

# Øving1

September 10, 2023

## 1 Øving 1

### 1.1 Oppgave 2

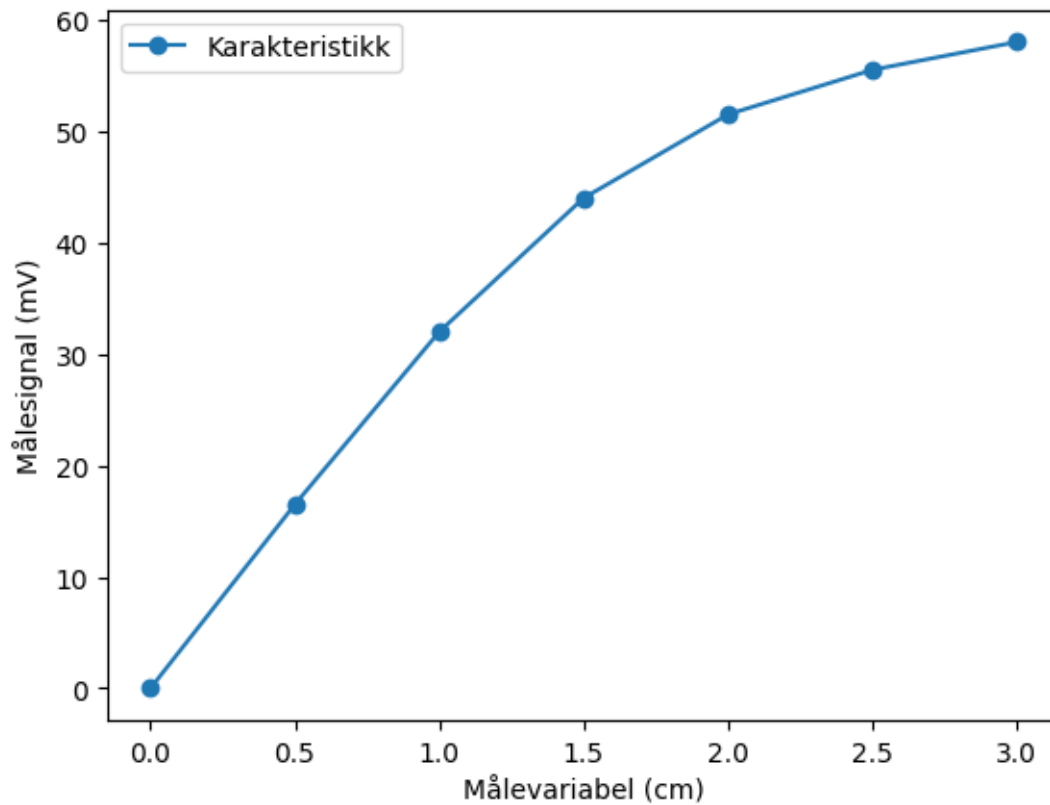
#### 1.1.1 a)

```
[ ]: import numpy as np
import matplotlib.pyplot as plt
import uncertainties as unc
```

```
[ ]: xs = [0.0, 0.5, 1.0, 1.5, 2.0, 2.5, 3.0]
ys = [0.0, 16.5, 32.0, 44.0, 51.5, 55.5, 58.0]
```

```
[ ]: def plot_characteristic():
    plt.plot(xs, ys, "-o", label="Karakteristikk")
    plt.xlabel('Målevariabel (cm)')
    plt.ylabel('Målesignal (mV)')
```

```
[ ]: plot_characteristic()
plt.legend()
plt.show()
```



