XCPC - Templates

north-h

Contents

1	数据	结构	2
	1.1	树状数组(单点修改,区间查询)	2
	1.2	树状数组(区间修改,单点查询)	2
	1.3	树状数组(区间修改,区间查询)	2
	1.4	线段树(朴素)	3
	1.5	线段树 (lazy)	4
	1.6	ST 表	6
	1.7	二维树状数组	7
2	字符串 7		
	2.1	单哈希	7
	2.2	双哈希	8
	2.3	自然溢出	8
	2.4	字典树	8
	2.5	马拉车	9
	2.6	正反哈希	10
3	杂项		10
	3.1	· 快读快写	10
	3.2	取模	11

SMU 第2页

1 数据结构

1.1 树状数组(单点修改,区间查询)

```
1
    template <class T>
 2
    struct BIT {
 3
       vector<T> tr;
 4
       int n;
 5
       BIT(int n) : n(n), tr(n) {}
       void add(int x, T k) {
 6
 7
           for(int i = x; i < n; i += (i & -i))</pre>
 8
              tr[i] += k;
 9
       }
10
       T query(int x) {
           T res = 0;
11
12
           for(int i = x; i; i -= (i & -i))
13
              res += tr[i];
14
           return res;
15
       }
16
       T range_query(int 1, int r) {
17
           return query(r) - query(l - 1);
18
       }
19
    };
```

1.2 树状数组(区间修改,单点查询)

```
template <class T>
1
 2
    struct BIT {
 3
       vector<T> tr;
 4
       int n;
 5
       BIT(int n) : n(n), tr(n), {}
 6
       void add(int x, T k) {
 7
           for(int i = x; i < n; i += (i & -i))</pre>
 8
              tr[i] += k;
 9
       }
10
       void range_add(int 1, int r) {
11
           add(1, k);
12
           add(r + 1, -k);
13
       }
14
       T query(int x) {
15
           T res = 0;
           for(int i = x; i; i -= (i & -i))
16
17
              res += tr[i];
18
           return res;
       }
19
20
    };
```

1.3 树状数组(区间修改,区间查询)

```
1 template <class T>
2 struct BIT {
```

SMU 第3页

```
3
       vector<T> sum1, sum2;
 4
       int n;
 5
       BIT(int n) : n(n), sum1(n + 1), sum2(n + 1) {}
 6
       void add(int x, T k) {
 7
           for(int i = x; i <= n; i += (i & -i))</pre>
              sum1[i] += k, sum2[i] += x * k;
 8
 9
10
       void range_add(int 1, int r, T x) {
           add(1, x), add(r + 1, -x);
11
12
13
       T query(int x) {
14
           T res = 0;
15
           for(int i = x; i > 0; i -= (i \& -i))
              res += (x + 1) * sum1[i] - sum2[i];
16
17
           return res;
18
       }
19
       T range_query(int 1, int r) {
20
           return query(r) - query(l - 1);
21
22
       }
23
    };
```

1.4 线段树(朴素)

```
1
    template<class T>
 2
    struct SegmentTree {
 3
       struct Node {
           int 1, r;
 4
 5
           T sum, lazy;
 6
       };
 7
 8
       vector<Node> tr;
9
       vector<T> a;
10
       SegmentTree(const vector<T> &arr, const int n) {
11
12
           tr.resize(n * 4);
13
           a = arr;
           build(1, 1, n);
14
15
       }
16
       void pushup(int u) {
17
18
           tr[u].sum = tr[u << 1].sum + tr[u << 1 | 1].sum;
19
20
21
       void pushdown(int u) {
22
           if (tr[u].lazy) {
              tr[u << 1].sum += tr[u].lazy * (tr[u << 1].r - tr[u << 1].l + 1);
23
              tr[u << 1 | 1].sum += tr[u].lazy * (tr[u << 1 | 1].r - tr[u << 1 | 1].l +
24
                  1);
25
              tr[u << 1].lazy += tr[u].lazy;</pre>
              tr[u << 1 | 1].lazy += tr[u].lazy;</pre>
26
27
              tr[u].lazy = 0;
```

