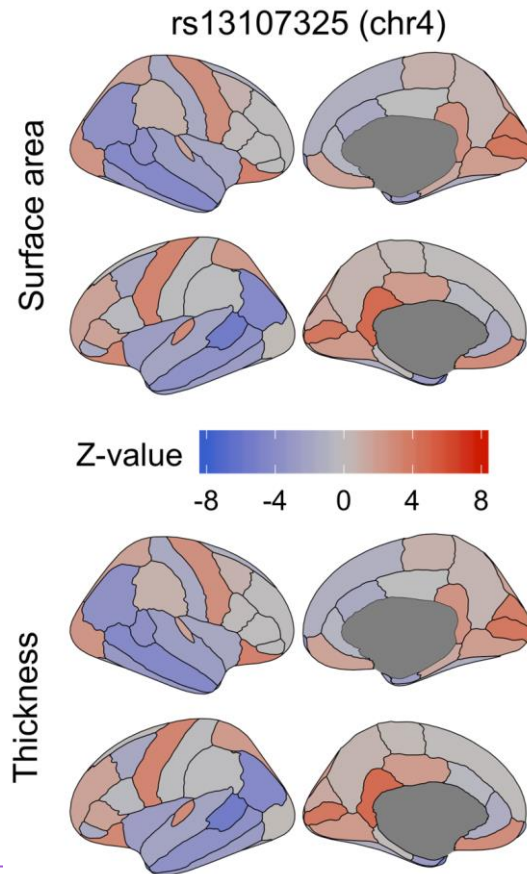
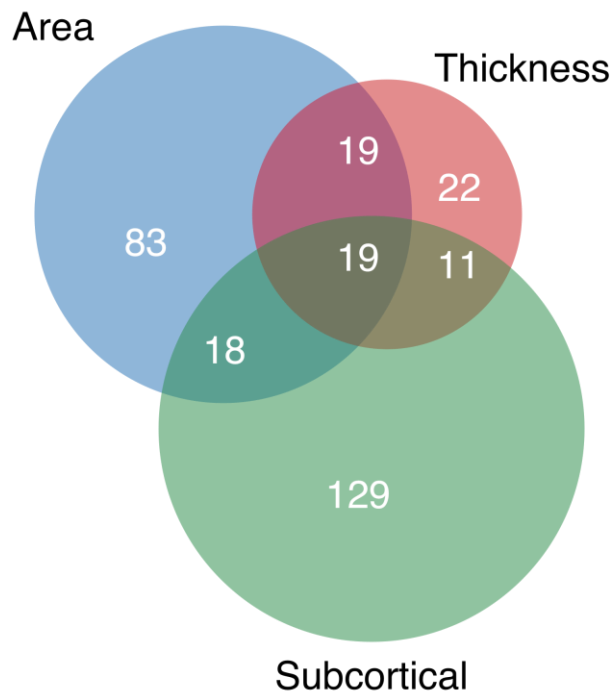
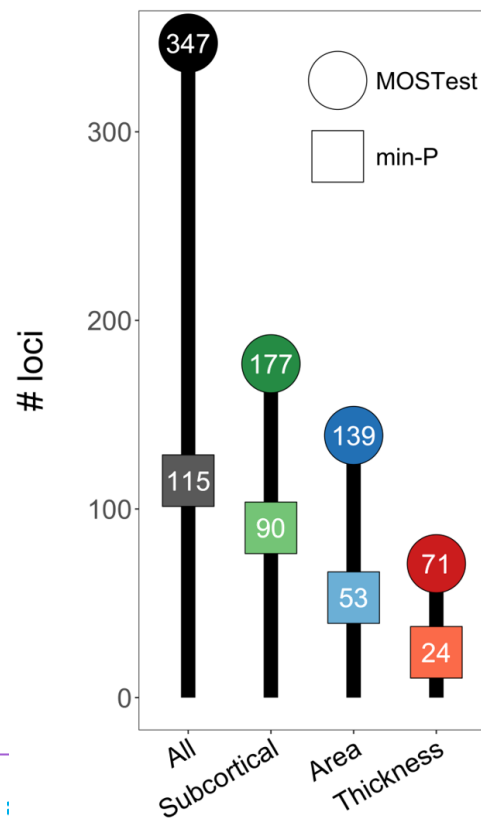
(B) Estimates of correlation of effect sizes in the shared component