### 1.1.2 b)

```
[ ]: min_x = xs[0]
      max_x = xs[-1]

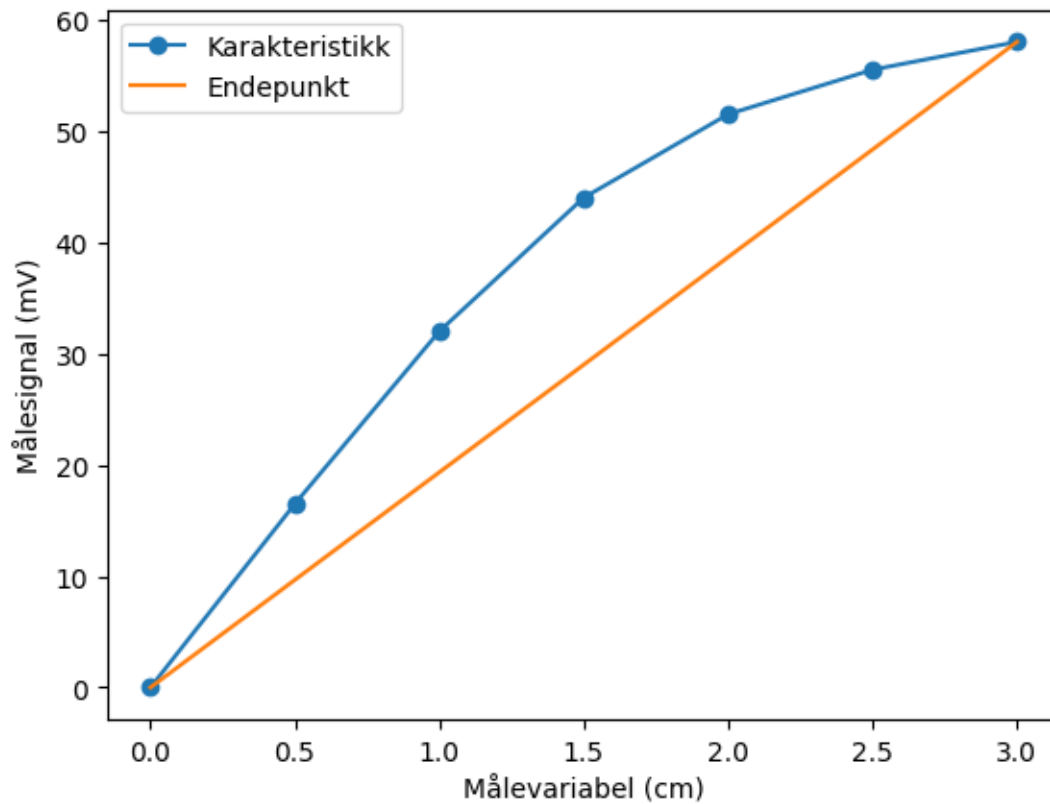
      min_y = ys[0]
      max_y = ys[-1]

      def f_endpoint(x):
          a = (max_y - min_y) / (max_x - min_x)
          b = min_y - a * min_x
          return a * x + b

      def plot_endpoints():
          xs = np.linspace(min_x, max_x, 10)
          ys = f_endpoint(xs)
          plt.plot(xs, ys, label="Endepunkt")
```

```
[ ]: plot_characteristic()
      plot_endpoints()
      plt.legend()
```

```
plt.show()
```



```
[ ]: print("a = ", (max_y - min_y) / (max_x - min_x))
```