SMU 第4页

```
28
           }
29
        }
30
        void build(int u, int l, int r) {
31
32
           tr[u] = {1, r, a[1], 0};
33
           if (1 == r)return;
34
           int mid = l + r \gg 1;
35
           pushdown(u);
           build(u << 1, 1, mid);</pre>
36
37
           build(u << 1 | 1, mid + 1, r);
38
           pushup(u);
39
        }
        //区间修改
40
41
        void modify(int u, int l, int r, int k) {
42
           if (tr[u].l >= l && tr[u].r <= r) {</pre>
43
               tr[u].sum += (tr[u].r - tr[u].l + 1) * k;
44
               tr[u].lazy += k;
45
               return;
46
           }
47
           pushdown(u);
48
           int mid = tr[u].l + tr[u].r >> 1;
49
           if (1 <= mid)modify(u << 1, 1, r, k);</pre>
50
           if (r > mid) modify(u << 1 | 1, 1, r, k);</pre>
51
           pushup(u);
52
        }
        //单点修改
53
54
        void modify(int u, int x, int k) {
55
           if (tr[u].l == tr[u].r) {
56
               tr[u].sum += k;
57
               return;
58
           }
59
           int mid = tr[u].l + tr[u].r >> 1;
           if (x \leftarrow mid)modify(u \leftarrow 1, x, k);
60
61
           else modify(u \langle\langle 1 | 1, x, k \rangle\rangle;
        }
62
63
        //区间查询
64
        T query(int u, int 1, int r) {
           if (tr[u].l >= l && tr[u].r <= r) return tr[u].sum;</pre>
65
           pushdown(u);
66
67
           int sum = 0;
68
           int mid = tr[u].l + tr[u].r >> 1;
69
           if (1 <= mid)sum += query(u << 1, 1, r);</pre>
70
           if (r > mid) sum += query(u << 1 | 1, 1, r);
71
           return sum;
72
        }
73
    };
```

1.5 线段树 (lazy)

```
template < class T>
template < class T>
struct SegmentTree {
struct Node {
```

SMU 第5页

```
4
           int 1, r;
 5
           T sum, lazy;
 6
       };
 7
 8
       vector<Node> tr;
 9
       vector<T> a;
10
11
       SegmentTree(const vector<T> &arr, const int n) {
           tr.resize(n * 4);
12
13
           a = arr;
14
           build(1, 1, n);
15
        }
16
17
       void pushup(int u) {
18
           tr[u].sum = tr[u << 1].sum + tr[u << 1 | 1].sum;
19
       }
20
21
       void pushdown(int u) {
22
           if (tr[u].lazy) {
              tr[u << 1].sum += tr[u].lazy * (tr[u << 1].r - tr[u << 1].l + 1);
23
24
              tr[u << 1 \mid 1].sum += tr[u].lazy * (tr[u << 1 \mid 1].r - tr[u << 1 \mid 1].l +
                   1);
25
              tr[u << 1].lazy += tr[u].lazy;</pre>
26
              tr[u << 1 | 1].lazy += tr[u].lazy;</pre>
27
              tr[u].lazy = 0;
28
           }
29
        }
30
       void build(int u, int l, int r) {
31
32
           tr[u] = {1, r, a[1], 0};
33
           if (1 == r) return;
           int mid = l + r \gg 1;
34
35
           pushdown(u);
36
           build(u << 1, 1, mid);
           build(u << 1 | 1, mid + 1, r);
37
38
           pushup(u);
39
40
41
       void modify(int u, int l, int r, T k) {
42
           if (tr[u].1 >= 1 && tr[u].r <= r) {</pre>
               tr[u].sum += (tr[u].r - tr[u].l + 1) * k;
43
44
               tr[u].lazy += k;
45
               return;
46
47
           pushdown(u);
48
           int mid = tr[u].l + tr[u].r >> 1;
           if (1 <= mid) modify(u << 1, 1, r, k);</pre>
49
50
           if (r > mid) modify(u << 1 | 1, 1, r, k);</pre>
51
           pushup(u);
52
        }
53
54
       T query(int u, int l, int r) {
55
           if (tr[u].1 >= 1 && tr[u].r <= r) return tr[u].sum;</pre>
```