(C) Estimates of genetic correlation

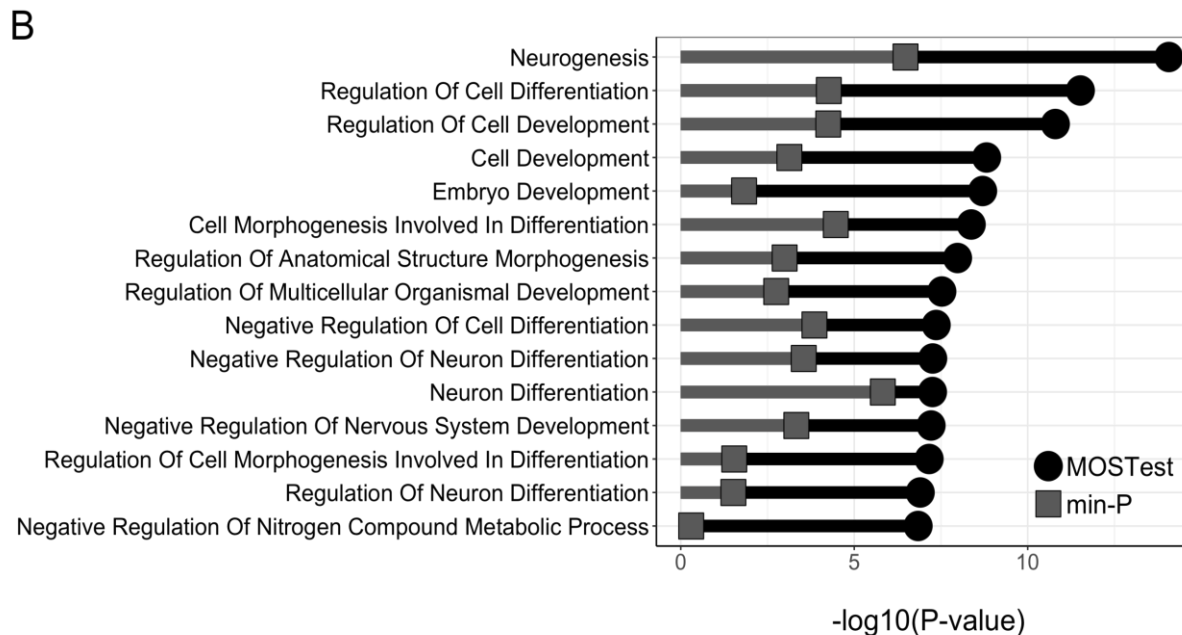
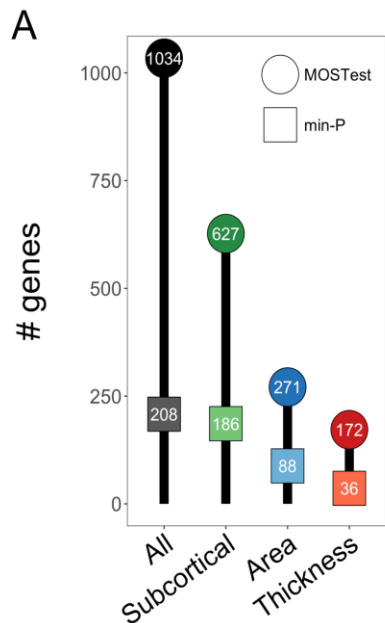
Polygenicity affects power to discover loci in GWAS



MOSTest – increase discovery (Multivariate Omnibus Statistical Test)