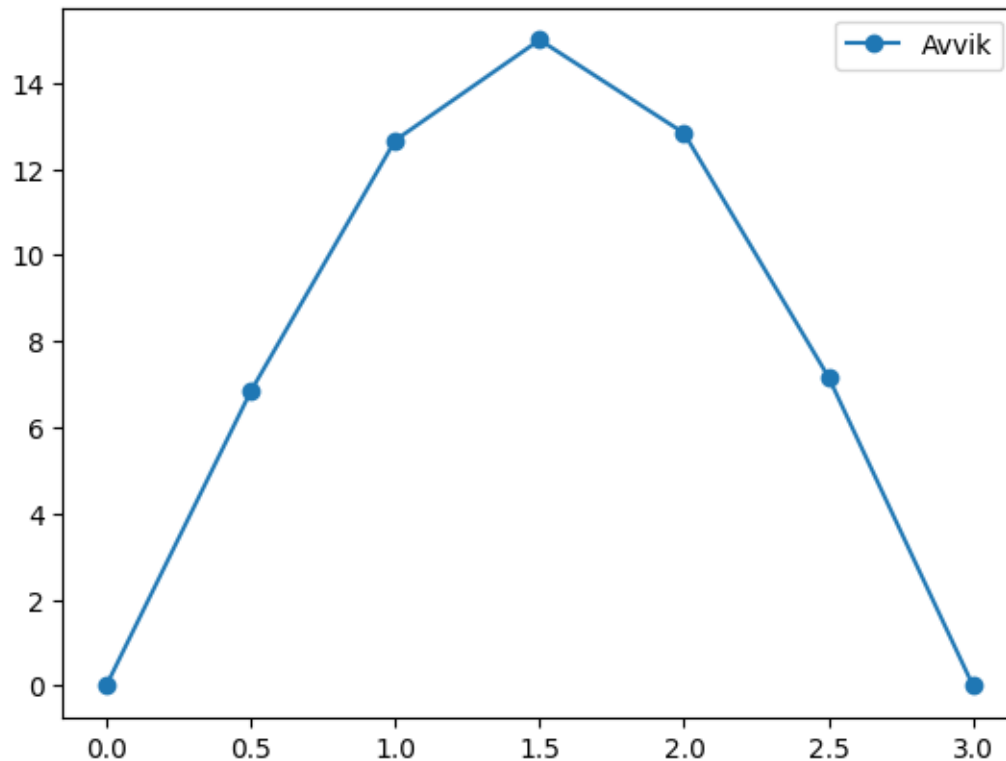
```
a = 19.333333333333332
```

### 1.1.3 c)

```
[ ]: error_xs = xs
error_ys = [y - f_endpoint(x) for x, y in zip(xs, ys)]

def plot_error():
    # TODO: Should this curve be in %?
    plt.plot(error_xs, error_ys, "-o", label="Avvik")
```

```
[ ]: plot_error()
plt.legend()
plt.show()
```



```
[ ]: max_error = max(zip(error_xs, error_ys), key=lambda item: item[1])
max_error_y = max_error[1]
max_endpoint_based_nonlinearity = max_error_y / (max_y - min_y) * 100
```

```
[ ]: print(f"Maksimalt endepunktbasert ulinearitet i prosent av måleomfanget:
↪ \n{max_error_y}%")
```

Maksimalt endepunktbasert ulinearitet i prosent av måleomfanget:  
15.0%

## 1.2 Oppgave 3

### 1.2.1 a)

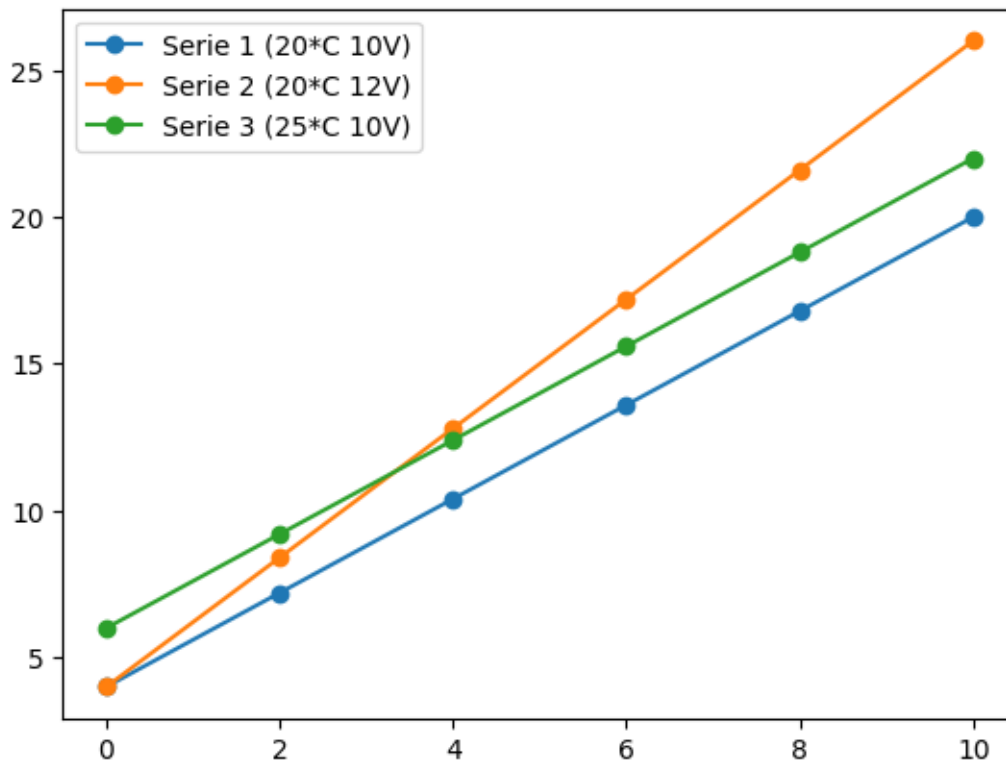
Plotte datasettet

```
[ ]: xs = [0.0, 2.0, 4.0, 6.0, 8.0, 10.0]
```

```
series_1_ys = [4.00, 7.20, 10.4, 13.6, 16.8, 20.0]
series_2_ys = [4.00, 8.40, 12.8, 17.2, 21.6, 26.0]
series_3_ys = [6.00, 9.20, 12.4, 15.6, 18.8, 22.0]
```

```
[ ]: plt.plot(xs, series_1_ys, "-o", label="Serie 1 (20°C 10V)")
plt.plot(xs, series_2_ys, "-o", label="Serie 2 (20°C 12V)")
```

```
plt.plot(xs, series_3_ys, "-o", label="Serie 3 (25*C 10V)")
plt.legend()
plt.show()
```