SMU 第6页

```
pushdown(u);

T sum = 0;

int mid = tr[u].l + tr[u].r >> 1;

if (l <= mid) sum += query(u << 1, 1, r);

if (r > mid) sum += query(u << 1 | 1, 1, r);

return sum;

};

};</pre>
```

1.6 ST 表

```
1
    template<class T>
 2
    struct RMQ {
 3
       Tn;
 4
       vector<T> arr;
 5
       vector<vector<T>> f, g;
 6
       vector<int> lg2;
 7
       RMQ(const vector<T> &a) :
           n(a.size()), arr(a),
 8
 9
           f(n, vector<T>(log2(n) + 1)),
10
           g(n, vector<T>(log2(n) + 1)),
11
           lg2(n + 1) {
12
           init();
13
       void init() {
14
15
           lg2[0] = -1;
16
           for(int i = 1; i <= n; i ++)</pre>
              lg2[i] = lg2[i >> 1] + 1;
17
18
           for (int i = 0; i < n; i++) {</pre>
19
              f[i][0] = arr[i];
20
              g[i][0] = arr[i];
21
           }
22
           for (int j = 1; (1 << j) <= n; j++) {
23
              for (int i = 0; i + (1 << j) - 1 < n; i++) {
                  f[i][j] = max(f[i][j - 1], f[i + (1 << (j - 1))][j - 1]);
24
25
                  g[i][j] = min(g[i][j - 1], g[i + (1 << (j - 1))][j - 1]);
26
              }
27
           }
28
       }
29
30
       T query_max(int 1, int r) {
31
           int k = \lg 2[r - l + 1];
32
           return max(f[1][k], f[r - (1 << k) + 1][k]);
33
       }
34
35
       T query_min(int 1, int r) {
36
           int k = \lg 2[r - l + 1];
           return min(g[1][k], g[r - (1 << k) + 1][k]);
37
38
       }
39
    };
```

SMU 第7页

1.7 二维树状数组

```
template <class T>
 2
    struct BIT_2D {
 3
       vector<vector<T>> tr;
 4
       int n, m;
 5
 6
       BIT_2D(int n, int m) : n(n), m(m), tr(n + 1, vector<T>(m + 1)) {}
 7
 8
       int lowbit(int x) { return x & (-x); }
 9
10
       void add(int x, int y, T k) {
11
           for (int i = x; i <= n; i += lowbit(i))</pre>
              for (int j = y; j <= m; j += lowbit(j))</pre>
12
13
                  tr[i][j] += k;
14
       }
15
16
       T query(int x, int y) {
17
           T res = 0;
18
           for (int i = x; i; i -= lowbit(i))
              for (int j = y; j; j -= lowbit(j))
19
20
                  res += tr[i][j];
21
           return res;
22
       }
23
24
       T query(int x1, int y1, int x2, int y2) {
25
           return query(x2, y2) - query(x2, y1-1) - query(x1-1, y2) + query(x1-1, y1-1);
26
       }
27
   };
```

2 字符串

2.1 单哈希

```
template<class T, int P, int mod>
 2
    struct Hash {
 3
       vector<T> p, h;
 4
       string s;
 5
       Hash(const string &str) :
           s(" " + str),
 6
 7
           p(str.size() + 1) {
 8
           p[0] = 1;
9
           for (int i = 1; i < s.size(); i++) {</pre>
10
              p[i] = (p[i - 1] * P) \% mod;
              h[i] = (h[i - 1] * P + s[i]) \% mod;
11
           }
12
13
       }
14
       T get(int 1, int r) {
           return (h[r] - h[l - 1] * p[r - l + 1] % mod + mod) % mod;
15
16
       }
17
   };
```