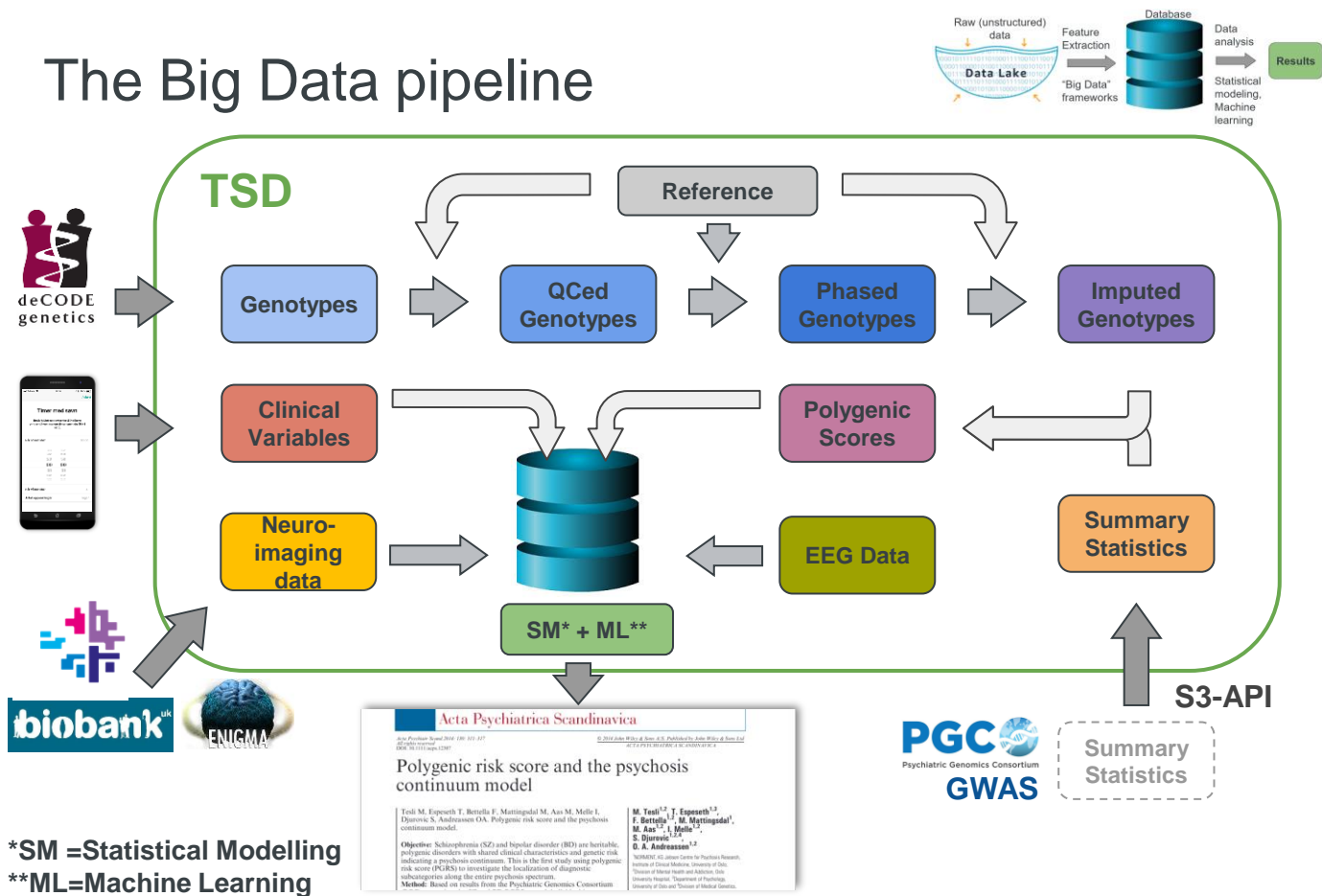
Boost in #genes associated with regional brain morphology



Comparison between tools

	pleioFDR github.com/precimed/pleiofdr	MiXeR github.com/precimed/mixer	MOSTest github.com/precimed/mostest
Input	GWAS sumstats for 2 traits + reference	GWAS sumstats for 2 traits + reference	Raw genotypes + N traits
Output	False Discovery Rate per SNP for each trait: condFDR and conjFDR	Genetic architecture: polygenicity, correlation and polygenic overlap	One P-value per SNP H0: none of the N traits are associated with the SNP
Sample overlap?	MUST NOT overlap	CAN overlap	MUST overlap (single cohort – multiple measures)
Tools that address similar questions	MTAG, pw-gwas, GenomicSEM	LDSR, HESS, GenomicSEM (cross-trait analysis) BayesS, RSS, Genesis (causal mixture model)	MV-PLINK, TATES, MultiPHEN, MultiABEL, MANOVA

The Big Data pipeline



*SM =Statistical Modelling
**ML=Machine Learning

Acknowledgement

Study participants

NORMENT part UiO

- Ole Andreassen
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- Lars Westley
- Alexey Shadrin
- Francesco Bettella
- Kevin O'Connell
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- Tobias Kaufmann
- Olav B. Smeland

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Mental Disorders Research

Thank you

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