**Bestemme parametrene** Leser av grafen og ser at temperaturen forsterker signalet hele vegen mens spenningen kun øker signalet med en konstant verdi. - IM: Spenning - II: Temperatur

$$K = \frac{O_{maks} - O_{min}}{I_{maks} - I_{min}}$$

```
[ ]: omax = series_1_ys[-1]
      omin = series_1_ys[0]

      imax = xs[-1]
      imin = xs[0]

      k = (omax - omin) / (imax - imin)
```

$$a = O(I_{min})$$

```
[ ]: a = omin
```

$$K_I = \frac{\Delta O(I_{min})}{\Delta I_I}$$

```
[ ]: ki = (series_3_ys[0] - series_1_ys[0]) / (25 - 20)
```

$$I_{50\%} = \frac{I_{maks} + I_{min}}{2}$$

```
[ ]: # Siden vi har en lineær funksjon, så kan imax brukes i stede
# i_center = ((imin + imax) / 2)
i_center = imax
```

$$K_M = \frac{1}{I_{50\%}} * \left( \frac{\Delta O(I_{50\%})}{\Delta I_M} \right)$$

```
[ ]: # Siden vi har en lineær funksjon, så kan omax brukes i stede
# lower_mid_index = len(series_2_ys) // 2
# series_1_o_center = (series_1_ys[lower_mid_index] +
↪ series_1_ys[lower_mid_index + 1]) / 2
# series_2_o_center = (series_2_ys[lower_mid_index] +
↪ series_2_ys[lower_mid_index + 1]) / 2
# delta_o_center = series_2_o_center - series_1_o_center

delta_o_center = series_2_ys[-1] - series_1_ys[-1]

km = (1/i_center) * ((delta_o_center / (12 - 10)))
```