SMU 第8页

2.2 双哈希

```
template<class T, int P1, int mod1, int P2, int mod2>
 2
    struct Hash {
 3
       vector<T> p1, p2, h1, h2;
 4
       string s;
       Hash(const string &str) :
 5
          s("" + str),
 6
 7
          p1(str.size() + 1),
 8
          h1(str.size() + 1),
9
          p2(str.size() + 1),
10
          h2(str.size() + 1) {
          p1[0] = p2[0] = 1;
11
12
          for (int i = 1; i < s.size(); i++) {</pre>
              p1[i] = (p1[i - 1] * P1) \% mod1;
13
              h1[i] = (h1[i - 1] * P1 % mod1 + s[i]) % mod1;
14
              p2[i] = (p2[i - 1] * P2) \% mod2;
15
              h2[i] = (h2[i - 1] * P2 \% mod2 + s[i]) \% mod2;
16
17
          }
       }
18
19
20
       T get1(int l, int r) {
          return (h1[r] - (h1[l - 1] * p1[r - l + 1] % mod1) + mod1) % mod1;
21
22
23
24
       T get2(int 1, int r) {
25
           return (h2[r] - (h2[1 - 1] * p2[r - 1 + 1] % mod2) + mod2) % mod2;
26
       }
27
   };
```

2.3 自然溢出

```
1
    template<class T, int P>
 2
    struct Hash {
 3
       vector<T> p, h;
 4
       string s;
 5
       Hash(const string &str) : s(" " + str), p(str.size() + 1) {
 6
           p[0] = 1;
 7
           for (int i = 1; i < s.size(); i++) {</pre>
 8
              p[i] = p[i - 1] * P;
 9
              h[i] = h[i - 1] * P + s[i];
10
           }
11
12
       T get(int 1, int r) {
13
           return h[r] - h[l - 1] * p[r - l + 1];
14
       }
15
   |};
```

2.4 字典树

```
1 template<class T>
```

SMU 第9页

```
struct Trie {
2
 3
       T idx = 0;
 4
       vector<vector<T>> s;
 5
       vector<T>cnt;
 6
       Trie(T n): cnt(n, 0), s(n, vector<T>(26, 0)) {}
 7
       void insert(string str) {
 8
           T p = 0;
 9
           for (int i = 0; i < str.size(); i++) {</pre>
              T u = str[i] - 'a';
10
11
              if (!s[p][u]) s[p][u] = ++idx;
12
              p = s[p][u];
13
14
           cnt[p]++;
15
       }
16
17
       T query(string str) {
18
           T p = 0;
19
           for (int i = 0; i < str.size(); i++) {</pre>
20
              T u = str[i] - 'a';
21
              if (!s[p][u]) return 0;
22
              p = s[p][u];
23
           }
24
           return cnt[p];
25
       }
26
   };
```

2.5 马拉车

```
1
    template <class T>
    struct Manacher {
 3
       vector<T> d;
 4
       string str = "$#";
 5
       Manacher(string s) : d((s.size() + 1) * 2) {
 6
           for(auto i : s) {
 7
               str += i;
               str += '#';
 8
 9
           }
10
           d[1] = 1;
11
           for(int i = 2, 1, r = 1; i < str.size(); i++) {</pre>
12
              if(i <= r)d[i] = min(d[r + l - i], r - i + 1);</pre>
13
              while(str[i - d[i]] == str[i + d[i]])d[i]++;
14
              if(i + d[i] - 1 > r)l = i - d[i] + 1, r = i + d[i] - 1;
15
           }
16
       }
17
       T query() {
18
19
           T len = 0;
20
           for(auto i : d)len = max(len, i);
           return len - 1;
21
22
        }
23
    };
```

SMU 第 10 页

2.6 正反哈希

```
template <class T, int P, int mod>
 2
    struct Palin {
 3
       vector<T> pre, suf, p;
 4
       string str = "$#";
 5
       T n;
 6
       Palin(const string &s) {
 7
           for(auto i : s) {
 8
              str += i;
              str += '#';
 9
10
           }
          n = (int)str.size() - 1;
11
12
          // pre((s.size() + 1) * 2),
          // suf((s.size() + 1) * 2),
13
14
          // p((s.size() + 1) * 2)
15
          pre(n + 1), suf(n + 1), p(n + 1);
          p[0] = 1;
16
           for(int i = 1, j = n; i <= n; i++, j--) {</pre>
17
              pre[i] = (pre[i - 1] * P % mod + str[i]) % mod;
18
              suf[i] = (suf[i - 1] * P % mod + str[j]) % mod;
19
20
              p[i] = p[i - 1] * P \% mod;
21
           }
22
23
       }
24
25
       T get(T h[], int l, int r) {
26
          return (h[r] - h[l - 1] * p[r - l + 1] % mod + mod) % mod;
27
28
       bool query(int 1, int r) {
29
30
          T x = get(pre, 1, r);
           T y = get(suf, n + 1 - r, n + 1 - 1);
31
32
          if(x == y)return true;
33
          return false;
34
       }
35
    };
```