### Svar

```
[ ]: print(f"K: {k}")
print(f"Km: {km}")
print(f"Ki: {ki}")
print(f"a: {a}")
```

K: 1.6  
Km: 0.30000000000000004  
Ki: 0.4  
a: 4.0

### 1.2.2 b)

```
[ ]: def signal(i, ii, im):
    return (k + km * im) * i + (ki * ii) + a
```

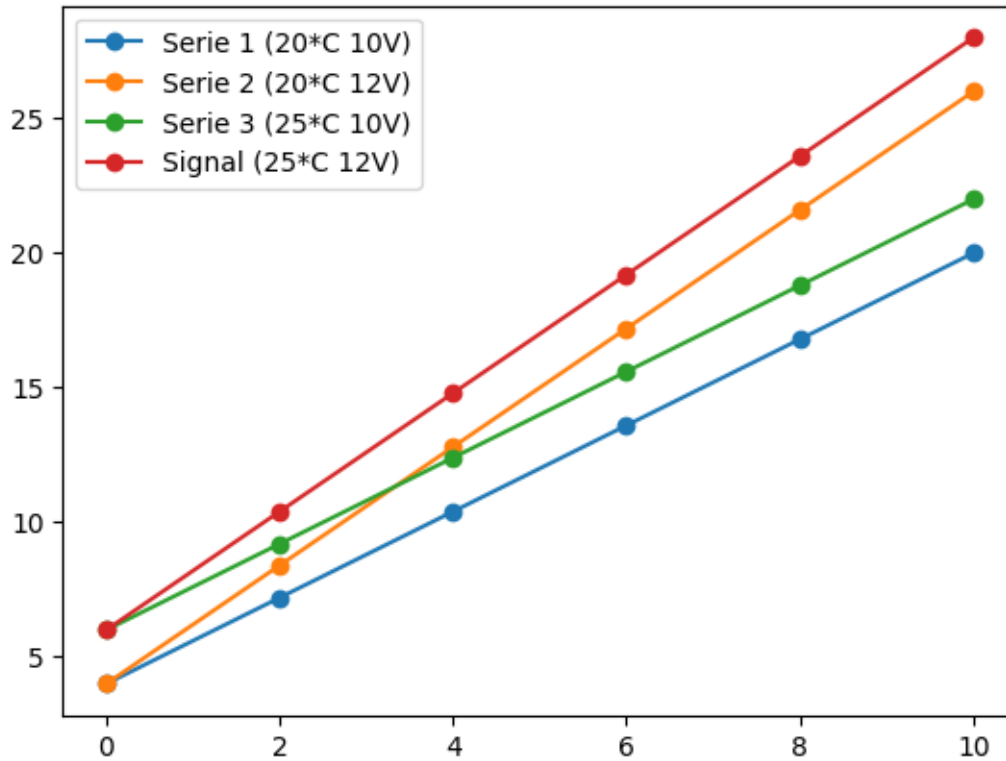
```
[ ]: o = signal(5.0, 5.0, 2.0)
```

```
[ ]: print(f"Signal: {o:.2f} mA")
```

Signal: 17.00 mA

```
[ ]: plt.plot(xs, series_1_ys, "-o", label="Serie 1 (20°C 10V)")
plt.plot(xs, series_2_ys, "-o", label="Serie 2 (20°C 12V)")
plt.plot(xs, series_3_ys, "-o", label="Serie 3 (25°C 10V)")
```

```
plt.plot(xs, [signal(x, 5.0, 2.0) for x in xs], "-o", label="Signal (25°C 12V)")
plt.legend()
plt.show()
```



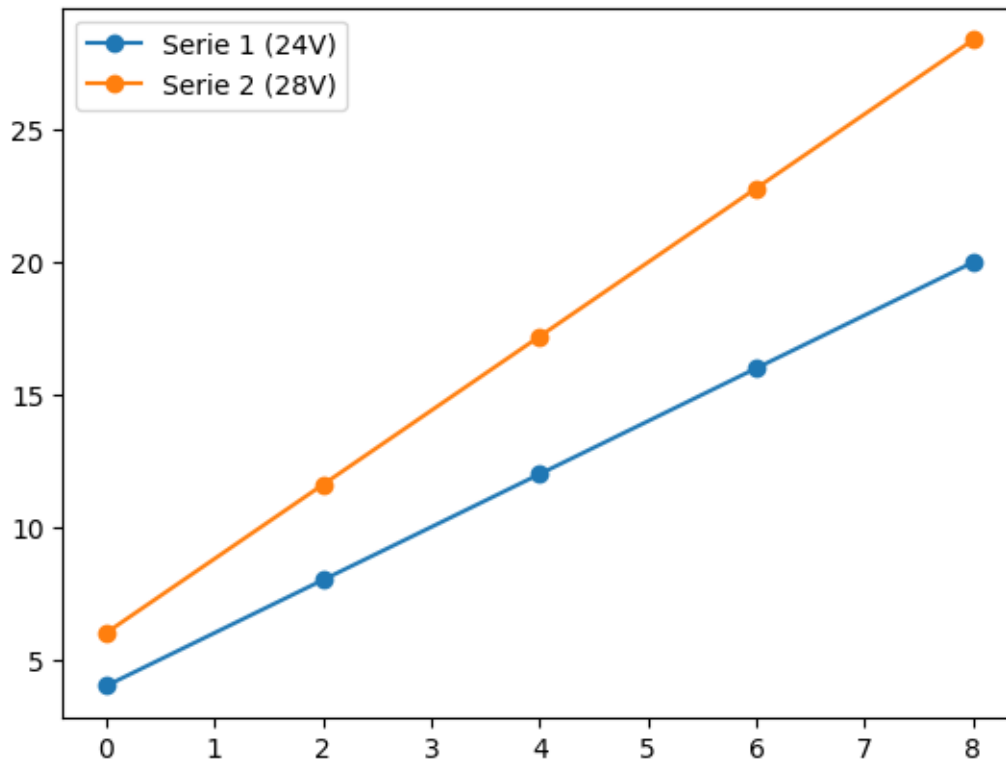
### 1.3 Oppgave 4

#### 1.3.1 a)

Plotte datasettet

```
[ ]: xs = [0.0, 2.0, 4.0, 6.0, 8.0]
      series_1_ys = [4.00, 8.00, 12.0, 16.0, 20.0]
      series_2_ys = [6.00, 11.6, 17.2, 22.8, 28.4]
```

```
[ ]: plt.plot(xs, series_1_ys, "-o", label="Serie 1 (24V)")
      plt.plot(xs, series_2_ys, "-o", label="Serie 2 (28V)")
      plt.legend()
      plt.show()
```



**Bestemme parametrene** Ser på grafen at spenningen bidrar både i form av konstantledd og forsterkning av signalet. - IM: Spenning - II: Spenning

$$K = \frac{O_{maks} - O_{min}}{I_{maks} - I_{min}}$$

```
[ ]: omax = series_1_ys[-1]
      omin = series_1_ys[0]

      imax = xs[-1]
      imin = xs[0]

      k = (omax - omin) / (imax - imin)
```

$$a = O(I_{min})$$

```
[ ]: a = omin
```

$$K_I = \frac{\Delta O(I_{min})}{\Delta I_I}$$

```
[ ]: ki = (series_2_ys[0] - series_1_ys[0]) / (28 - 24)
```

$$I_{50\%} = \frac{I_{maks} + I_{min}}{2}$$



```
[ ]: # Siden vi har en lineær funksjon, så kan imax brukes i stede
# i_center = ((imin + imax) / 2)
i_center = imax
```

Siden spenningen påvirker både konstantledd og forsterkningen må vi ta hensyn til det ved å trekke fra  $K_I$ .

$$K_M = \frac{1}{I_{50\%}} * \left( \frac{\Delta O(I_{50\%})}{\Delta I_M} - K_I \right)$$

```
[ ]: # Siden vi har en lineær funksjon, så kan omax brukes i stede
# lower_mid_index = len(series_2_ys) // 2
# series_1_o_center = (series_1_ys[lower_mid_index] +
    ↪ series_1_ys[lower_mid_index + 1]) / 2
# series_2_o_center = (series_2_ys[lower_mid_index] +
    ↪ series_2_ys[lower_mid_index + 1]) / 2
# delta_o_center = series_2_o_center - series_1_o_center

delta_o_center = series_2_ys[-1] - series_1_ys[-1]

km = (1/i_center) * ((delta_o_center / (28 - 24)) - ki)
```

**Svar**

```
[ ]: print(f"K: {k}")
print(f"Km: {km}")
print(f"Ki: {ki}")
print(f"a: {a}")
```

```
K: 2.0
Km: 0.19999999999999996
Ki: 0.5
a: 4.0
```