3 杂项

3.1 快读快写

```
inline int read() {
1
2
      int x = 0;
3
      char ch = getchar();
      while (ch < '0' || ch > '9') ch = getchar();
4
5
      while (ch >= '0' && ch <= '9')x = (x << 3) + (x << 1) + ch - '0', ch = getchar()
          ;
      return x;
6
7
8
  inline void write(int x) {
      if (x < 0) putchar('-'), x = -x;
```

SMU 第 11 页

```
10     if (x > 9) write(x / 10);
11     putchar(x % 10 + '0');
12  }
```

3.2 取模

```
1
    template<const int T>
 2
    struct ModInt {
 3
       const static int mod = T;
 4
       int x;
 5
       ModInt(int x = 0) : x(x \% mod) \{ \}
 6
       ModInt(long long x) : x(int(x % mod)) {}
 7
       int val() {
 8
          return x;
 9
10
       ModInt operator + (const ModInt &a) const {
11
           int x0 = x + a.x;
12
           return ModInt(x0 < mod ? x0 : x0 - mod);</pre>
13
14
       ModInt operator - (const ModInt &a) const {
15
          int x0 = x - a.x;
           return ModInt(x0 < 0 ? x0 + mod : x0);
16
17
       ModInt operator * (const ModInt &a) const {
18
          return ModInt(1LL * x * a.x % mod);
19
20
21
       ModInt operator / (const ModInt &a) const {
          return *this * a.inv();
22
23
24
       bool operator == (const ModInt &a) const {
25
           return x == a.x;
26
       };
27
       bool operator != (const ModInt &a) const {
28
          return x != a.x;
29
       };
30
       void operator += (const ModInt &a) {
31
           x += a.x;
32
           if (x >= mod) x -= mod;
33
34
       void operator -= (const ModInt &a) {
35
          x -= a.x;
36
          if (x < 0) x += mod;
37
38
       void operator *= (const ModInt &a) {
          x = 1LL * x * a.x % mod;
39
40
       void operator /= (const ModInt &a) {
41
42
           *this = *this / a;
43
44
       friend ModInt operator + (int y, const ModInt &a) {
45
          int x0 = y + a.x;
46
          return ModInt(x0 < mod ? x0 : x0 - mod);</pre>
```

SMU 第 12 页

```
47
       friend ModInt operator - (int y, const ModInt &a) {
48
           int x0 = y - a.x;
49
50
          return ModInt(x0 < 0 ? x0 + mod : x0);
51
       friend ModInt operator * (int y, const ModInt &a) {
52
53
          return ModInt(1LL * y * a.x % mod);
54
       }
55
       friend ModInt operator / (int y, const ModInt &a) {
56
          return ModInt(y) / a;
57
       }
       friend ostream &operator<<(ostream &os, const ModInt &a) {</pre>
58
59
          return os << a.x;</pre>
60
       }
       friend istream &operator>>(istream &is, ModInt &t) {
61
62
          return is >> t.x;
63
       }
64
65
       ModInt pow(int64_t n) const {
          ModInt res(1), mul(x);
66
67
          while(n) {
              if (n & 1) res *= mul;
68
              mul *= mul;
69
70
              n >>= 1;
          }
71
72
          return res;
73
       }
74
75
       ModInt inv() const {
76
           int a = x, b = mod, u = 1, v = 0;
          while (b) {
77
78
              int t = a / b;
79
              a -= t * b;
80
              swap(a, b);
              u -= t * v;
81
82
              swap(u, v);
83
84
           if (u < 0) u += mod;
85
          return u;
86
       }
87
88
    };
   using mint = ModInt<998244353>;
```