### 1.3.2 b)

```
[ ]: def signal(i, ii, im):
    return (k + km * im) * i + (ki * ii) + a
```

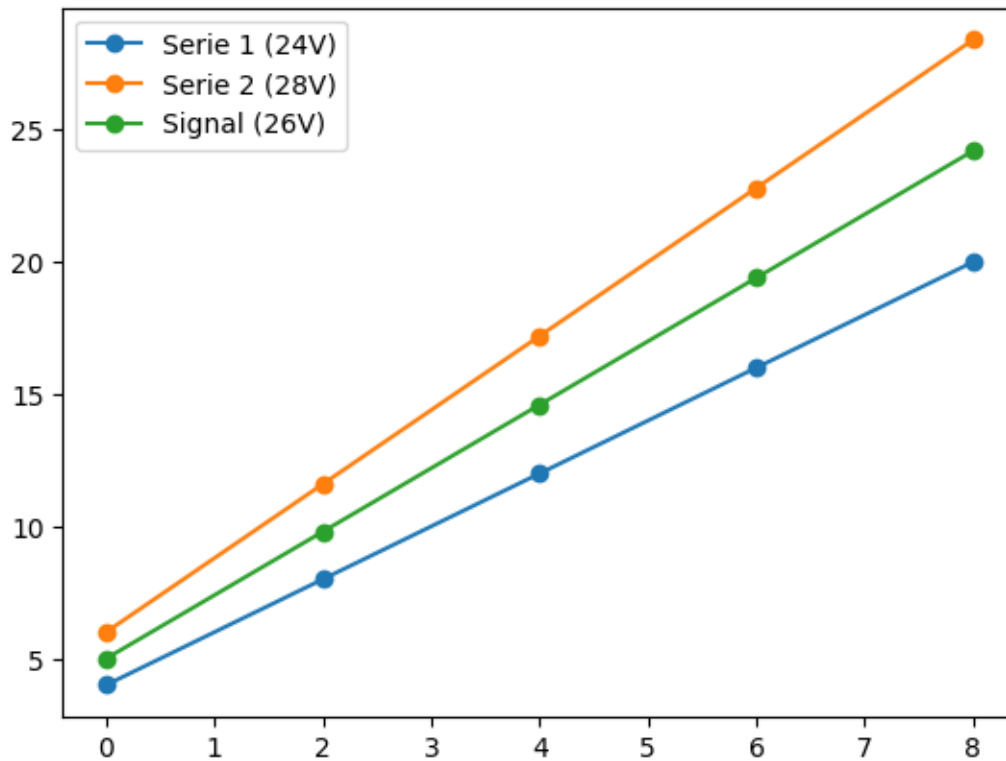
```
[ ]: o = signal(5.0, 2.0, 2.0)
```

```
[ ]: print(f"Signal: {o:.2f} mA")
```

```
Signal: 17.00 mA
```

```
[ ]: plt.plot(xs, series_1_ys, "-o", label="Serie 1 (24V)")
plt.plot(xs, series_2_ys, "-o", label="Serie 2 (28V)")
plt.plot(xs, [signal(x, 2.0, 2.0) for x in xs], "-o", label="Signal (26V)")
plt.legend()
```

```
plt.show()
```



```
[ ]:
```

## 1.4 Oppgave 5

### 1.4.1 a)

Tilbakekoblingen under slipper kun gjennom signaler hvis viseren ikke er i riktig posisjon. Hvis viseren ble flyttet manuelt og inngangssignalet forblir likt vil tilbakekoblingen motarbeide den eksterne kraften påtrykt viseren.

flowchart LR

A[I]  
B((+))  
C[Kv]  
D[Ks]  
E[O]  
F[K]

A -->|+| B --> C --> D --> E

D --> F -->|-| B

$$\frac{O}{I} = \frac{Kv*Ks}{1+Kv*Ks*K}$$

$$\frac{O}{I} = \frac{0.2*0.05}{1+0.2*0.05*1000}$$

$$\frac{O}{I} = \frac{0.01}{1+0.01*1000}$$

$$\frac{O}{I} = \frac{0.01}{1+10}$$

$$\frac{O}{I} = \frac{1}{1100}$$

#### 1.4.2 b)

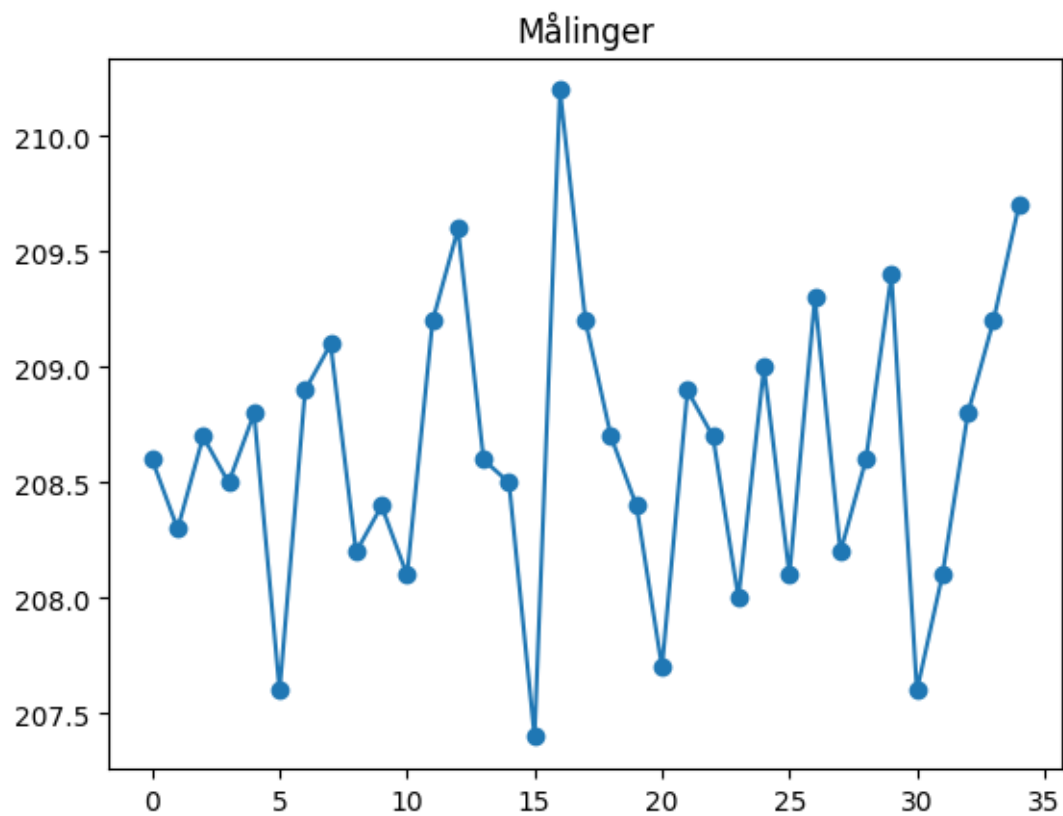
```
[ ]: 0.1*(1/1100)
```

```
[ ]: 9.090909090909092e-05
```

### 1.5 Oppgave 6

```
[ ]: values = [  
    *[208.6, 208.3, 208.7, 208.5, 208.8, 207.6, 208.9, 209.1, 208.2, 208.4],  
    *[208.1, 209.2, 209.6, 208.6, 208.5, 207.4, 210.2, 209.2, 208.7, 208.4],  
    *[207.7, 208.9, 208.7, 208.0, 209.0, 208.1, 209.3, 208.2, 208.6, 209.4],  
    *[207.6, 208.1, 208.8, 209.2, 209.7],  
]
```

```
[ ]: plt.plot(values, "-o")  
plt.title("Målinger")  
plt.show()
```



```
[ ]: midvalue = sum(values)/len(values)
```

```
[ ]: S = np.sqrt((1/(len(values) - 1))*sum([(x-midvalue)**2 for x in values]))
```

```
[ ]: print(f"Estimat: {unc.ufloat(midvalue, S):.1f}")
```

Estimat: 208.6+/-0.6

```
[ ]: plt.hist(values)
plt.show()
```

